

Computational Phonology Workshop

Introduction & Tutorial

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Outline

- 1 The Subregular Enterprise
- 2 (Tier-Based) Strictly Local Phonotactics
- 3 Subregular Mappings for Phonology
- 4 (Tier-Based) Strictly Local Syntax

Computational View of Language

In formal language theory, string sets are classified according to their formal complexity.

regular < context-free < mildly context-sensitive < ...

Phonology

Morphology

Syntax

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Kaplan and Kay (1994)

Phonology

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Phonology

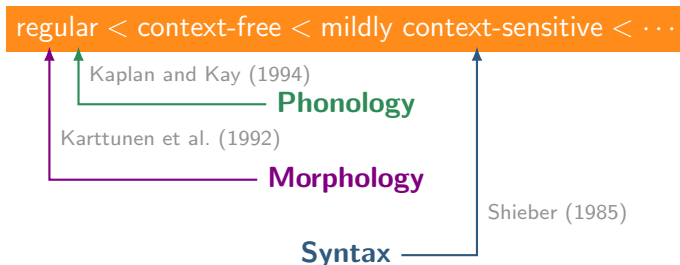
Karttunen et al. (1992)

Morphology

Syntax

Computational View of Language

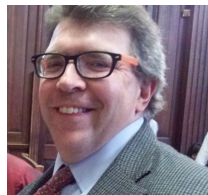
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Implications of Formal Complexity

Heinz and Idsardi (2011, 2013) highlight the implications:

- ▶ different typology
center embedding, crossing dependencies
- ▶ different memory architecture
flat & finite VS unbounded nested stacks
- ▶ different learning algorithms
much harder for syntax



Too Many Patterns are Regular

► Problem

- All phonological and morphological patterns are regular.
- But not all regular patterns occur in phonology.
- Regularity is **too loose an upper bound**.

Example

- First-last consonant harmony
- Every word with a plosive contains an open syllable
- Word with at least 3 suffixes must have exactly 5 prefixes

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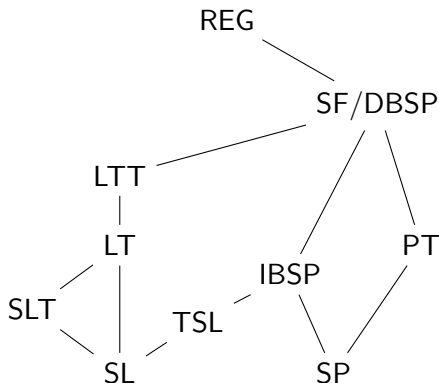
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Subregular Languages

Often forgotten: hierarchy of **subregular languages**

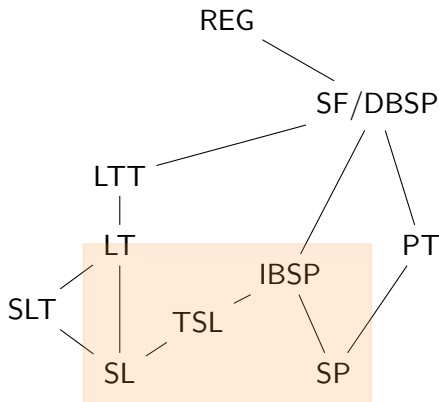
(McNaughton and Papert 1971; Rogers et al. 2010; Ruiz et al. 1998; Rogers and Pullum 2011; Heinz et al. 2011; Graf 2016)



Subregular Languages

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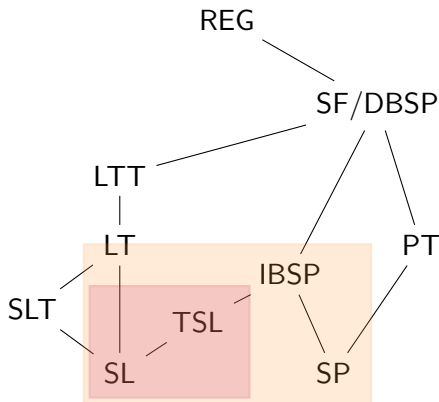
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SL: Strictly Local

- ▶ SL formalizes **local dependencies**.
- ▶ SL grammars are collections of markedness constraints that are
 - ▶ hard/non-violable,
 - ▶ locally bounded.

Strictly Local Grammars & Languages

SL_n grammar finite set of forbidden n -grams

SL_n language all strings except those with forbidden n -grams

Example: SL Constraints

Process	Constraint	Forbidden <i>n</i> -grams
Word-final devoicing	* [+voice] ×	z ×, v ×, ...
Intervocalic voicing	* V[-voice] V	asa , asi , ..., isa , isi , ..., afa , afi , ..., ifa , ifi , ...
CV template	* × V * CC * VV * C ×	× a , × i , ... pp , pb , ... bp , bb , ... aa , ai , ..., ia , ii , ... p ×, b ×, ...

SL is Too Weak

- ▶ SL grammars only handle unbounded dependencies.
- ▶ But some processes in phonology are unbounded.

Samala Sibilant Harmony (Heinz 2015:16)

ʃtojonowonowɛʃ

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Samala Sibilant Harmony (Heinz 2015:16)

ʃtojonowonowaf

*stojonowonowaf

*ʃtojonowonowas

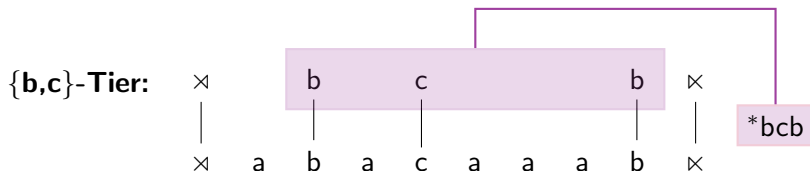
TSL: Tier-Based Strictly Local

We can make Samala SL-like if we **create new locality domains**.

Tier-Based Strictly Local Grammars & Languages

TSL_n grammar finite set of forbidden n -grams + tier alphabet

TSL_n language all strings except those with forbidden n -grams
over tier



Example: Sibilant Harmony

Constraint

* $[\alpha \text{ ant}] \cdots [-\alpha \text{ ant}]$

Forbidden tier- n -grams

$\int s, s \int$

Tier contains all sibilants

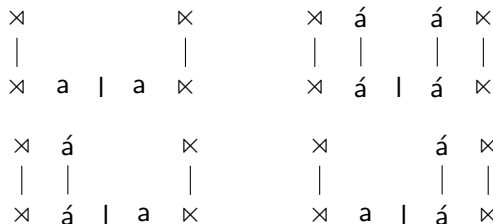
Tier:	×		\int		s		×
Base:	×	e	\int	i	s	i	×

Tier:	×		\int		\int		×
Base:	×	e	\int	i	\int	i	×

Example: Stress Assignment

Culminativity every word has exactly one primary stress

Tier contains segments with primary stress
n-grams **ś** and **×**



A Non-TSL Pattern: Sour Grapes Harmony

Sour Grapes vowel harmony applies only if it can apply to the whole word (i.e. there is no blocker)

Why Sour Grapes isn't TSL

- ▶ All vowels **V** must be on the vowel harmony tier.
- ▶ The blocker **B** must be on the same tier in order to block it.
- ▶ But there is no bound on the number of vowels per tier.
- ▶ The tier thus may have the shape
... **V V V** ... **B** ...
- ▶ **B** can be arbitrarily far away from **VVV** \Rightarrow not a local relation
- ▶ But we need to know whether **B** is on the tier in order to determine the well-formedness of **VVV**.

More Patterns Beyond TSL?

A few other patterns may go beyond TSL.

- ▶ **Non-Final RHOL**

- ▶ discussed in **Hyunah Baek's talk**
- ▶ a minor extension of TSL suffices

- ▶ **Multiple Harmony**

- ▶ discussed in **Alëna Aksënova's talk**
- ▶ is actually TSL due to important restrictions

Complexity of Phonology

- ▶ All local phonological constraints are SL.
- ▶ All segmental long-distance constraints are TSL.
- ▶ Suprasegmental constraints (tone, stress) may go beyond TSL.
(Graf 2010a,b; Jardine 2015)
- ▶ TSL avoids instances of OT overgeneration:
 - ▶ cannot generate *sour-grapes* or *majority rules* patterns
 - ▶ does not allow *agreement by proxy*
 - ▶ explains why consonant harmony is unbounded or transvocalic, but never transconsonantal
(McMullin and Hansson 2015)

Cognitive Implications

- ▶ SL and TSL languages are **learnable** from positive data.
(Heinz et al. 2012; Jardine and Heinz 2016)
 - ▶ UG: specifies upper bound on size of n -grams
 - ▶ memorize which sequences have not been seen so far
 - ▶ induce tier (more complex)
 - ▶ learning input can be relatively small
- ▶ What cognitive resources are required?
 - ▶ Only memorization of the last n segments of a specific type
 - ▶ For most processes $n \leq 3$, and for all $n \leq 7$
 - ▶ Fits **within bounds of human working memory**

Interim Summary: Phonotactics

- ▶ Natural languages have **TSL phonotactics**.
- ▶ gives tighter bound on typology
- ▶ solves poverty of stimulus by greatly simplifying learning
- ▶ reduces cognitive resource requirements

Next

- ▶ phonological mappings
- ▶ SL & TSL syntax

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Phonological Mappings

- ▶ So far we have only considered phonotactics.
- ▶ But mappings from underlying representations to surface forms can be studied, too.
- ▶ Regular mappings are enough.
(Kaplan and Kay 1994)
- ▶ What about subregular mappings?

Input Strictly Local Mappings

Input Strictly Local (ISL)

- ▶ Move through string from left to right.
- ▶ Rewrite x as y based on previous n symbols in input string.
- ▶ Output is **not considered!**

A Note on TSL

Every TSL_n grammar can be decomposed into

- 1 an **ISL₁** function (the tier projection), and
- 2 an SL_n grammar.

An Interesting Puzzle

- ▶ What happens if we use an ISL_k function for tier projection?
- ▶ Addressed in **Aniello De Santo's** talk

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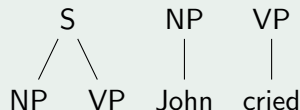
- ▶ What happens if we use an ISL_k function for tier projection?
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(Tier-Based) Strictly Local Syntax

- ▶ SL tree grammars are common in computational linguistics:
context-free grammars
- ▶ By adding tier projection, we get TSL tree grammars.

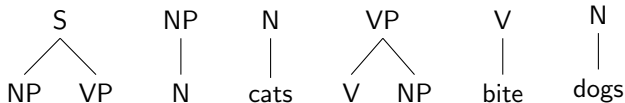
Example: CFGs as SL_2 Tree Grammars

S → NP VP
NP → John
VP → cried

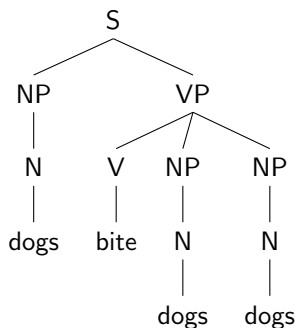


Example: An Illicit Tree

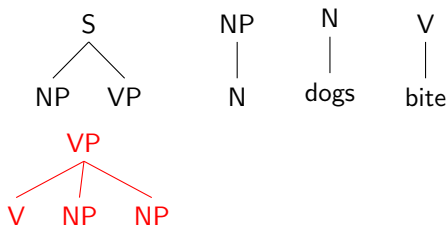
SL₂ Tree Grammar



Example Tree



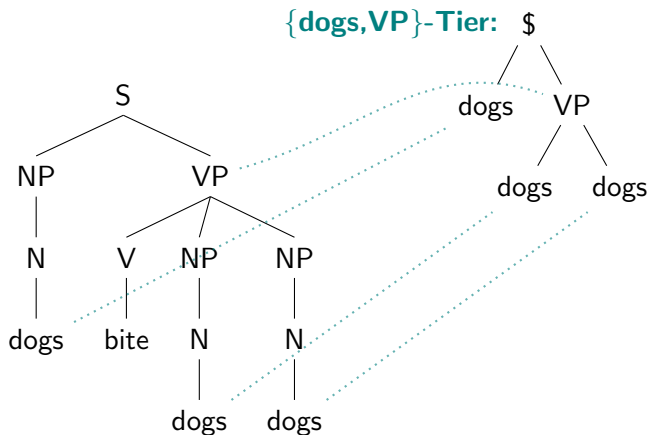
Tree Bigrams of Example Tree



Tier Projection for Trees

Just as for strings, we can project tiers for trees.

(Graf and Heinz 2016)



Towards TSL-Syntax

While TSL-Syntax is still young, it holds promise:

- ▶ movement dependencies are TSL (Graf and Heinz 2016)
- ▶ scope ambiguities in **Lei Liu's blitz talk**
- ▶ Mandarin negation in **Hongchen Wu's talk**

Conclusion

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