

```

    public double getStepSize();
}

```

A system of first-order differential equations is now solved by creating an object that implements a particular algorithm and repeatedly invoking the step method for that solver class. The argument for the solver class constructor must be a class that implements the ODE interface. As an example of the use of ODESolver, we again consider the dynamics of a falling particle.

**Listing 3.7** A falling particle program that uses an ODESolver.

```

package org.opensourcephysics.sip.ch03;
import org.opensourcephysics.controls.*;
import org.opensourcephysics.numerics.*;

public class FallingParticleODEApp extends AbstractCalculation {
    public void calculate() {
        // gets initial conditions
        double y0 = control.getDouble("Initial y");
        double v0 = control.getDouble("Initial v");
        // creates ball with initial conditions
        FallingParticleODE ball = new FallingParticleODE(y0, v0);
        // note how particular algorithm is chosen
        ODESolver solver = new Euler(ball);
        // sets time step dt in the solver
        solver.setStepSize(control.getDouble("dt"));
        while(ball.state[0]>0) {
            solver.step();
        }
        control.println("final time = "+ball.state[2]);
        control.println("y = "+ball.state[0]+" v = "+ball.state[1]);
    }

    public void reset() {
        // sets default input values
        control.setValue("Initial y", 10);
        control.setValue("Initial v", 0);
        control.setValue("dt", 0.01);
    }

    // creates a calculation control structure for this class
    public static void main(String[] args) {
        CalculationControl.createApp(new FallingParticleODEApp());
    }
}

```

The ODE classes are located in the numerics package, and thus we need to import this package as done in the third statement of FallingParticleODEApp. We declare and instantiate the variables ball and solver in the calculate method. Note that ball, an instance of FallingParticleODE, is the argument of the Euler constructor. The object ball can be an argument because FallingParticleODE implements the ODE interface.

It would be a good idea to look at the source code of the ODE Euler class in the numerics package. The Euler class gets the state of the system using getState and then sends this state to getRate which stores the rates in the rate array. The state array is then modified

using the rate array in the Euler algorithm. You don't need to know the details, but you can read the step method of the various classes that implement ODESolver if you are interested in how the different algorithms are programmed.

Because FallingParticleODE appears to be more complicated than FallingParticle, you might ask what we have gained. One answer is that it is now much easier to use a different numerical algorithm. The only modification we need to make is to change the statement

```
ODESolver solver = new Euler(ball);
```

to, for example,

```
ODESolver solver = new EulerRichardson(ball);
```

We have separated the physics (in this case a freely falling particle) from the implementation of the numerical method.

### Exercise 3.6 ODE solvers

Run FallingParticleODEApp and compare your results with our previous implementation of the Euler algorithm in FallingParticleApp. How easy is it to use a different algorithm?

## 3.7 ■ EFFECTS OF DRAG RESISTANCE

We have introduced most of the programming concepts that we will use in the remainder of this text. If you are new to programming, you will likely feel a bit confused at this point by all the new concepts and syntax. However, it is not necessary to understand all the details to continue and begin to write your own programs. A prototypical simulation program is given in Listings 3.8 and 3.9. These classes simulate a projectile on the surface of the Earth with no air friction, including a plot of position versus time and an animation of a projectile moving through the air. In the following, we discuss more realistic models that can be simulated by modifying the projectile classes.

**Listing 3.8** A simple projectile simulation that is useful as a template for other simulations.

```

package org.opensourcephysics.sip.ch03;
import java.awt.*;
import org.opensourcephysics.display.*;
import org.opensourcephysics.numerics.*;

public class Projectile implements Drawable, ODE {
    static final double g = 9.8;
    double[] state = new double[5]; // {x,vx,y,vy,t}
    // pixel radius for drawing projectile
    int pixRadius = 6;
    EulerRichardson odeSolver = new EulerRichardson(this);

    public void setStepSize(double dt) {
        odeSolver.setStepSize(dt);
    }

    public void step() {

```