

Visual quality metrics

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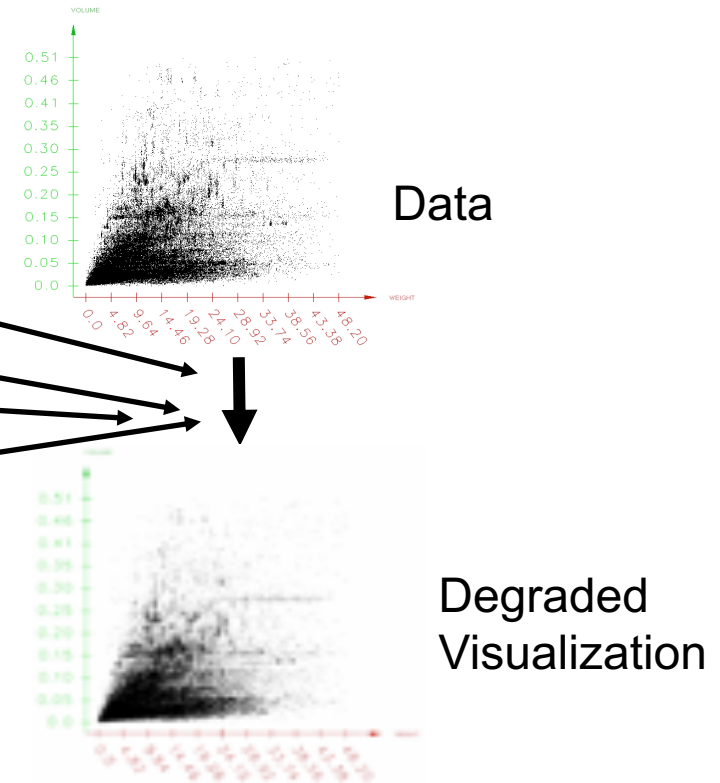
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The problem

- Very often data visualizations do not convey data features in a correct way !
- Infovis' enemies:
 - clutter
 - collisions
 - user perception
 - pixel dimension
 - ...

You cannot control what you cannot measure [T. De Marco, 1982]



What are we measuring?

We propose the following taxonomy:

1. Size metrics
2. Visual effectiveness metrics
3. Features preservation metrics



Size metrics

- **purpose:** basis of any other computation
- examples:
 - number of data items
 - size of pixels
 - ...
- can benefit from perceptual studies (e.g., numerosity), indicating the limits of human perception and thus providing some useful threshold values
- quite intuitive and we do not discuss them anymore (but we use them!)



Visual effectiveness metrics

- **purpose:** measuring the image degradation, taking into account some disturbing factors
- examples:
 - number of collisions
 - number of outliers
 - ...
- most of the available metrics belong to this class
- we discuss how to **use** these metrics



Features preservation metrics

- **purpose:** intended for measuring how correctly an image is representing some data characteristics
- examples:
 - Tufte' s lie factor, that is the ratio between the size of an effect, as shown graphically, to its size in the data
 - ???
 - The idea of **comparing** data characteristics against visualization effects, pioneered by Tufte, has not been pursued anymore...
- As a consequence, few proposals are available in this class and we intend to analyze these metrics in detail, discussing how to **define** and **use** them



A four steps methodology for defining feature preservation metrics

1. *Choose the feature to preserve*
 2. *Formally define the feature in (1) the data space and (2) in the visualization space*
 3. *Validate and tune the definition in the visualization space through user perception*
 4. *Define the metric **comparing** figures coming from data space against figure coming from the visualization space*
- We detail these steps through a 2D scatter plot example



A (not simple) example: step 1

1. Choose the target feature: **density differences**

Therefore our goal is to measure how density differences that **exist** in the data set are presented to the user using a 2D scatter plot.



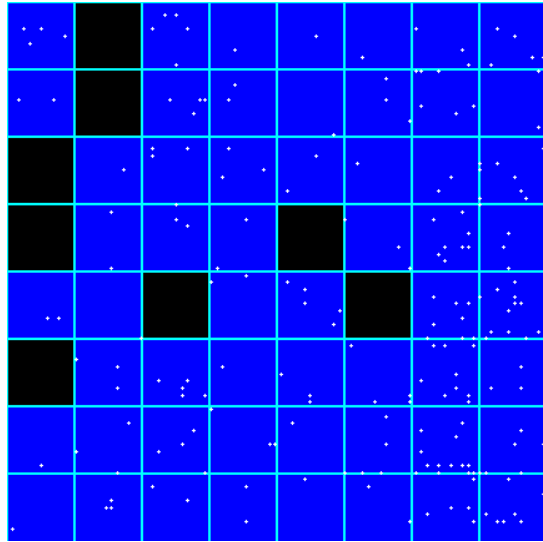
A (not simple) example: step 2

2. Formally define the feature in (1) the data space and (2) in the visualization space

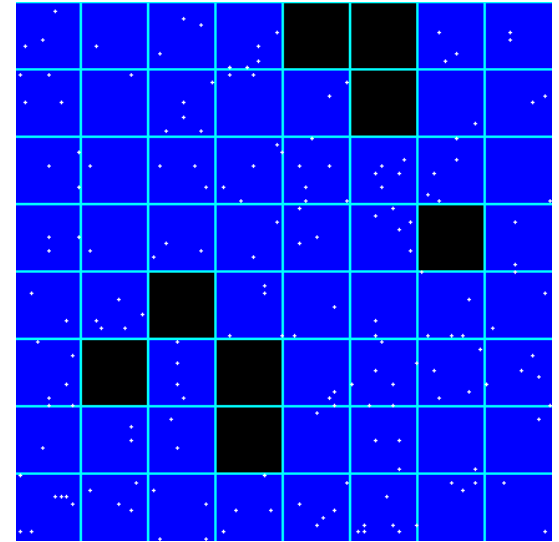
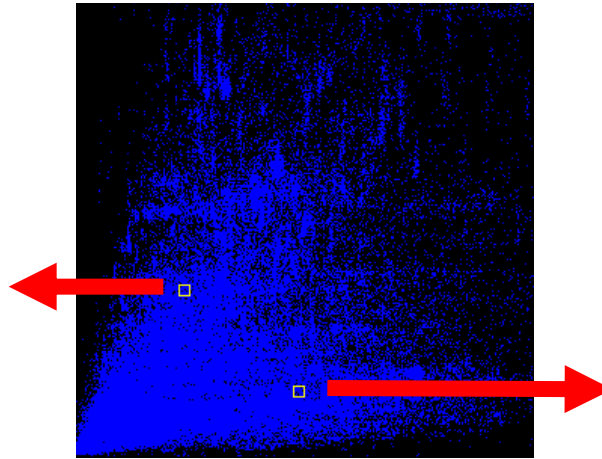
- to formalize density differences we split the 2D plane in little squares that we call **sample areas** (typical dimension: 0,08x0,08 inches / 8x8 pixels)
- in the **data space** we measure the **Data Density**, the number of **data points** within a sample area
- in the **visualization space** we measure the **Represented Density**, the number of **active pixels** within a sample area
- because of collisions we have that in a sample area:
$$\text{Represented Density} \leq \text{Data Density}$$



A (not simple) example: step 2



Data density=205
Rep density=56



Data density=189
Rep density=56

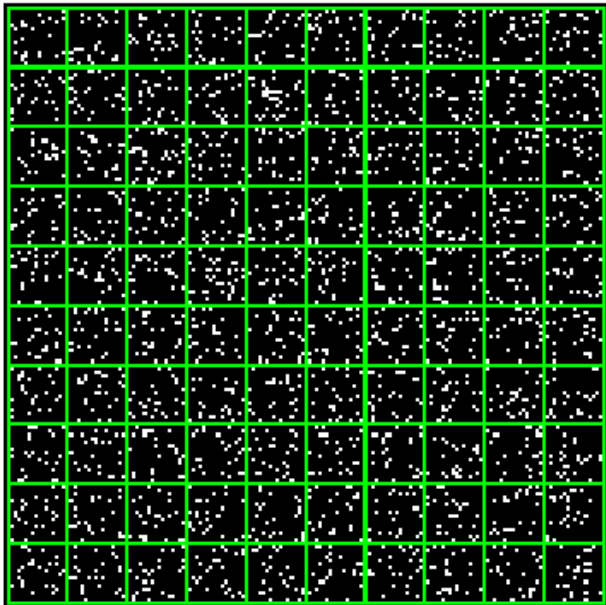
The actual visualization hides this difference



A (not simple) example: step 3

3. Validate and tune the definition in the visualization space through user perception

the question is: are Represented Density **numerical** differences adequate?



100 sample areas

97 contain 25 pixels

3 contain 38 pixels

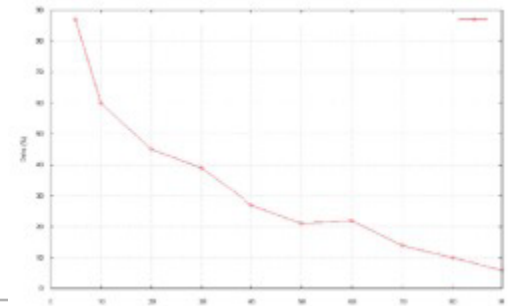
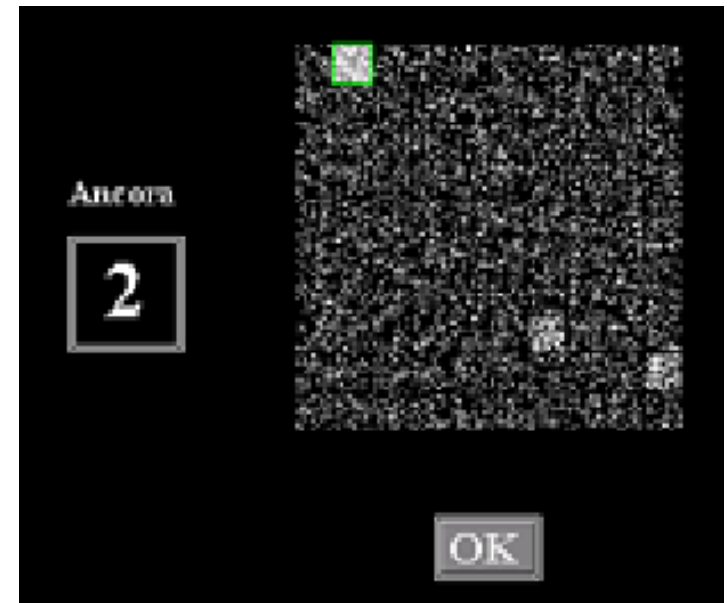
Which ones ?



A (not simple) example: step 3

3. Validate and tune the definition in the visualization space through user perception

- What is the smallest difference in pixels between two sample areas that produces the perception of density difference?
- User test step:
 - image with 100 sample areas
 - 97 with the same number of pixels (basis)
 - 3 filled with extra (delta) pixels
 - the user has to recognize the three more dense areas
- repeated for different basis and deltas



A (not simple) example: step 4

4. Define the metric **comparing** figures coming from data space against figure coming from the visualization space

WPLDDr (Weighted *Perceptually* Lost Data Densities ratio)

the metric counts the sample area pairs whose represented density **does not match** the real data density (we weight the comparisons with the involved data points).

$$PDiff(x, y) = \begin{cases} 1 & \text{if } x \geq y + y \times \text{minimum}\delta(y) \\ -1 & \text{if } y \geq x + x \times \text{minimum}\delta(x) \\ 0 & \text{otherwise} \end{cases}$$

$match(i, j, k, l) = \text{true iff}$

$$PDiff(D_{i,j}, D_{k,l}) = PDiff(RD_{i,j}, RD_{k,l})$$

```
function WPLDDr(){
  Let couples=0; /* weighted SA couples
  Let sum=0;      /* weighted non matching SA couples
  foreach distinct pair(SA[i][j], SA[k][l]){
    couples = couples + pt(SA[i][j]) + pt(SA[k][l]);
    if ( NOT match(i, j, k, l) )
      sum = sum + pt(SA[i][j]) + pt(SA[k][l]);
  }
  return (sum / couples);}
```



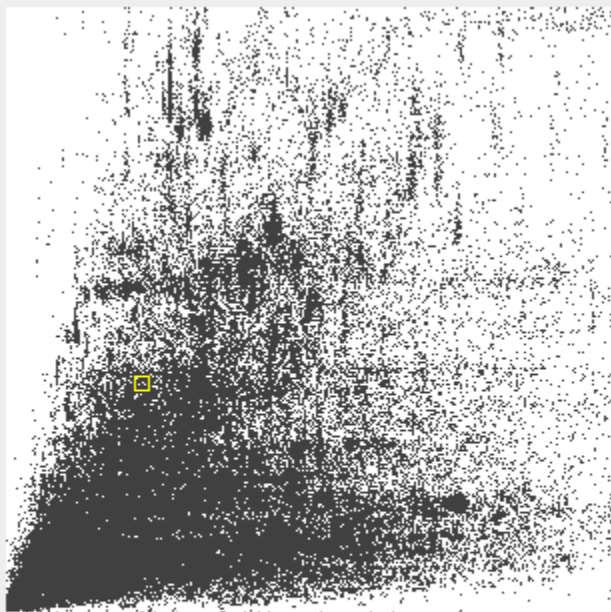
Visual quality metrics usage

- Threshold comparison
 - to discard/accept the visualization
 - to activate ameliorating algorithms
- Comparison and evaluation of algorithms and visual techniques
- Algorithm driving

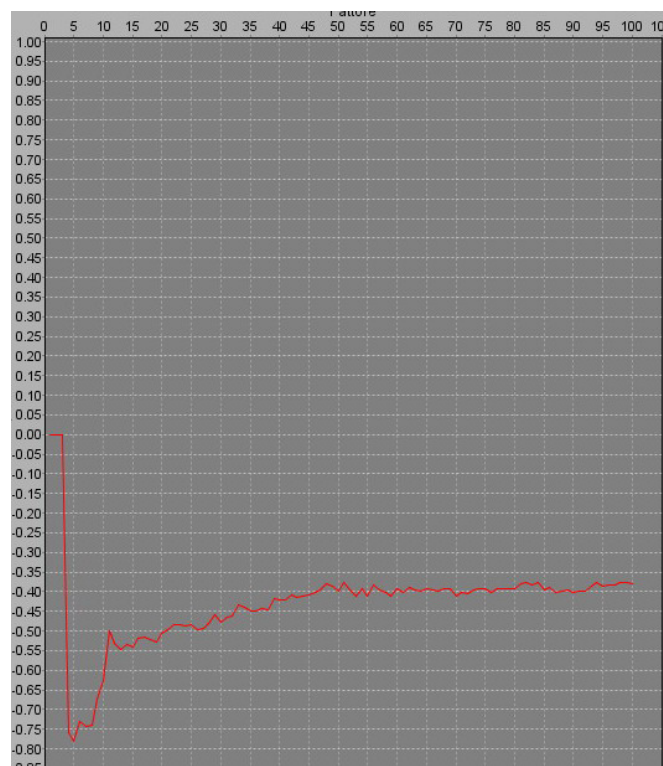


Practical usage of quality metrics

Not Sampled Image

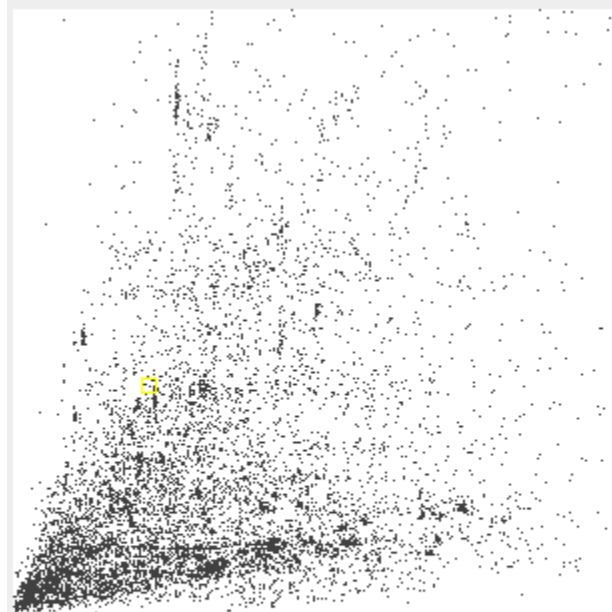


$1-WPLDDr=0.392$
i.e., 60% hidden



Best uniform sampling
minimizing the metric

Best Uniform Sampling



$1-WPLDDr=0.738$
i.e., 26% hidden



Conclusions

- Visual quality metrics **definition** and **usage** are critical issues
- A better comprehension of **what** we are measuring and **how** to use the measures is needed
- We believe that features preservation metrics produces **objective** indications about an image quality
 - but their definition is not a simple task

