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SUPERIOR SCHOOL OF COMPUTER SCIENCES (ESCOM)  
INSTITUTO POLITÉCNICO NACIONAL (IPN)

# How long would it take to break AES?

PARTIAL 2

Oscar Andrés Rosas Hernandez

October 16, 2019

# Chapter 1

## Exercise

So, we have 128 bits, that means that we have to test  $2^{128}$  keys.

- We have a budget of 1000000 dollars.
- Each processor cost 10 dollars.
- So, we can have up to 100000 processors.
- Each processor take  $t$  time to check a key. (let  $t = 10^{-9}$  seconds)
- So all of them will take  $\frac{t}{100000}$  to check a key.

Now, we have to divide the result by  $\frac{1}{60*24}$  to get days, not seconds.

So, the expression look something like:

$$num\_days = 2^{128} \times \frac{t}{100000} \times \frac{1}{60 * 24}$$

Now, Moore's law says that each 18 months we double we performance, so:

$$num\_days = 2^{128} (0.5)^{times} \times \frac{t}{100000} \times \frac{1}{60 * 24}$$

We can solve for times and get this formula:

$$times = \log_{0.5} \left( \frac{7}{2^{128} \times \frac{t}{100000} \times \frac{1}{60 \times 24}} \right)$$

This gives: 68.2 iterations, that means 102.291 years.