```
Transformation getTransformation() {
   rotation.setCoordinates(state[0], state[2], state[4], state[6]);
   return rotation:
void setBodyFrameOmega(double[] omega) {
   // use components for clarity
   double q0 = state[0], q1 = state[2], q2 = state[4],
        a3 = state[6]:
   double wx = omega[0]:
   double wv = omega[1]:
   double wz = omega[2];
   state[1] = 0.5*(-q1*wx-q2*wy-q3*wz): // dq0/dt
   state[3] = 0.5*(q0*wx-q3*wy+q2*wz); // dq1/dt
   state[5] = 0.5*(q3*wx+q0*wy-q1*wz): // dq2/dt
   state[7] = 0.5*(-q2*wx+q1*wy+q0*wz); // dq3/dt
   updateVectors():
public double[] getBodyFrameOmega() {
   return omegaBody:
public double[] getBodyFrameAngularMomentum() {
   return angularMomentumBody:
void updateVectors() {
   double q0 = state[0], q1 = state[2], q2 = state[4].
        q3 = state[6];
   omegaBody[0] = 2*(-q1*state[1]+q0*state[3]+q3*state[5]-
        q2*state[7]);
   omegaBody[1] = 2*(-q2*state[1]-q3*state[3]+q0*state[5]+
        g1*state[7]):
   omegaBody[2] = 2*(-q3*state[1]+q2*state[3]-q1*state[5]+
        g0*state[7]):
   angularMomentumBody[0] = I1*omegaBody[0]:
   angularMomentumBody[1] = I2*omegaBody[1];
   angularMomentumBody[2] = I3*omegaBody[2];
public void advanceTime() {
   solver.step():
   double norm = 1/Math.sqrt(state[0]*state[0]+state[2]*state[2]+
        state[4]*state[4]+state[6]*state[6]):
   state[0] *= norm;
   state[2] *= norm;
   state[4] *= norm;
   state[6] *= norm:
   updateVectors():
public double[] getState() {
   return state:
```

```
public void getRate(double[] state. double[] rate) {
   computeBodyFrameAcceleration(state);
   double sum = 0:
  for (int i = 1; i < 9; i += 2) { // sum the g dot values
     sum += state[i]*state[i]:
   sum = -2.0*sum:
  // use g components for clarity
  double q0 = state[0], q1 = state[2], q2 = state[4],
        \sigma 3 = state[6]:
   rate[0] = state[1]:
   rate[1] = 0.5*(-g1*wxdot-g2*wydot-g3*wzdot+g0*sum):
   rate[2] = state[3]:
   rate[3] = 0.5*(a0*wxdot-a3*wvdot+a2*wzdot+a1*sum):
   rate[4] = state[5]:
   rate[5] = 0.5*(q3*wxdot+q0*wydot-q1*wzdot+q2*sum);
  rate[6] = state[7];
  rate[7] = 0.5*(-q2*wxdot+q1*wydot+q0*wzdot+q3*sum);
  rate[8] = 1.0; // time rate
void computeBodyFrameTorque(double[] state) {
  t1 = t2 = t3 = 0:
void computeBodyFrameAcceleration(double[] state) {
  // use components for clarity
  double q0 = state[0], q1 = state[2], q2 = state[4],
          g3 = state[6]:
  double wx = 2*(-g1*state[1]+g0*state[3]+g3*state[5]-g2*state[7]):
   double wy = 2*(-g2*state[1]-g3*state[3]+g0*state[5]+g1*state[7]):
   double wz = 2*(-q3*state[1]+q2*state[3]-q1*state[5]+q0*state[7]);
   computeBodyFrameTorque(state);
   wxdot = (t1-(I3-I2)*wz*wy)/I1: // Euler's equations of motion
  wydot = (t2 - (I1 - I3) * wx * wz) / I2;
  wzdot = (t3 - (I2 - I1) * wy * wx) / I3;
```

The RigidBody class makes use of the RigidBodyUtil utility class in the ch17 package to handle quaternion normalization and transformations between space and body frames. The RigidBodyUtil class is not listed. The static spaceToBody method multiplies a given vector by (17.34) and the static bodyToSpace method multiplies the given vector by the inverse.

FreeRotationApp and FreeRotationView use a subclass of RigidBody to display the dynamics of free rotation. The FreeRotation subclass does a number of simple housekeeping chores such as computing the principal moments using the formulas for an ellipsoid in Table 17.1. FreeRotationApp animates torque-free rotation by extending AbstractSimulation and implementing the doStep method. These classes are not listed because they are similar to other classes we have studied.

FreeRotationSpaceView shown in Listing 17.13 displays the body, the angular momentum vector, and the angular velocity vector in a Display3DFrame. The body is represented using an ellipsoid whose principal axes are (2a, 2b, 2c), and the orientation of