To Achieve Harmony We Only Need One Tier

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 Several TSL grammars are needed to capture several long-distance phonological dependencies.

Unattested patterns

- For a single vowel harmony, only one tier is enough.
- There are double vowel harmonies, where primary and secondary features are being spread.
- Do we need more than one tier to model such harmonies?

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- For a single vowel harmony, only one tier is enough.
- There are double vowel harmonies, where primary and secondary features are being spread.
- Do we need more than one tier to model such harmonies?

One tier is always enough!

Outline

- TSL phonology
- Secondary harmony
- Unattested patterns
- 4 Discussion

Tier-based Strictly Local grammars capture non-local dependencies in a local fashion by projecting elements of a certain type on a *tier*.

TSL phonology

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FINNISH, HUNGARIAN: front/back harmony LOKAA: ATR harmony among non-high vowels

KINGALA: height harmony

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- Transparent elements are ignored.

Harmony in Lokaa

TSL phonology

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Example (Vowel harmony in LOKAA)

Non-high vowels harmonize in ATR. (Akinlabi 2009)

'smoke' lèjìmà 'matriclan' èsìsòn tense: ótú:má 'need' lax: èsísòn 'housefly'

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 - èsísòn 'housefly' ótú:má 'need' lax:
- $T = \{e, o, a, \epsilon, a\}, H_{ATR} = \{*e\epsilon, *ea, *ea, *oa, *\epsilon o, ...\}$

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• In numerous languages we observe double harmony, where two features are being transmitted.

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TURKISH, YAKUT, KIRGHIZ: front/back and rounding

BURYAT, MONGOLIAN: ATR and rounding

COEUR D'ALENE: ATR and height

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- We expect to need a separate tier for secondary harmonies.
- Is it true?

TSL phonology

- Primary: all vowels harmonize in ATR.
- Secondary: non-high vowels agree in rounding, high ones block it.

TSL phonology

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- **Roots:** or 'enter' to:r 'wander'
- Affixes: $-\upsilon$:l, -u:l 'CAUS' (V: $^{+hi}$ l)
 -a:d, -o:d, -e:d, -o:d 'PERF' (V: $^{-hi}$ d)

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lax word; two adjacent non-high vowels harmonize or-o:d 'enter-PERF' *or-a:d

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```

```
# lax word; two adjacent non-high vowels harmonize
             'enter-PERF'
                                      *or-a:d
or-oid
# lax word; high vowel blocks labial harmony
or-v:l-a:d 'enter-CAUS-PERF' *or-v:l-o:d
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or-ບ:l-a:d 'enter-CAUS-PERF' *or-ບ:l-o:d
# tensed word; two adjacent non-high vowels harmonize
             'wander-PERF' *to:r-e:d
to:r-o:d
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• Tier $T = \{a, e, o, o, v, u\}$

TSL phonology

- Tier $T = \{a, e, b, o, v, u\}$
- Primary: all vowels harmonize in ATR.
- No $*V_{\alpha ATR}V_{-\alpha ATR}$ bigrams $H_{ATR} = \{*$ 50, *05, *vu, *uv, *ae, *ea, *vo, *ve, *ve, *ev, *ve, *v*uɔ, *ɔe, *eɔ, *oa, *au, *ua}

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- Secondary: non-high vowels harmonize in rounding, high vowels are blockers: rounded non-high vowels can either occur in the first syllable, or be licensed by harmony.
- No $*V_{\alpha round}^{-hi}V_{-\alpha round}^{-hi}$ and $*V_{+round}^{-hi}$ bigrams $H_{round} = \{*a, *a, *eo, *oe, *v, *uo\}$

- $T = \{a, e, o, o, v, u\}$
- *uɔ, *ɔe, *eɔ, *oa, *ao, *au, *ua}

Unattested patterns

• $H_{round} = \{*$ a, *a, *eo, *oe, *v, *uo}

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• $H_{round} = \{*a, *a, *e, *oe, *oe, *uo\}$

Example (Double vowel harmony in Buryat)

to:r-o:d 'wander-PERF' *to:r-e:d

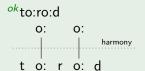
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TSL phonology

- *uo. *oe, *eo, *oa, *ao, *au, *ua}
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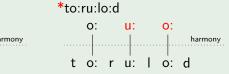
TSL phonology

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ok to:ru:le:d o: u: e: t o: r u: l e: d



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TSL phonology

- Primary: all vowels harmonize in ATR.
- Secondary: non-high vowels harmonize in rounding, high vowels block this spreading.
- Only one tier is needed:
 - Transparent elements are same for both harmonies.
 - Secondary harmony is bounded on the vowel tier, high vowels block the spreading of [round] feature.

Unattested patterns

It is possible to imagine a language where a separate tier for the secondary harmony will be needed:

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- Secondary harmony is also unbounded and affects only subset of the vowels that take part in the primary spreading.
- Secondary harmony involves a blocker that was not presented on the tier of the primary one.

Unattested patterns: Pseudo-Buryat

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```
brulod *oruled
```

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Example (Double vowel harmony in PSEUDO-BURYAT)

- Primary: all vowels harmonize in ATR
- Secondary: all non-high vowels harmonize in rounding

```
*arulad
orulad
torulod
        *toruled
```

 One tier is not enough: there can be unbounded amount of high vowels in-between the two harmonizing non-high ones.

- Primary: all vowels harmonize in ATR.
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Unattested patterns: Pseudo-Buryat [cont.]

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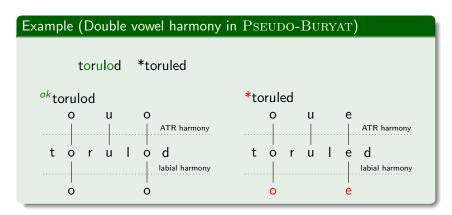
Example (Double vowel harmony in PSEUDO-BURYAT)

*toruled torulod

TSL phonology

Unattested patterns: Pseudo-Buryat [cont.]

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TSL phonology

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Characteristics of the secondary harmony:

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- Secondary harmony spreads together with the main one, and
- Transparent elements for the primary harmony are transparent for the secondary one, and
- Blockers for the secondary harmony are presented on a tier of the primary one.

It is always possible to fit vowel harmony on one tier!

TSL phonology

• What is the algebra of tier alphabets?

TSL phonology

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- If there is more than one tier needed to capture different phenomena in a language, their possible relations are:

TSL phonology

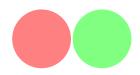
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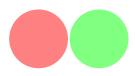
Unattested patterns



Disjoint KIYAKA i.a. Hyman (1995, 1998)

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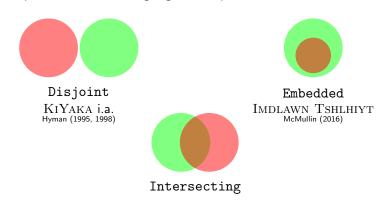


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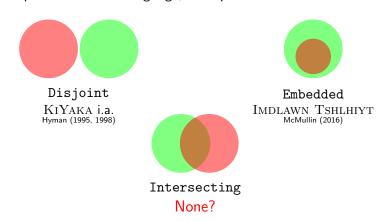
Embedded Imdlawn Tshlhiyt McMullin (2016)

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TSL phonology

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- If there is more than one tier needed to capture different phenomena in a language, their possible relations are:



- What are double harmonies telling us?
- What are natural tiers and how do they differ from the unnatural ones?
- What are the limitations on the tier projection?

The more complex the mind, the greater the need for the simplicity of play.

James T. Kirk

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Secondary harmony: Kirghiz

- Primary harmony is frontness.
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Example (Double vowel harmony in KIRGHIZ)

From (Kaun 1995), dialect described in (Herbert & Poppe 1963)

- Primary: all vowels harmonize in frontness.
- Secondary:
 - In [+front] words, all vowels agree in rounding.
 - In [-front] words, only adjacent non-high vowels harmonize in rounding, high vowels are blockers.

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```
köl-dön 'lake-ABL' *köl-den

üy-dön 'house-ABL' *üy-den

tokoy-don 'forest-ABL' *tokoy-dan

tormuš-tan 'life-ABL' *tormuš-ton
```

• $T = \{o, \ddot{o}, e, a, z, a, u, \ddot{u}\}$

- $T = \{ o, \ddot{o}, e, a, z, a, u, \ddot{u} \}$
- Primary: all vowels harmonize in frontness.
- No * $V_{\alpha front}V_{-\alpha front}$ bigrams $H_{front} = \{\text{""oo, "ea, "a"o, "u"u, "ae, ...}\}$

- $T = \{ o, \ddot{o}, e, a, z, a, u, \ddot{u} \}$
- Primary: all vowels harmonize in frontness.
- No *V $_{\alpha front}$ V $_{-\alpha front}$ bigrams $H_{front} = \{$ *öo, *ea, *aö, *uü, *ae, ... $\}$
- Secondary: in [+front] words, all vowels agree in rounding.
- No $*V^{+front}_{\alpha round}V^{+front}_{-\alpha round}$ bigrams $H_{round}=\left\{ \text{""üe, ""e"i, ""oe, ""e"i, ""ii, ""ii, ""} \right\}$

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- Secondary: ... and in [-front] words, only adjacent non-high vowels harmonize in rounding.
- No $*V_{\alpha round}^{-hi}V_{-\alpha round}^{-hi}$ bigrams $H'_{round} = H_{round} + \{*ao, *oa, *uo, *zo\}$

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- $H_{front} = \{ *\ddot{o}o, *ea, *a\ddot{o}, *u\ddot{u}, *ae, ... \}$
- $H_{round} = \{$ *üe, *eü, *öe, *iü, *üi, ... $\} + \{$ *ao, *oa, *uo, *zo $\}$

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- $H_{round} = \{ *\ddot{u}e, *e\ddot{u}, *\ddot{o}e, *\ddot{u}\ddot{u}, *\ddot{u}\ddot{u}, ... \} + \{ *ao, *oa, *uo, *zo \}$

Example (Double vowel harmony in KIRGHIZ)

üy-dön 'house-ABL' *üy-den

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- $H_{front} = \{*\ddot{o}o, *ea, *a\ddot{o}, *u\ddot{u}, *ae, ...\}$
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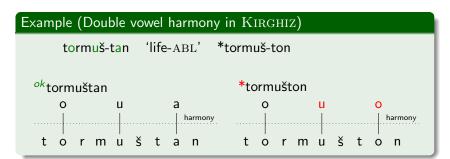


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Example (Double vowel harmony in KIRGHIZ)

tormuš-tan 'life-ABL' *tormuš-ton

- $T = \{ o, \ddot{o}, e, a, z, a, u, \ddot{u} \}$
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- Secondary: in [+front] words, all vowels harmonize in rounding, and in [-front] words, only adjacent non-high vowels agree in it, whereas high vowels function as blockers.

- Primary: all vowels harmonize in frontness.
- Secondary: in [+front] words, all vowels harmonize in rounding, and in [-front] words, only adjacent non-high vowels agree in it, whereas high vowels function as blockers.
- Only one tier is needed:
 - Both harmonies operate over the same alphabet.
 - Secondary harmony is bounded on the vowel tier for [-front] words, or spreads together with the [+front] feature.

 Secondary harmony involves blocker that was not presented at the tier of the primary one.

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Example (Double vowel harmony in QUASI-BURYAT)

- Primary: all vowels except *i* harmonize in ATR.
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```
borc* berc* berc*
definition between two definition berc*
berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* berc* be
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 One tier is not enough: i MUST NOT presented on the ATR harmony tier, and MUST BE presented on the labial assimilation tier.

• Primary: all vowels except *i* harmonize in ATR.

- Primary: all vowels except *i* harmonize in ATR.
- $T_{ATR} = \{ s, o, a, e \}$
- $H_{ATR} = \{*$ 50, *60, *ae, *ea, *5e, *ao, ... $\}$

- Primary: all vowels except i harmonize in ATR.
- $T_{ATR} = \{ \text{o, o, a, e} \}$
- $H_{ATR} = \{*50, *05, *ae, *ea, *5e, *ao, ...\}$
- Secondary: adjacent non-high vowels harmonize in rounding, high vowel *i* blocks this spreading.

- Primary: all vowels except i harmonize in ATR.
- $T_{ATR} = \{ s, o, a, e \}$
- $H_{ATR} = \{*$ 50, *60, *ae, *ea, *5e, *ao, ... $\}$
- Secondary: adjacent non-high vowels harmonize in rounding, high vowel *i* blocks this spreading.
- $T_{round} = \{i, o, o, a, e\}$
- $H_{round} = \{*$ a, *a, *oe, *eo, *io, *io}

- $T_{ATR} = \{ s, o, a, e \}$
- $H_{ATR} = \{*$ 50, *60, *ae, *ea, *5e, *ao, ...}
- $T_{round} = \{i, o, o, a, e\}$
- $H_{round} = \{*$ a, *a, *oe, *eo, *io, *io}

- $T_{ATR} = \{ s, o, a, e \}$
- $H_{ATR} = \{\text{*}, \text{*}, \text{*}, \text{*}, \text{*}, \text{*}, \text{*}, \text{*}, \text{*}, \dots \}$
- $T_{round} = \{i, o, o, a, e\}$
- $H_{round} = \{*$ a, *a, *oe, *eo, *i, *io}

Example (Double vowel harmony in PSEUDO-BURYAT)

toriled *torilod *torilad

- $T_{ATR} = \{ s, o, a, e \}$
- $H_{ATR} = \{*50, *05, *ae, *ea, *5e, *ao, ...\}$
- $T_{round} = \{i, o, o, a, e\}$
- $H_{round} = \{*$ a, *a, *oe, *eo, *i, *io}

Example (Double vowel harmony in PSEUDO-BURYAT) toriled *torilod *torilad ok toriled *torilod ATR harmony ATR harmony labial harmony labial harmony

- $T_{ATR} = \{ s, o, a, e \}$
- $H_{ATR} = \{*50, *05, *ae, *ea, *5e, *ao, ...\}$
- $T_{round} = \{i, o, o, a, e\}$
- $H_{round} = \{*$ a, *a, *oe, *eo, *i, *io}

Example (Double vowel harmony in PSEUDO-BURYAT) toriled *torilod *torilad ok toriled *torilad ATR harmony ATR harmony labial harmony labial harmony