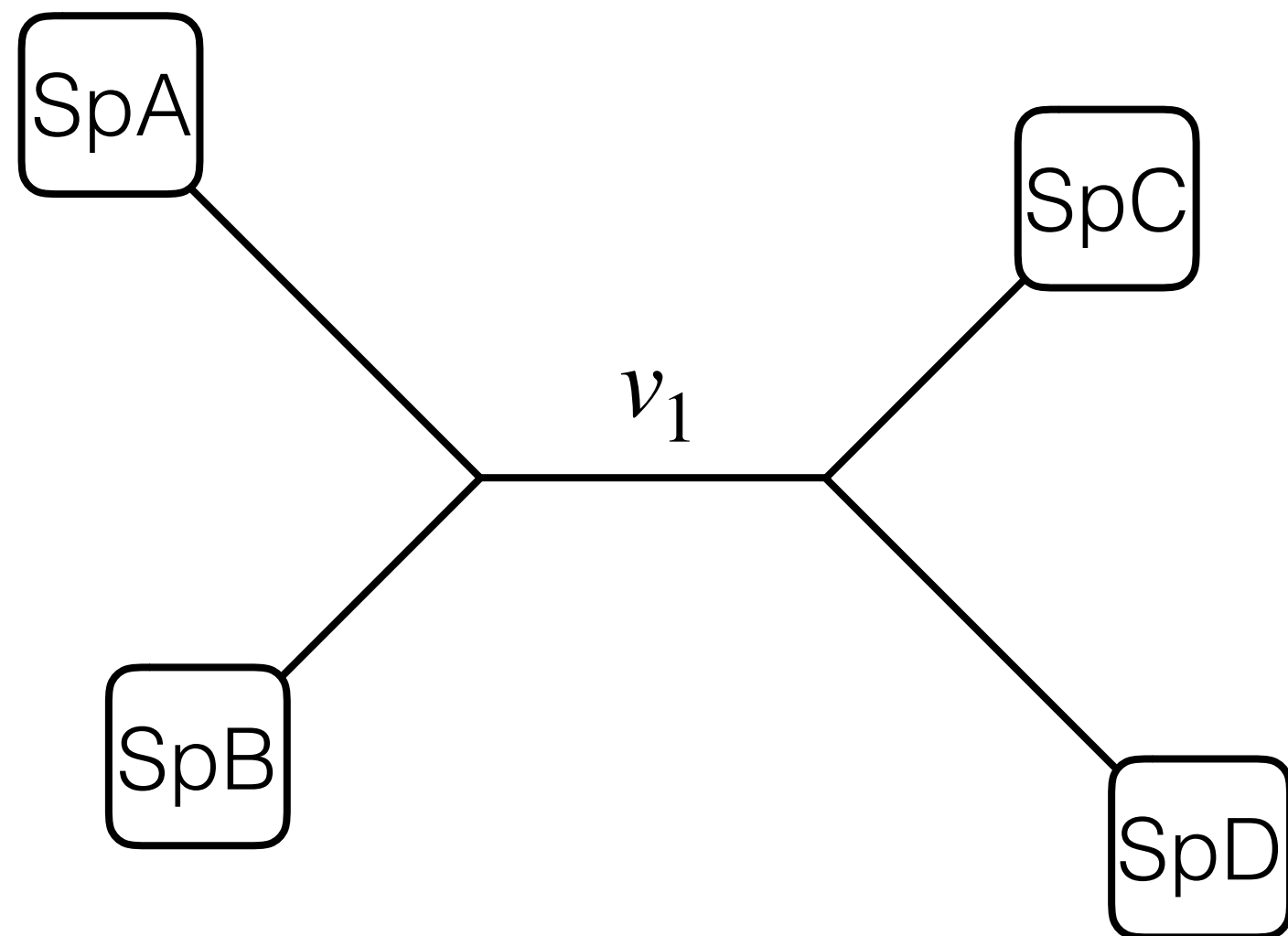


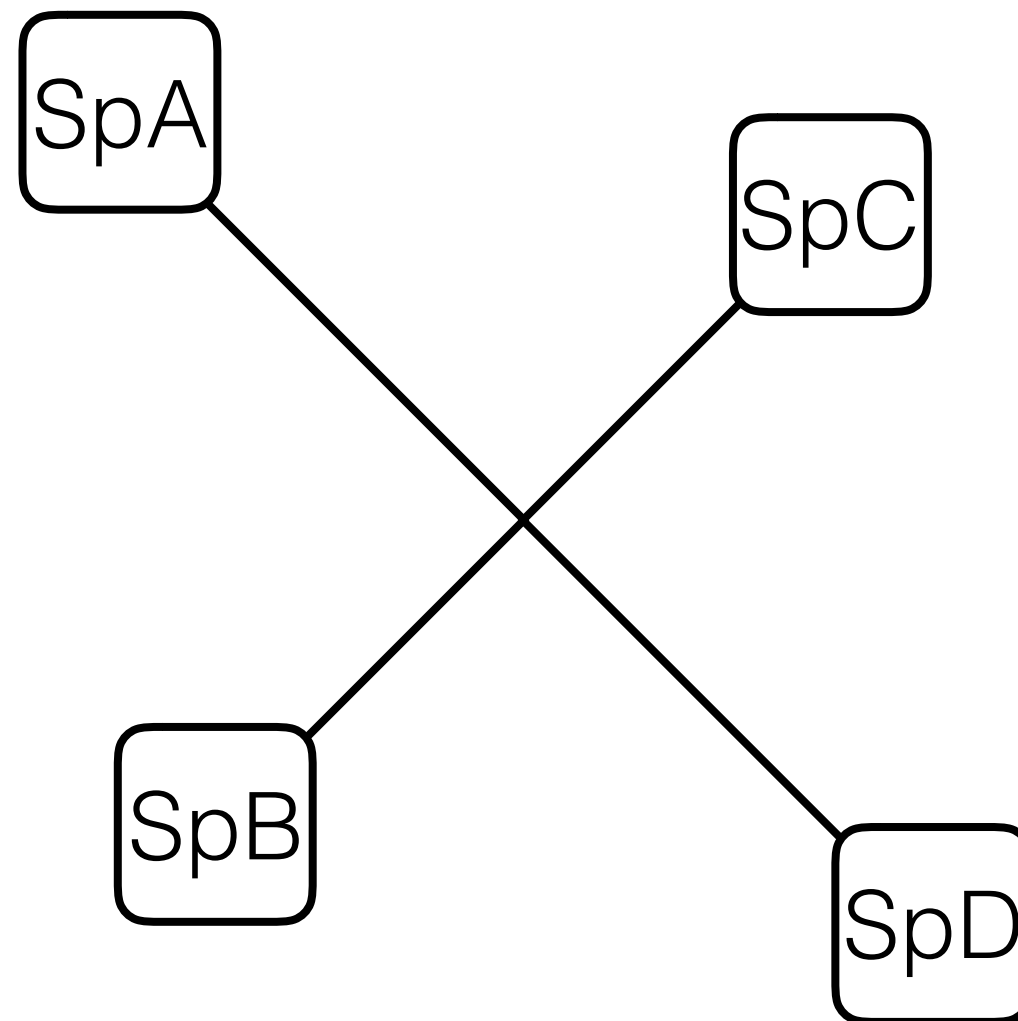
Testing Topological Hypotheses

Interior Branch Test



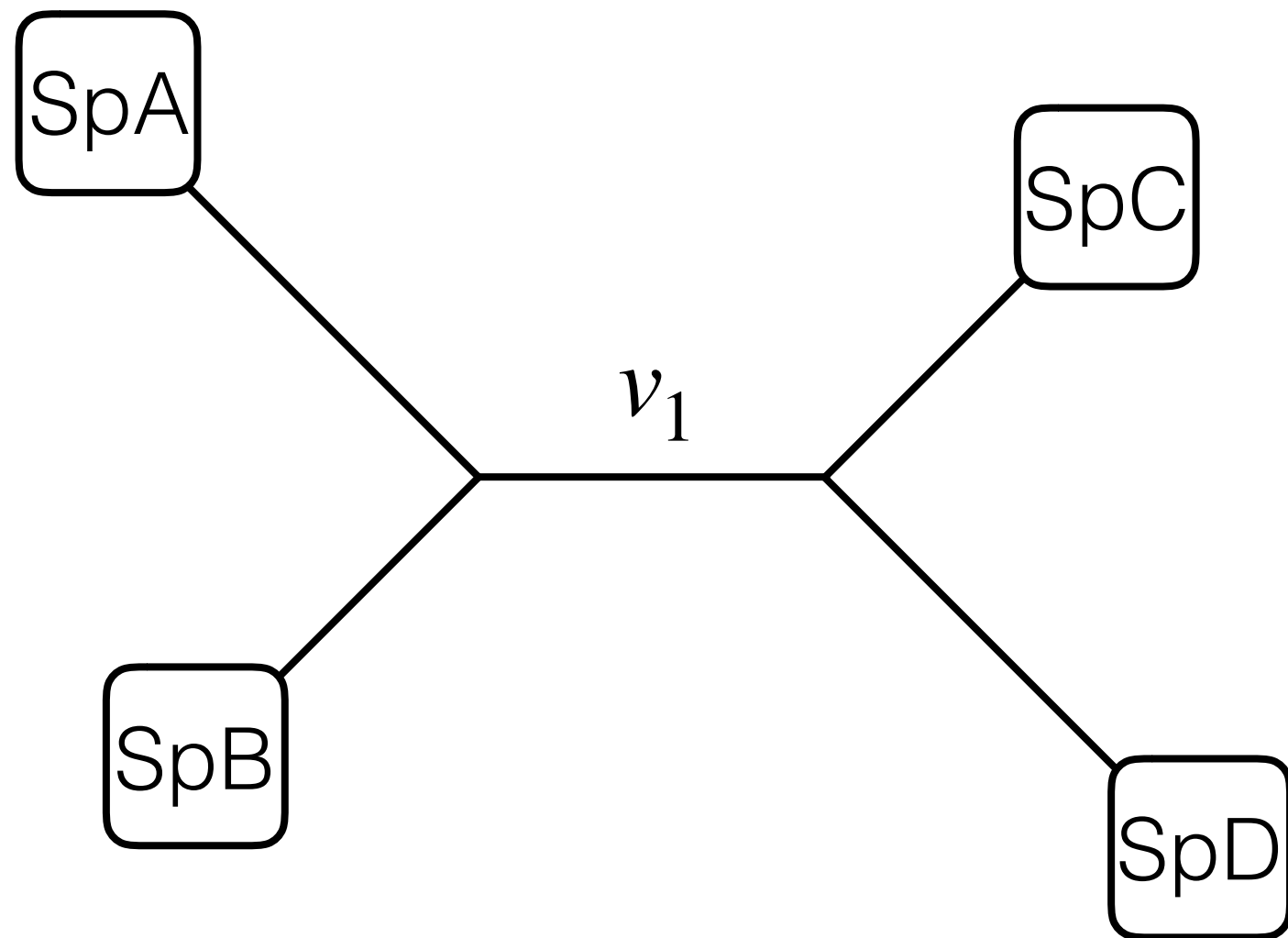
Interior Branch Test

H_0 : The length of this branch is 0
(effectively, it does not exist).



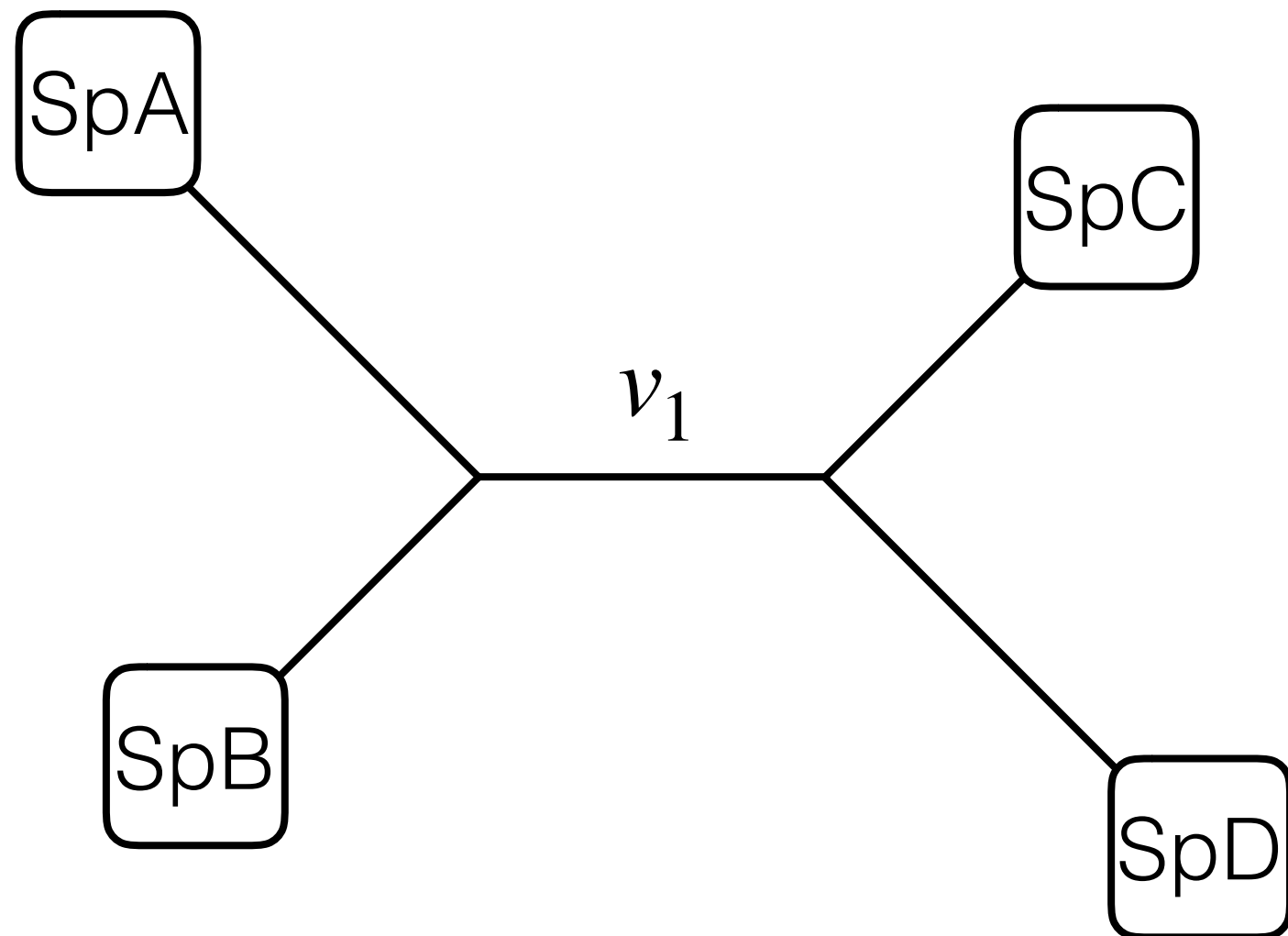
Interior Branch Test

H_1 : The length of this branch is > 0 .



Interior Branch Test

H_0 and H_1 are nested, so we can use an LRT.

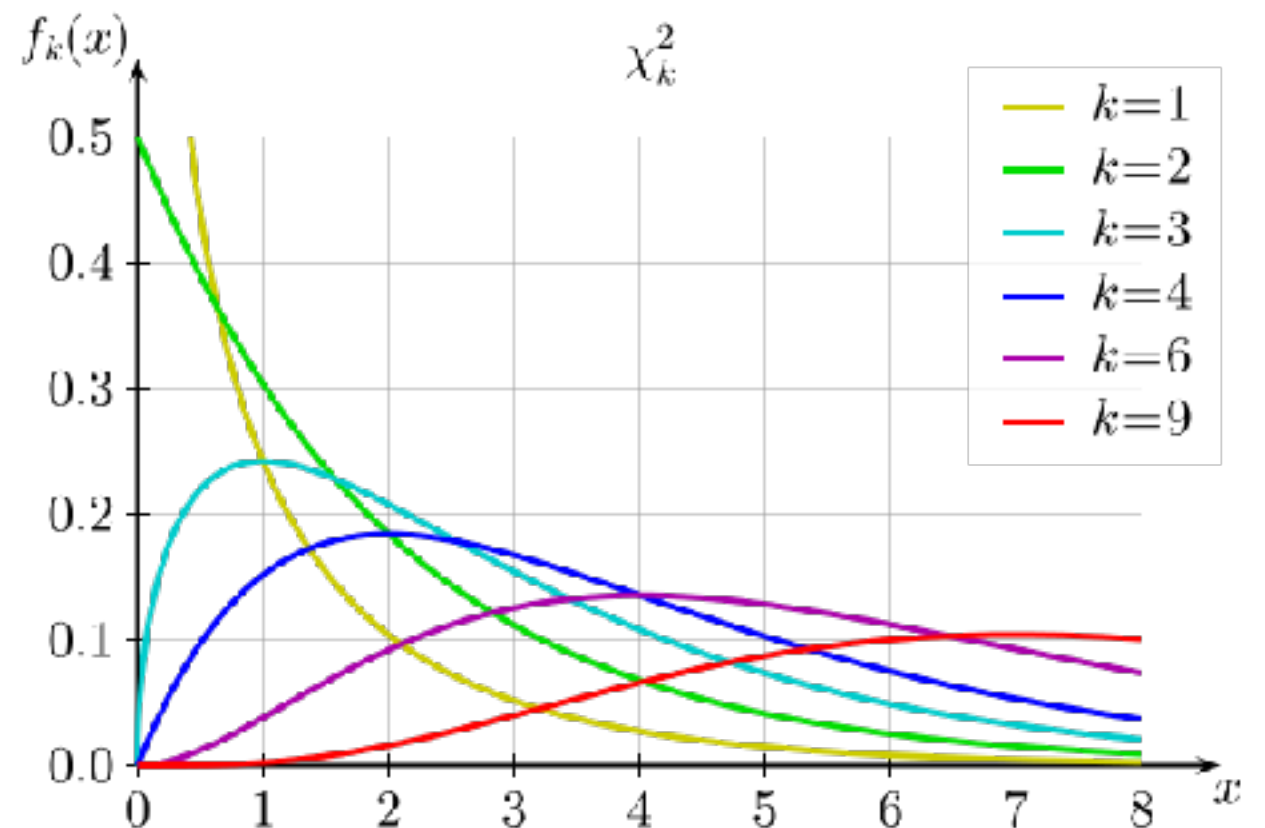


Interior Branch Test

H_0 and H_1 are nested, so we can use an LRT.

$$LR = \frac{\mathcal{L}(v_1 = 0)}{\mathcal{L}(v_1 > 0)}$$

Because the value of v_1 is at a boundary of parameter space, we should use a 50:50 mixture of χ_0^2 and χ_1^2 .



Interior Branch Test

Challenges and Drawbacks

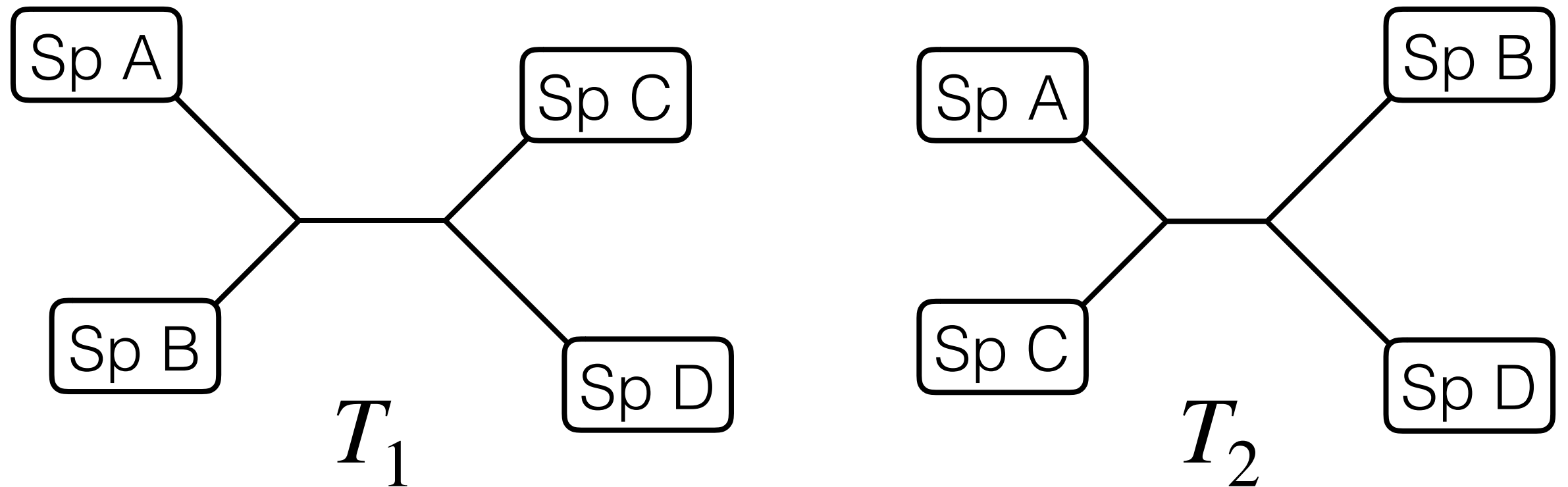
- Hypothesis not really specified *a priori* (only after inferring ML tree)
- Multiple tests if applied to all branches
- Not clear that H_0 is actually correct/useful.
Branch lengths may have expectations > 0 even for incorrect trees.

Interior Branch Test

Challenges and Drawbacks

- Hypothesis testing after
 - Multiple comparisons
 - No Branch even for
- Not really used in empirical studies.

K-H Test



Test Statistic

$$\Delta = \ln(\mathcal{L}_1) - \ln(\mathcal{L}_2)$$

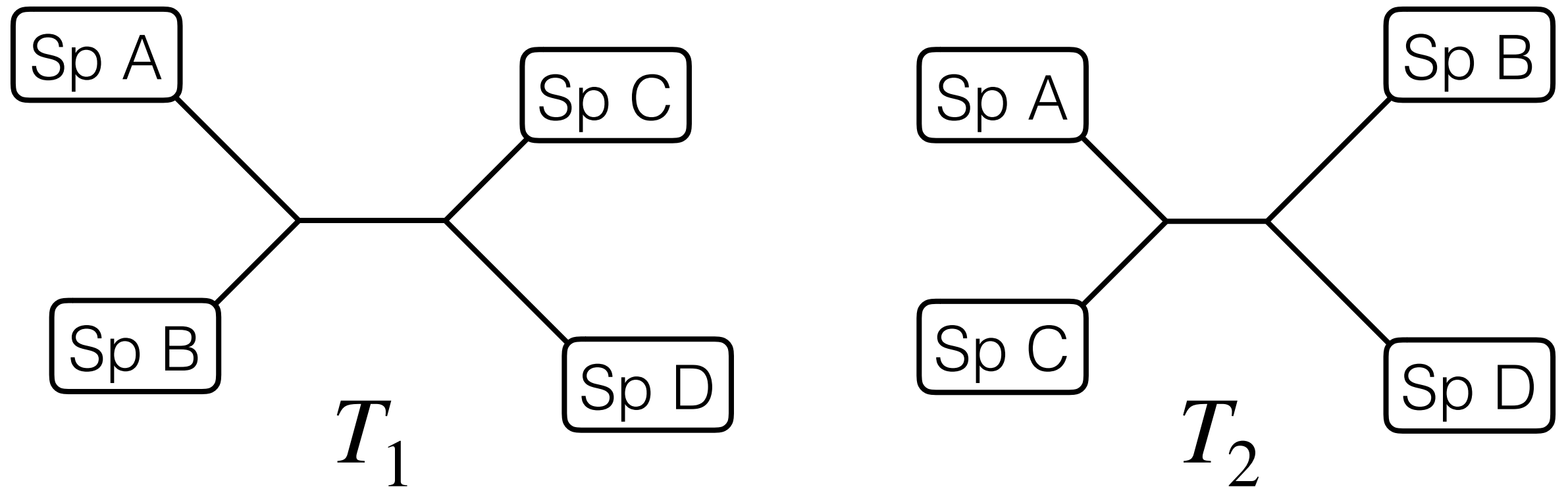
K-H Test

$$\Delta = \ln(\mathcal{L}_1) - \ln(\mathcal{L}_2)$$

The Intuitive Approach (*priNPfcd*)

1. Bootstrap data
2. Reoptimize and recalculate likelihood differences
3. After all bootstraps, take mean of differences and center distribution, so avg. difference is 0 (H_0).
4. Compare observed difference to centered, bootstrap distribution.

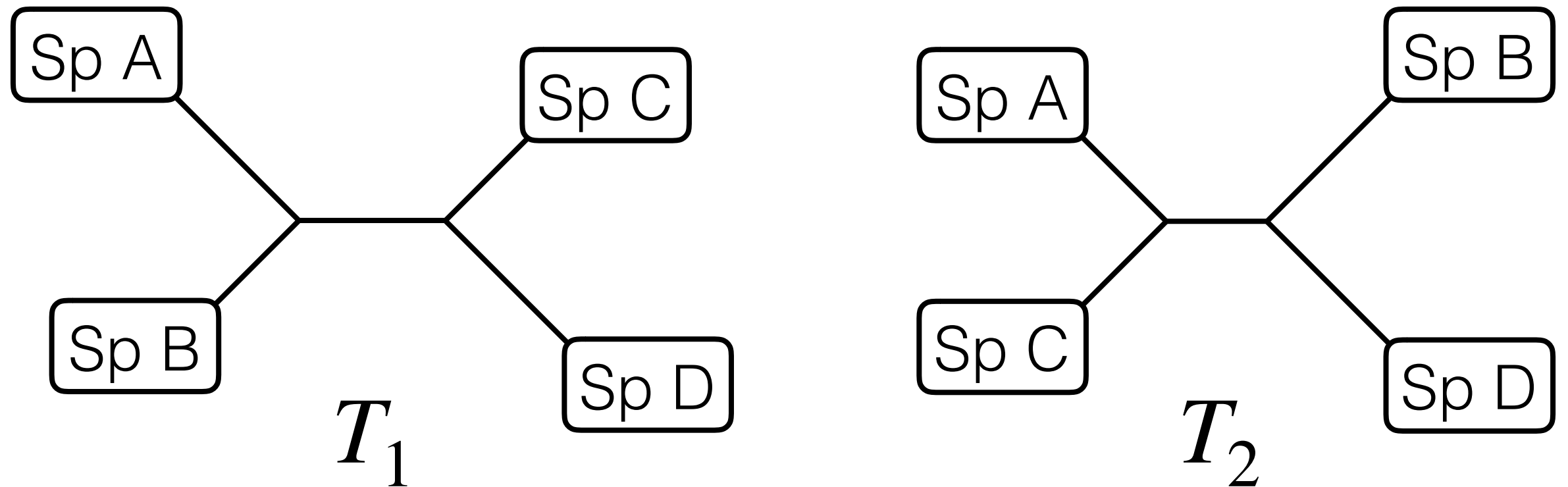
K-H Test



A Faster Approach (*priNPnca*)

This is the one described in Yang's book.

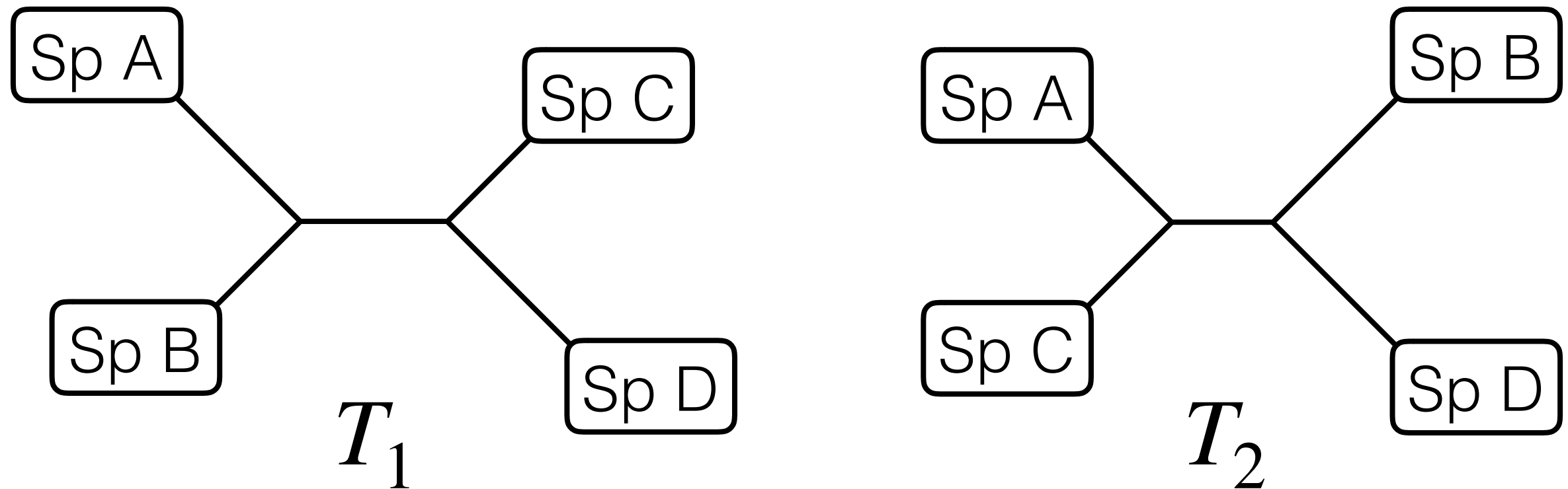
K-H Test



$$\ln(\mathcal{L}_1) = \sum_{h=1}^n \ln P(\mathbf{x}_h | \hat{\theta}_1)$$

Site Likelihoods

K-H Test

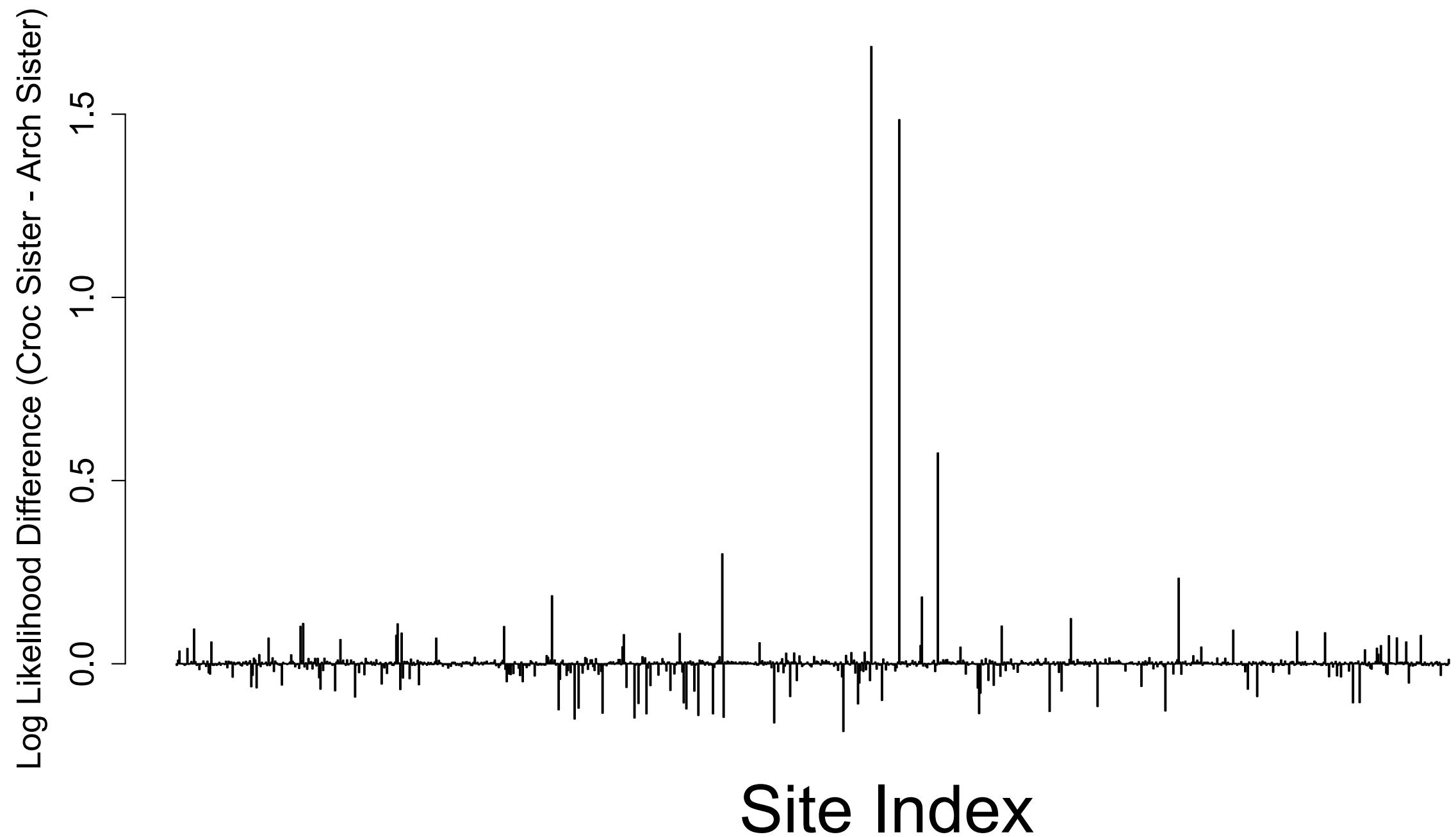


$$d_h = \ln P(\mathbf{x}_h | \hat{\theta}_1) - \ln P(\mathbf{x}_h | \hat{\theta}_2)$$

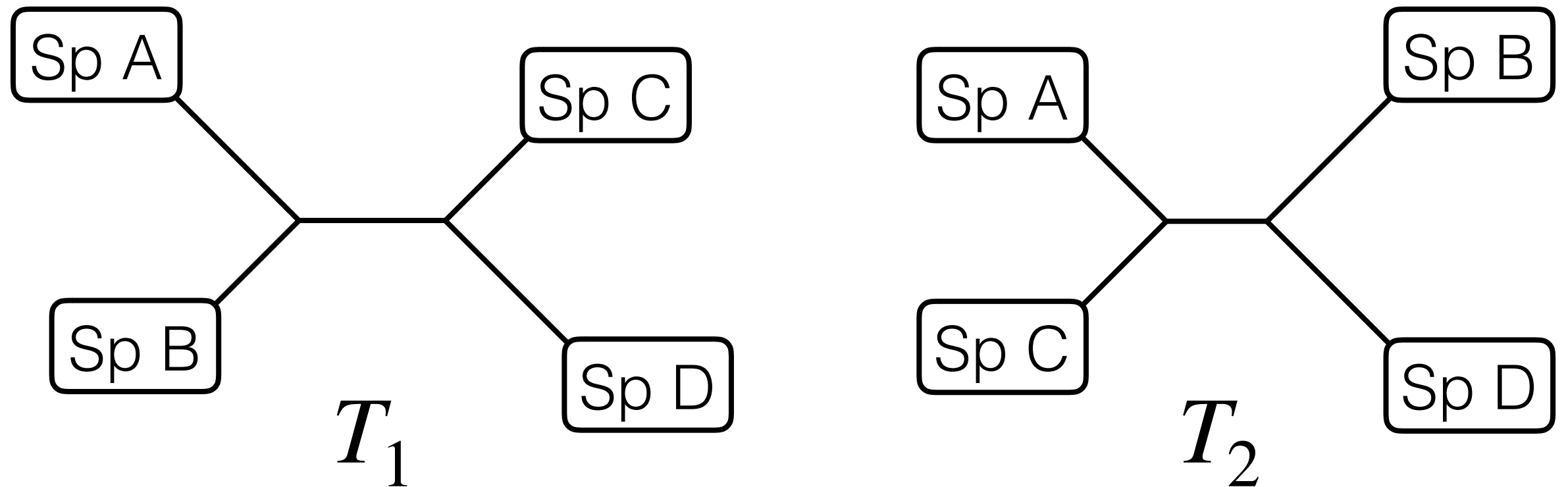
These can be used to estimate
expected variance of Δ
(with some assumptions)

$$\longrightarrow \bar{d} = \frac{\Delta}{n}$$

Site Likelihood Example



K-H Test

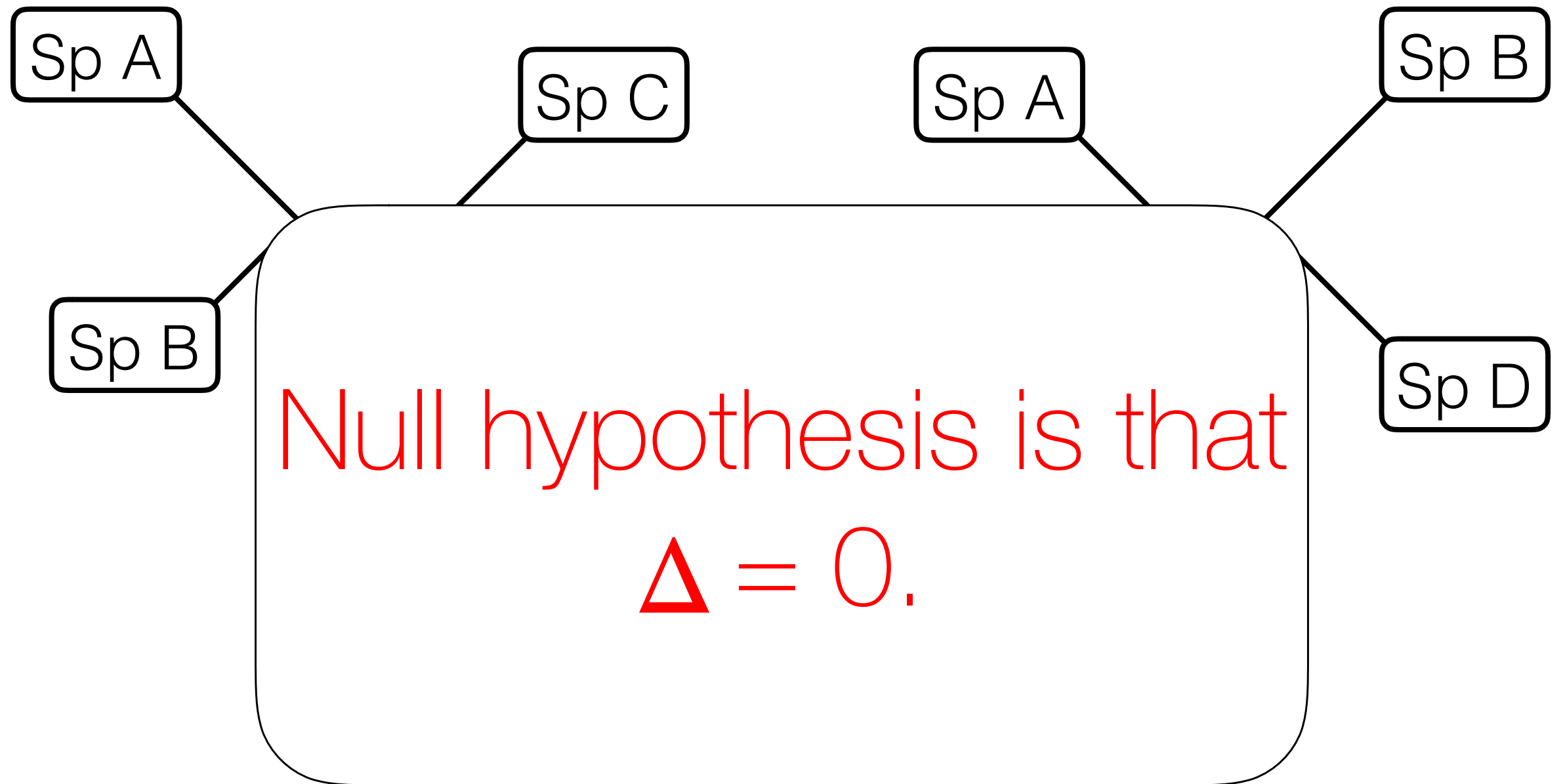


$$var(\Delta) = \frac{n}{n-1} \sum_{h=1}^n (d_h - \bar{d})^2$$

Reject T_2 if Δ is $> [var(\Delta)]^{1/2}$

prINPnca from Goldman et al. (2000)

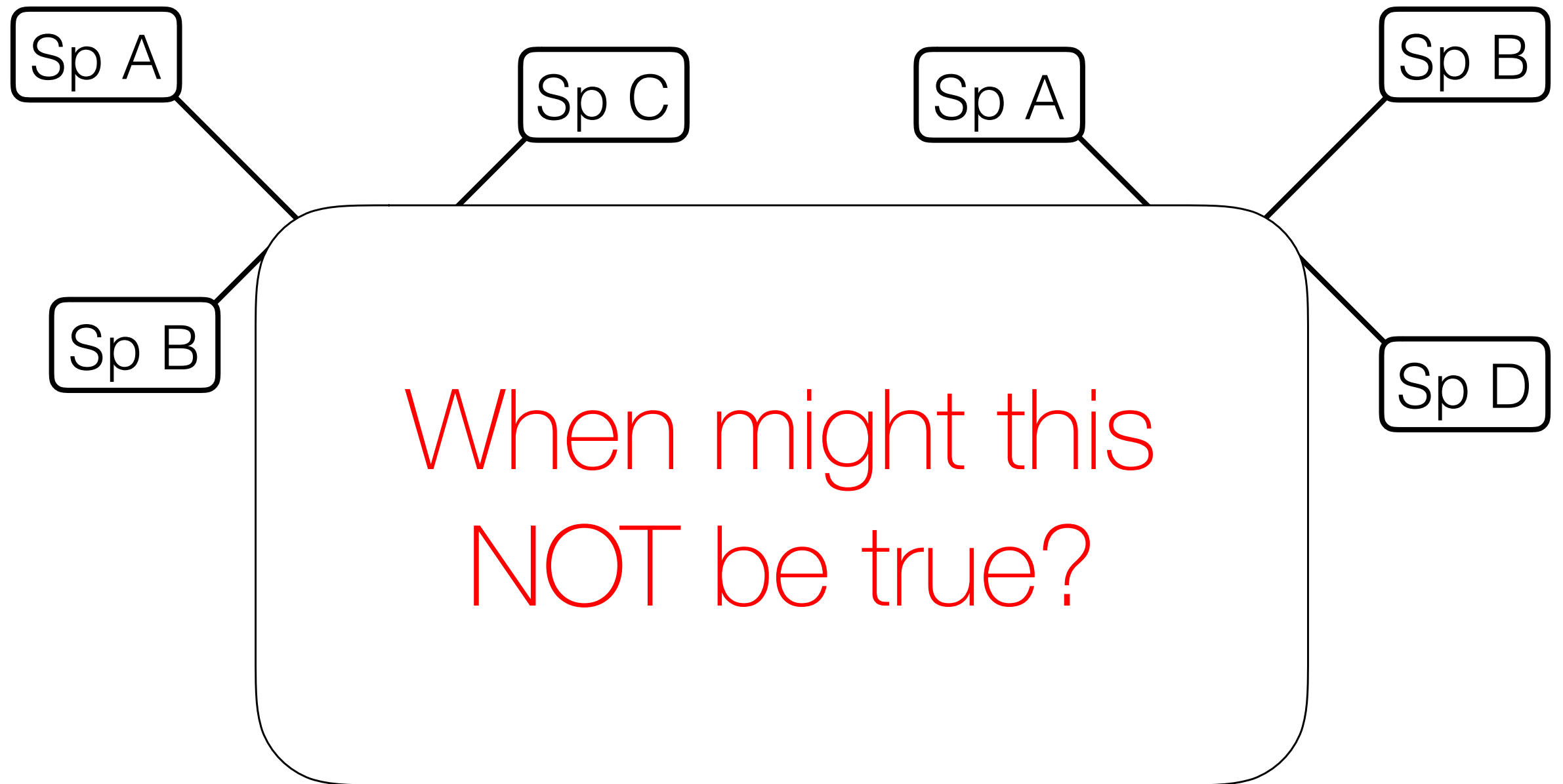
K-H Test



Reject T2 if Δ is $> [var(\Delta)]^{1/2}$

prINPnca from Goldman et al. (2000)

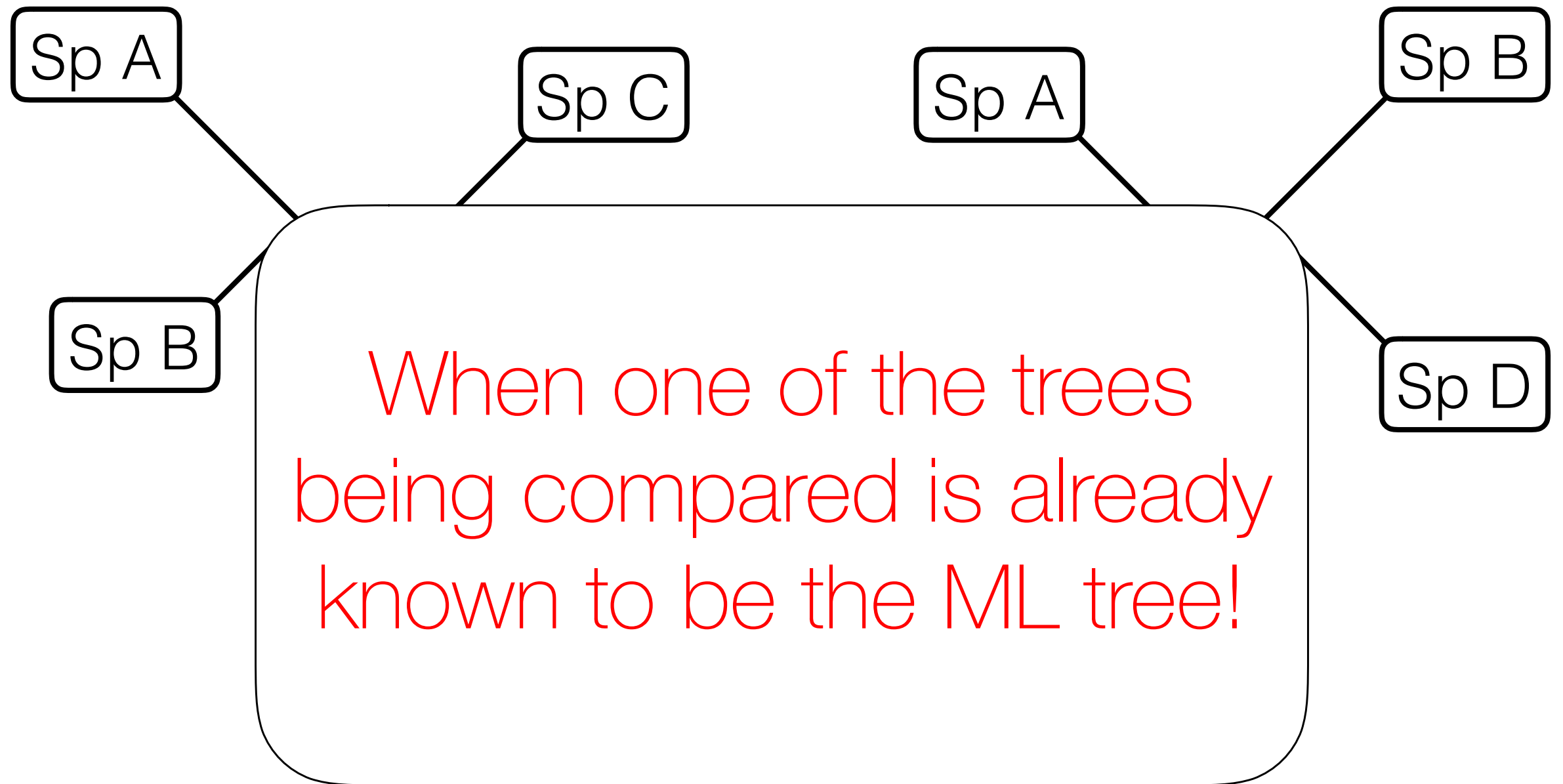
K-H Test



Reject T2 if Δ is $> [var(\Delta)]^{1/2}$

prINPnca from Goldman et al. (2000)

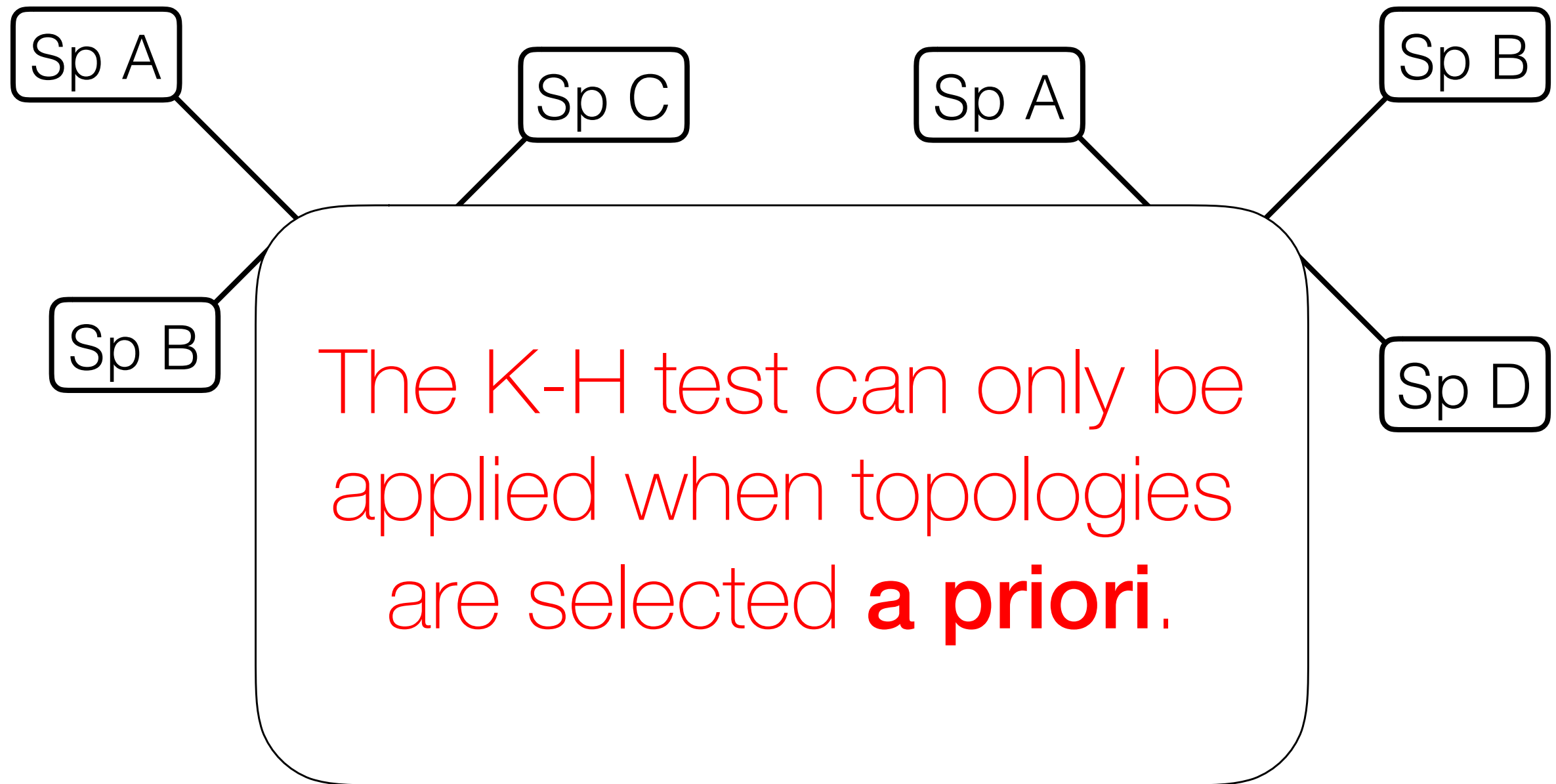
K-H Test



Reject T2 if Δ is $> [var(\Delta)]^{1/2}$

prINPnca from Goldman et al. (2000)

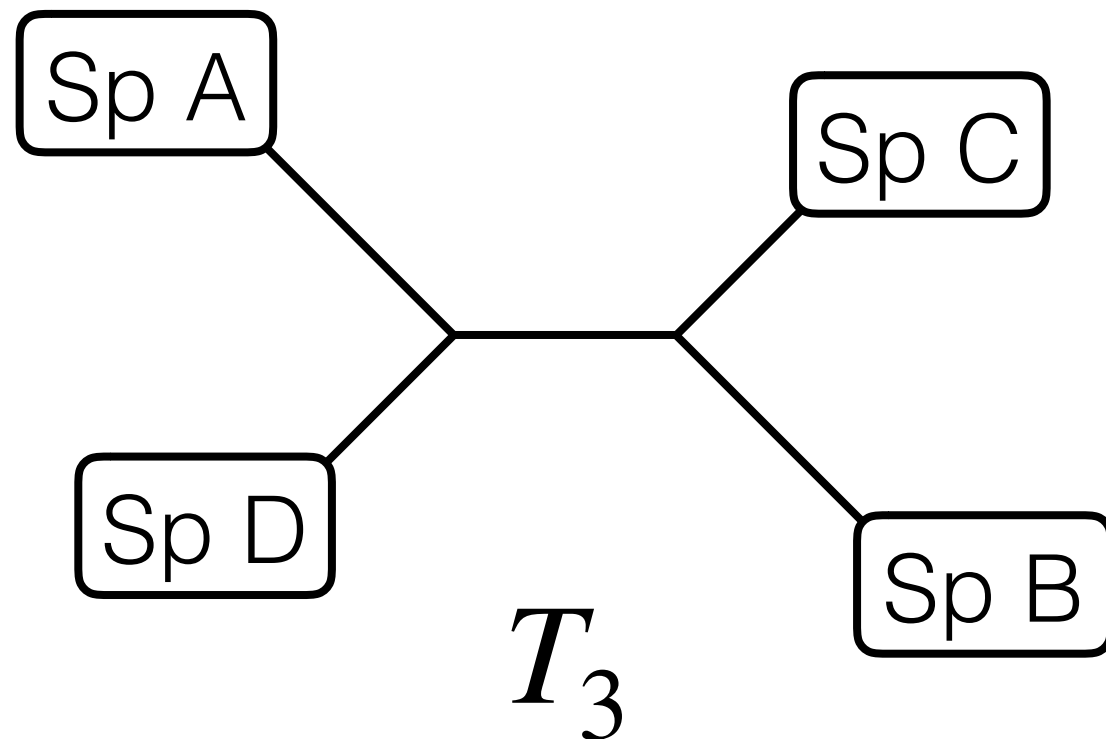
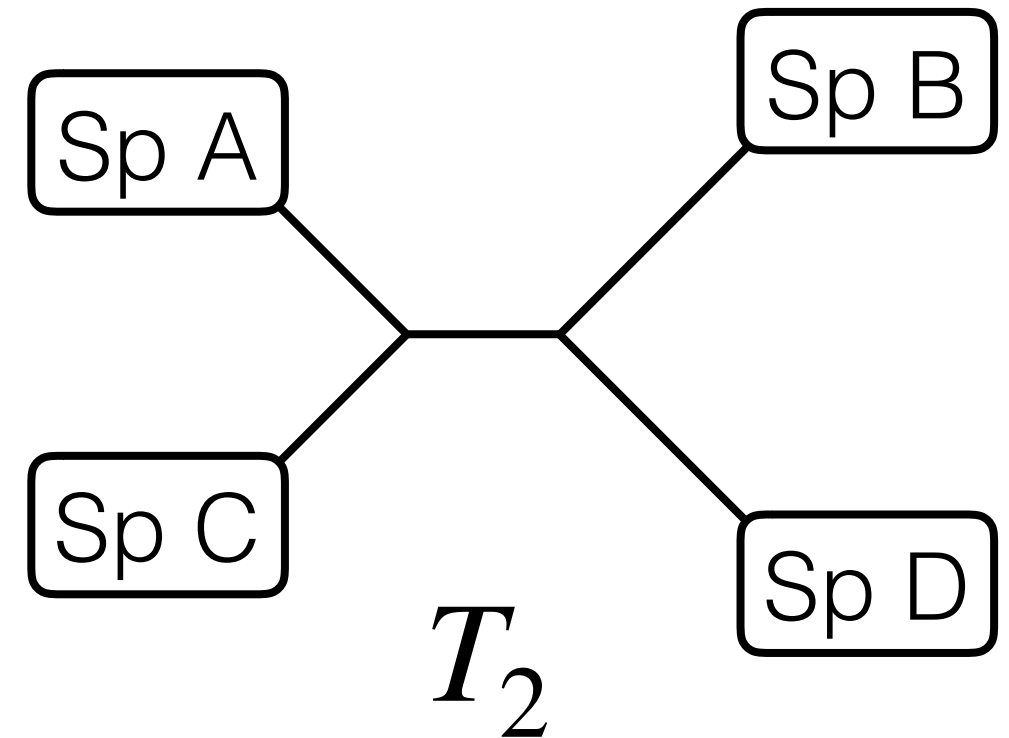
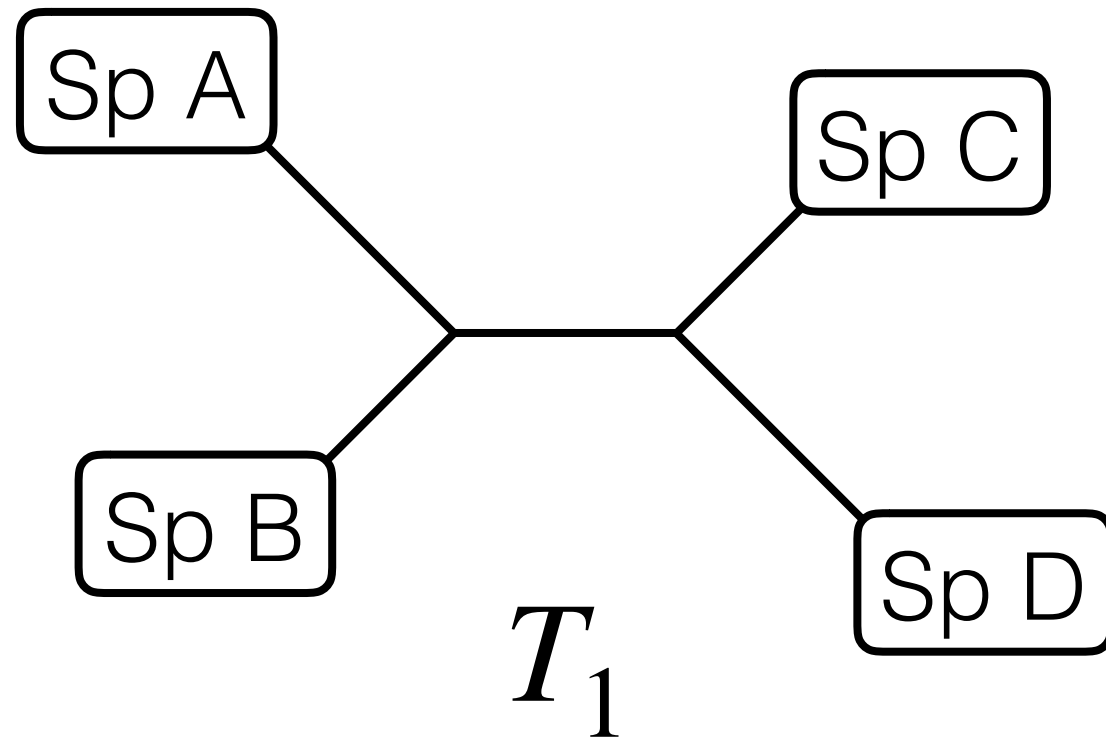
K-H Test



Reject T2 if Δ is $> [var(\Delta)]^{1/2}$

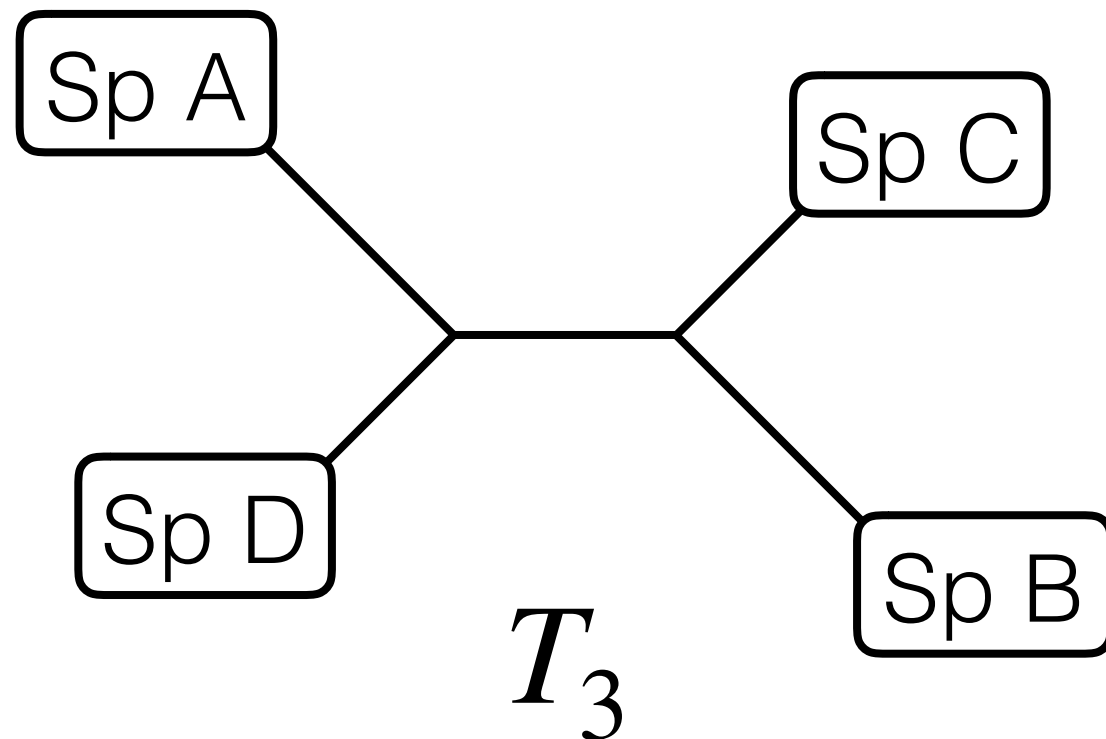
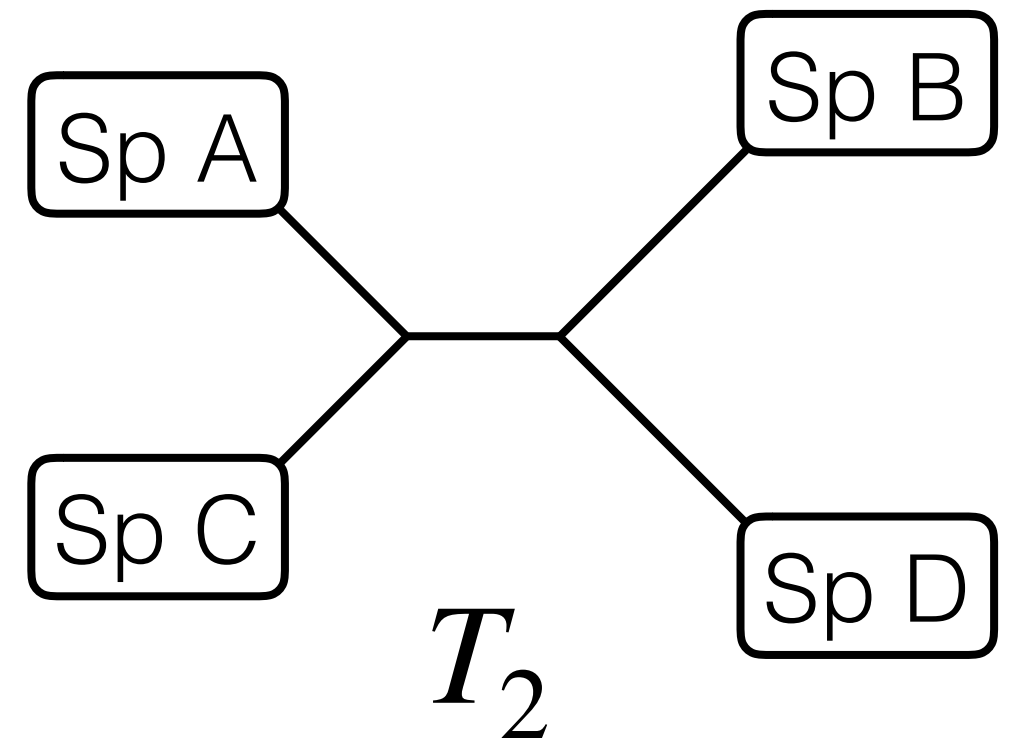
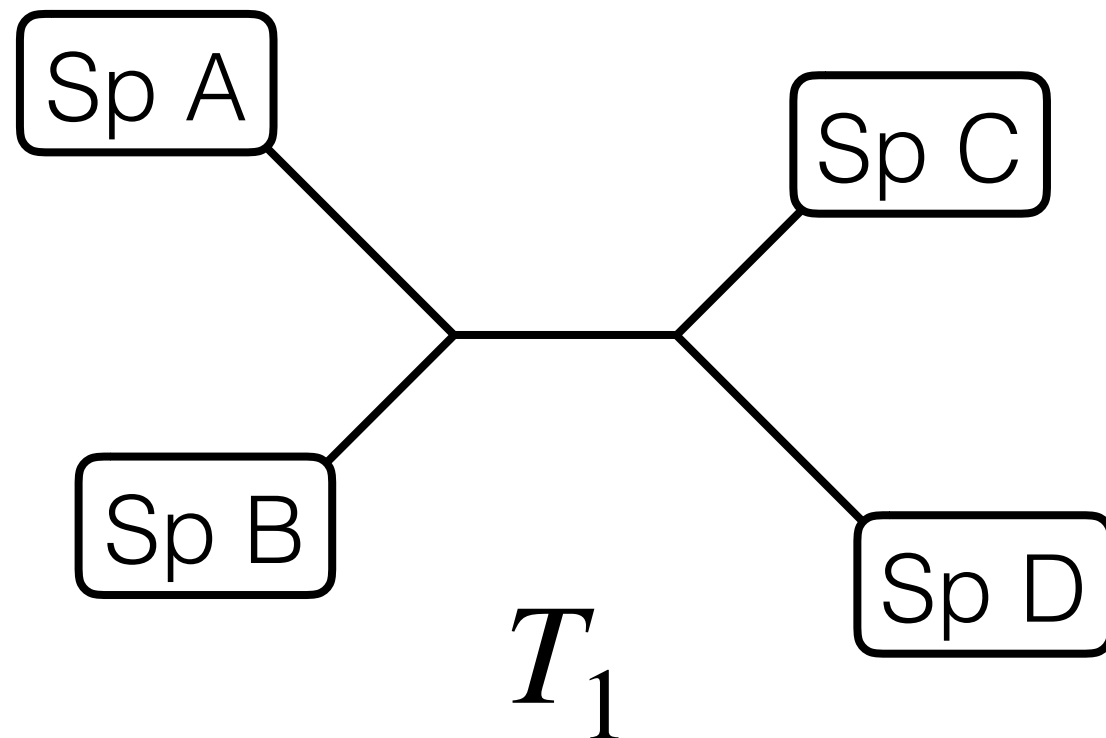
prINPnca from Goldman et al. (2000)

S-H Test



Start by considering all possible trees.
Or a set that MUST contain the true tree.
This set must be selected a priori.

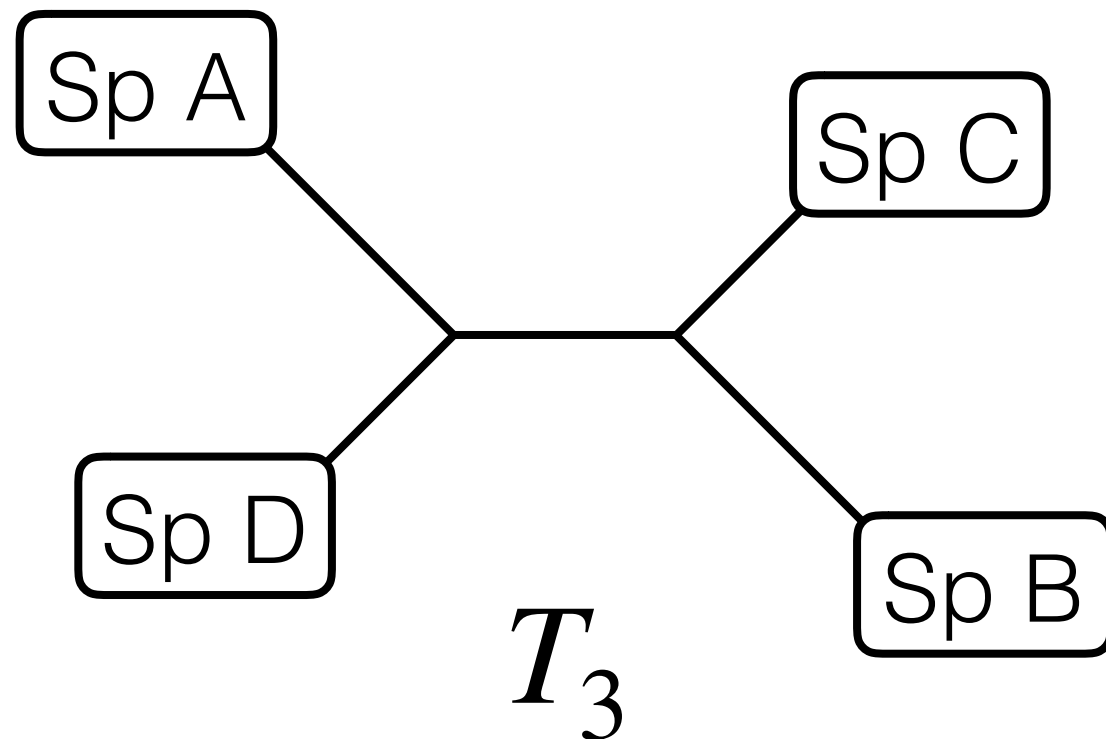
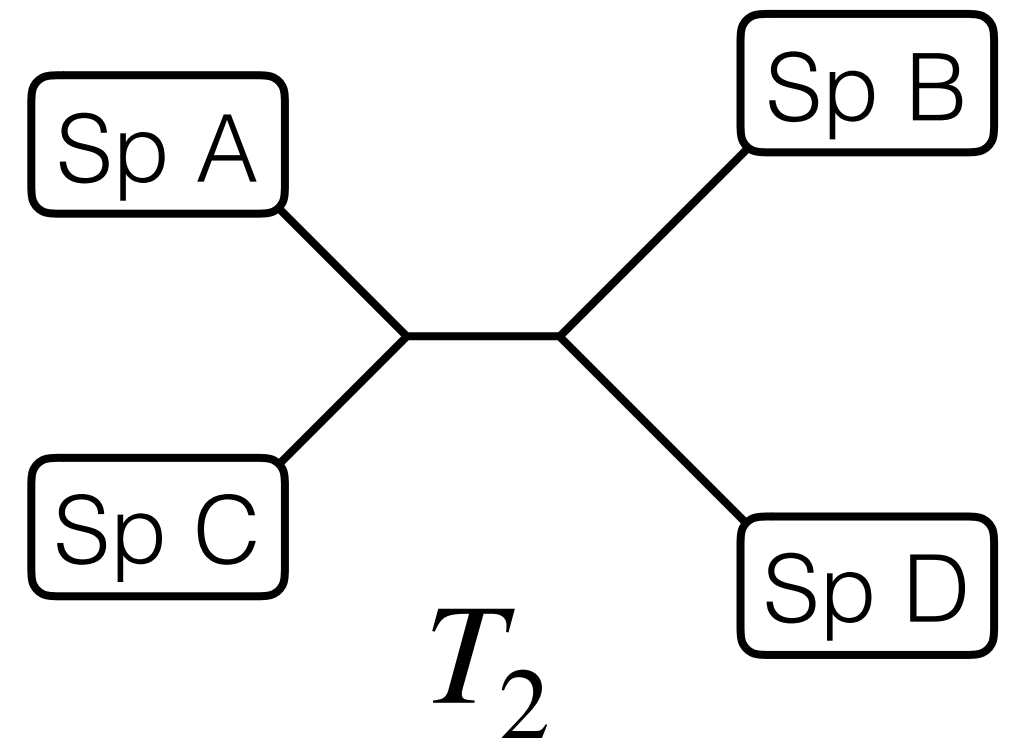
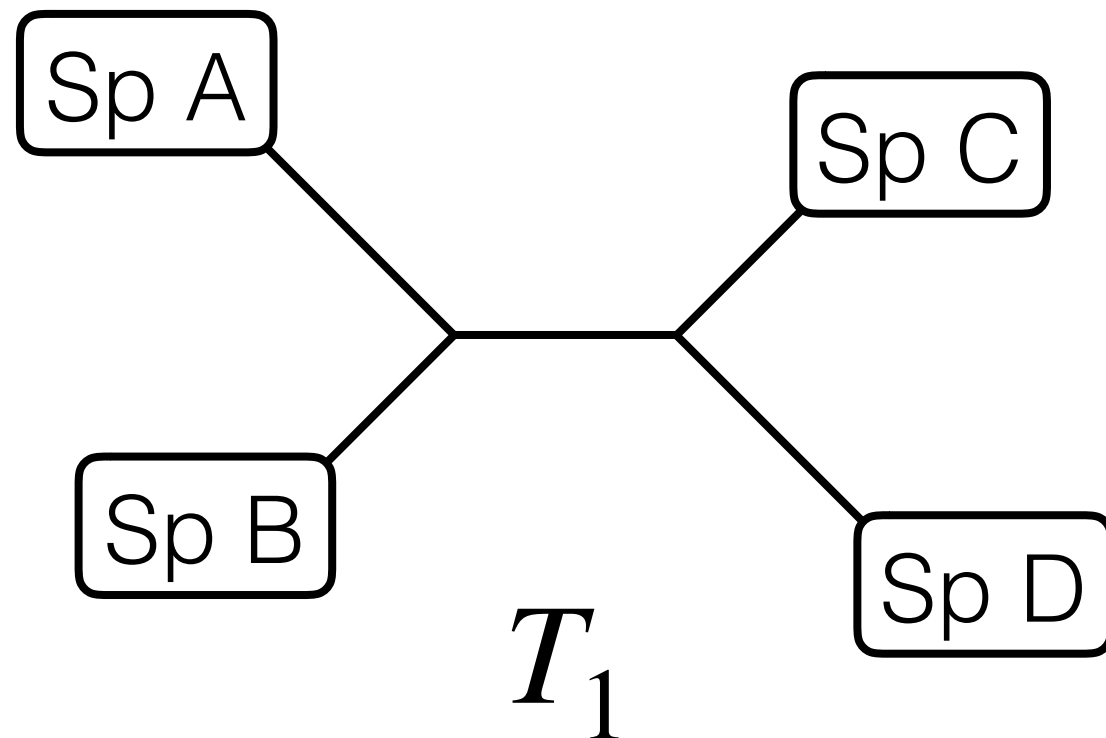
S-H Test



H₀: All T are equally good explanations of the data.

H_A: Some T are not equally good explanations.

S-H Test



H₀: All T are equally good explanations of the data.

H_A: Some T are not equally good explanations.

S-H Test

The Intuitive Explanation (*posNPfcd*)

1. Calculate $L_{ML} - L_x$.
2. Bootstrap
3. Reoptimize for each bootstrap
4. Center the bootstrapped likelihoods for each topology across replicates.
5. For each replicate, recalculate $L_{ML} - L_x$ from the recentered values.
6. For each topology, compare observed difference to the reentered, bootstrap distribution. This test is one-sided and gives a P-value for each topology.