

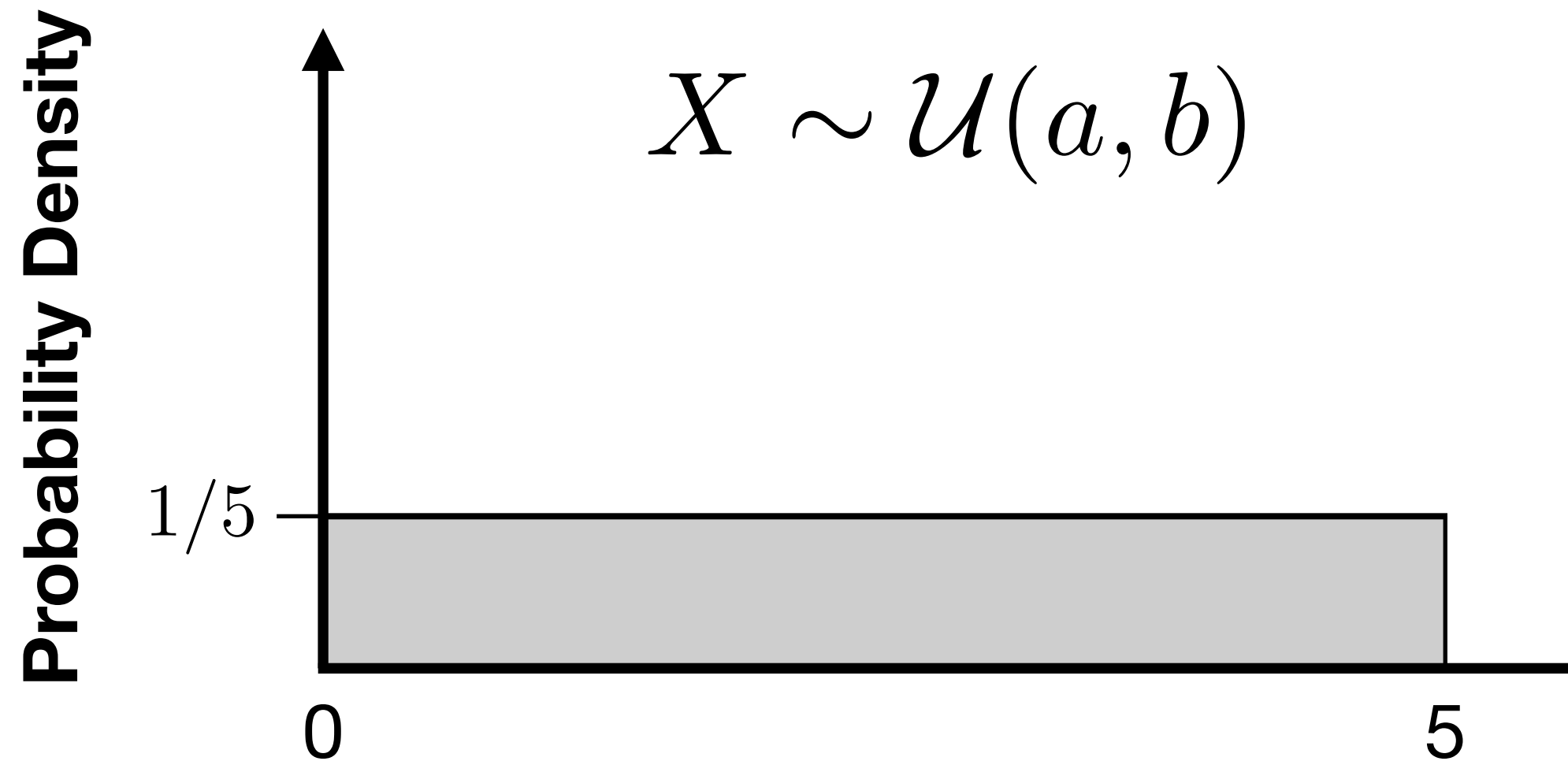
# Differences Between Discrete and Continuous Distributions

- Probability masses in discrete distributions sum to 1, while probability densities in continuous distributions integrate to 1.
- Probability densities can be greater than 1 (yet they can still integrate to 1).
- The probability mass of any precise value (e.g., 1.000...) in a continuous distribution is always infinitely small.

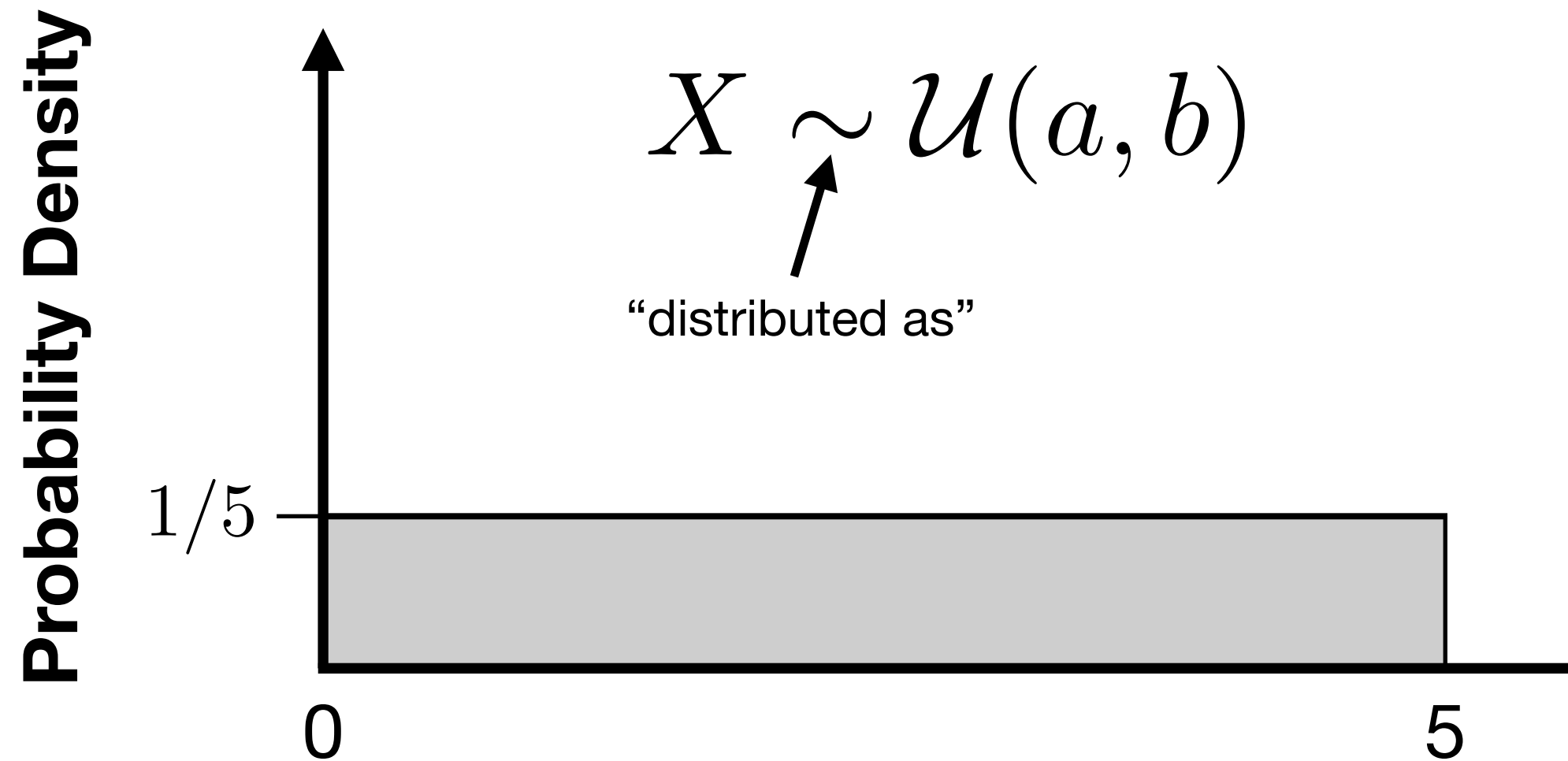
# Continuous Uniform Distribution



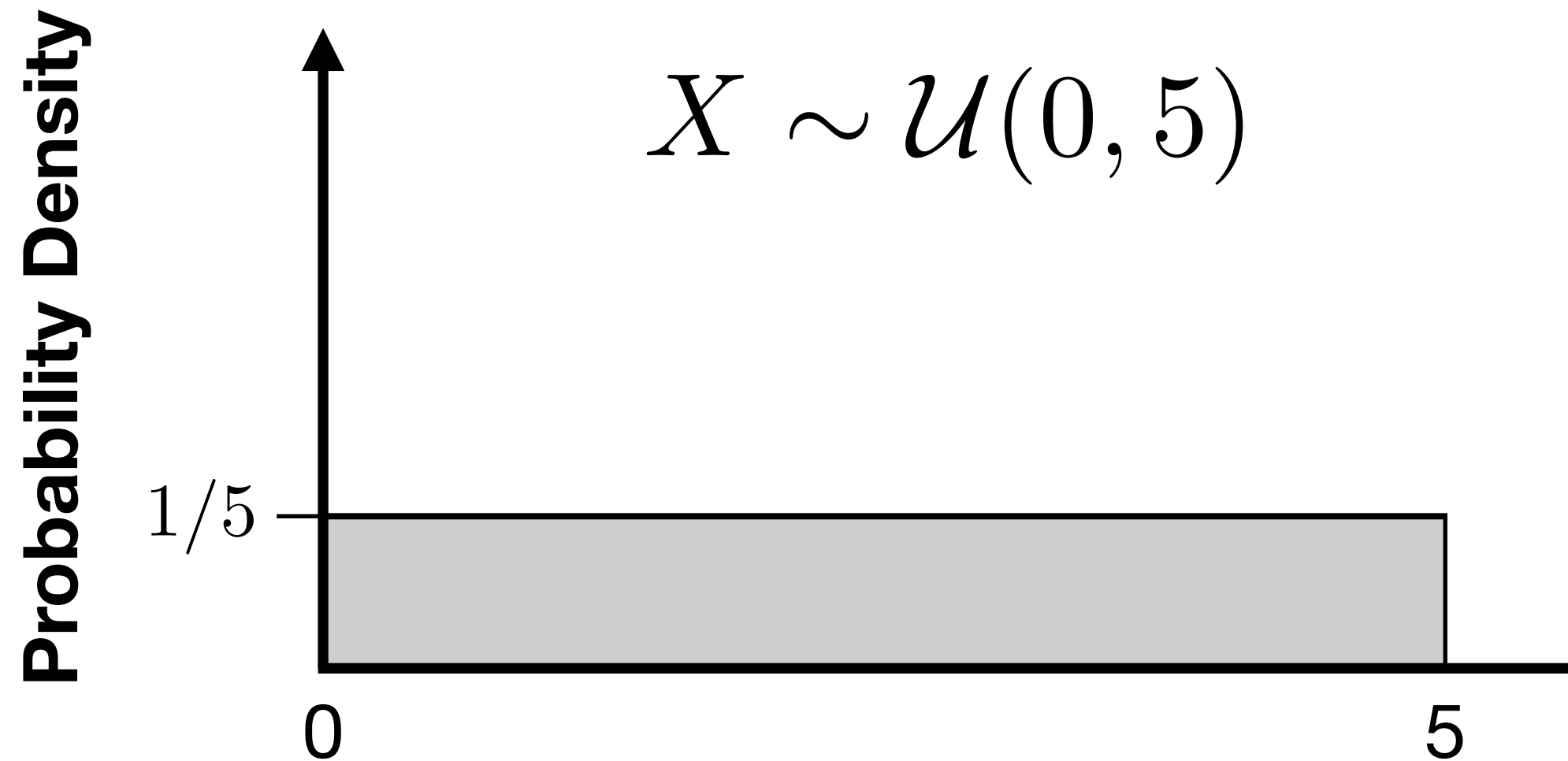
# Continuous Uniform Distribution



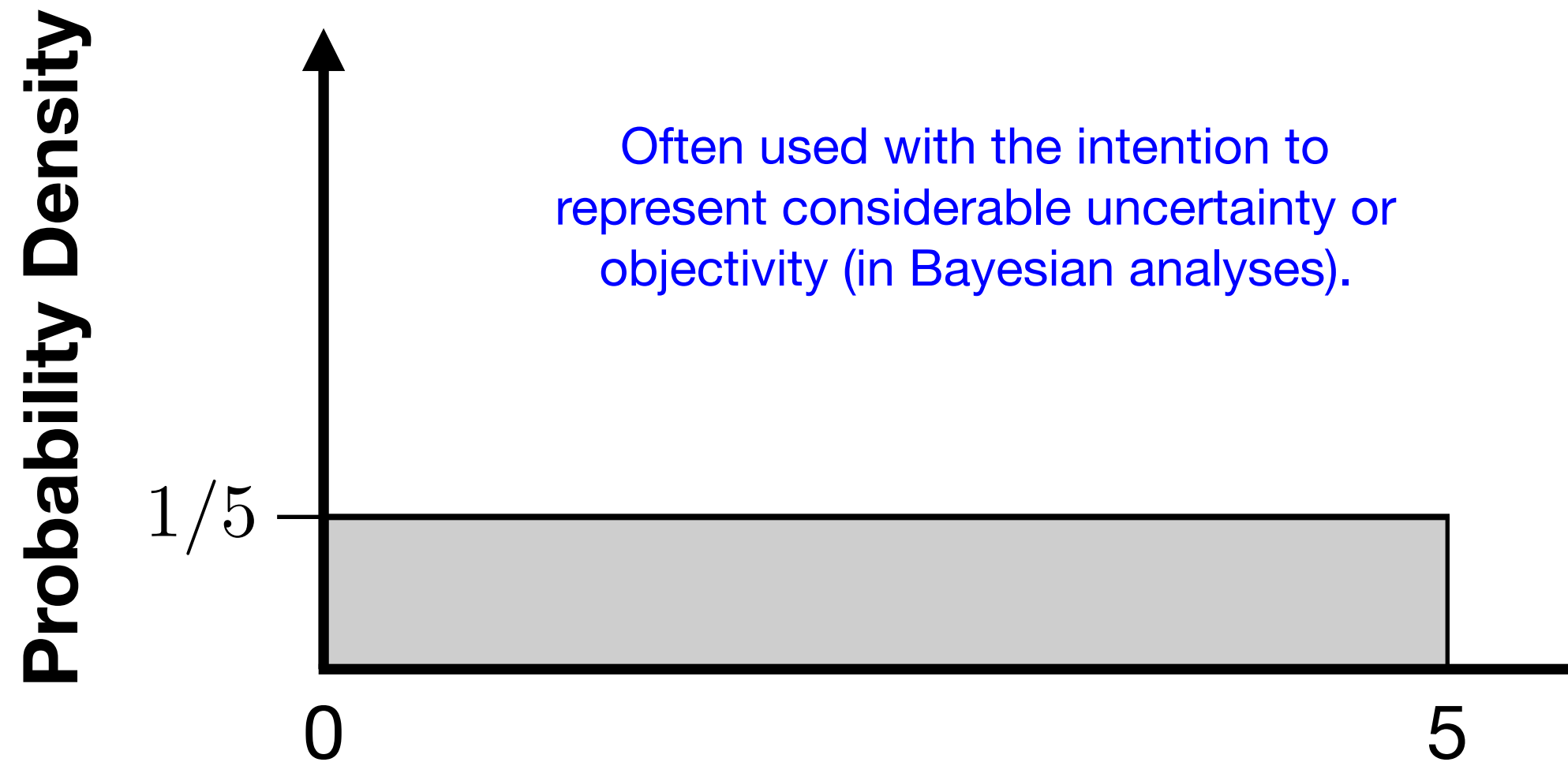
# Continuous Uniform Distribution



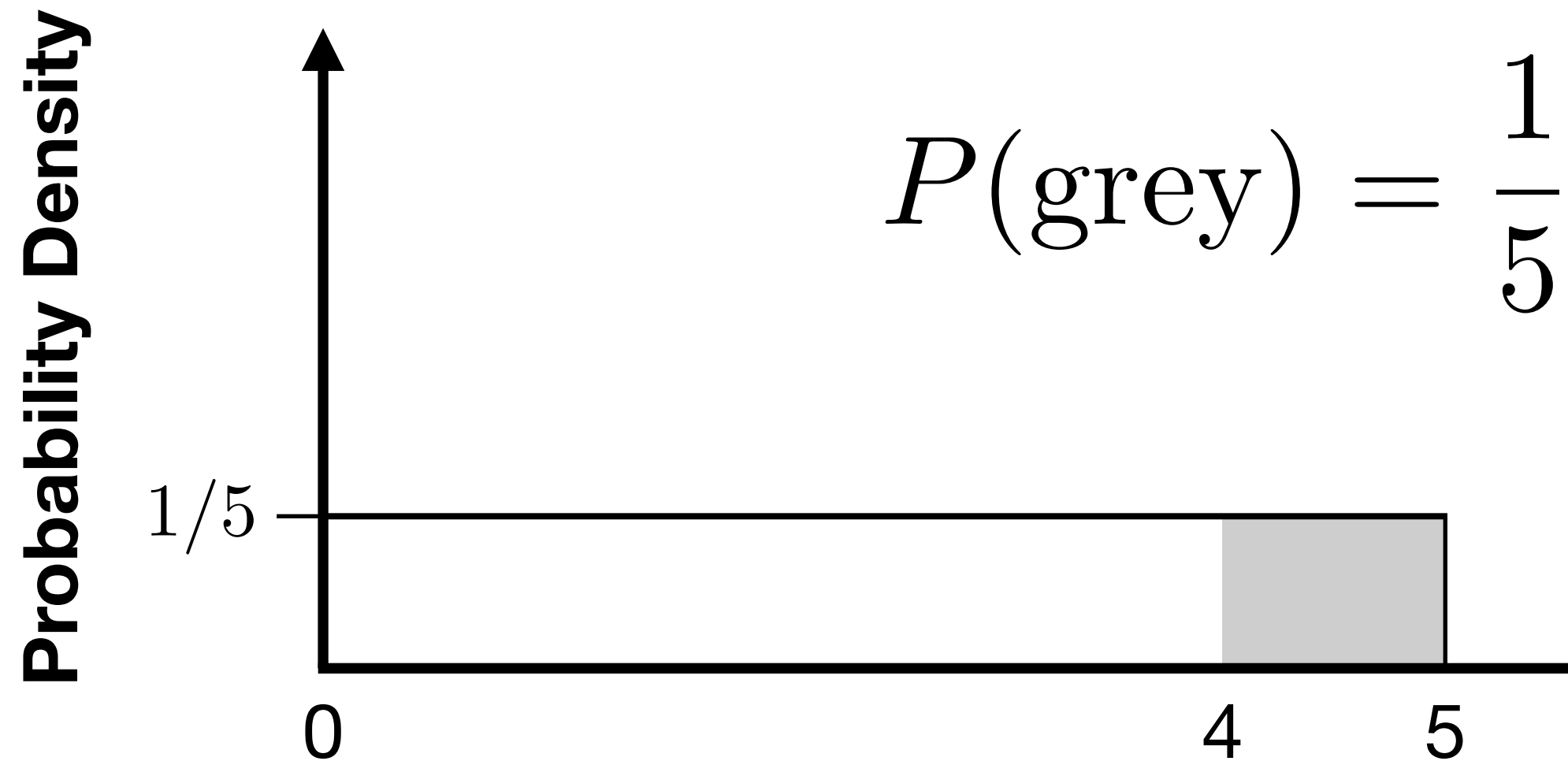
# Continuous Uniform Distribution



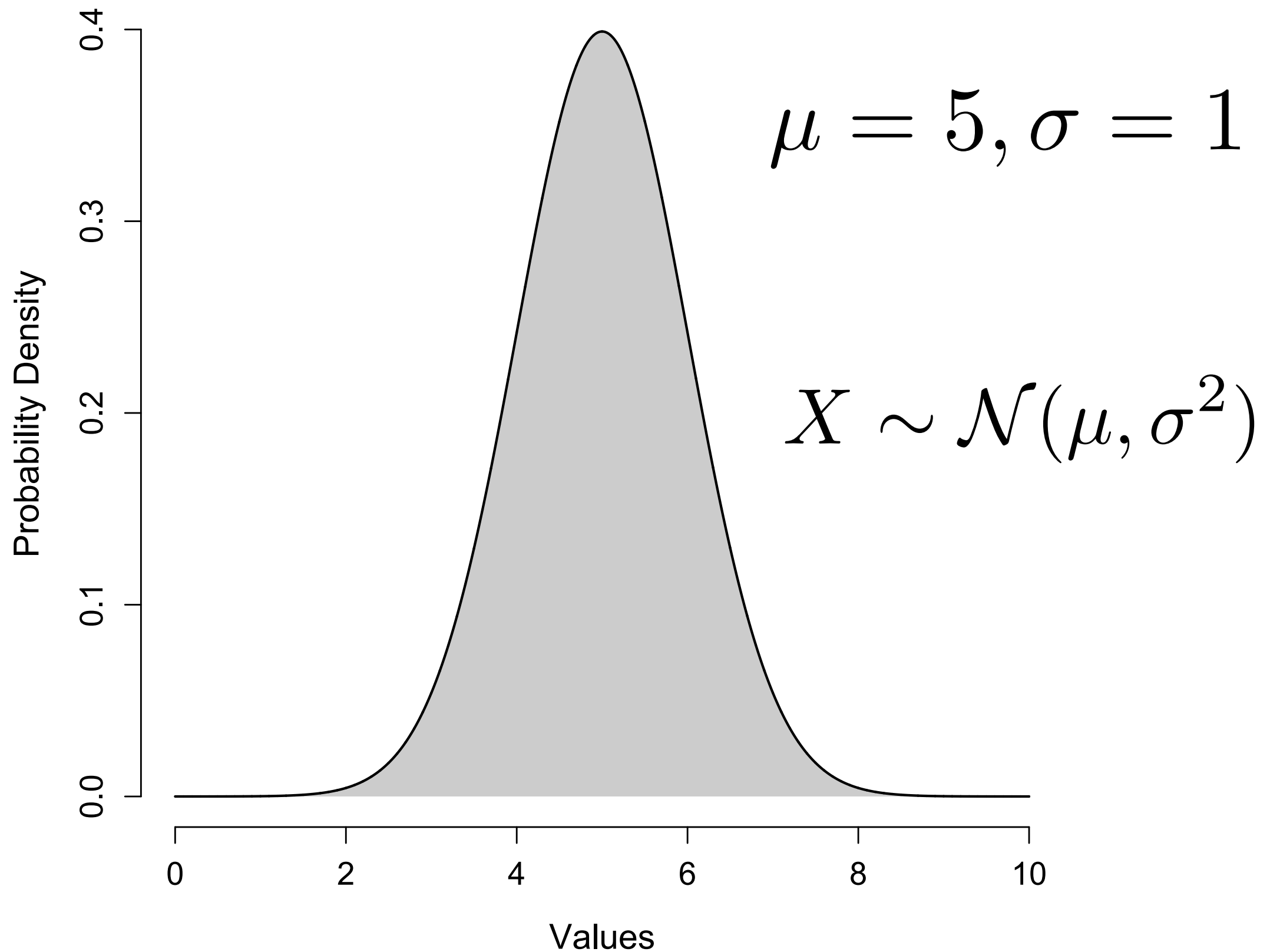
# Continuous Uniform Distribution



# Continuous Uniform Distribution

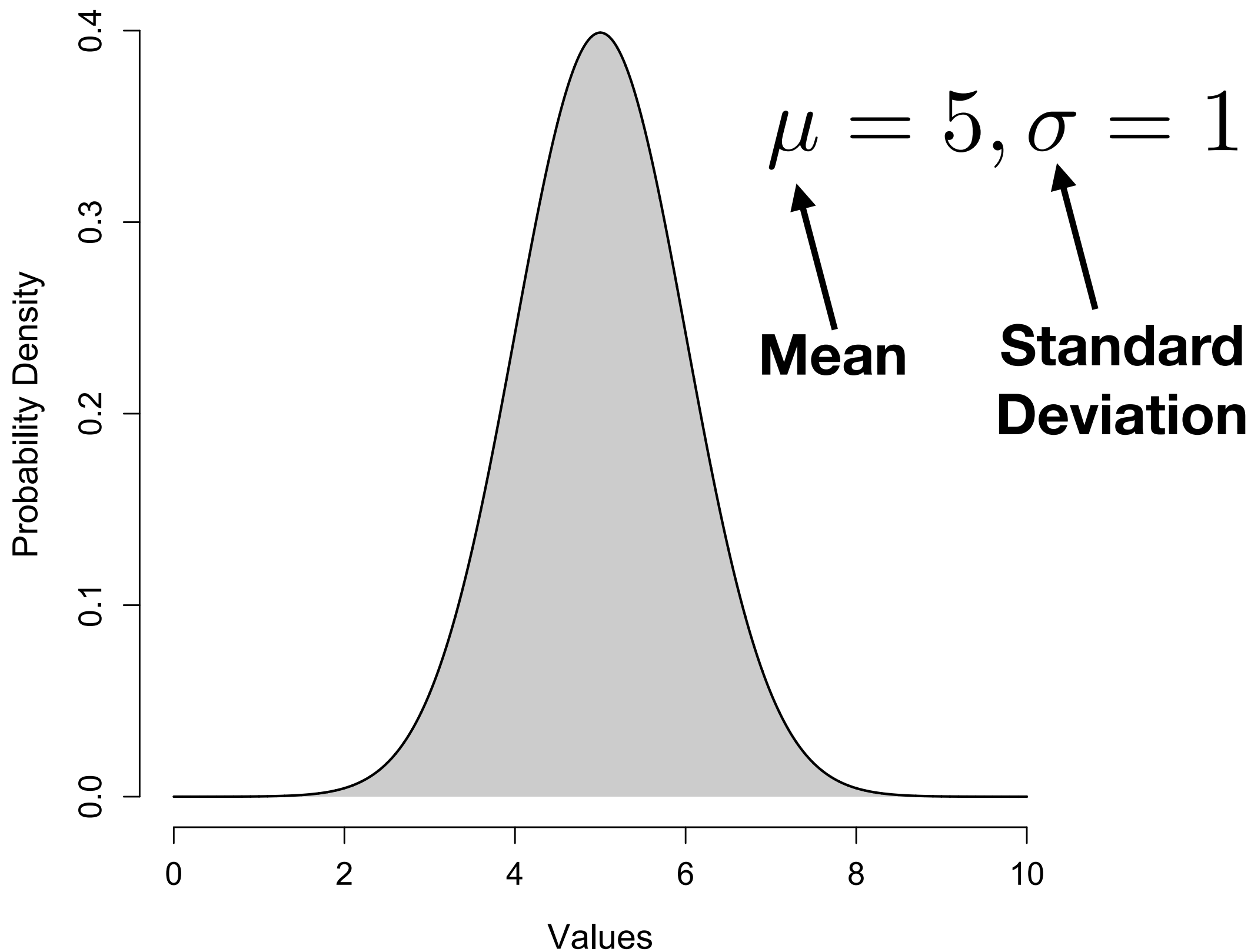


# Normal Distribution

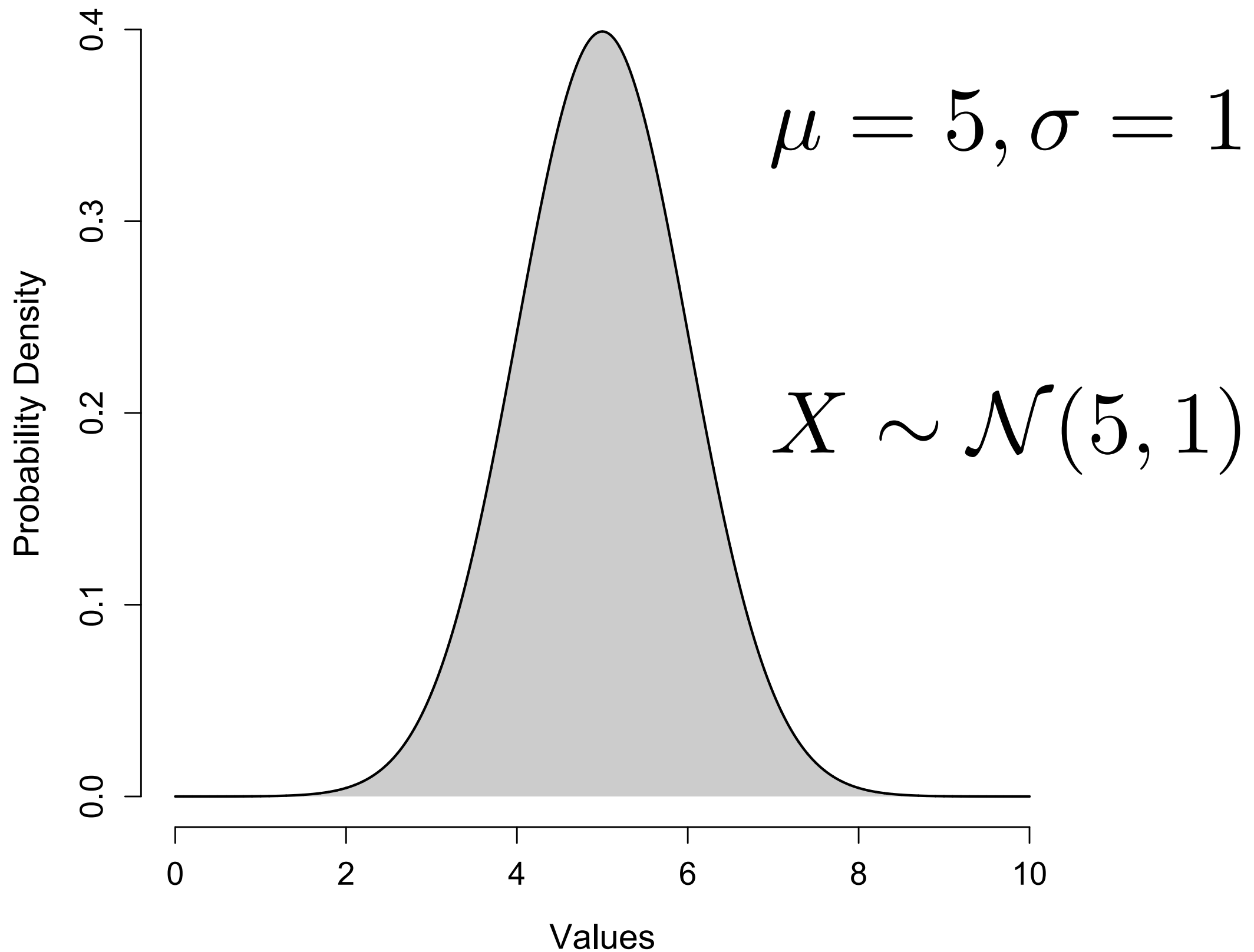




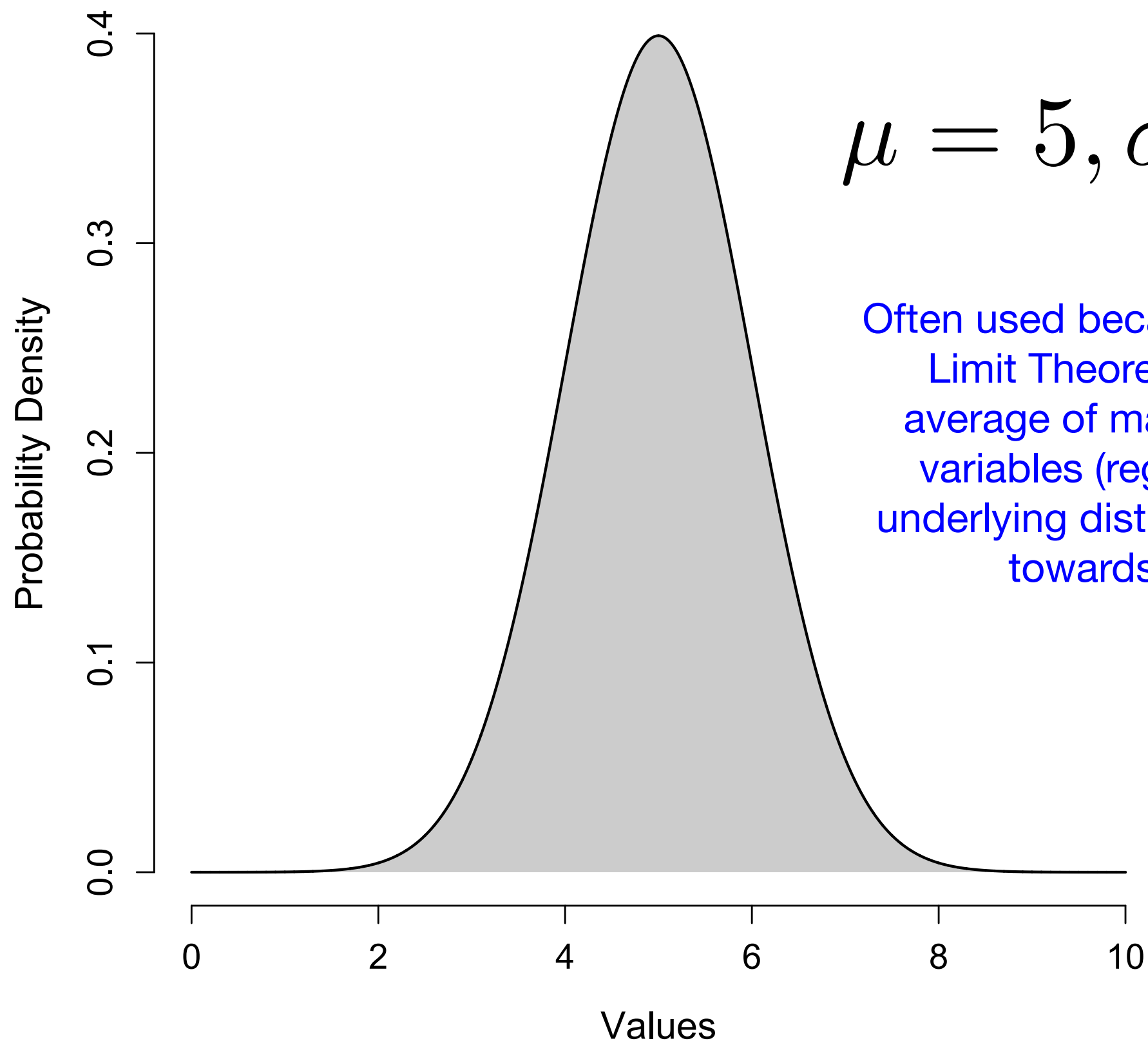
# Normal Distribution



# Normal Distribution



# Normal Distribution



$$\mu = 5, \sigma = 1$$

Often used because of the Central Limit Theorem - the sum or average of many independent variables (regardless of their underlying distributions) will tend towards a Normal.

# Variance

Variance is the expectation of the squared deviation of a random variable from its mean.

$$\text{Var}(X) = \sigma^2(X) = \text{E}[(X - \mu)^2]$$

# Variance (Standard Deviation)

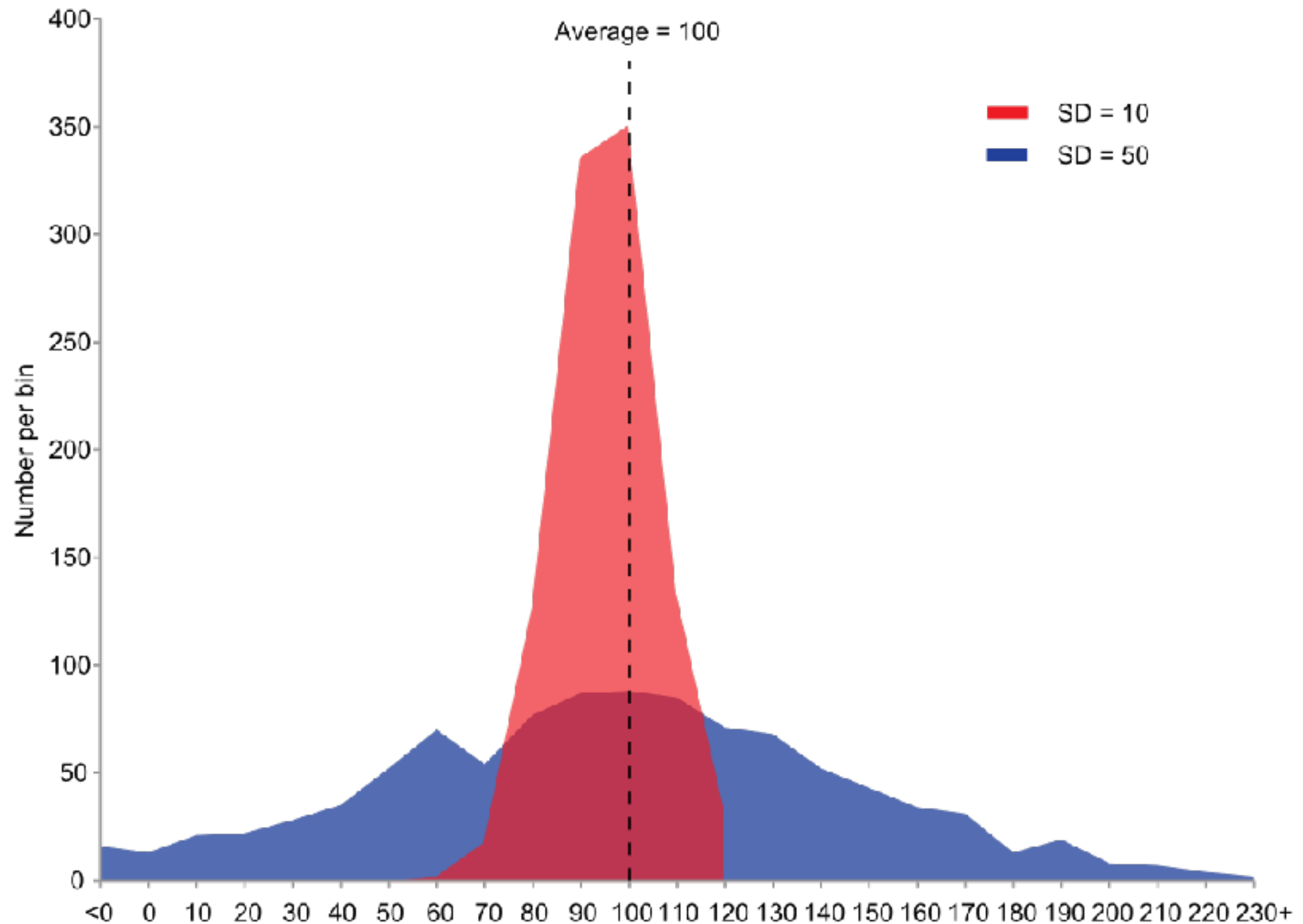
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$$\text{Var}(X) = \sigma^2(X) = \text{E}[(X - \mu)^2]$$

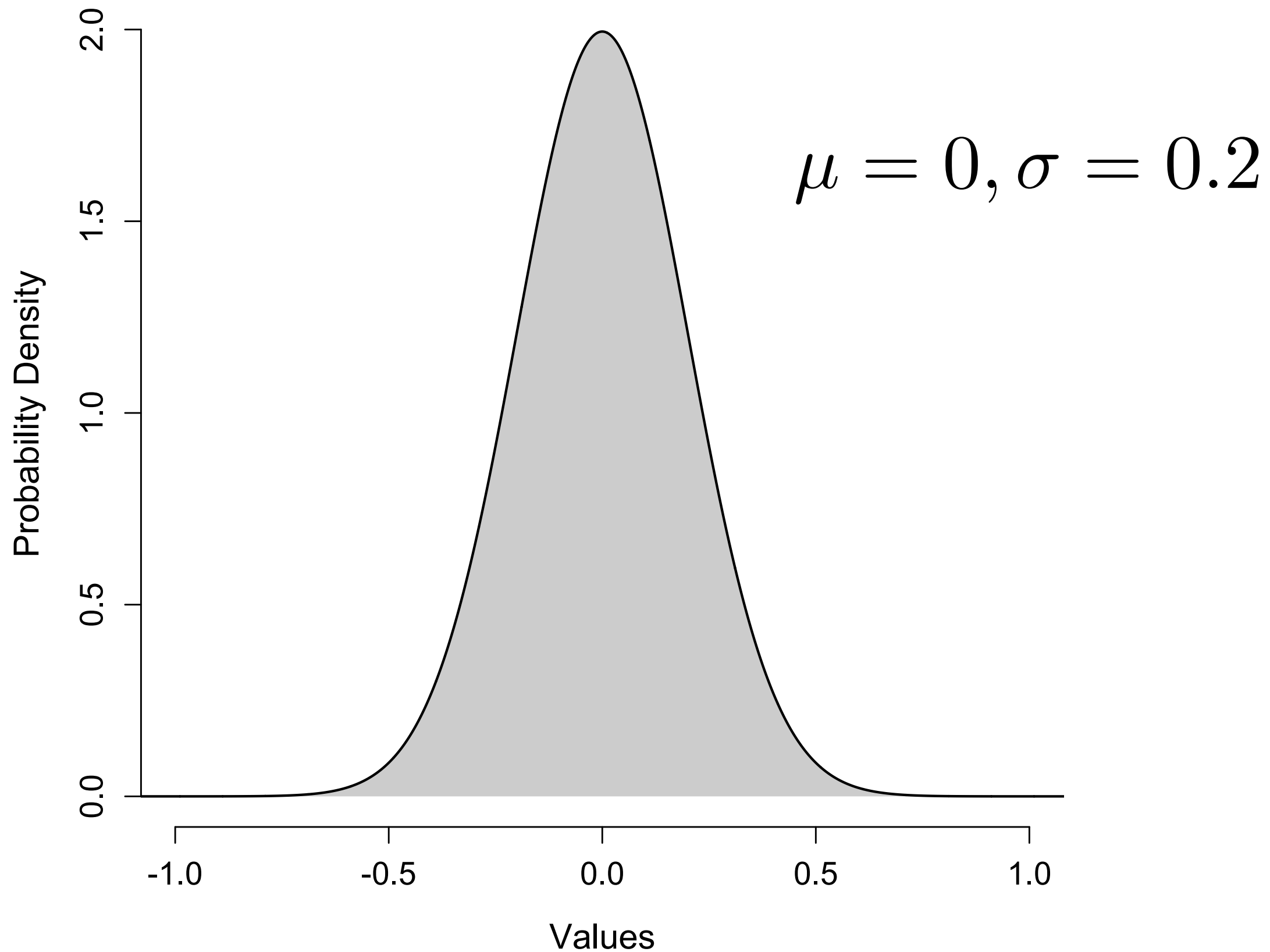
The standard deviation of a random variable is the square root of its variance.

$$\text{sd}(X) = \sigma(X) = \sqrt{\text{E}[(X - \mu)^2]}$$

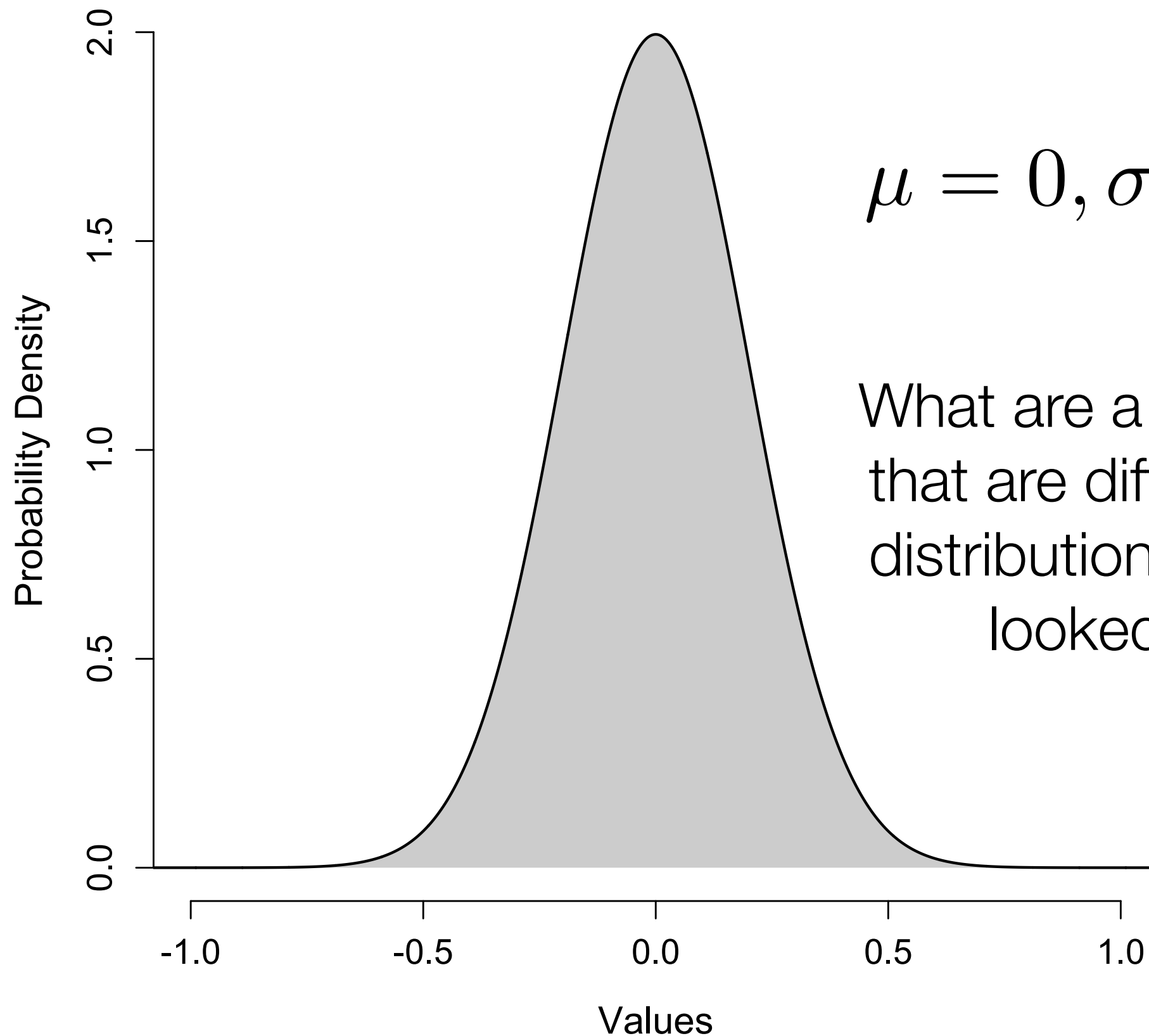
# Standard Deviation / Variance



# Normal Distribution



# Normal Distribution

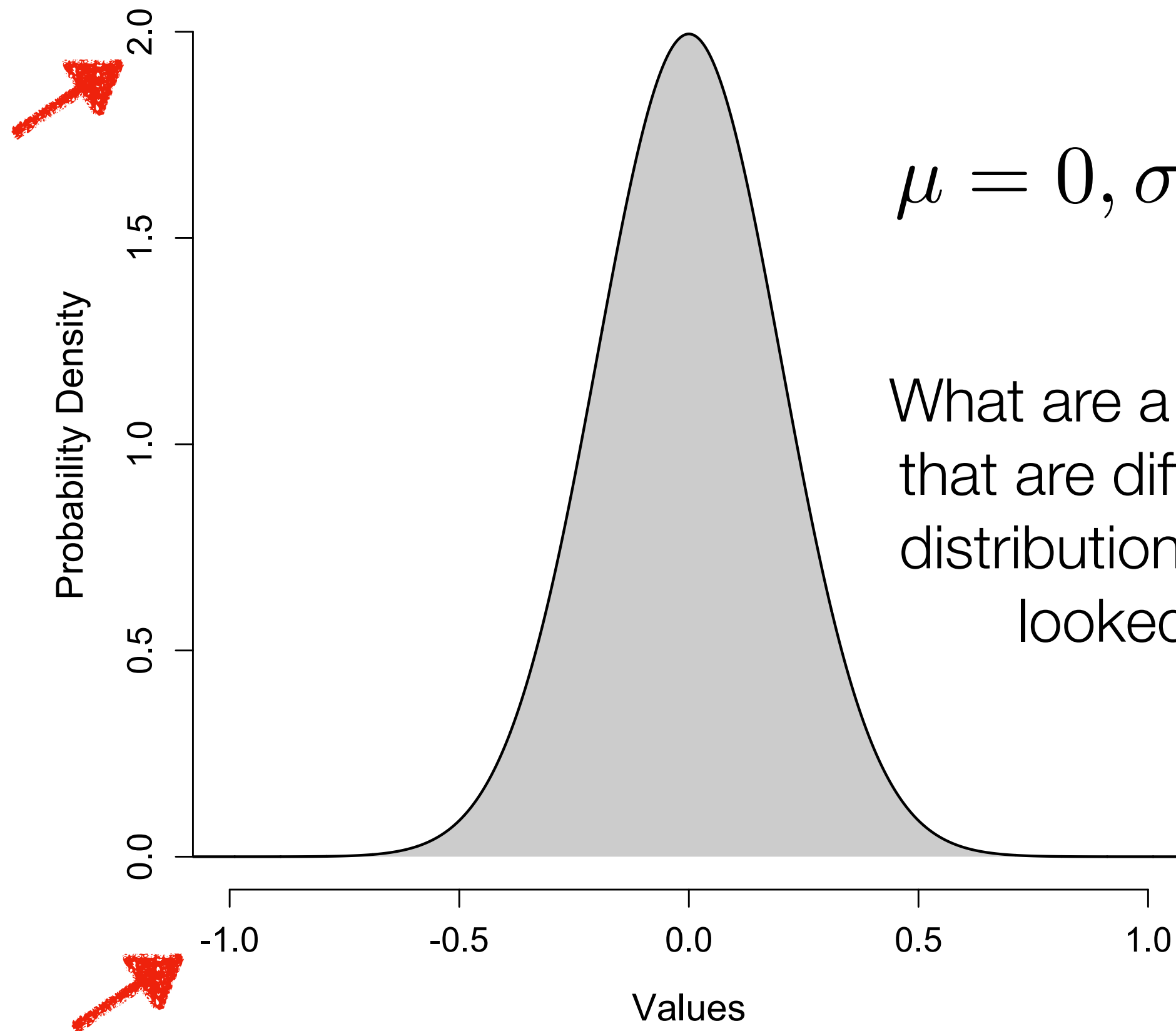


$$\mu = 0, \sigma = 0.2$$

What are a couple of things that are different about this distribution than any we've looked at before?



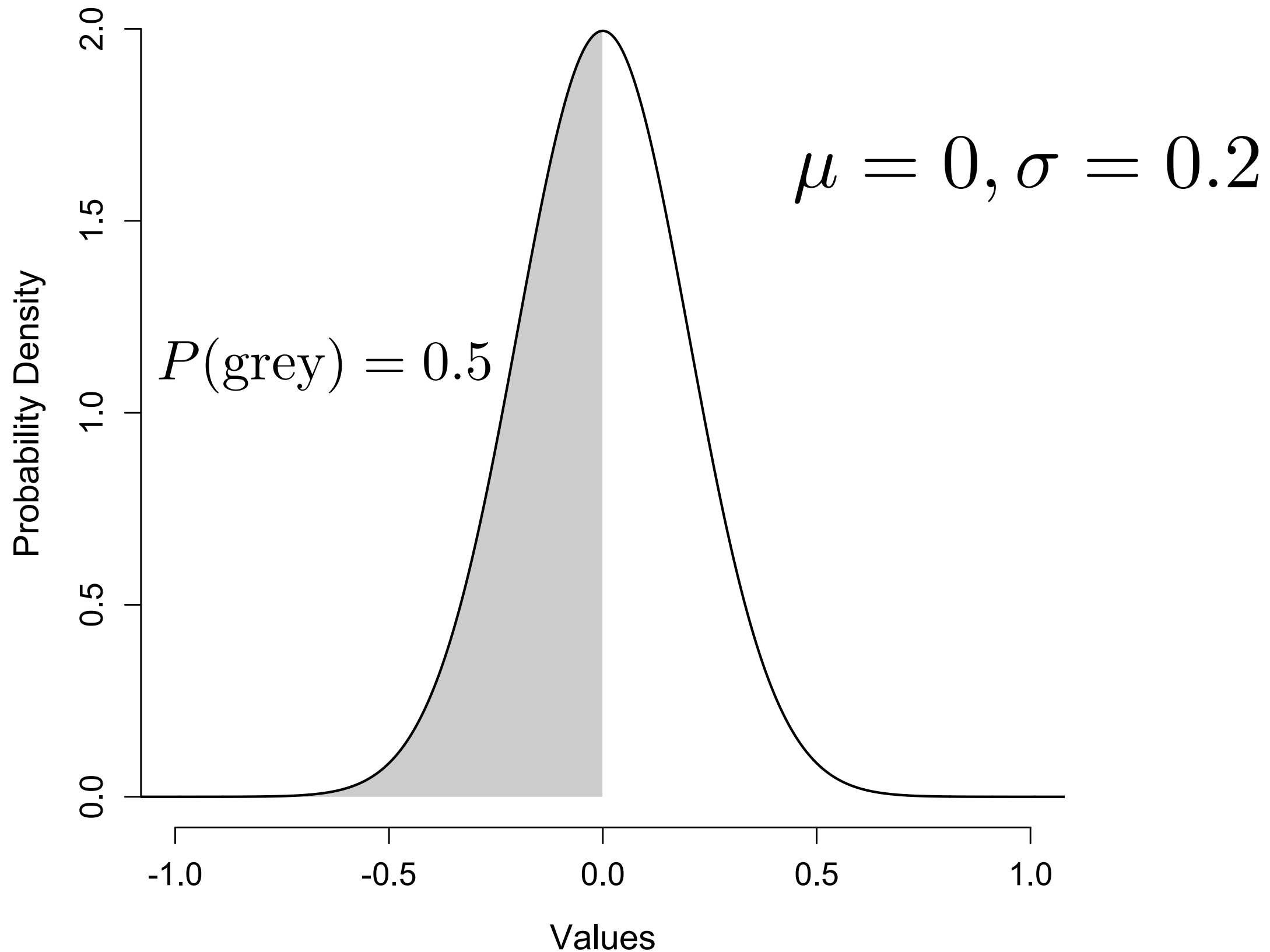
# Normal Distribution



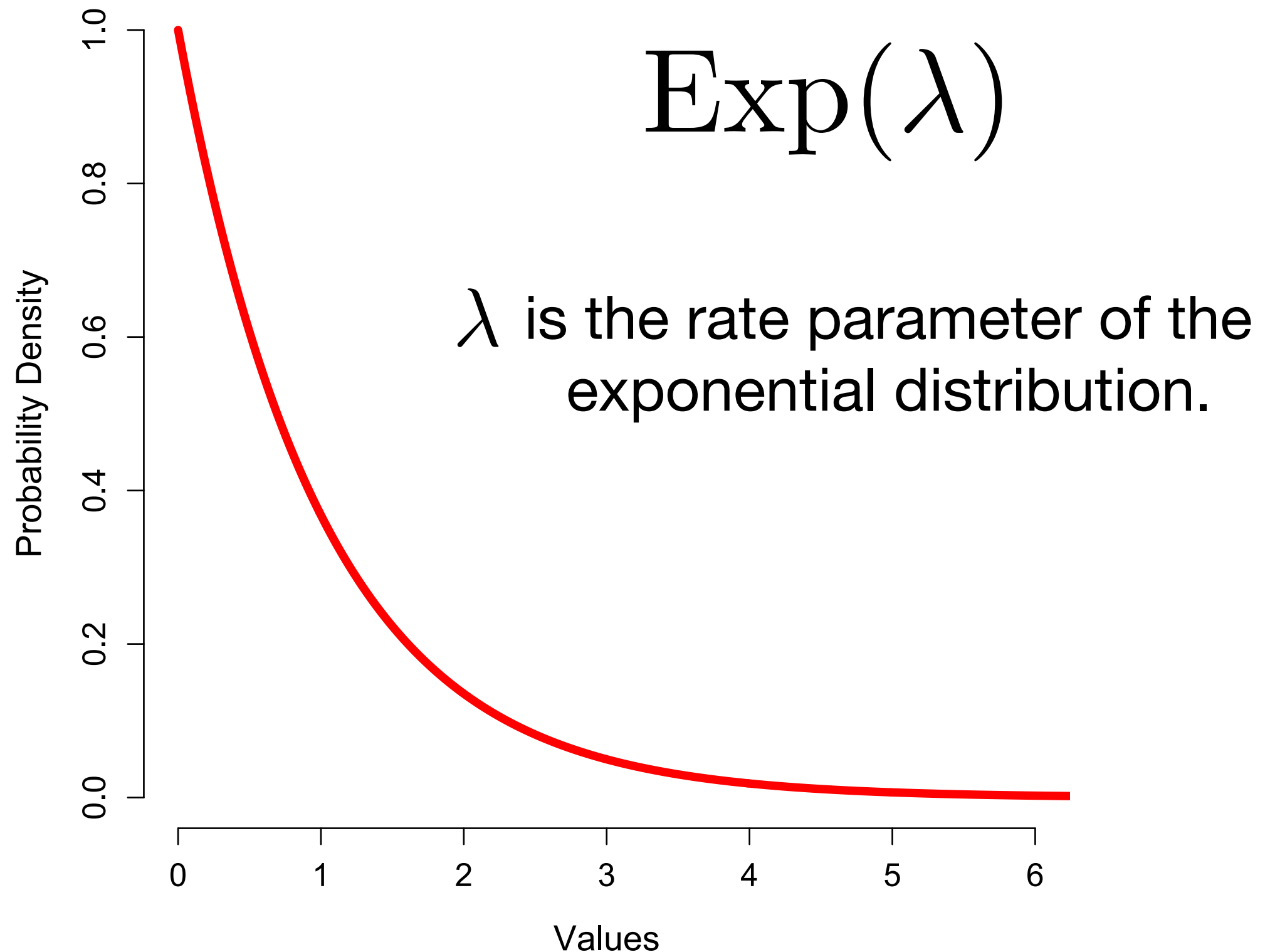
$$\mu = 0, \sigma = 0.2$$

What are a couple of things that are different about this distribution than any we've looked at before?

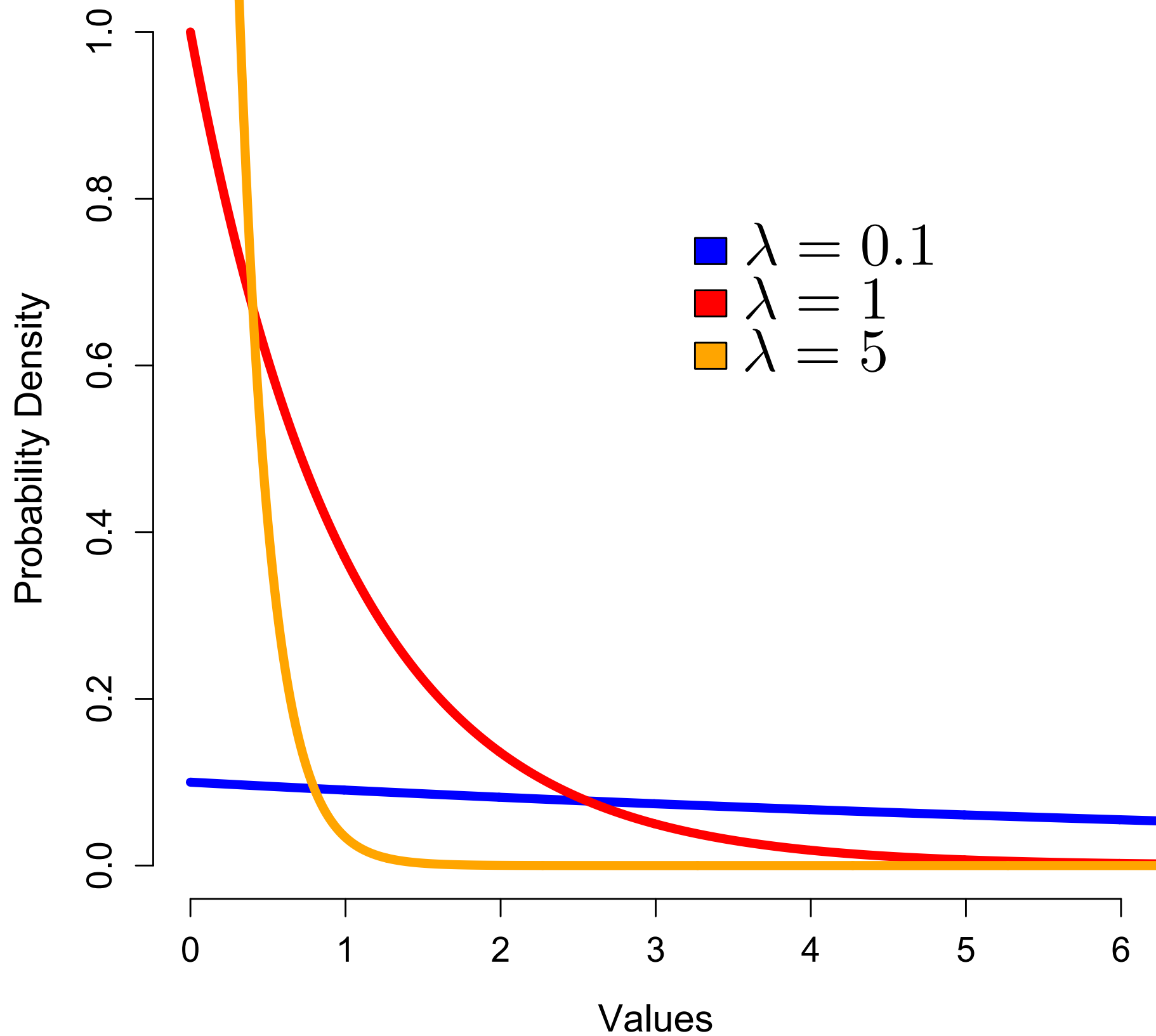
# Normal Distribution



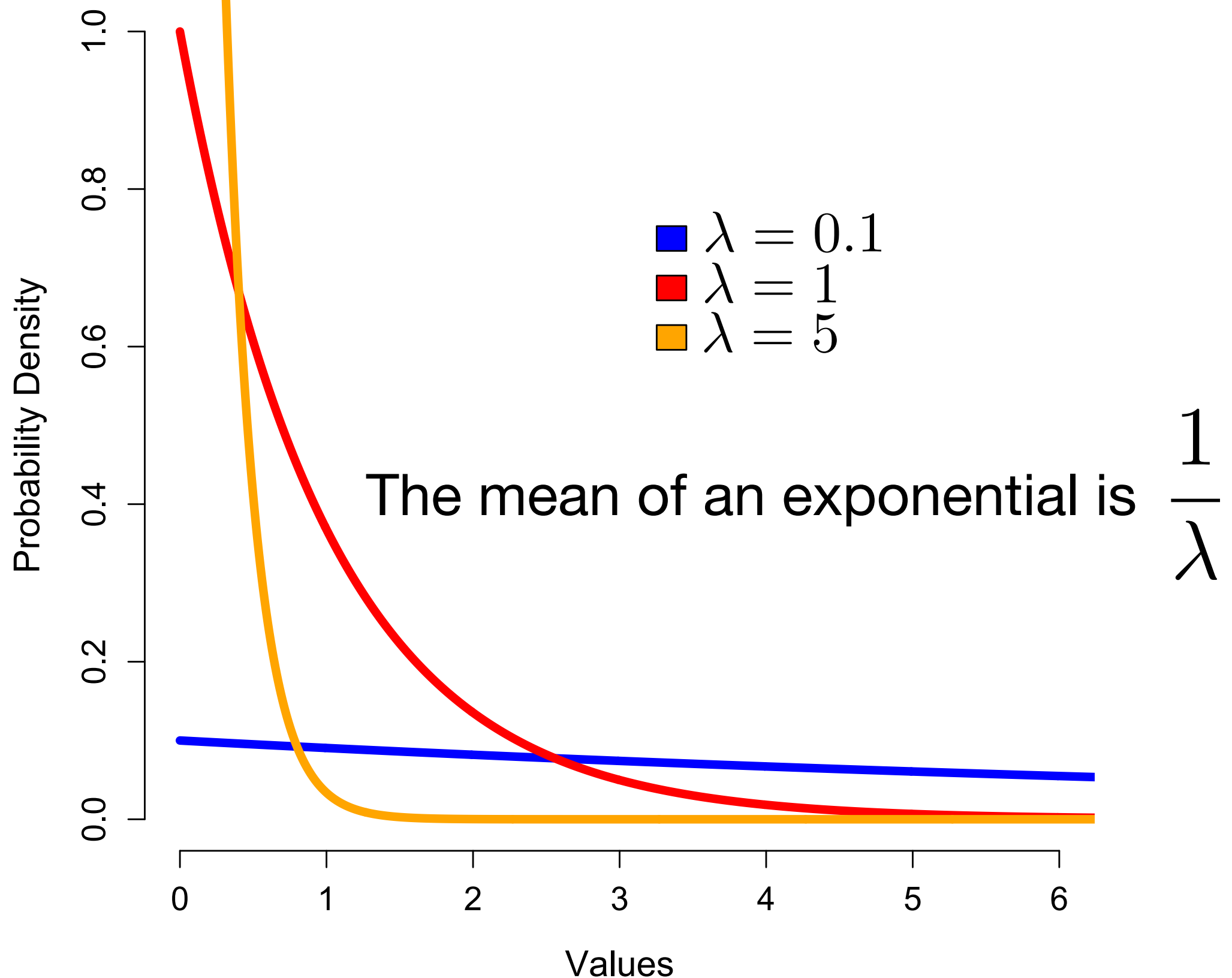
# Exponential Distribution



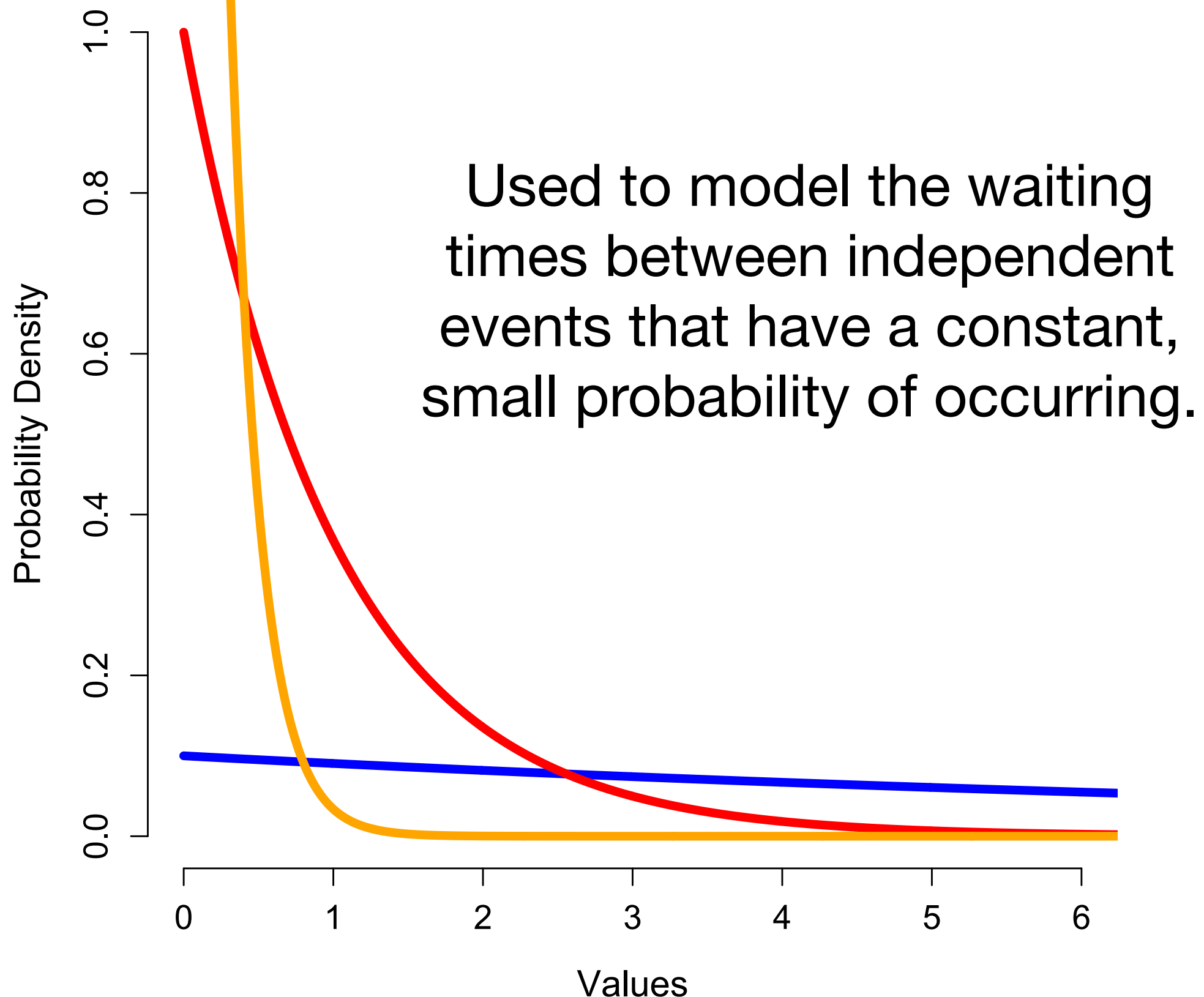
# Exponential Distribution



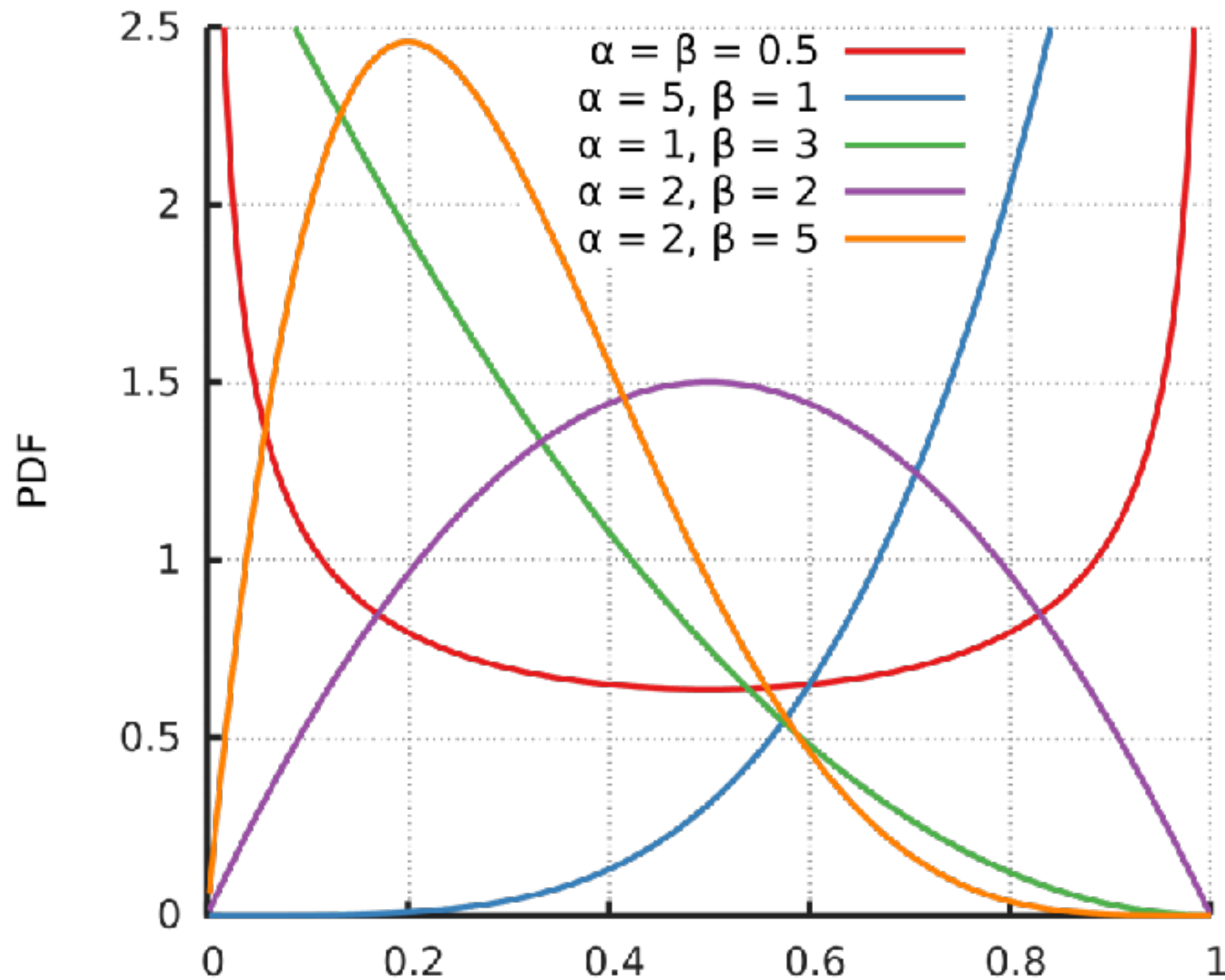
# Exponential Distribution



# Exponential Distribution



# Beta Distribution

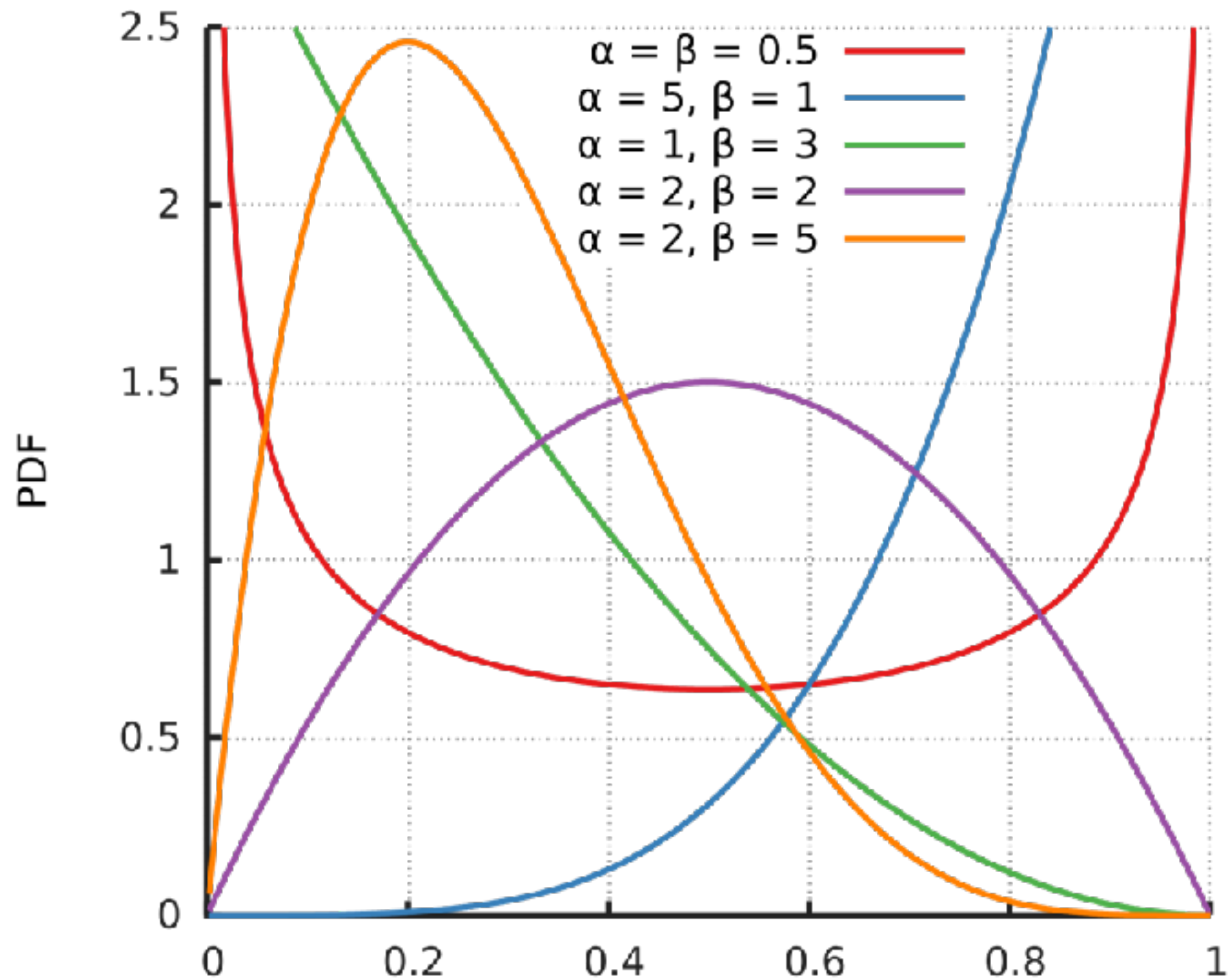


Two Shape Parameters  
 $\alpha$  and  $\beta$

What is the effect of  
changing these  
parameter values?

What is the **support** of  
this distribution?

# Beta Distribution

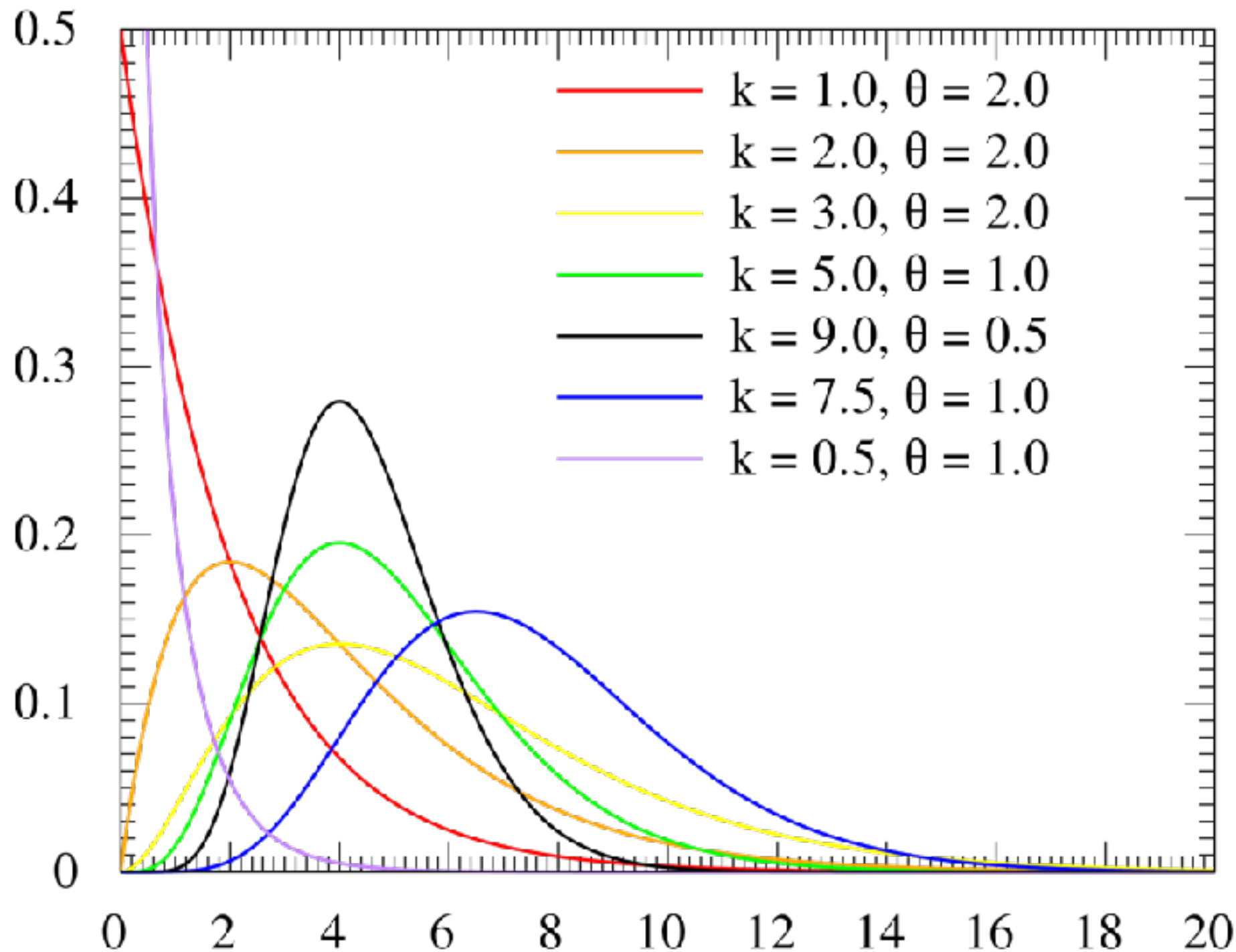


Support  
 $x \in (0, 1)$

Often used as a flexible  
distribution to model  
values between 0 and 1.



# Gamma Distribution

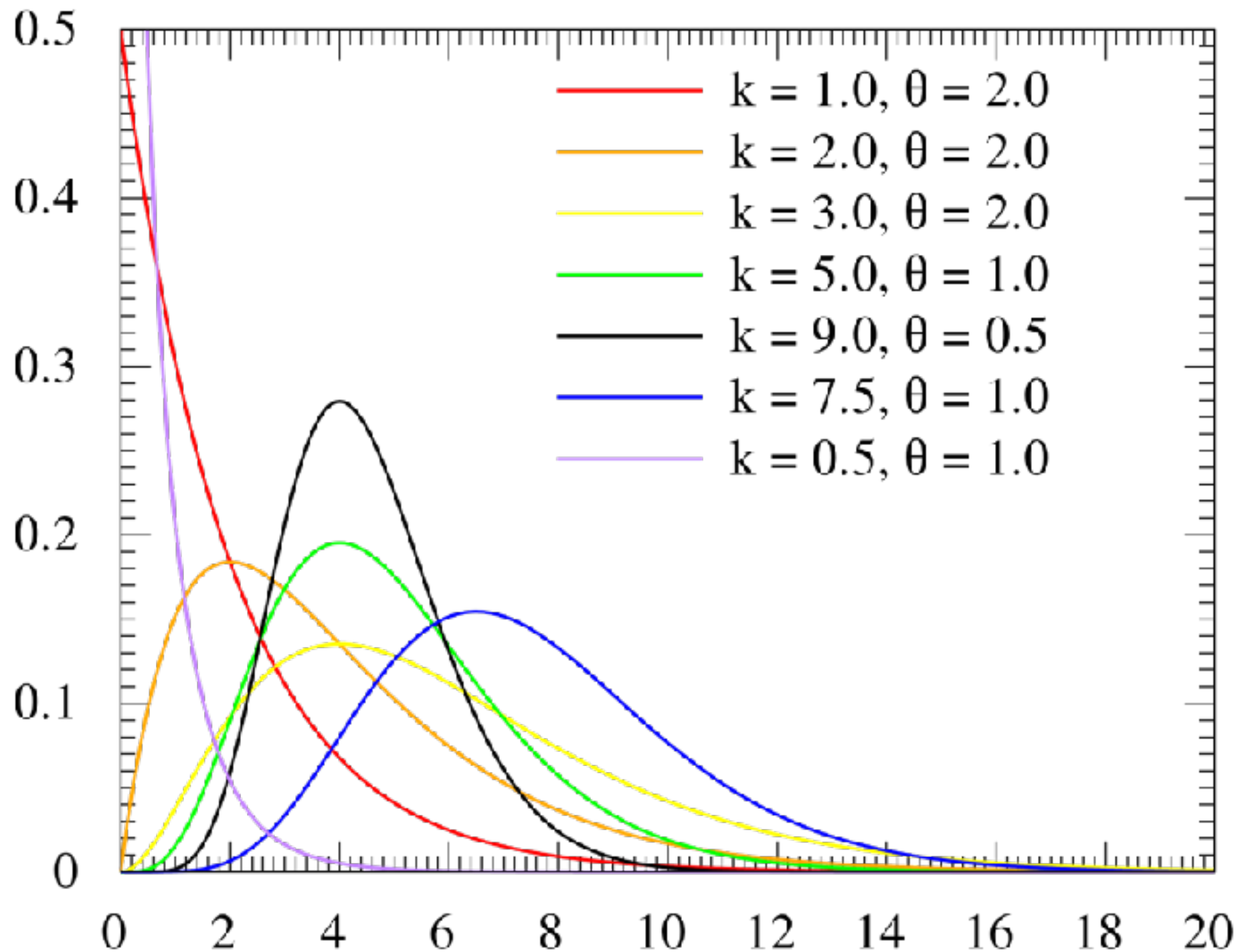


Two Shape Parameters

Shape and Scale  
 $k$  and  $\theta$

Shape and Rate  
 $\alpha$  and  $\beta$

# Gamma Distribution



$$X \sim \Gamma(k, \theta)$$

$$X \sim \Gamma(\alpha, \beta)$$

$$E[X] = k\theta = \frac{\alpha}{\beta}$$

Support

$$x \in (0, \infty)$$

# Gamma Distribution

