Input: Initial path  $X_0$ , initial index  $k_0$ , initial displacement direction  $s_0$ , displacement magnitude  $\Delta k$ ,

```
\{X^{\rm o}, k^{\rm o}, s^{\rm o}\} \ \leftarrow \{X_0, k_0, s_0\}
```

for trial < n\_trials do

```
Draw uniform \hat{k}^{\circ} \in \{k^{\circ}, k^{\circ} + s^{\circ} \Delta k\}: return \hat{k}^{\circ}
if InBounds(\hat{k}^{\circ}, L(X^{\circ})) then
      r^{\text{SP}} \leftarrow X^{\text{o}} \text{ at } \hat{k}^{\text{o}}
      X^{\text{fwd}} \leftarrow \text{IntegrateToState}(x^{\text{SP}})
      X^{\text{rv}} \leftarrow \text{IntegrateToState}(\bar{x}^{\text{SP}})
      X^{\text{n}} \leftarrow \texttt{ConcatenatePath}(\bar{X}^{\text{rv}}, X^{\text{fwd}})
      \hat{k}^{\rm n} \leftarrow {\rm Index \ of \ } x^{\rm SP} {\rm \ on \ } X^{\rm n}
      Draw uniform s^n \in \{-1, 1\}: return s^n
      Draw uniform k^{n} \in \{\hat{k}^{n}, \hat{k}^{n} + s^{n}\Delta k\}:
         return k^n
      p_{\rm acc}(X^{\rm o} \to X^{\rm n}) \leftarrow H_{\rm AB}(X^{\rm n}) \min \left[1, \frac{L(X^{\rm o})}{L(X^{\rm n})}\right]
      if rand() < p_{acc}(X^{o} \rightarrow X^{n}) and
         InBounds(k^n, L(X^n)) then
        \{X^{o}, k^{o}, s^{o}\} \leftarrow \{X^{n}, k^{n}, s^{n}\}
      end
end
```

Add  $\{X^{o}, k^{o}, s^{o}\}$  to the ensemble

 $trial \leftarrow trial+1$ 

end