

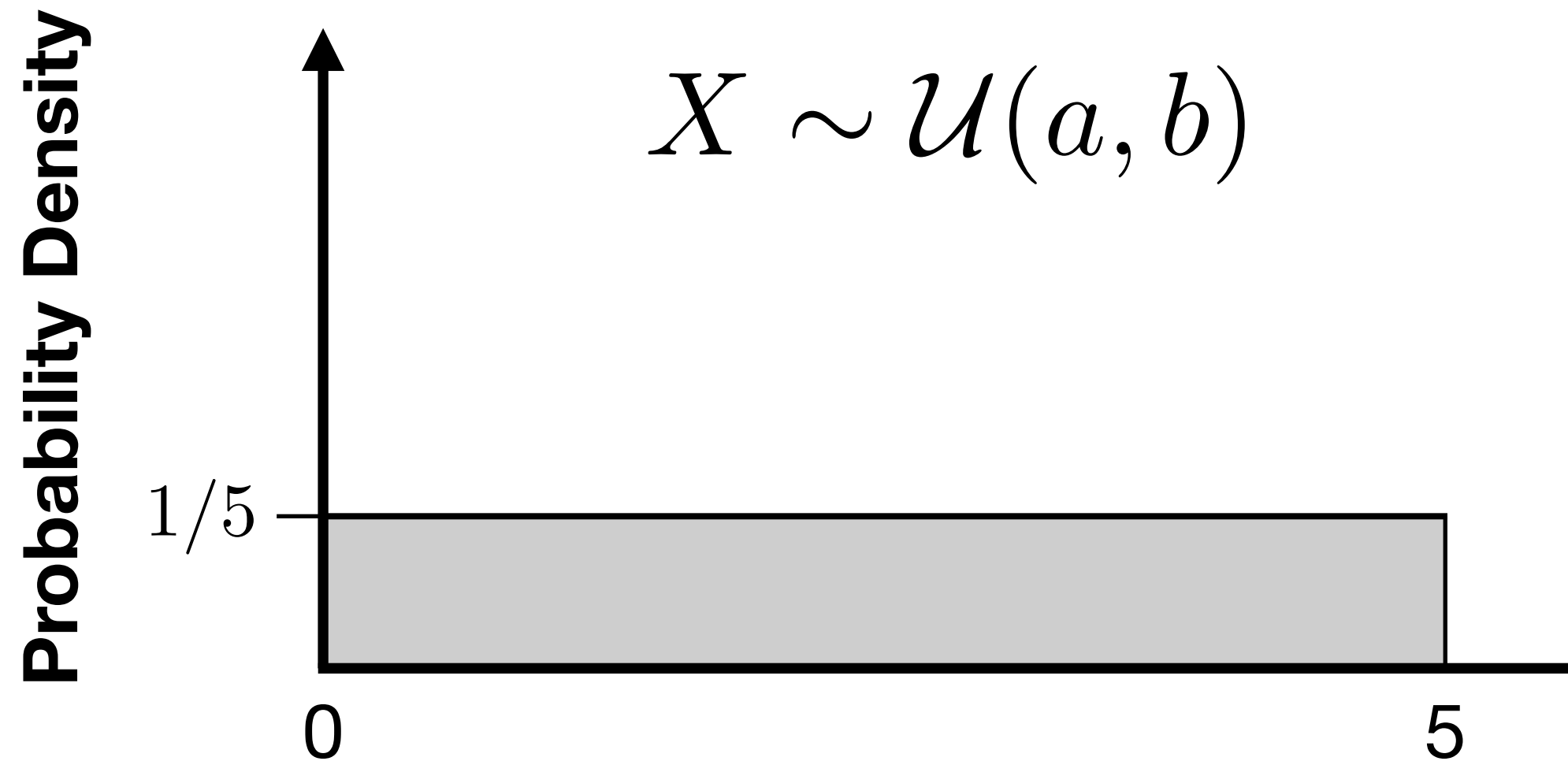
Differences Between Discrete and Continuous Distributions

- Probability masses in discrete distributions sum to 1, while probability densities in continuous distributions integrate to 1.
- Probability densities can be greater than 1 (yet they can still integrate to 1).
- The probability mass of any precise value (e.g., 1.000...) in a continuous distribution is always infinitely small.

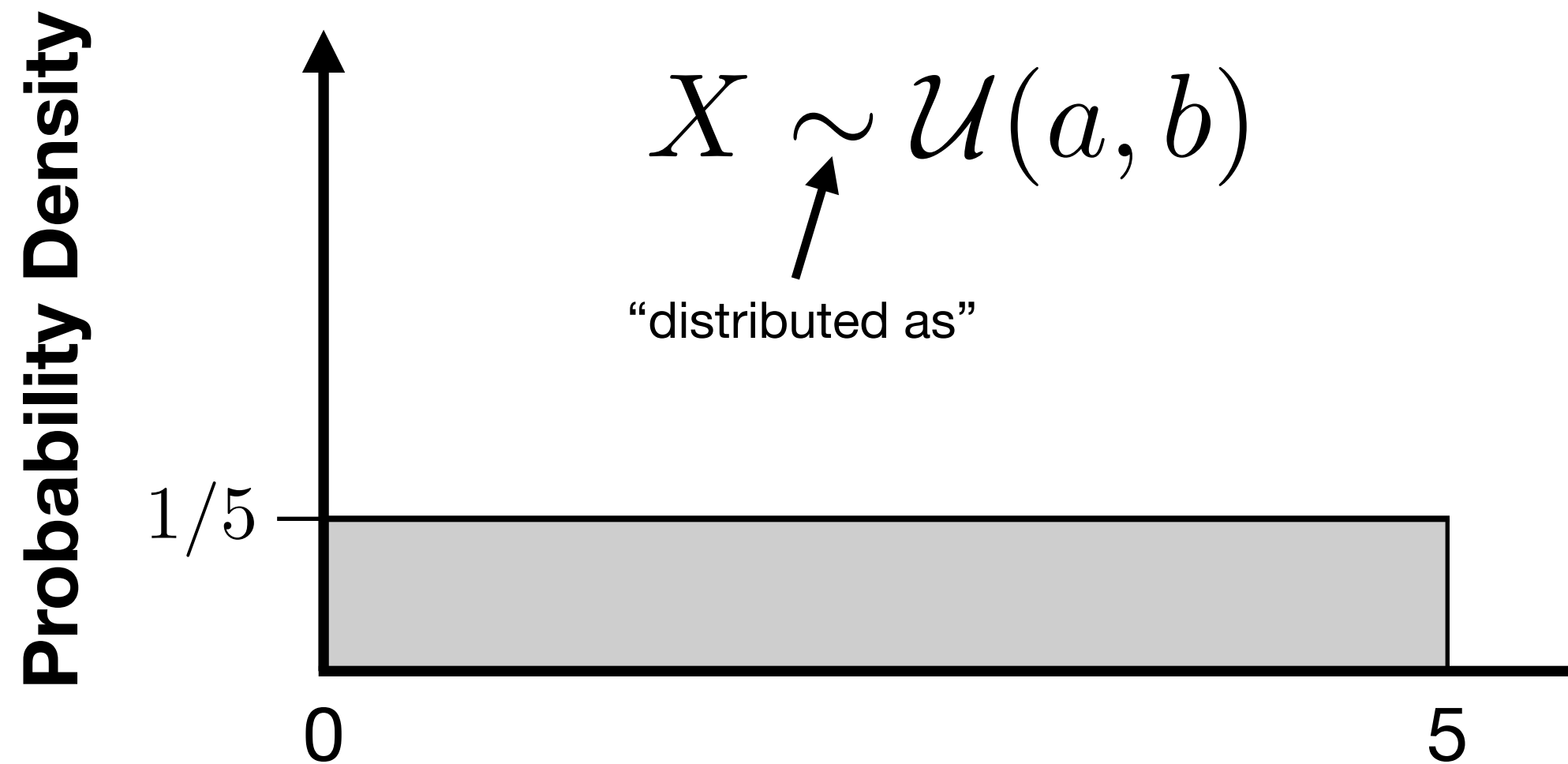
Continuous Uniform Distribution



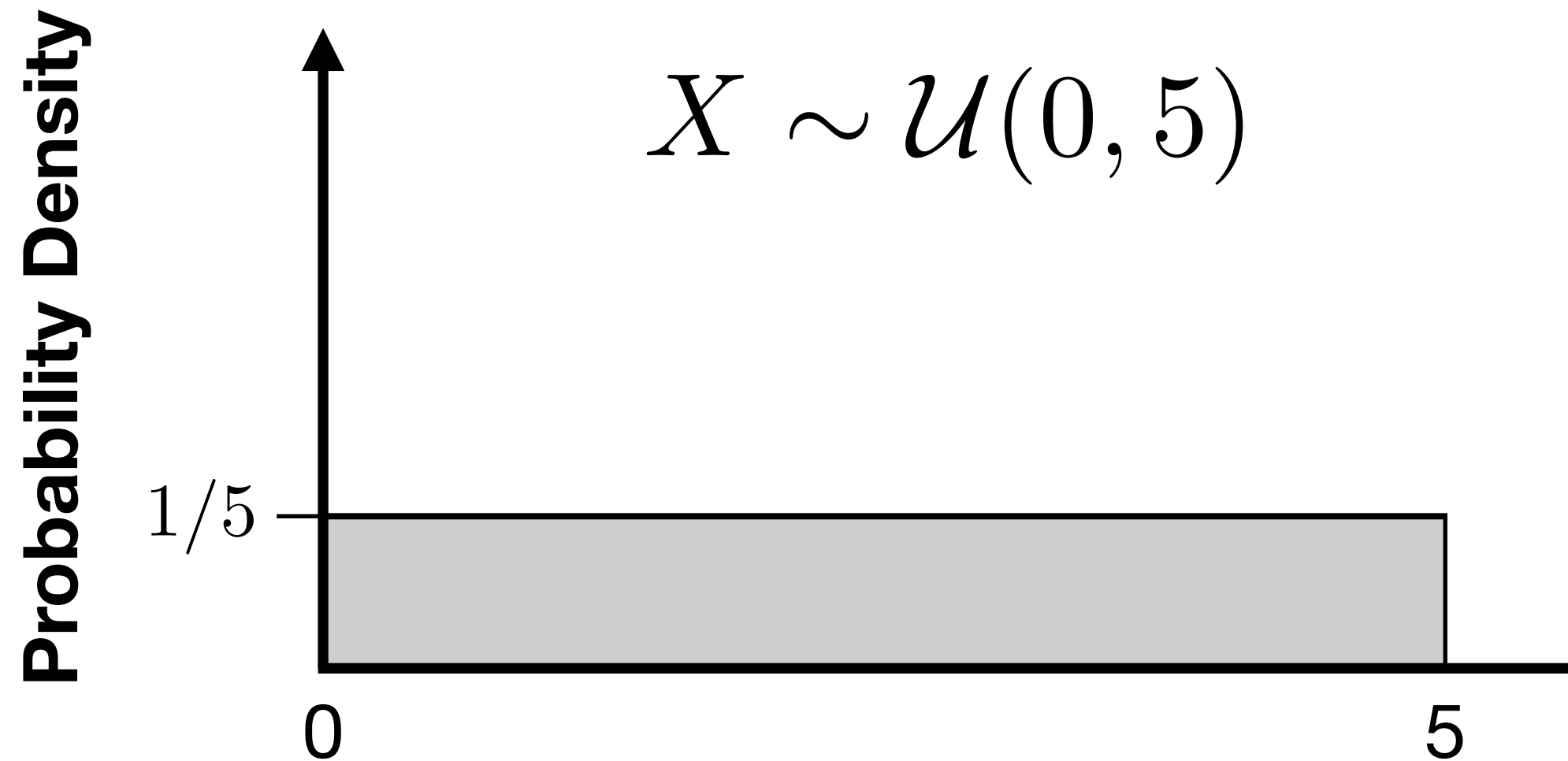
Continuous Uniform Distribution



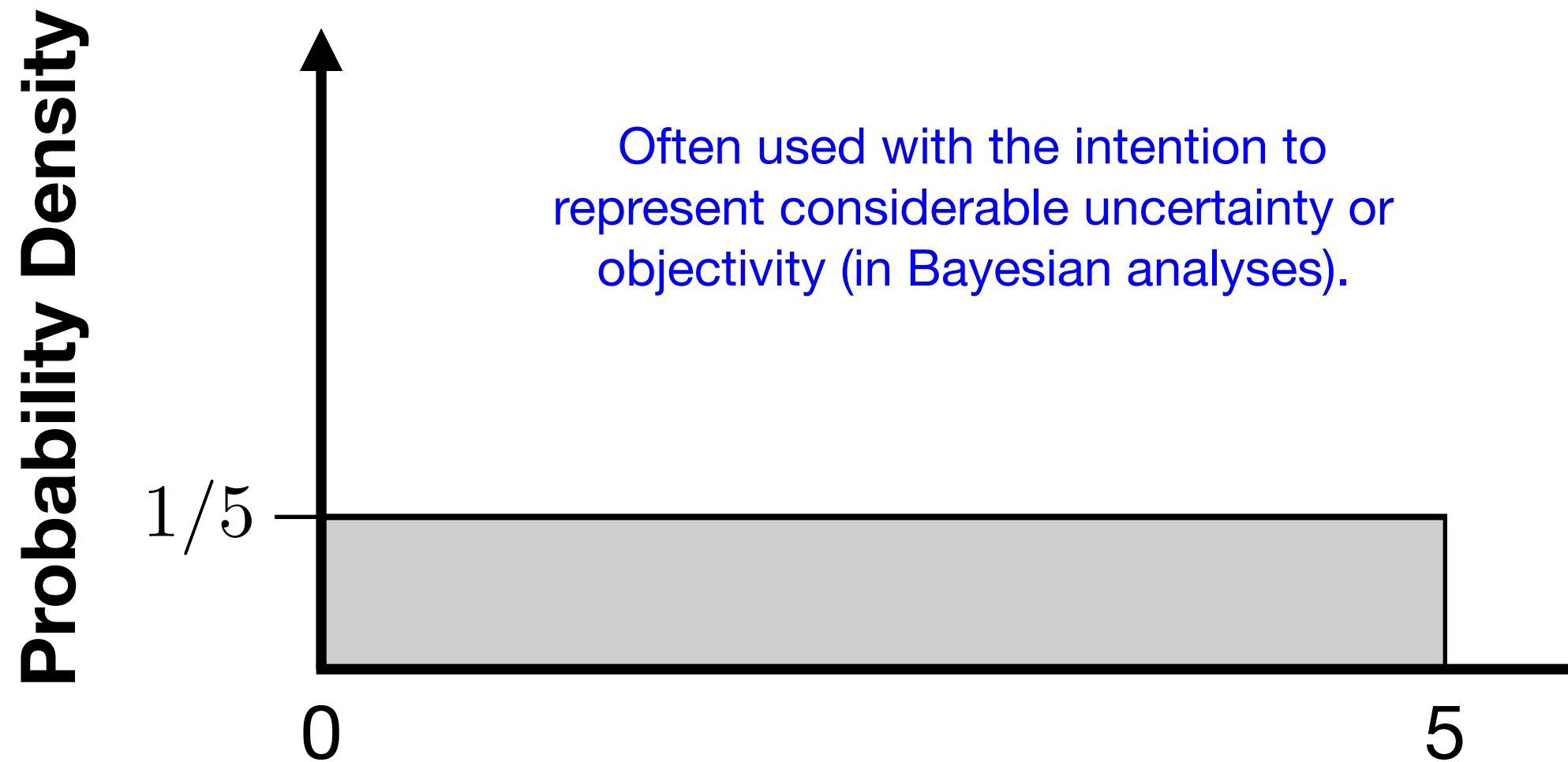
Continuous Uniform Distribution



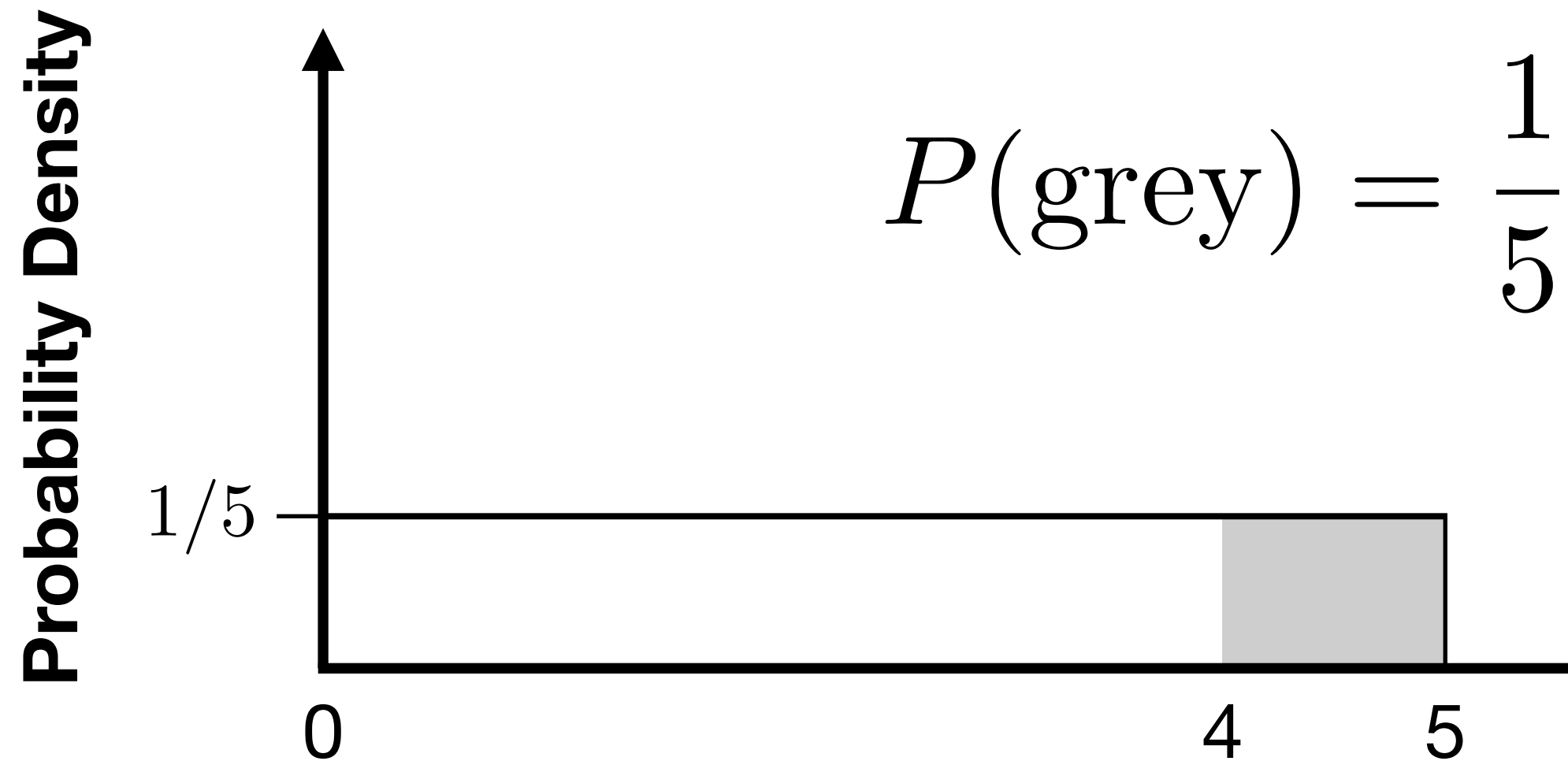
Continuous Uniform Distribution



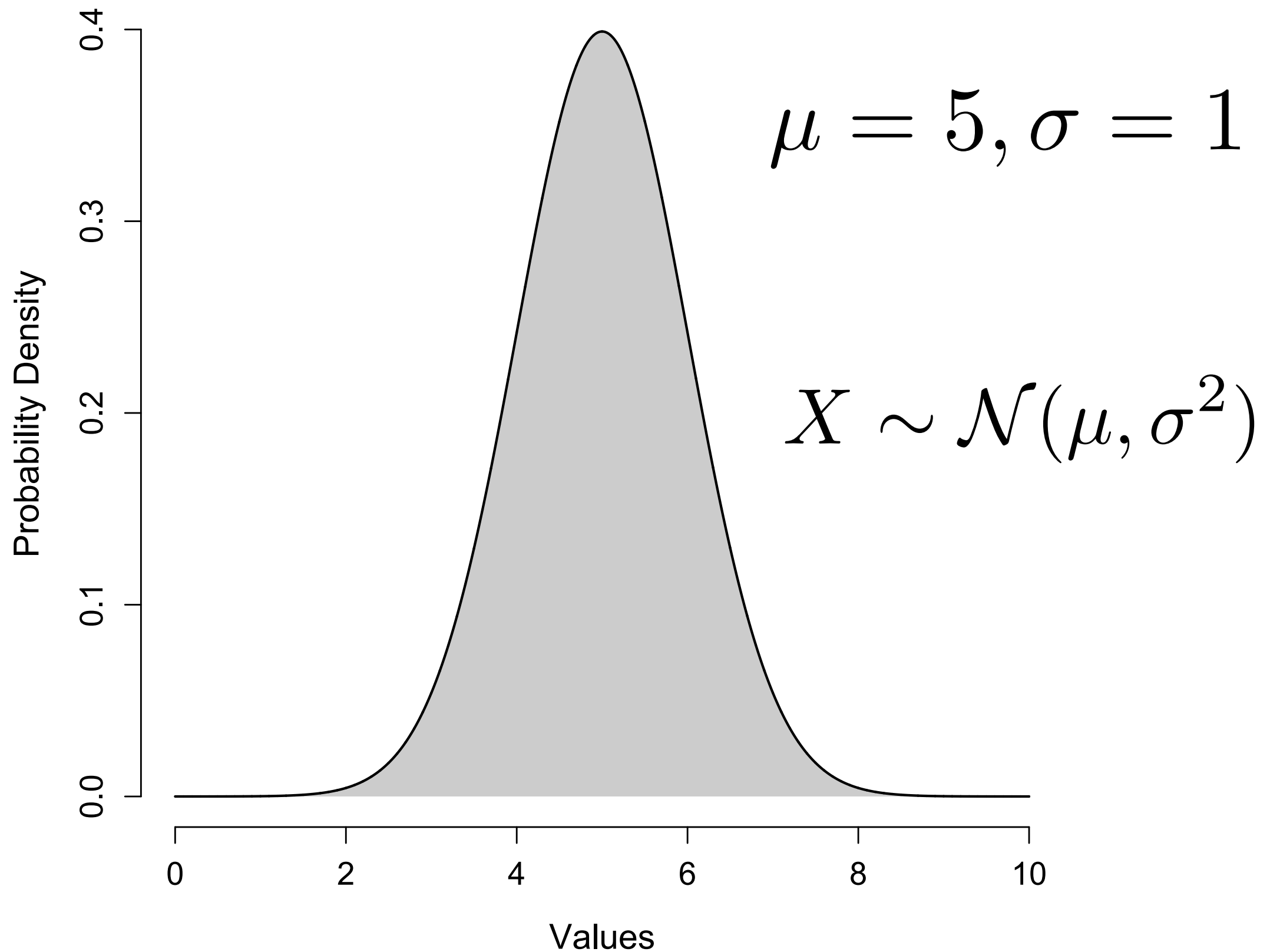
Continuous Uniform Distribution



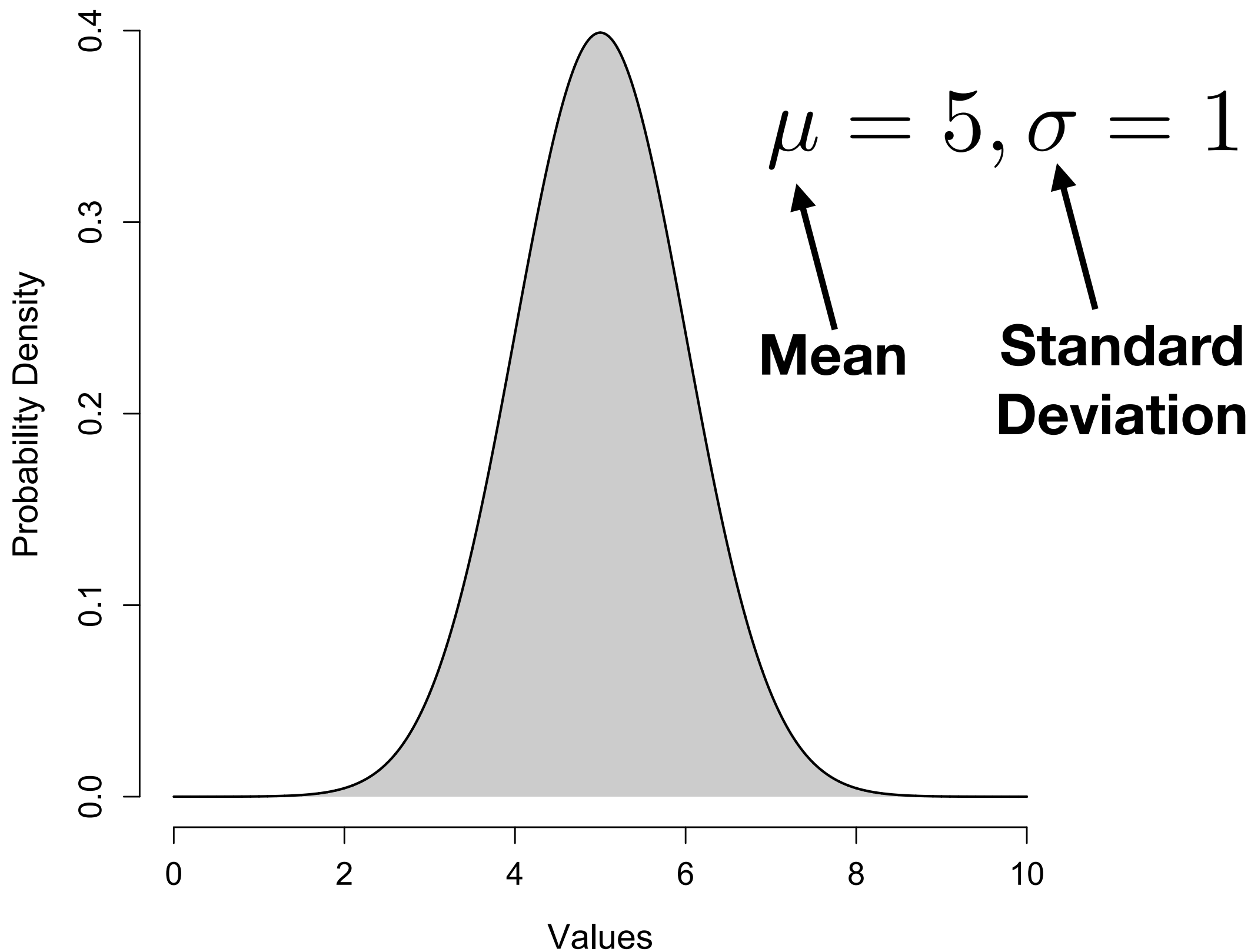
Continuous Uniform Distribution



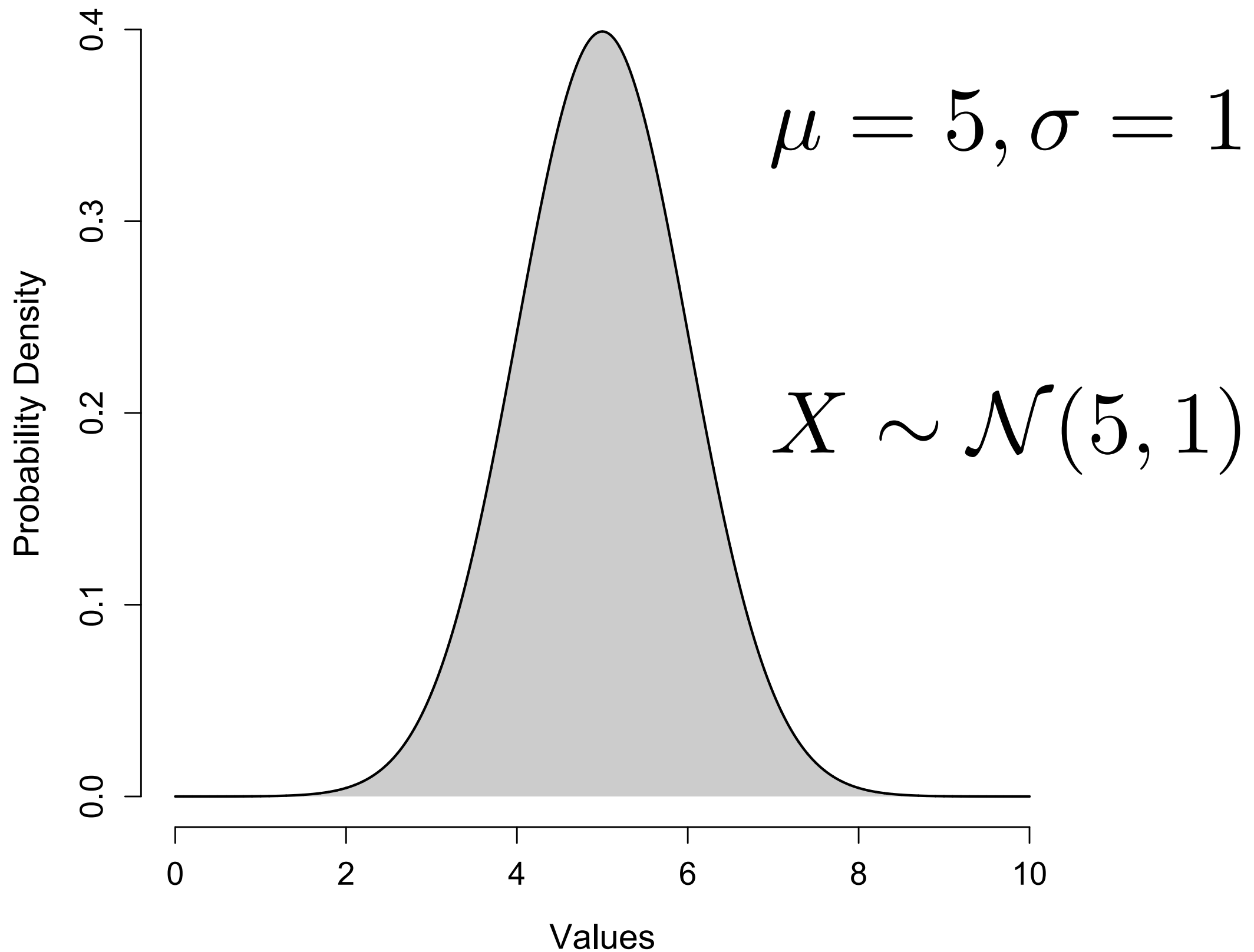
Normal Distribution



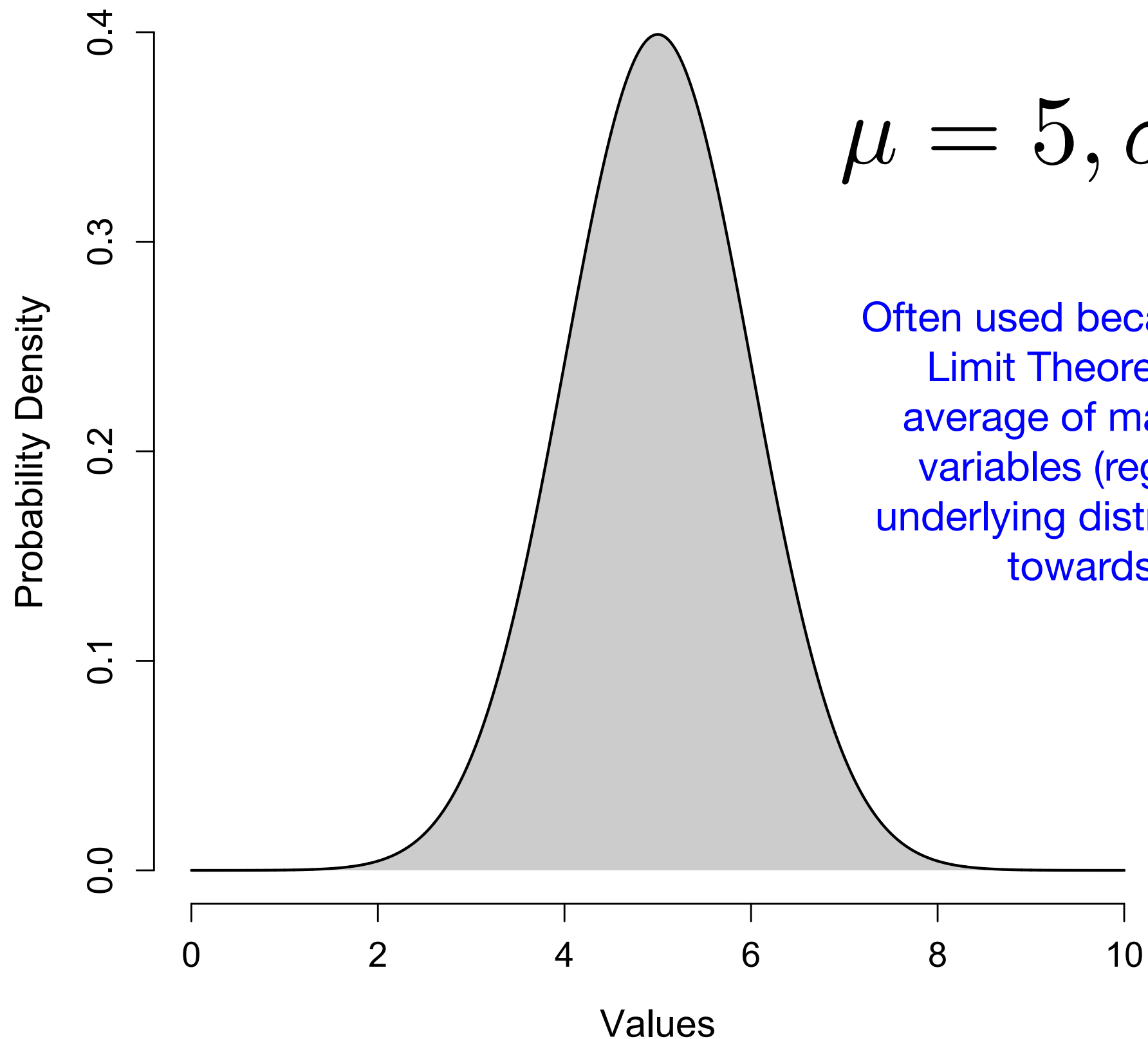
Normal Distribution



Normal Distribution



Normal Distribution



$$\mu = 5, \sigma = 1$$

Often used because of the Central Limit Theorem - the sum or average of many independent variables (regardless of their underlying distributions) will tend towards a Normal.

Variance

Variance is the expectation of the squared deviation of a random variable from its mean.

$$\text{Var}(X) = \sigma^2(X) = \text{E}[(X - \mu)^2]$$

Variance (Standard Deviation)

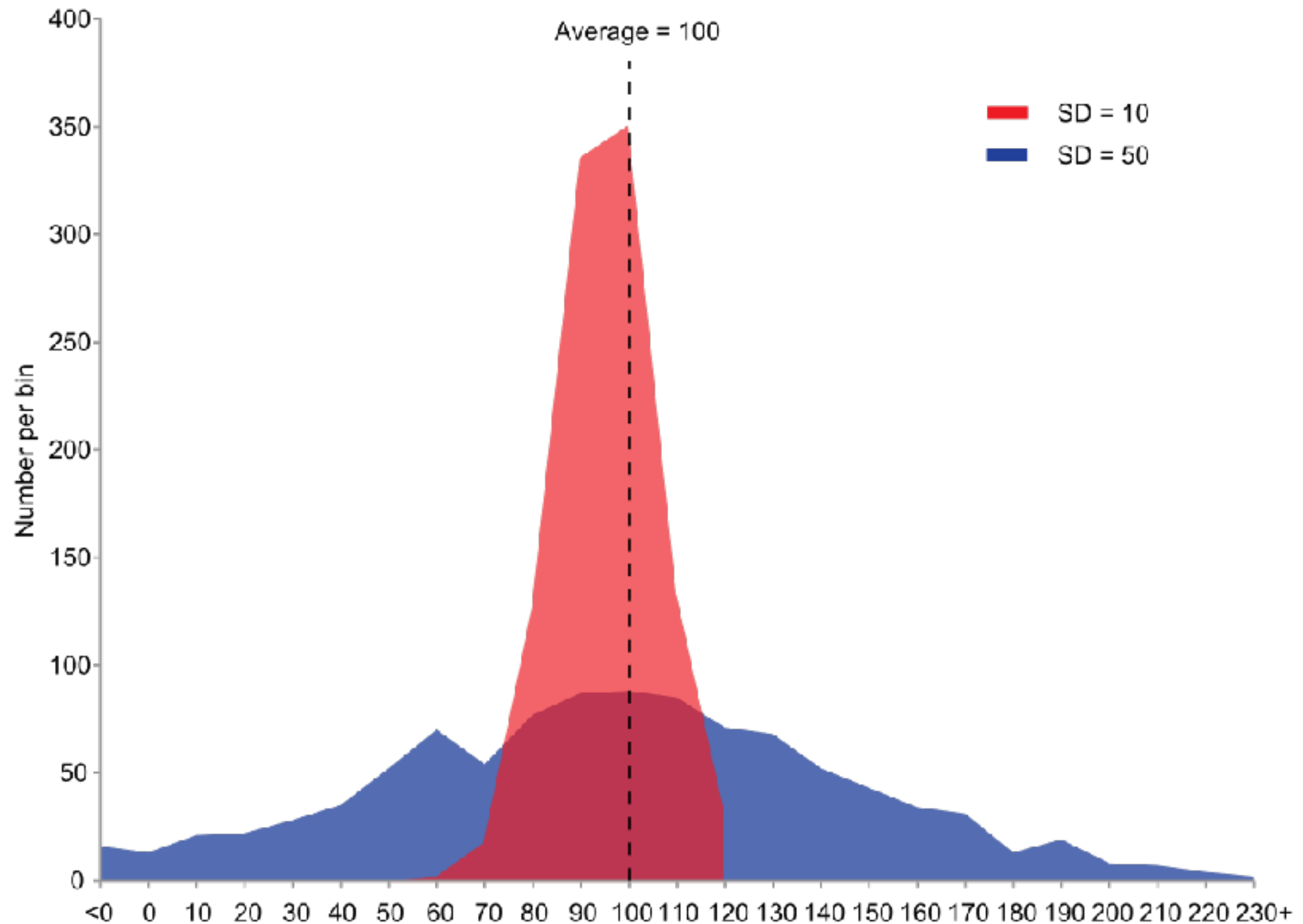
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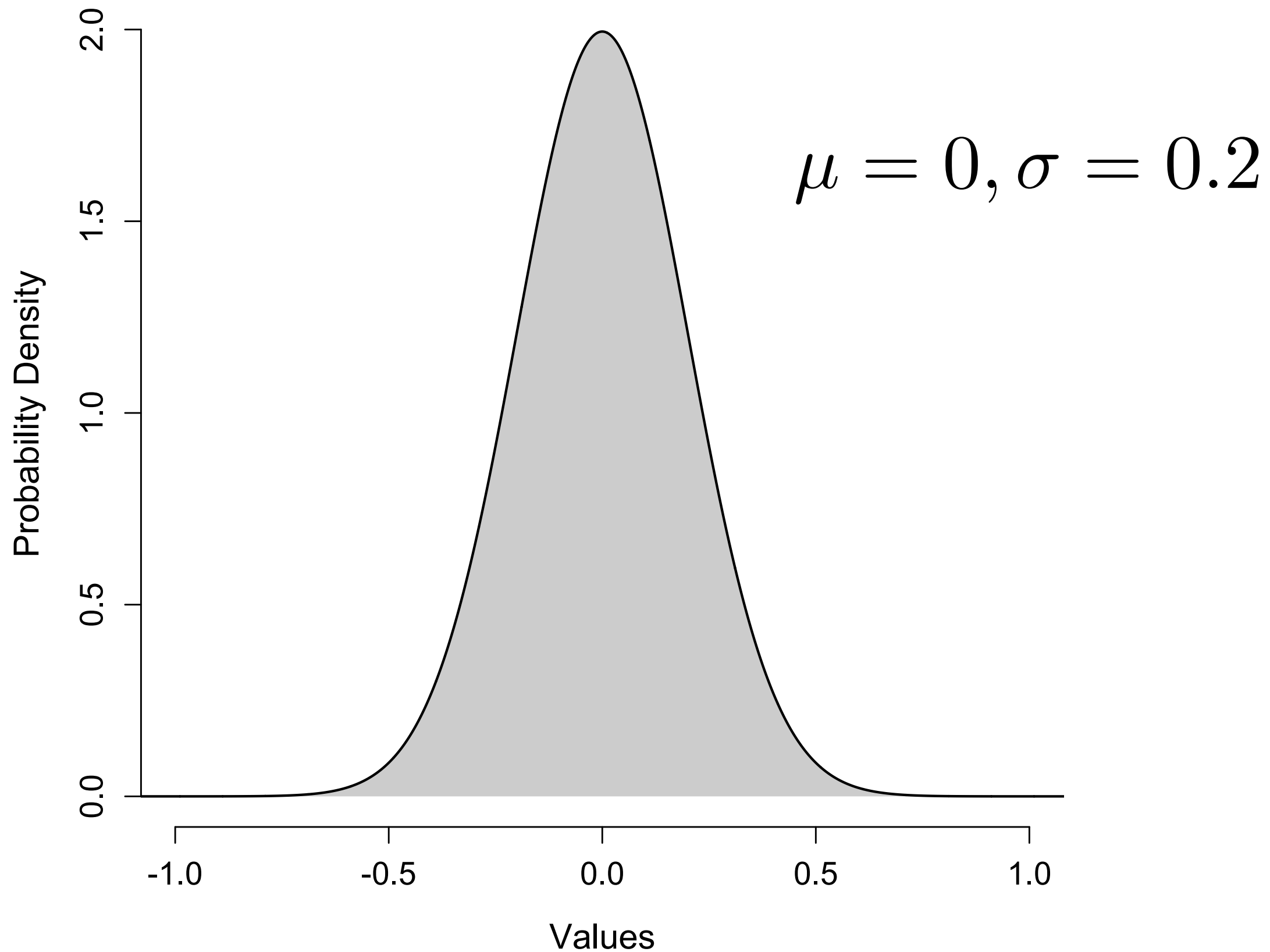
The standard deviation of a random variable is the square root of its variance.

$$\text{sd}(X) = \sigma(X) = \sqrt{\text{E}[(X - \mu)^2]}$$

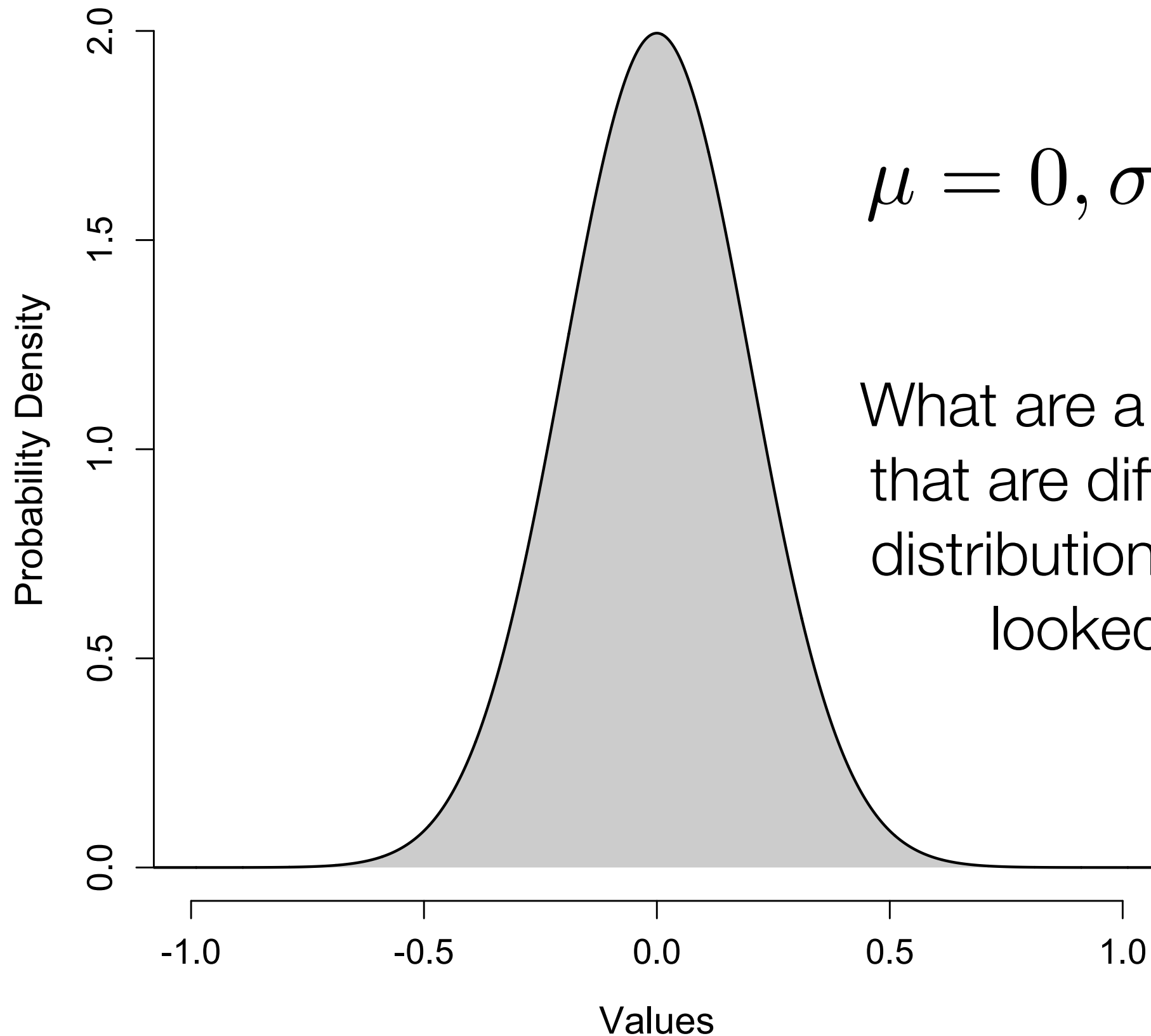
Standard Deviation / Variance



Normal Distribution



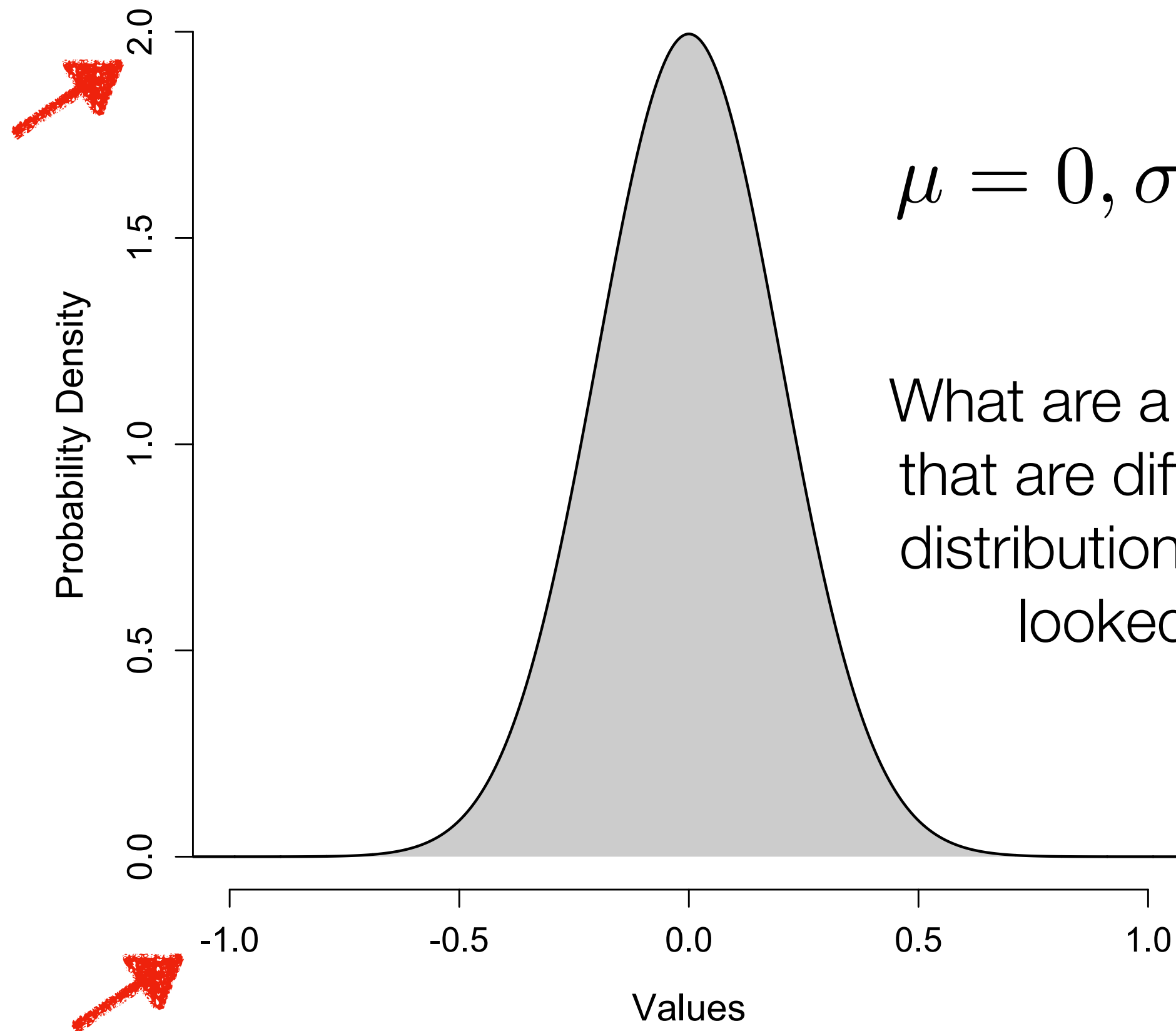
Normal Distribution



$$\mu = 0, \sigma = 0.2$$

What are a couple of things that are different about this distribution than any we've looked at before?

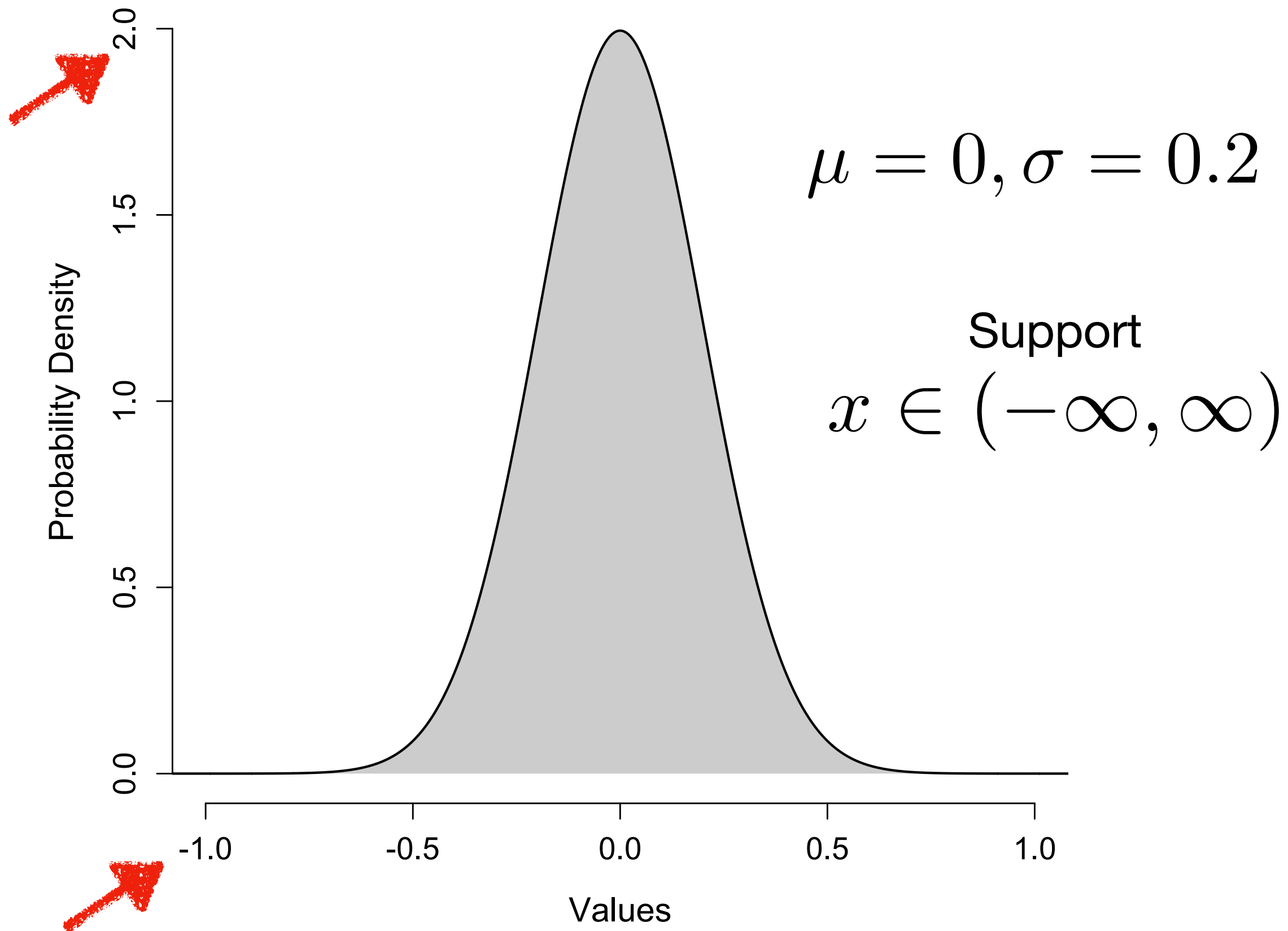
Normal Distribution



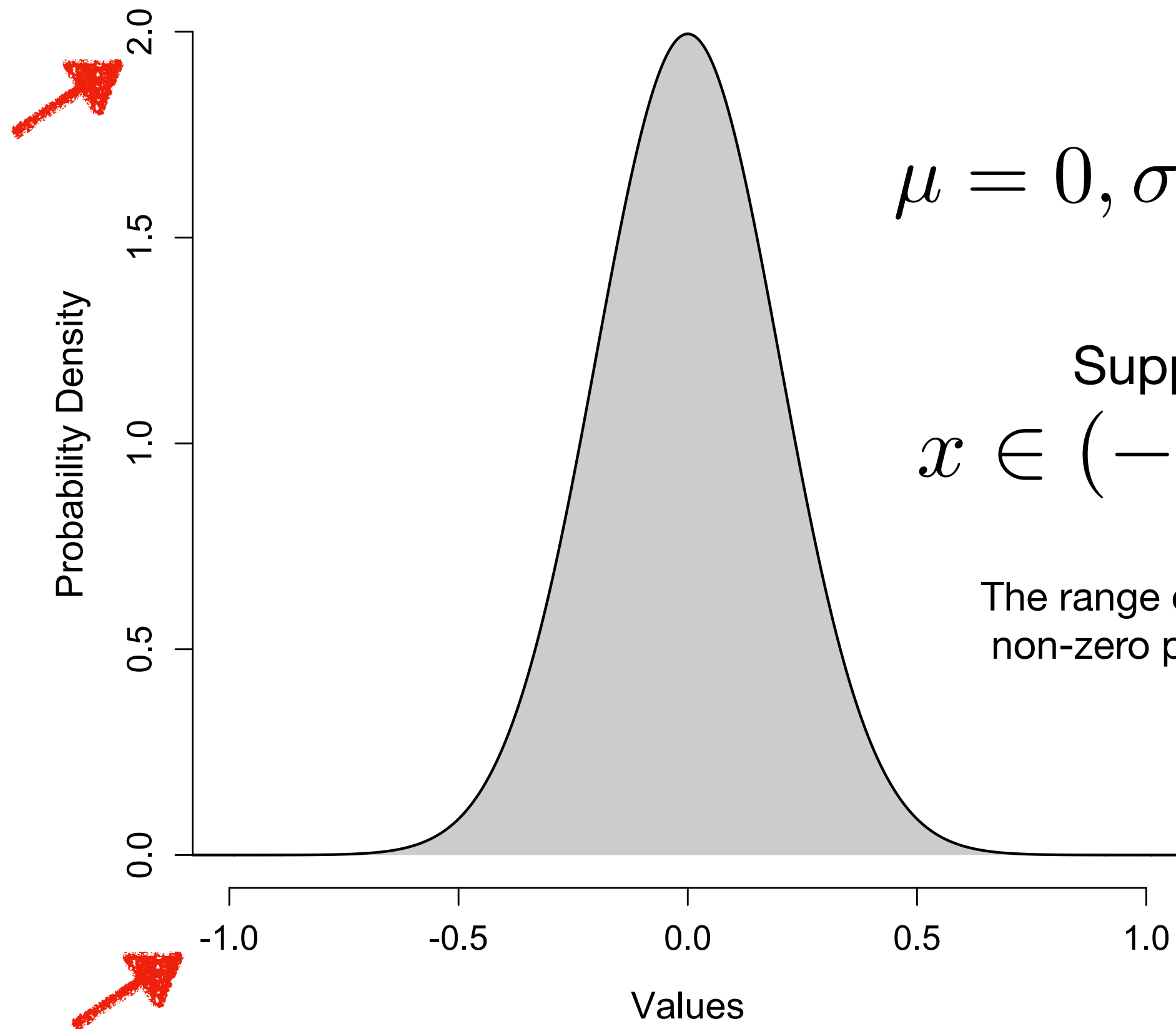
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What are a couple of things that are different about this distribution than any we've looked at before?

Normal Distribution



Normal Distribution



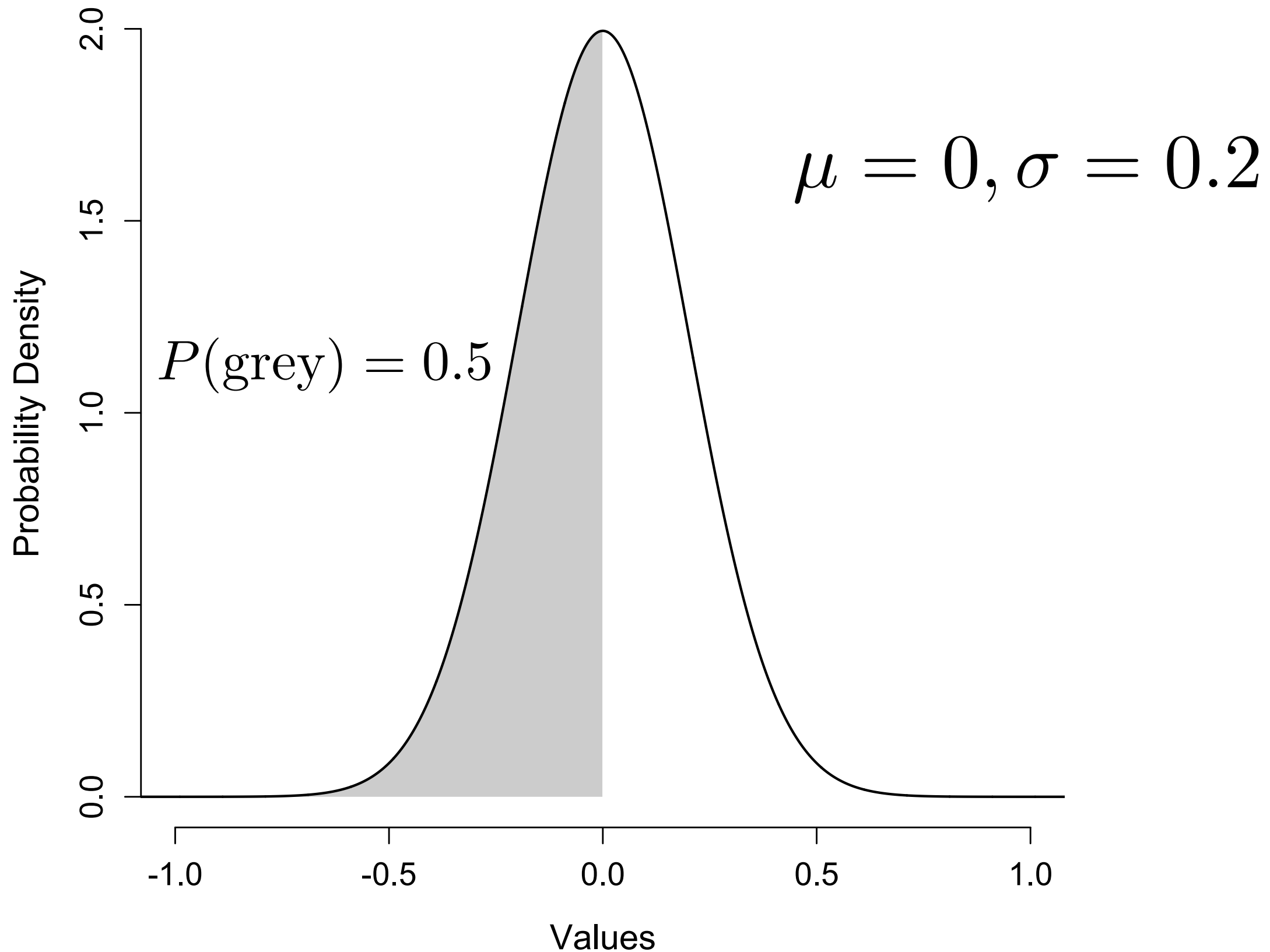
$$\mu = 0, \sigma = 0.2$$

Support

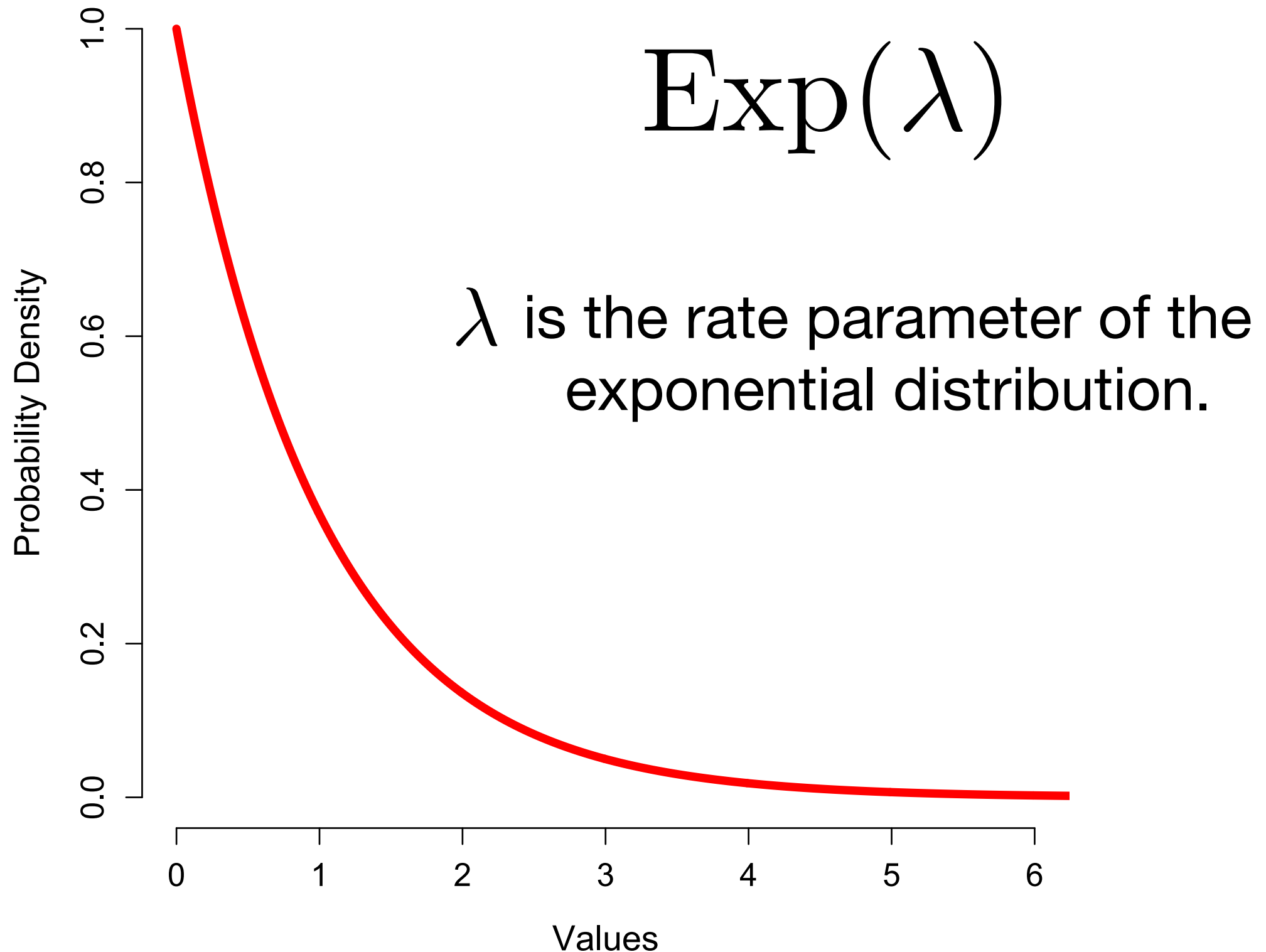
$$x \in (-\infty, \infty)$$

The range of values that have
non-zero probability density.

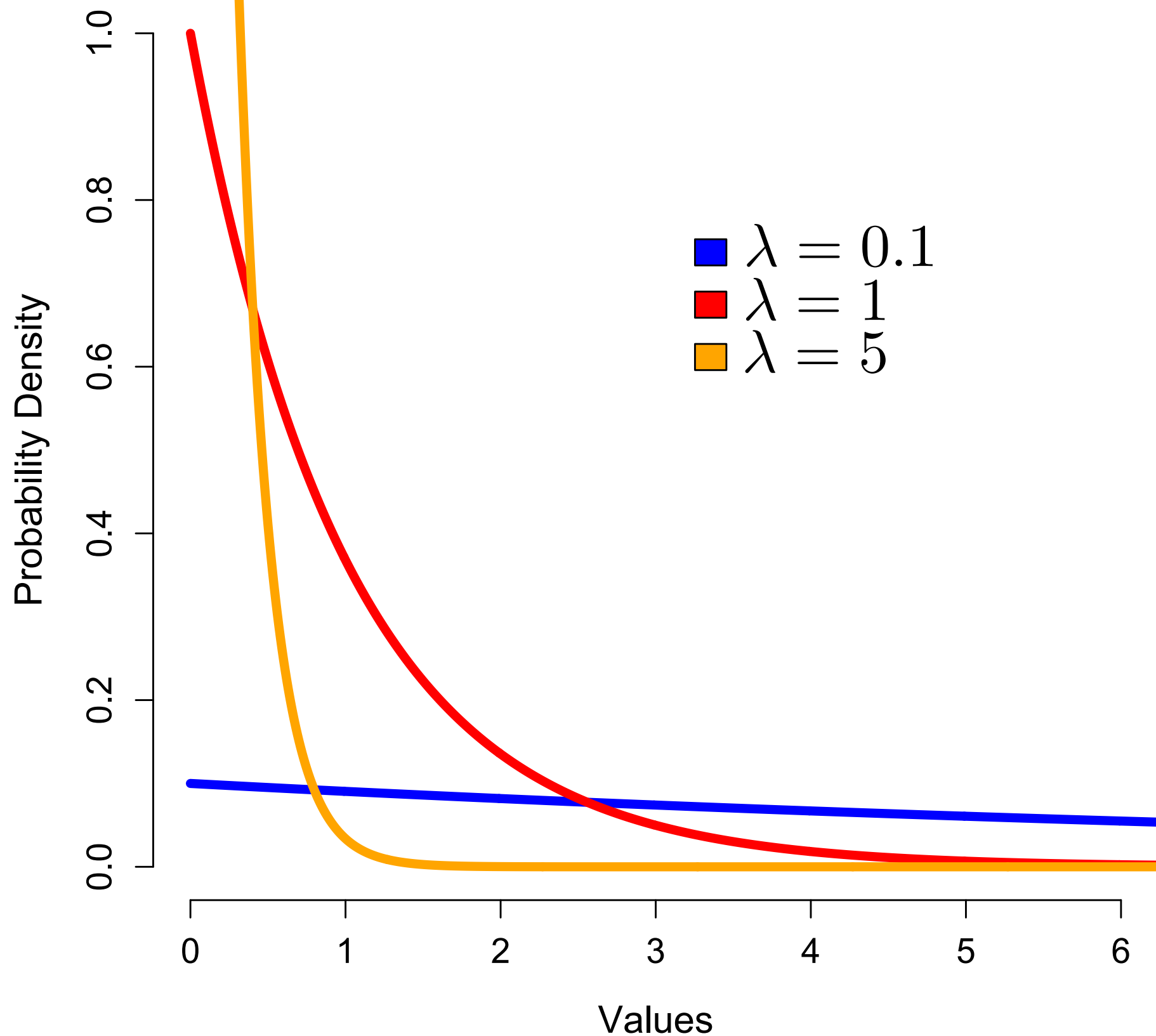
Normal Distribution



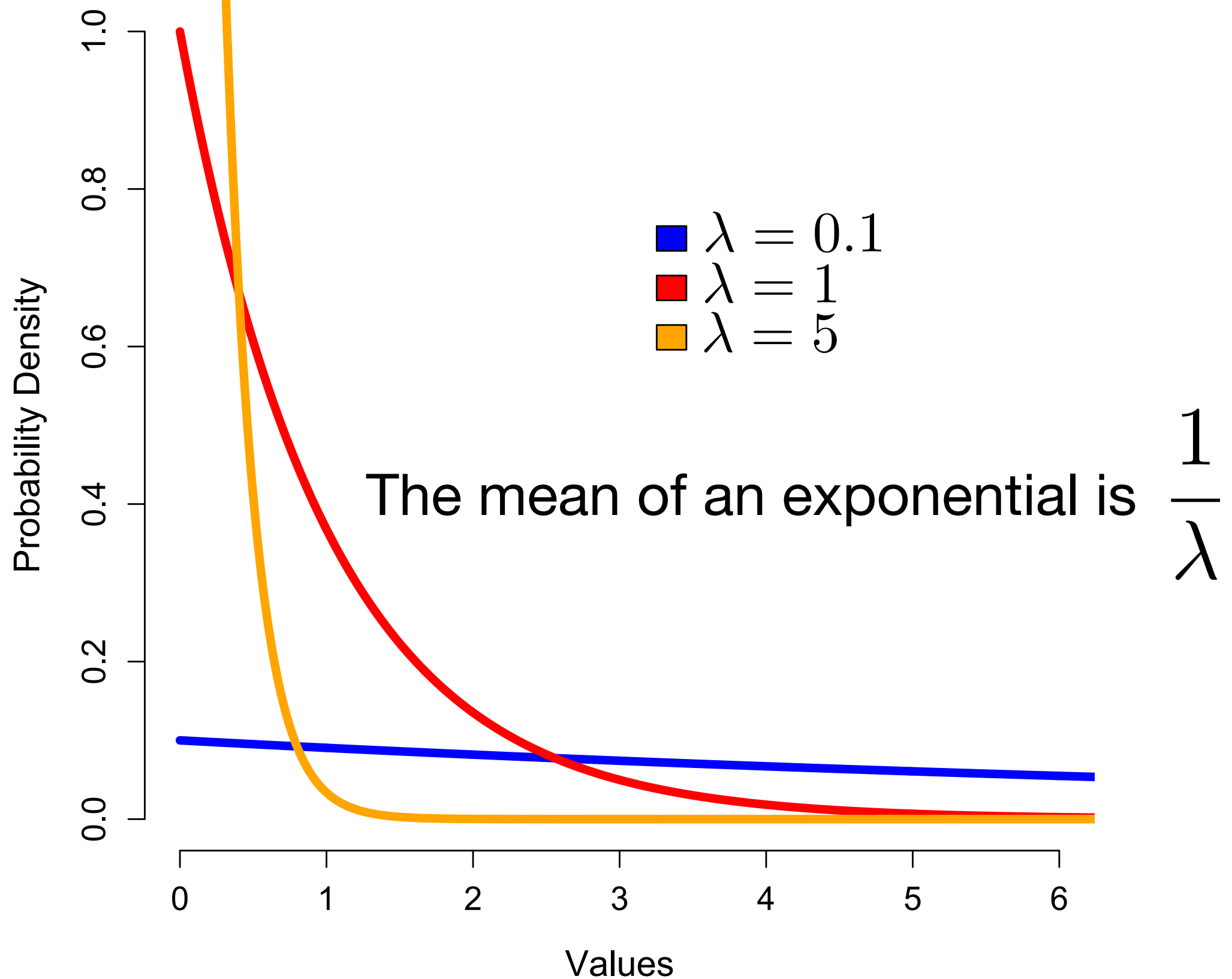
Exponential Distribution



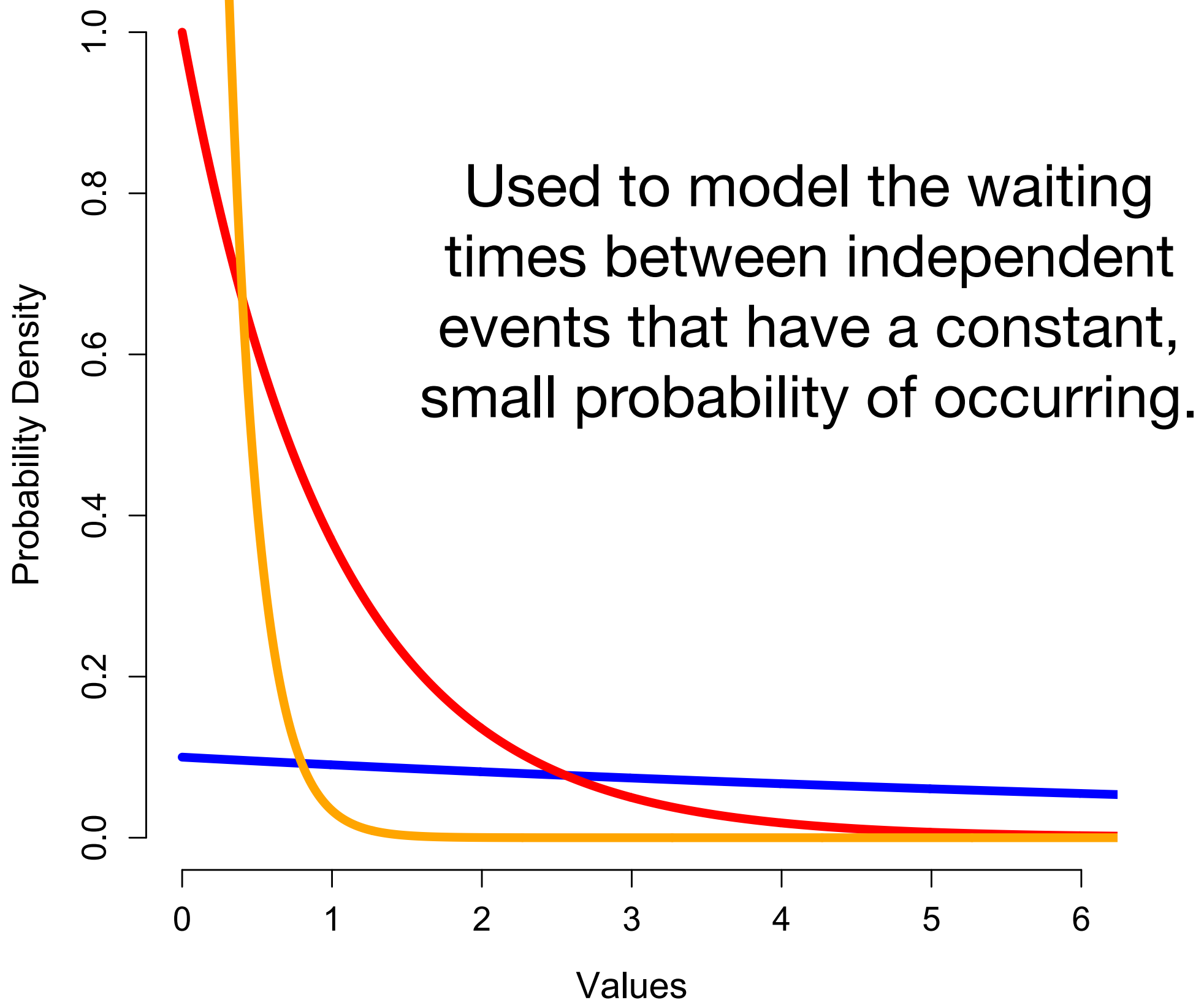
Exponential Distribution



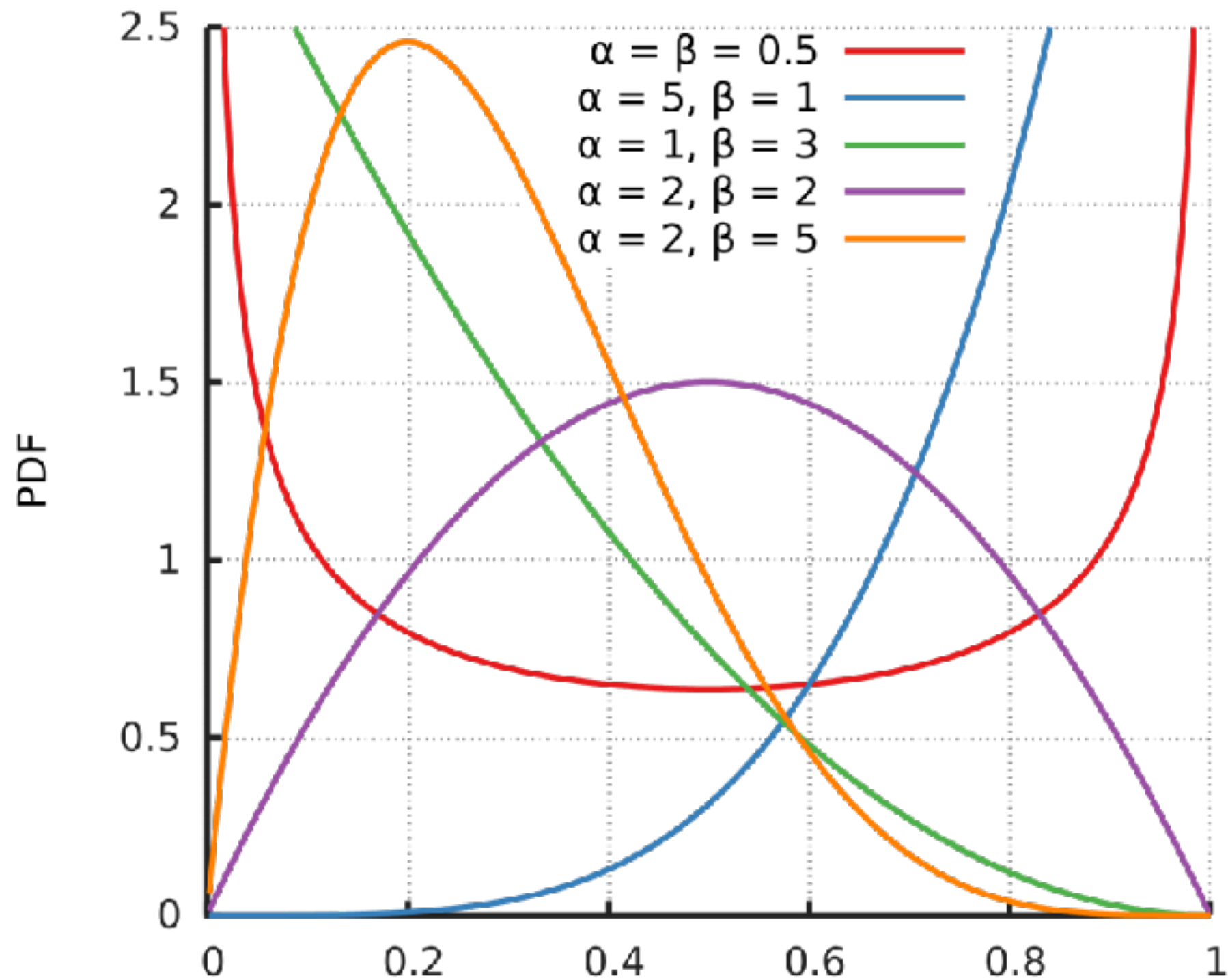
Exponential Distribution



Exponential Distribution



Beta Distribution

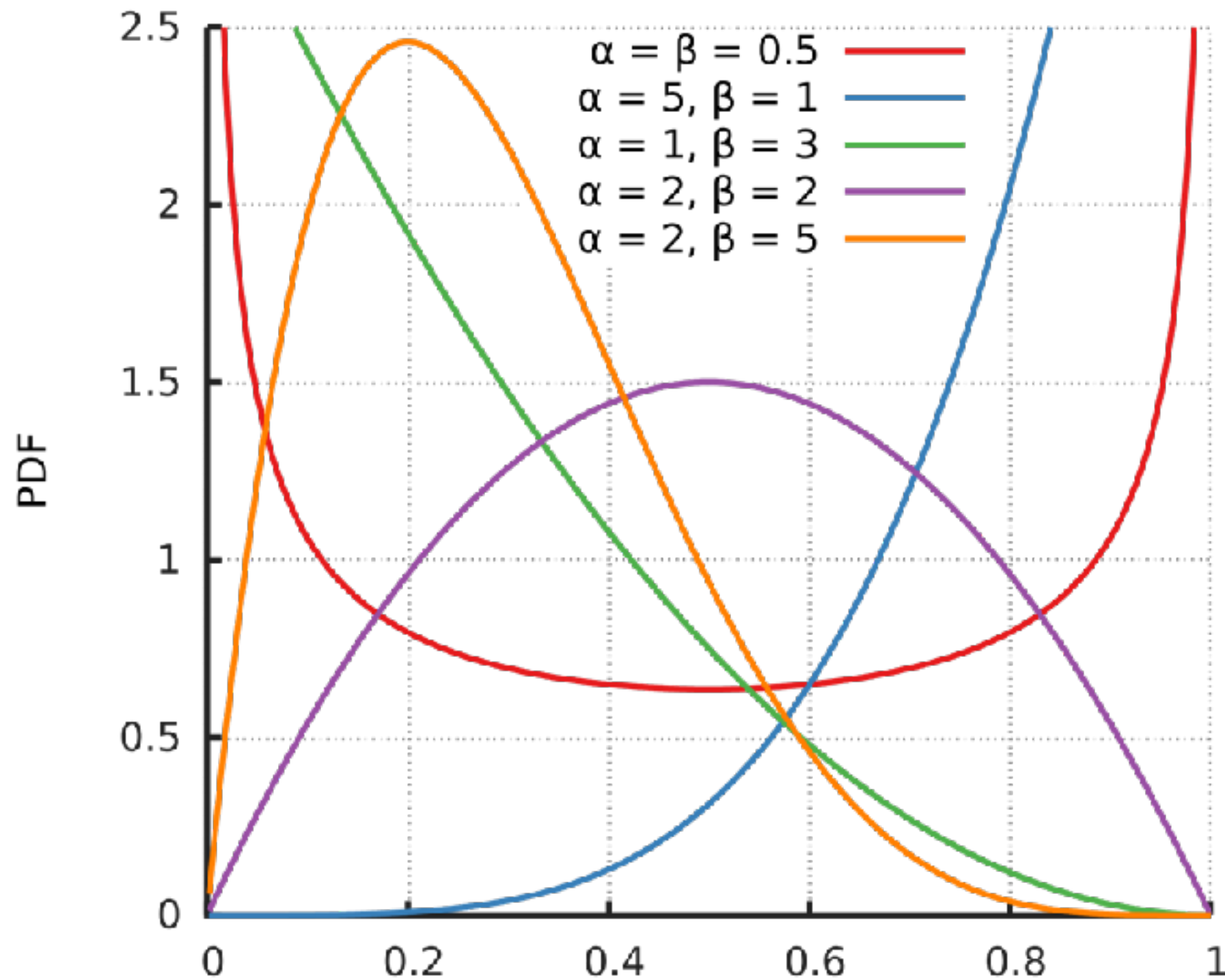


Two Shape Parameters
 α and β

What is the effect of
changing these
parameter values?

What is the **support** of
this distribution?

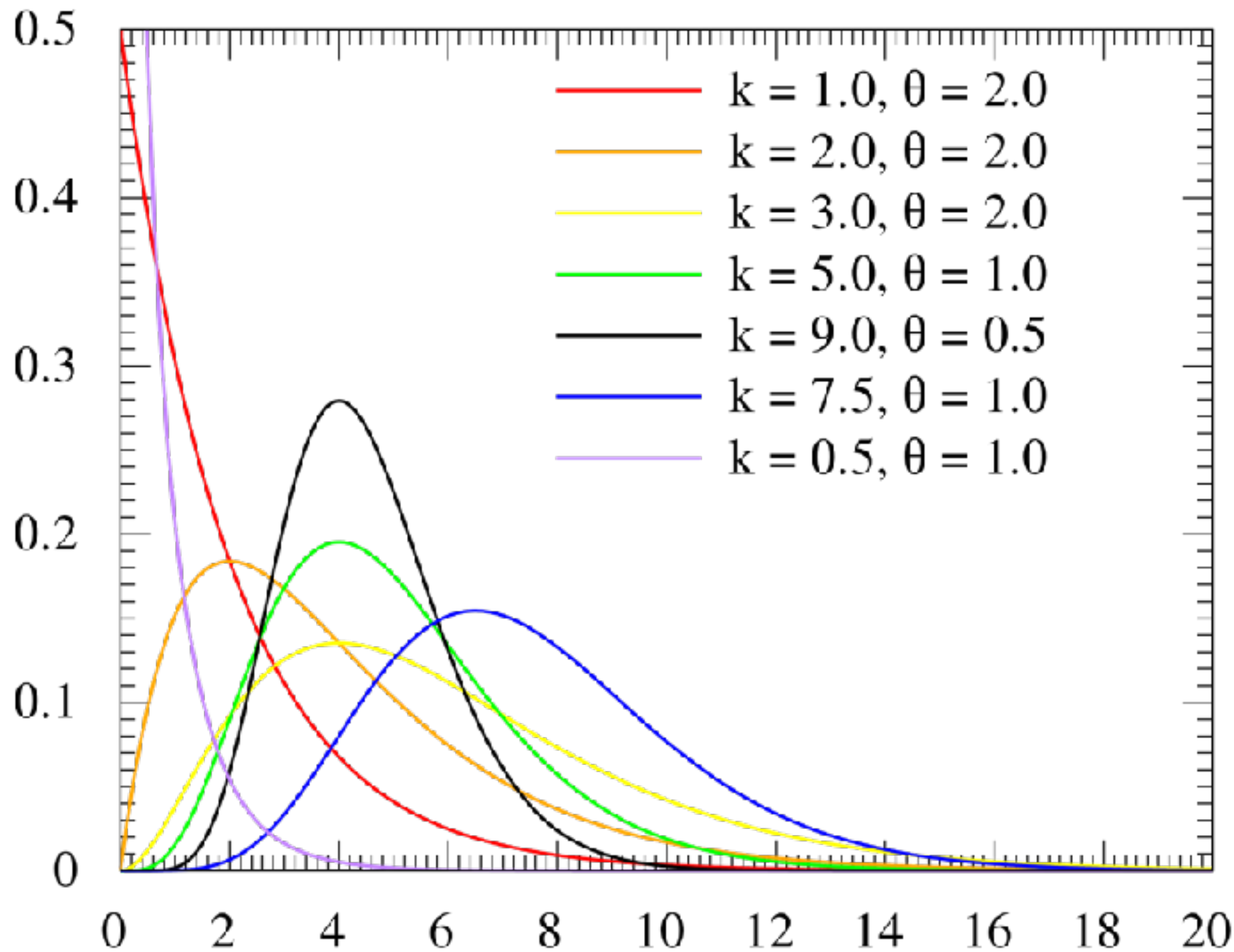
Beta Distribution



Support
 $x \in (0, 1)$

Often used as a flexible
distribution to model
values between 0 and 1.

Gamma Distribution

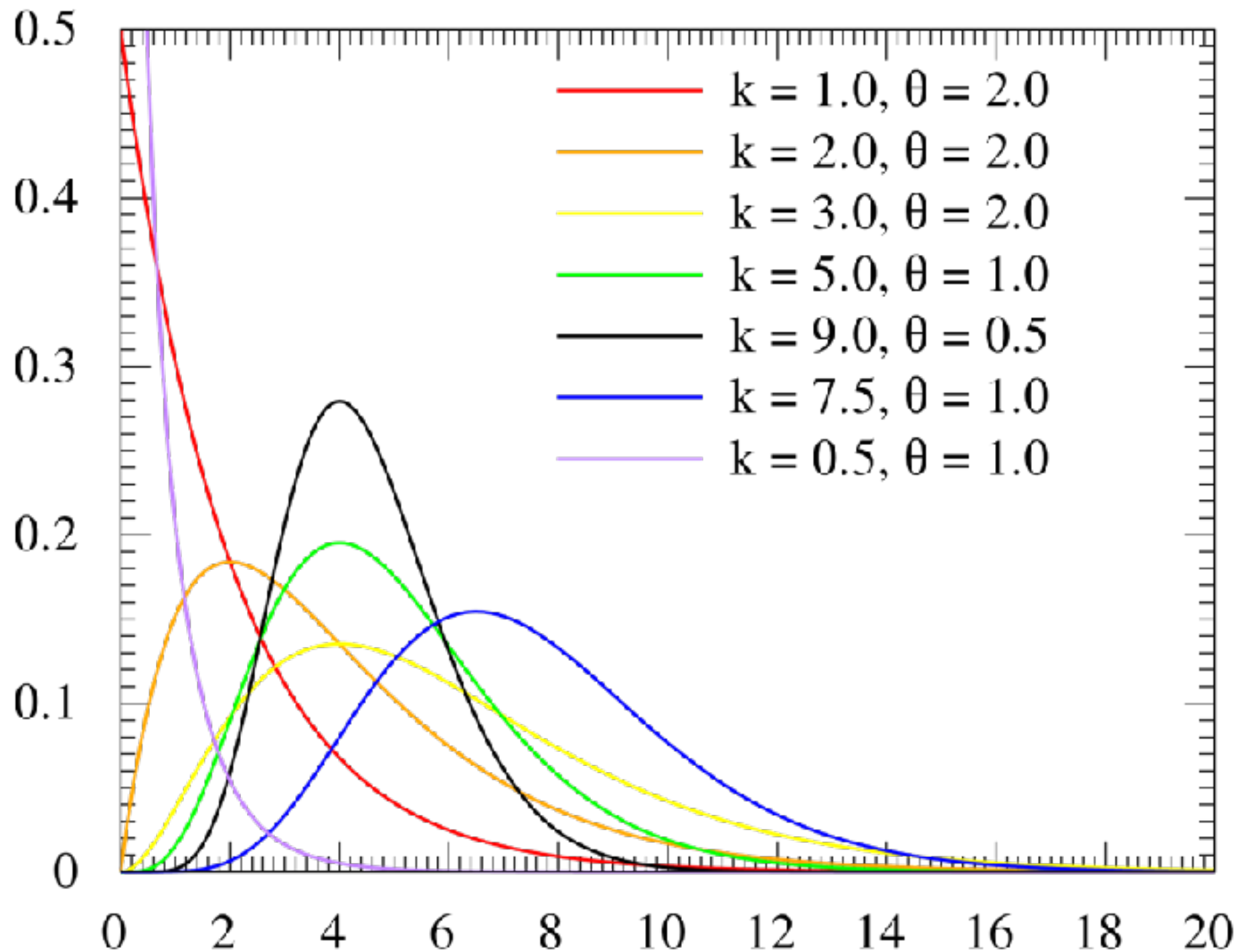


Two Shape Parameters

Shape and Scale
 k and θ

Shape and Rate
 α and β

Gamma Distribution



$$X \sim \Gamma(k, \theta)$$

$$X \sim \Gamma(\alpha, \beta)$$

$$E[X] = k\theta = \frac{\alpha}{\beta}$$

Support

$$x \in (0, \infty)$$

Gamma Distribution

