Word Completion

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Word completion: a simple problem(?)

- When you write something on your phone, it automatically suggests words while you're typing them.
- Seems easy, but it's fairly intricate.

Key Insights/Skills

- transition probabilities with n-grams
- "More than 1, but less than 5."
- efficient data structures: tries/prefix trees

Attempt 1: simple lookup

 To make suggestions for completions, we only need an English/German/...dictionary.

```
# load English dictionary from nltk package
from nltk.corpus import words
# and see if "test" is in the list
"test" in words.words()
>>> True
```

Given word w, the set of possible completions for w consists of all listed words that start with w:

```
completions(\mathbf{w}) = \{w' \mid w' \text{ starts with } \mathbf{w}\}\
```

Attempt 1 [cont.]

1

► completions(w) is easily computed in Python.

def completions(word, wordlist):

>>> {"testing", "testingly"}

```
"""Return set of all known completions for word."""

return {comp for comp in wordlist

if comp.startswith(word)}

completions("testing", words.words())
```

Is this a good solution?

Pro Contra

```
completions("test", words.words())

"test", "testa", "testable", "testacean", ...}
```

Is this a good solution?

Pro	Contra
simple	

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simple	too many completions

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completions("test", words.words())

; "test", "testa", "testable", "testacean", ...}
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Is this a good solution?

Pro	Contra
simple	too many completions
	unlikely completions

```
completions("test", words.words())

; "test", "testa", "testable", "testacean", ...}
```

Improving attempt 1

► We can limit the number of suggestions, if we use a **list** instead of a **set**.

- But this still includes unlikely completions like testa.
- We need probabilities!

Probability = $\overline{Frequency}$ (?)

- We only want to show the most likely completions.
- But what is most likely?
- ▶ Naive proposal: the most frequent word!

Probability = Frequency (?)

- We only want to show the most likely completions.
- But what is most likely?
- ▶ Naive proposal: the most frequent word!

Um, but how do we figure out what is most common?

How to find common words

- ► Task: determine which words are common
- Solution:
 - Collect sufficiently large sample of texts
 - 2 For each word (type), count how often it occurs in the entire sample (= its number of tokens).
 - 3 Calculate the **frequency** of the word in the sample:

$$freq(\textit{word}, \textit{sample}) = \frac{\text{number of tokens of } \textit{word}}{\text{word length of whole } \textit{sample}}$$

Types vs tokens

We have to distinguish **word types** (a, the, Mary, red, ...) from their **word tokens**, which are the instances of a specific word type. For instance, the type "word" has 4 tokens in this box.

How to find common words

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$$freq(word, sample) = \frac{number of tokens of word}{word length of whole sample}$$

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Sample: 1000 words long

Words: be, bed, bee, bell

Type be bed bee bell Tokens 13 2 0 3

$$freq(be) = \frac{13}{1000} = 1.3\%$$
 $freq(bee) = \frac{0}{1000} = 0.0\%$

$$treq(bee) = \frac{0}{1000} = 0.0\%$$

$${\sf freq}({\sf bed}) = \frac{{\color{red}2}}{1000} = 0.2\% \qquad {\sf freq}({\sf bell}) = \frac{{\color{red}3}}{1000} = 0.3\%$$

$$freq(bell) = \frac{3}{1000} = 0.3\%$$

Sample: 1000 words long

Words: be, bed, bee, bell

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 = 1.3% freq(bee) = $\frac{0}{1000}$ = 0.0% freq(bed) = $\frac{2}{1000}$ = 0.2% freq(bell) = $\frac{3}{1000}$ = 0.3%

Ordered completions for be:

Sample: 1000 words long

Words: be, bed, bee, bell

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7 1000

Ordered completions for be: be

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Types of corpora

Corpus = large, structured collections of texts mono-/multilingual just one language, or many? annotated not just text, but additional annotations (e.g. tags for part of speech, syntax trees)

Some common corpora

```
Brown 1 million words, tagged, 500 samples across 15 genres (fiction, news paper, ...)

Gutenberg 1.8 million words, 18 classic texts of fiction
Penn 40k words, tagged and parsed
Reuters 1.3 million words, news documents

Switchboard 36 phone calls, fully transcribed and parsed
Wordlist 960k words (no repetitions) and 20k affixes for 8 languages
```

Getting probabilities from the corpus

```
from nltk.corpus import brown
from collections import Counter

# load Brown corpus as sequence of words
brown_text = brown.words()
# total number of words = length of text
total = len(brown_text)
# calculate counts
brown_counts = Counter(brown_text)
# convert counts to frequencies
for word in brown_counts:
brown_counts[word] = brown_counts[word]/total
```

Alright, we have frequencies for each word. Now what?

Ordering completions by frequency

► For a good user experience, completions should appear in descending order of probability.

```
completions("test", words.words(), brown_counts)
>>> ["test", "testimony", "tested", "testing", ...]
```

Summary for revised attempt 1

- Needed resources: corpus
- Compute frequencies for all words in corpus
- Look up possible completions for user input
- 4 Sort completions by their frequency

Great, we're done, right?! Not quite...

Probability \neq word frequency

► The probability of a word isn't fixed, it varies by **context**.

Example			
	tested	testing	testimony
I have	hi	low	mid
I have been	hi	hi	low
I have the	low	low	hi

► The frequency of words is not enough, we need frequencies of sequences of words ⇒ n-grams

n-gram a contiguous sequence of n words

n	Name	Example
1	unigram	John
2	bigram	John to
3	trigram	John to be
4	4-gram	John to be in
5	5-gram	John to be in the

Example

String

n-gram a contiguous sequence of n words

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Example
String
John and Marie are not Bill and Sue

n-gram a contiguous sequence of n words

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Frequencies can be computed for n-grams, too.

Example: Calculating Bigram Frequencies

- String
 when buffalo buffalo buffalo buffalo buffalo
- Bigram token list

Bigram counts and frequencies

Frequencies can be computed for n-grams, too.

- String
 when buffalo buffalo buffalo buffalo buffalo
- Bigram token list when buffallo.
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- String
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- ➤ Bigram token list when buffallo, buffalo buffalo, buffalo buffalo, buffalo buffalo, buffalo buffalo buffalo
- Bigram counts and frequencies
 - 1 when buffalo: $1 \Rightarrow \frac{1}{6} = 16.7\%$
 - 2 buffalo buffalo: $5 \Rightarrow \frac{5}{6} = 83.3\%$

- Needed resources: corpus
- Convert corpus to list of n-gram tokens
- Compute frequencies for all n-grams
- 4 Look up possible completions for user input
- **5** Look at previous n-1 words.
- 6 Sort completions by n-gram probability

Example

Trigram frequencies

bus is late	30%	train is late	15%
bus is lovely	25%	train is lovely	8%
bus is lazy	10%	train is lazy	2%

Input
I will text you if the train is I

Sorted completions

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Sorted completions late

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Sorted completions late, lovely

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Input
I will text you if the train is I

Sorted completions late, lovely, lazy

How it is done: The easy generalization step

```
def bigrams(text):
    """Convert text to list of bigram tokens."""
    return [text[n:n+2] for n in range(len(text) - 1)]

brown.words()[:5]

>>> ["The", "Fulton", "County", "Grand", "Jury"]

bigrams(brown.words())[:3]

>>> [["The", "Fulton"], ["Fulton", "County"],

["County", "Grand"]]
```

```
brown_bigrams = bigrams(brown.words())

total = len(brown_bigrams)

brown_bicounts = Counter(brown_bigrams)

for bigram in brown_bicounts:

brown_bicounts[bigram] = brown_bicounts[bigram]/total
```

How it is done: The trickier part

```
def bigram_completions(word, previous_word, counts):
2
             # set of all compatible bigrams
             comps = [comp for comp in counts
3
                      if comp[0] == previous_word and
4
                         comp[-1].startswith(word)]
5
             # sort the bigram completions
6
             ordered_ngrams = sorted(comps,
                                      key=lambda x: counts[x],
8
                                      reverse=True)
9
             # only keep second word of each bigram
10
             return [ngram[-1] for ngram in ordered_ngrams]
11
```

Linguistic evaluation

We now use the local context to choose word completions.

The n-Gram Hypothesis

One can reliably predict the next word based on the **preceding** n-1 words.

► The n-gram hypothesis is **not quite true**, though.

Context matters a lot

Words do not exist in a vacuum.

Example

The word *hypothyroidism* is rarely heard or seen, unless you're an endocrinologist.

Word choices depend greatly on genre, target audience, age of the speaker, and so on.

Common fixes

- Use frequencies from the appropriate genre (BUT: must be able to determine genre first)
- Learn directly from the use case (e.g. analyze all text messages on phone)

Long-distance dependencies in language

Word choice can be influenced by words that are very far away.

Subject-verb agreement

- ▶ The key to the cabinet **is** on the table.
- ► The keys to the cabinets **are** on the table.
- ► The key to the cabinets **is**/are on the table.
- ► The keys to the cabinet **is/are** on the table.
- ▶ Psycholinguistic observation: humans get those "wrong" too
- Potential fix: larger n-grams

How long can n-grams be?

- It is tempting to move to longer and longer n-grams in order to handle long-distance dependencies.
- ► But this has two problems: data sparsity longer n-grams require too much data storage longer n-grams require lots of storage
- Data sparsity is much more severe than storage.

Sparse data: A simple calculation

Words	bigrams	trigrams	5-grams	6-grams
10	100	1000	10,000	100,000
100	10,000	1,000,000	10,000,000,000	1,000,000,000,000
10,000	10^{8}	${f 10}^{12}$	10^{20}	10^{24}
25,000	6.3×10^{8}	$1.6 imes 10^{13}$	9.7×10^{21}	2.4×10^{26}

Some comparison values

```
4.3 \times 10^{17} number of seconds since the Big Bang 5 \times 10^{22} number of stars in observable universe 10^{24} milliliters of water in the Earth's oceans 8.8 \times 10^{26} diameter of observable universe, in meters 10^{80} number of atoms in observable universe
```

► Conclusion: with large n, most n-grams are never encountered

Things get worse: A more realistic estimate

- ► The Unix dictionary american-english-insane has 650,000 entries.
- ► This makes the numbers much worse. Can you guess how many 5-grams there are then?

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116 octillion $\approx 10^{29}$

Things get worse: A more realistic estimate

- ► The Unix dictionary american-english-insane has 650,000 entries.
- This makes the numbers much worse.
 Can you guess how many 5-grams there are then?

116 octillion $\approx 10^{29}$

 10^{29} is larger than the number of shotglasses it takes to drain the Earth's oceans over 2000 times.

Trick 1: Stemming and Lemmatization

- Removing inflectional markers reduces number of words
- Two solutions:
 - stemming is quick and dirty
 - lemmatization is accurate but complex

stemming cut off word ends that look like inflection

Example

- ▶ cats ⇒ cat
- ▶ tasks ⇒ task (noun and verb)
- ▶ asking ⇒ ask
- ▶ meeting ⇒ meet (noun and verb)
- ▶ staging ⇒ stag

Trick 1: Stemming and Lemmatization [cont.]

lemmatization stemming with context information

Example

- ightharpoonup cats \Rightarrow cat
- ▶ tasks ⇒ task (noun and verb)
- ▶ asking ⇒ ask
- ▶ meeting ⇒ meet (only verb)
- ▶ staging ⇒ stag/stage

Evaluation

- Stemming/lemmatization reduces the number of words.
- \blacktriangleright But we still have at least 10,000 words and thus 10^{20} 5-grams.

Trick 2: Statistics

- ▶ Backoff Method If an n-gram has frequency 0, use the frequency of the corresponding (n-1)-gram.
- ► Good-Turing Smoothing Change frequency from 0 to a very low value while lowering high frequency values.

Evaluation

- ► These tricks solve the issue of n-grams with 0% frequency.
- But they do not solve the basic problem that large n-gram models are incredibly data hungry.

Another problem: storage

Summary

A good word completion model needs a lot of components:

- corpora from various genres
- n-grams for limited context information
- sophisticated statistics to deal with sparse data
- a fast and compact data structure for storage
- extensions: stemming/lemmatizer

We have barely scratched the surface of any of those.

New concepts

- corpora (common words, what types there are)
- n-grams (word = unigram)
- ▶ types VS tokens
- data sparsity
- smoothing and backoff
- stemming, tagging

New Python concepts

```
# New Python tricks
        sorted(some_list,
3
                # reverse order
4
               reverse=True,
                # what property to use for sorting
5
               key=lambda x: something_with_x)
6
7
        range(n) # all numbers from 0 to n-1
8
9
        some_string.startwith(x) # does some_string start with x?
10
```