

# Word Completion

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Lecture 2

# Word completion: a simple problem(?)

- ▶ When you write something on your phone, it automatically suggests words while you're typing them.
- ▶ Seems easy, but it's **fairly intricate**.

## Key Insights/Skills

- ▶ transition probabilities with n-grams
- ▶ "More than 1, but less than 5."
- ▶ efficient data structures: tries/prefix trees

# Attempt 1: simple lookup

- ▶ To make suggestions for completions, we only need an English/German/... dictionary.

```
1  # load English dictionary from nltk package
2  from nltk.corpus import words
3  # and see if "test" is in the list
4  "test" in words.words()
5  >>> True
```

- ▶ Given word **w**, the set of possible completions for **w** consists of all listed words that start with **w**:

$$\text{completions}(\mathbf{w}) = \{\mathbf{w}' \mid \mathbf{w}' \text{ is a word of English, and } \mathbf{w}' \text{ starts with } \mathbf{w}\}$$

## Attempt 1 [cont.]

- completions(**w**) is easily computed in Python.

```
1  def completions(word, wordlist):  
2      """Return set of all known completions for word."""  
3      return {comp for comp in wordlist  
4              if comp.startswith(word)}
```

```
1  completions("testing", words.words())  
2  >>> {"testing", "testingly"}
```

# Evaluating attempt 1

- Is this a **good solution?**

Pro	Contra

```
1 completions("test", words.words())
2 >>> {"test", "testa", "testable", "testacean", ...}
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# Improving attempt 1

- We can limit the number of suggestions, if we use a **list** instead of a **set**.

```
1  def completions(word, wordlist):
2      """Return list of all known completions for word."""
3      return [comp for comp in wordlist
4              if comp.startswith(word)]
5
6  completions("test", words.words())[:3]
7  >>> ["test", "testa", "testable"]
```

- But this still includes unlikely completions like *testa*.
- We need **probabilities**!

# Probability = frequency (?)

- ▶ We only want to show the **most likely completions**.
- ▶ But what is most likely?
- ▶ **Naive proposal:** the most frequent word!

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- ▶ **Naive proposal:** the most frequent word!

Um, but how do we figure out what is most common?

# How to find common words

- ▶ **Task:** determine which words are common
- ▶ **Solution:**
  - 1 Collect sufficiently large sample of texts
  - 2 For each word (**type**), count how often it occurs in the entire sample (= its number of **tokens**).
  - 3 Calculate the **frequency** of the word in the sample:

$$\text{freq}(\text{word}, \text{sample}) = \frac{\text{number of tokens of word}}{\text{word length of whole sample}}$$

## Types vs tokens

We have to distinguish **word types** (*a, the, Mary, red, ...*) from their **word tokens**, which are the instances of a specific word type. For instance, the type “word” has 4 tokens in this box.

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# Example calculation

**Sample:** 1000 words long

**Words:** be, bed, bee, bell

Type	be	bed	bee	bell
Tokens	13	2	0	3

$$\text{freq}(\text{be}) = \frac{13}{1000} = 1.3\%$$

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Ordered completions for *be*:



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# Types of corpora

- **Corpus** = large, structured collections of texts
  - mono-/multilingual just one language, or many?
  - annotated not just text, but additional annotations (e.g. tags for part of speech, syntax trees)

## Some common corpora in Python's NLTK

- Brown 1 million words, tagged, 500 samples across 15 genres (fiction, news paper, ...)
- Gutenberg 1.8 million words, 18 classic texts of fiction
- Penn 40k words, tagged and parsed
- Reuters 1.3 million words, news documents
- Switchboard 36 phone calls, fully transcribed and parsed
- Wordlist 960k words (no repetitions) and 20k affixes for 8 languages

# Getting probabilities from the corpus

```
1  from nltk.corpus import brown
2  from collections import Counter
3
4  # load Brown corpus as sequence of words
5  brown_text = brown.words()
6  # total number of words = length of text
7  total = len(brown_text)
8  # calculate counts
9  brown_counts = Counter(brown_text)
10 # convert counts to frequencies
11 for word in brown_counts:
12     brown_counts[word] /= total
```

- Alright, we have frequencies for each word. Now what?

# Ordering completions by frequency

- For a good user experience, completions should appear in **descending order of probability**.

```
1 def completions(word, counts):
2     """Return set of all known completions for word.
3
4     The completions are sorted by frequency,
5     in descending order.
6     """
7     comps = [comp for comp in counts
8                if comp.startswith(word)]
9     return sorted(comps,
10                   key=counts.get,
11                   reverse=True)
```

```
1 completions("test", words.words(), brown_counts)
2 >>> ["test", "testimony", "tested", "testing", ...]
```

# Summary for revised attempt 1

- 1 **Needed resources:** corpus
- 2 Compute frequencies for all words in corpus
- 3 Look up possible completions for user input
- 4 Sort completions by their frequency

Great, we're done, right?! Not quite. . .



# Probability $\neq$ word frequency

- ▶ The probability of a word isn't fixed, it varies by **context**.

## Example

	<b>tested</b>	<b>testing</b>	<b>testimony</b>
<b>I have</b>	hi	low	mid
<b>I have been</b>	hi	hi	low
<b>I have the</b>	low	low	hi

- ▶ The frequency of words is not enough,  
we need frequencies of sequences of words  $\Rightarrow$  **n-grams**

# Defining n-grams

**n-gram** a contiguous sequence of n words

<b>n</b>	<b>Name</b>	<b>Example</b>
1	unigram	John
2	bigram	John to
3	trigram	John to be
4	4-gram	John to be in
5	5-gram	John to be in the

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**String**

John and Marie are not Bill and Sue

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# Frequencies for n-grams

Frequencies can be computed for n-grams, too.

## Example: Calculating Bigram Frequencies

- ▶ **String**

when buffalo buffalo buffalo buffalo buffalo

- ▶ **Bigram token list**

- ▶ **Bigram counts and frequencies**

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- ▶ **Bigram counts and frequencies**

- 1 when buffalo:  $1 \Rightarrow \frac{1}{6} = 16.7\%$
- 2 buffalo buffalo:  $5 \Rightarrow \frac{5}{6} = 83.3\%$



# Adapting the strategy

- 1 **Needed resources:** corpus
- 2 Convert corpus to list of n-gram tokens
- 3 Compute frequencies for all n-grams
- 4 Look up possible completions for user input
- 5 Look at previous  $n - 1$  words.
- 6 Sort completions by n-gram probability

## Example

### ► Trigram frequencies

bus is late	30%	train is late	15%
bus is lovely	25%	train is lovely	8%
bus is lazy	10%	train is lazy	2%

### ► Input

I will text you if the train is I

### ► Sorted completions

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# How it is done: The easy generalization step

```
1  def bigrams(text):
2      """Convert text to list of bigram tokens."""
3      return [text[n:n+2] for n in range(len(text) - 1)]
4
5
6  brown.words()[:5]
7  >>> ["The", "Fulton", "County", "Grand", "Jury"]
8  bigrams(brown.words())[:3]
9  >>> [["The", "Fulton"], ["Fulton", "County"],
10      ["County", "Grand"]]
```

```
1  brown_bigrams = bigrams(brown.words())
2  total = len(brown_bigrams)
3  brown_bicounts = Counter(brown_bigrams)
4  for bigram in brown_bicounts:
5      brown_bicounts[bigram] /= total
```

## How it is done: The trickier part

```
1 bigram_completions(word, previous_word, counts):
2     # set of all compatible bigrams
3     comps = [comp for comp in counts
4                 if comp[:-1] == previous_word and
5                     comp[-1].startswith(word)]
6     # sort the bigram completions
7     ordered_ngrams = sorted(comps,
8                             key=counts.get,
9                             reverse=True)
10    # only keep last word of each bigram
11    return [ngram[-1] for ngram in ordered_ngrams]
```

- ▶ We now use the local context to choose word completions.

## The n-Gram Hypothesis

One can reliably predict the next word based on the **preceding  $n - 1$  words**.

- ▶ The n-gram hypothesis is **not quite true**, though.

# Context matters a lot

- ▶ Words do not exist in a vacuum.

## Example

The word *hypothyroidism* is rarely heard or seen, unless you're an endocrinologist.

- ▶ Word choices depend greatly on genre, target audience, age of the speaker, and so on.

## Common fixes

- ▶ Use frequencies from the appropriate genre (**BUT:** must be able to reliably determine genre first)
- ▶ Learn directly from the use case (e.g. analyze all text messages on phone)



# Long-distance dependencies in language

- ▶ Word choice can be influenced by words that are very far away.

## Subject-verb agreement

- ▶ The key to the cabinet **is** on the table.
  - ▶ The keys to the cabinets **are** on the table.
  - ▶ The key to the cabinets **is/are** on the table.
  - ▶ The keys to the cabinet **is/are** on the table.
- 
- ▶ Psycholinguistic observation: humans get those “wrong” too
  - ▶ Potential fix: **larger n-grams**

# How long can n-grams be?

- ▶ It is tempting to move to longer and longer n-grams in order to handle long-distance dependencies.
- ▶ But this has **two problems**:
  - data sparsity longer n-grams require too much data
  - storage needs longer n-grams require lots of storage
- ▶ Data sparsity is much more severe than storage needs.

# Sparse data: A simple calculation

Words	bigrams	trigrams	5-grams	6-grams
10	100	1000	10,000	100,000
100	10,000	1,000,000	10,000,000,000	<b>1,000,000,000,000</b>
10,000	$10^8$	<b><math>10^{12}</math></b>	$10^{20}$	$10^{24}$
25,000	$6.3 \times 10^8$	$1.6 \times 10^{13}$	$9.7 \times 10^{21}$	$2.4 \times 10^{26}$

## Some comparison values

$4.3 \times 10^{17}$  number of seconds since the Big Bang

$5 \times 10^{22}$  number of stars in observable universe

$10^{24}$  milliliters of water in the Earth's oceans

$8.8 \times 10^{26}$  diameter of observable universe, in meters

$10^{80}$  number of atoms in observable universe

- **Conclusion:** with large  $n$ , most  $n$ -grams are **never encountered** in a corpus  $\Rightarrow$  frequency 0

## Things get worse: A more realistic estimate

- ▶ The Linux dictionary `american-english-insane` has 650,000 entries.
- ▶ This makes the numbers much worse.  
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$$116 \text{ octillion} \approx 10^{29}$$

$10^{29}$  is larger than the number of shotglasses it takes to drain the Earth's oceans over 2000 times.

# Trick 1: Stemming and lemmatization

- ▶ Removing inflectional markers reduces number of words
- ▶ Two solutions:
  - ▶ stemming is quick and dirty
  - ▶ lemmatization is accurate but complex

**stemming** cut off word ends that look like inflection

## Example

- ▶ cats  $\Rightarrow$  cat
- ▶ tasks  $\Rightarrow$  task (noun and verb)
- ▶ asking  $\Rightarrow$  ask
- ▶ meeting  $\Rightarrow$  meet (**noun and verb**)
- ▶ staging  $\Rightarrow$  stag

# Trick 1: Stemming and lemmatization [cont.]

lemmatization stemming with context information

## Example

- ▶ cats  $\Rightarrow$  cat
- ▶ tasks  $\Rightarrow$  task (noun and verb)
- ▶ asking  $\Rightarrow$  ask
- ▶ meeting  $\Rightarrow$  meet (**only verb**)
- ▶ staging  $\Rightarrow$  stag/stage

## Evaluation

- ▶ Stemming/lemmatization reduces the number of words.
- ▶ But we still have at least 10,000 words and thus  $10^{20}$  5-grams.



## Trick 2: POS tagging

- ▶ Every word has a part of speech (POS).
- ▶ If we know the POS of a word, we can use that for estimating probabilities.

### Example

- ▶ **User input:** an
- ▶ **Preceding words:** to
- ▶ **Completions:** an (Det), annoint (V)
- ▶ **Suggestion:** to annoint
- ▶ **Reasoning:** even though *to an* is more common than *to annoint*, *to V* is more common than *to Det*.

## Trick 3: Statistics

- ▶ **Backoff Method**

If an  $n$ -gram has frequency 0, use the frequency of the corresponding  $(n - 1)$ -gram.

- ▶ **Good-Turing Smoothing**

Change frequency from 0 to a very low value while lowering high frequency values.

### Evaluation

- ▶ These tricks solve the issue of  $n$ -grams with 0% frequency.
- ▶ But they do not solve the basic problem that large  $n$ -gram models are incredibly data hungry.

## Another problem: Storage

- ▶ While storage space is increasing with each year, you don't want to waste GB on storing n-gram frequencies.
- ▶ We want a storage solution that is
  - ▶ compact,
  - ▶ easy to expand,
  - ▶ **fast to search.**

# Searching through a list

List search is a much studied problem.

## Simplest Algorithm: Linear Search

- ▶ Start at beginning of list.
- ▶ Move from left to right until the wanted item has been found.
- ▶ If no match is found before end of list, item is not in list.

Searching for yogurt



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### Searching for yogurt



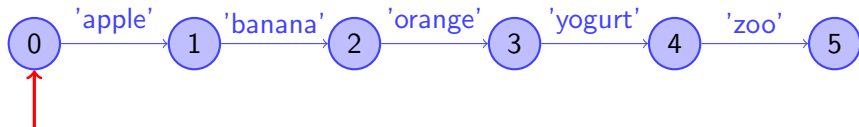
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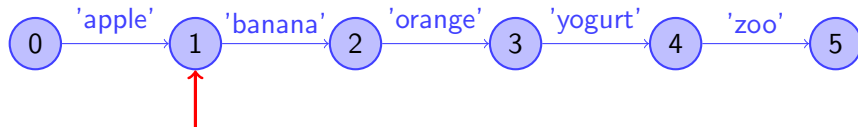
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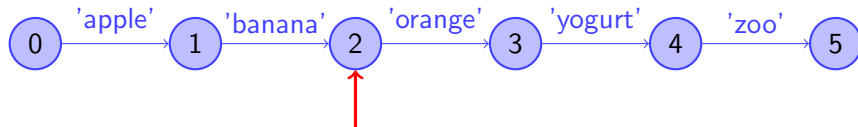
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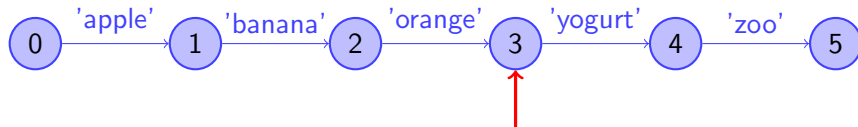
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# Evaluating linear search

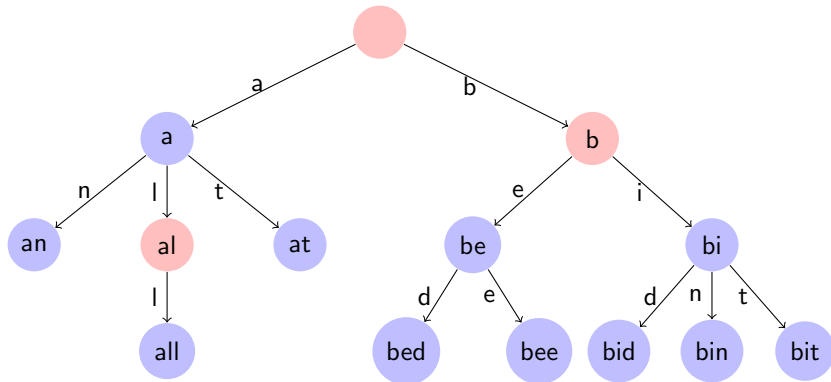
- ▶ Two criteria for evaluating algorithms: correctness and efficiency
- ▶ An algorithm is **correct** if and only if it is both sound and complete.
  - ▶ **sound** algorithm only returns correct solutions
  - ▶ **complete** algorithm can find all correct solutions
- ▶ Linear search is correct.
  - ▶ if item is not in list, linear search will not claim otherwise
  - ▶ if item is in list, linear search will find it
- ▶ But it is also slow.
  - ▶ In a list with  $n$  items, it may take  $n$  steps to find item.
  - ▶ And we have tons of n-grams!

# Improving on lists: Prefix trees/Tries

## Prefix Trees: The Basic Idea

Exploit the fact that many items share a common start

**Example: Prefix tree for word list**



# Searching through a prefix tree

**Query:** Is word  $w$  in our dictionary?

**Algorithm:** follow branches that spell  $w$ ; do we finish in accepting (= blue) node?

## Example

1 **Query:** bit

**Search Path:** b-i-t, blue  $\Rightarrow$  accept

2 **Query:** al

**Search Path:** al, red  $\Rightarrow$  reject

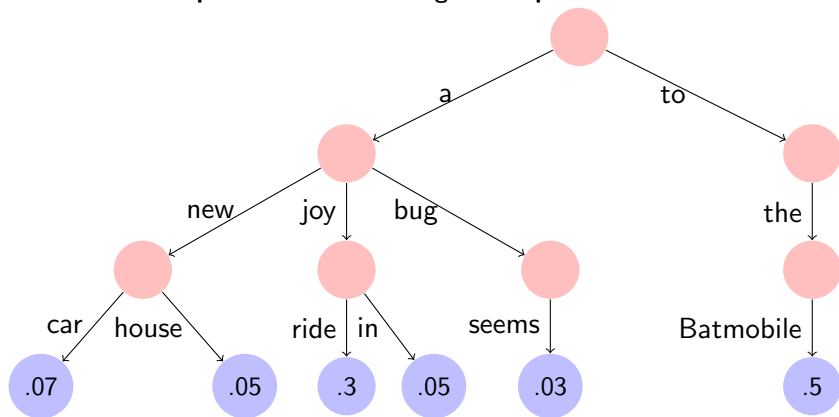
3 **Query:** bits

**Search Path:** b-i-t, stuck  $\Rightarrow$  reject

# Prefix tree for n-grams

- ▶ A prefix tree for a list of n-grams works exactly the same way, except that each arc is **labeled with a word** instead.

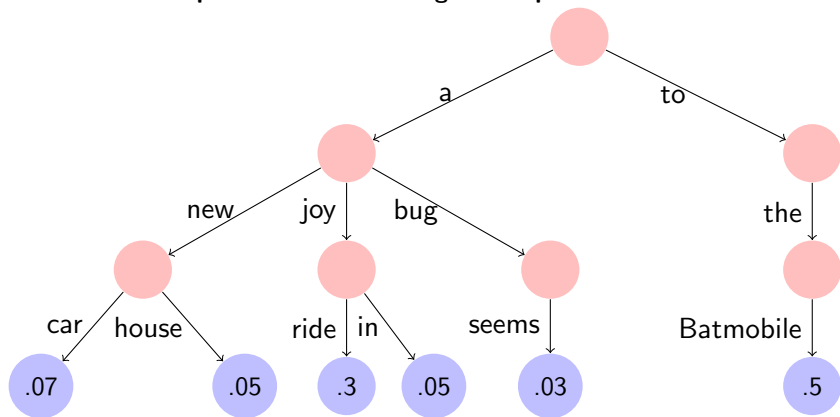
**Example: Prefix tree for trigram frequencies**



# A mixed prefix tree

- ▶ Prefix trees can store frequencies for all  $m < n$
- ▶ useful for backoff methods

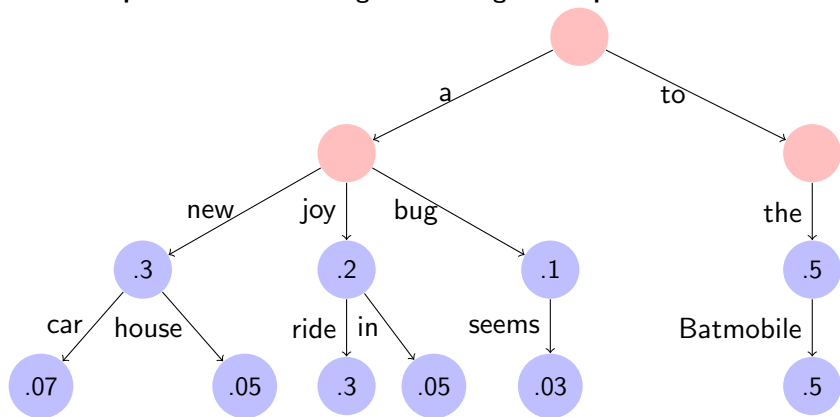
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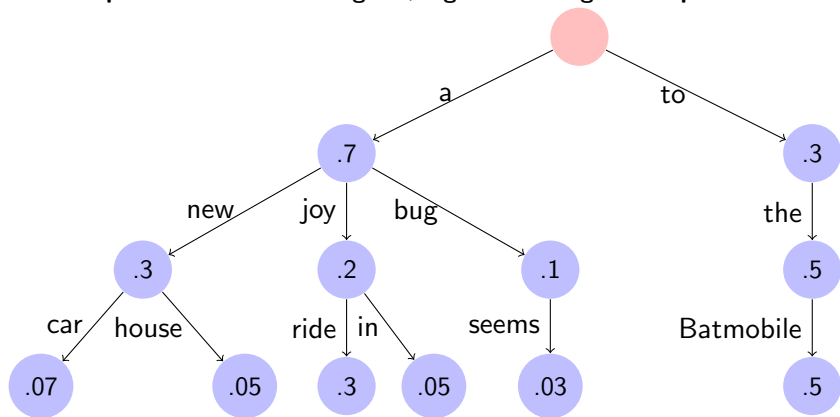
**Example: Prefix tree for bigram and trigram frequencies**



# A mixed prefix tree

- ▶ Prefix trees can store frequencies for all  $m < n$
- ▶ useful for backoff methods

**Example: Prefix tree for unigram, bigram and trigram frequencies**





## Excursus: It's the software, stupid!

- ▶ We usually think of technological progress in terms of faster hardware, more memory, and so on.
- ▶ A good **algorithm trumps hardware** improvements.

### Example

- ▶ Even the fastest current gen processor will take a long time to do linear search on a list with 18 quintillion items.
- ▶ With prefix trees it is almost instantaneous (and incremental!).
- ▶ They are also more memory efficient, as long as your items have lots of overlap.
- ▶ **BUT:** They are harder to implement.

## Yet another problem: bad input

- ▶ What if a user makes a mistake?

<b>Input</b>	<b>Intended?</b>
trian	train, trying, Brian, ...
your	your, you're
@rdvark	aardvark

- ▶ This requires a spellchecker.  
But more on that next time...

A good word completion model needs **lots of components**:

- ▶ corpora from various genres
- ▶ n-grams for limited context information
- ▶ sophisticated statistics to deal with sparse data
- ▶ a fast and compact data structure for storage
- ▶ extensions:
  - ▶ stemming/lemmatizer
  - ▶ POS tagging
  - ▶ spell checker
  - ▶ efficient storage

We have barely scratched the surface of any of those.

# New concepts

- ▶ corpora (common words, what types there are)
- ▶ n-grams (word = unigram)
- ▶ types VS tokens
- ▶ data sparsity
- ▶ smoothing and backoff
- ▶ stemming, lemmatization
- ▶ POS tagging

# New Python concepts

```
1  sorted(some_list,  
2         # sort in reverse?  
3         reverse=True,  
4         # what property to use for sorting  
5         key=some_function)  
6  
7  range(n)  # all numbers from 0 to n-1, in order  
8  
9  some_string.startswith(x)  # does some_string start with x?
```