PWDFT.jl Documentation

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Part I. User Guide

1 Overview

PWDFT.jl is a Julia package to carry out (electronic) density functional theory calculations on materials. It uses plane wave basis sets to discretize Kohn-Sham equations. It also uses pseudopotentials to replace strong Coulombic nuclei-electron interactions ¹.

I assumes that the readers already have some experience with similar electronic structure programs such as Quantum Espresso, ABINIT, VASP, and others.

PWDFT.jl uses Hartree atomic units internally.

2 Installation

You need the following to use PWDFT. jl:

- Julia version 0.7 or higher
- LibXC
- SPGLIB
- C compiler to compile LibXC and SPGLIB

PWDFT.jl is a Julia package, so you need to copy (or clone) under Julia's package depot so that it can be used within Julia. Presently, it is not yet a registered package. There are at least two ways of doing this.

The first way is using Julia's package manager. The following command can be issued at the Julia's console.

```
Pkg.add(PackageSpec(url="https://github.com/f-fathurrahman/PWDFT.jl"))
```

The second way is to use Julia's development directory located at \$HOME/.julia/dev. To enable this, please put the following in the your \$HOME/.julia/config/startup.jl file:

```
push!(LOAD_PATH, expanduser("~/.julia/dev"))
```

I usually sym-links my original PWDFT.jl directory to a directory named PWDFT (without .jl part) under \$HOME/.julia/dev.

```
ln -fs /path/to/PWDFT.jl ~/.julia/dev/PWDFT
```

To test the installation, you can run the following:

```
using PWDFT
```

at the Julia's console. If there are no error messages then the installation is OK. 2

¹ You can carry out the calculation with full potential anyway, however this will requires a lot of plane waves (large cutoff energy)

² This does not check the LibXC or SPGLIB installation.

2.1 LibXC

PWDFT.jl uses LibXC to calculate exchange correlation energy and potential. The following commands can be used to configure, build, and install LibXC in your computer.

```
./configure --prefix=/home/user/softwares/libxc \
   --disable-fortran --enable-shared
make
make install
```

2.2 SPGLIB

PWDFT.jl uses SPGLIB to generate reduced k-point for integration over Brillouin zone. The following commands can be used to configure, build, and install SPGLIB in your computer.

```
cd spglib-master
mkdir build
cd build
cmake -D CMAKE_INSTALL_PREFIX=/home/user/softwares/spglib
make
make install
```

3 Total energy calculation

We need to prepare several things before using PWDFT.jl:

- Atomic structures: coordinates and unit cell
- Pseudopotentials

This code will initialize a hydrogen molecule (H₂) inside a box of $16 \times 16 \times 16$ bohr.

```
atoms = Atoms(
    xyz_string="""
2

H     3.83653478     4.23341768     4.23341768
    H     4.63030059     4.23341768     4.23341768
""",
    LatVecs=gen_lattice_sc(16.0))
```

After creating an instance of Atoms, we need to create an instance of Hamiltonian:

```
DIR_PWDFT = joinpath(dirname(pathof(PWDFT)), "..")
DIR_PSP = joinpath(DIR_PWDFT, "pseudopotentials", "pade_gth")
pspfiles = [joinpath(DIR_PSP, "H-q1.gth")]
ecutwfc = 30.0
Ham = Hamiltonian(atoms, pspfiles, ecutwfc)
```

Once the instance of Hamiltonian is initialized, we can solve the Kohn-Sham problem by SCF method (or your own solver!), for example:

```
KS_solve_SCF! (Ham)
```

During the call of this function several info will be printed to stdout. You can redirect this print out to file if you want to save the print out and analyze it later

```
# save the reference to original stdout
stdout_orig = stdout
# Open file for writing
fileout = open("LOG_"*molname, "w")
# Redirect stdout
redirect_stdout(fileout)
# Solve the Kohn-Sham problem
KS_solve_SCF!(Ham)
# Close IO
close(fileout)
```

KS_solve_SCF! has several options that you can used. For more information you can see the original code in src/KS_solve_SCF.jl.

Part II. Implementation Notes

In this note, I will describe several user-defined data types that are used throughout PWDFT.jl. Beginners are not expected to know them all, however they are needed to know the internal of PWDFT.jl.

When referring to a file, I always meant to the file contained in the src/ directory.

Even though it is not strictly required in Julia, I have tried to always use type annotations.

4 Atoms

Atoms can be used to represent molecular or crystalline structures. This type is implemented in the file src/Atoms.jl.

It has the following fields:

- Natoms::Int64: number of atoms present in the system
- Nspecies:: Int64: number of atomic species present in the system
- positions::Array{Float64, 2}: An array containing coordinates of atoms in bohr units. Its shape is (3, Natoms)
- atm2species::Array{Int64,1}: An array containing mapping between atom index to species index. Its shape is (Natoms,)
- atsymbs::Array{String,1}: An array containing atomic symbols for each atoms. Its shape is (Natoms,).
- SpeciesSymbols::Array{String, 1}: An array containing unique symbols for each atomic species present in the system. Its shape is (Nspecies,).
- LatVecs::Array{Float64, 2}: A 3 by 3 matrix describing lattice vectors for unit cell of the system.

5 Hamiltonian 5

• Zvals::Array{Float64,1}: An array containing number of (valence) electrons of each atomic species. Its shape is (Nspecies,).

An instance of Atoms can be initialized using any of the following ways:

• Using Atoms constructor, which has the following signature

• Using init_atoms_xyz or init_atoms_xyz which takes either a string containing path to xyz file or the content of the xyz file itself. When using this function, one must set LatVecs field manually. The Atoms constructor mentioned before is actually a wrapper for the functions init atoms xyz and init atoms xyz string.

A note about Zvals:

Both Atoms and init_atoms_* function set Zvals to zeros (Nspecies). After passed to Hamiltonian constructor Zvals will be set according to the pseudopotentials used.

TODO: examples

5 Hamiltonian

An instance Hamiltonian is a central object in PWDFT.jl. It is used to store various instances of other important types such as atoms, plane wave grids, pseudopotentials, etc. It is implemented in the file src/Hamiltonian.jl.

To create an instance of Hamiltonian, we normaly need to provide at least three arguments to the Hamiltonian constructor:

- atoms:: Atoms: an instance of Atoms
- pspfiles::Array{String, 1}: a list of strings specifying the locations of pseudopotentials used in the calculations. Note that, the order should be the same as species ordering of atoms, i.e. pspfiles[isp] is the path of pseudopotentials of species with symbols atoms.SpeciesSymbols[isp].
- ecutwfc::Float64: cutoff energy for wave function expansion using plane wave basis set

A simplified version of Hamiltonian constructor only needs two arguments: atoms::Atoms and ecutwfc::Float64. In this case, full Coulomb potential will be used. We usually need very large cutoff energy in this case (probably in the order or 10^2 Hartree to obtain good convergence). The structure of Hamiltonian is designed such that we can perform application or multiplication of Hamiltonian to wave function:

³ The operator * is actually implemented as function in Julia

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6 Plane wave basis

The plane wave basis is described by the type PWGrid. This type is defined in the file PWGrid.jl. It has the following fields:

```
• ecutwfc::Float64:
  cutoff for wave function expansion
• ecutrho::Float64:
  cutoff for electron density expansion, for norm-converving pseudopotential we have
  ecutrho = 4 * ecutwfc.
• Ns::Tuple{Int64, Int64, Int64}:
  parameters defining real-space grid points.
• LatVecs:: Array {Float 64, 2}: lattice vectors of unit cell (3 × 3 matrix)
• RecVecs::Array{Float64,2}:
  reciprocal lattice vectors (3 \times 3 matrix)
• CellVolume::Float64:
  the volume of real-space unit cell
• r::Array{Float64,2}:
  real-space grid points. Its shape is (3, Npoints)
• gvec::GVectors:
  an instance of GVectors, for potentials and density expansion
• gvecw::GVectorsW:
  an instace of GVectorsW, for wave function expansion
```

• planfw: FFTW forward plan

• planbw: FFTW backward plan

The following constructor can be used to create an instance of PWGrid:

6.1 G-vectors for potentials and densities expansion

G-vectors are described by type GVectors. It is defined in the file PWGrid.jl. It has the following fields:

- Ng:: Int 64: total number of G-vectors
- G::Array{Float64, 2} The array containing the actual G-vectors. Its shape is (3, Ng).

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• G2::Array{Float64,1}: The array containing magnitude of G-vectors. Its shape is (Ng,).

• idx_g2r::Array{Int64,1} The array containing mapping between G-vectors to real space grid points. Its shape is (Ng,).

The following function is used as the constructor:

```
function init_gvec( Ns, RecVecs, ecutrho )
```

This function takes the following arguments

- Ns: a tuple of three Int64's specifying sampling points along the 1st, 2nd, and 3rd lattice vector directions.
- RecVecs: 3 by 3 matrix describing reciprocal lattice vectors
- ecutrho: cutoff energy (in Hartree). For norm-conserving PP, it is 4 times ecutwfc.

6.2 G-vectorsW

The G-vectors for wave function expansion is described by the type GVectorsW. They are a subset of GVectors. It has the following fields:

- Ngwx:: Int64: maximum number of G-vectors for all kpoints.
- Ngw:: Array { Int 64, 1 }: number of G-vectors for each kpoints
- idx_gw2g::Array{Array{Int64,1},1}: mapping between indices of GVectorsW to indices of GVectors.
- idx_gw2r::Array{Array{Int64,1},1}: mapping between indices of GVectorsW to indices of real space grid points PWGrid.r
- kpoints::KPoints: an instance of KPoints

Constructor: TODO

6.3 Bloch wave vector

The type describing Bloch wave vectors, or commonly referred to as k-points, is KPoints. It is defined in the file KPoints.jl. It has the following fields

- Nkpt::Int64: total number of k-points.
- k::Array{Float64, 2}: the actual k-points. Its shape is (3, Nkpt).
- wk::Array{Float64,1}: the weight of each k-points needed for integration over Brillouin zone
- RecVecs::Array{Float64,2}: a copy of PWGrid.RecVecs.

7 Wave functions 8

Monkhorst-Pack grid points:

$$k_i = \frac{2n_i - N_i - 1}{2N_i} \mathbf{b}_i. \quad i = 1, 2, 3$$
 (1)

where $n_i = 1, 2, ..., N_i$ size = (N_1, N_2, N_3) and the \mathbf{b}_i 's are reciprocal lattice vectors.

Constructor:

SPGLIB is used to generate reduced k-points within the first Brillouin zone.

7 Wave functions

In the present implementation, I have chosen to use the simplest data structure for representing wave functions, namely Array (ComplexF64, 2). In PWDFT.jl, an alias has been defined:

```
const Wavefunc = Array{ComplexF64,2}
```

I also differentiate between wave function and Bloch wave function. A Bloch wave function is composed of several wave functions having different Bloch wave vectors \mathbf{k} or \mathbf{k} -points. The following alias also has been defined

```
const BlochWavefunc = Array{Array{ComplexF64,2},1}
```

Spin index is merged with kpoint index

Conventions: psi for an instance of Wavefunc and psiks for an instance of BlochWavefunc Functions related to wave functions:

- rand_Wavefunc
- zeros_Wavefunc
- rand_BlochWavefunc
- zeros_BlochWavefunc

Wave functions in real and reciprocal space.

Converting between wave functions in real and reciprocal space

 $Orthonormalization\ functions\ {\tt ortho_gram_schmidt}\ and\ {\tt ortho_sqrt}$

8 Total energy components

Total energy components are stored in the type Energies. Currently its fields are as follows.

- Kinetic: kinetic energy
- Ps_loc: local pseudopotential energy

9 Local potentials

- Ps_nloc: nonlocal pseudopotential energy
- Hartree: classical electrostatic energy
- xc: exchange correlation energy
- NN: nuclear-nuclear (repulsive) interaction energy
- PspCore: core (screened) pseudopotential energy
- mTs: electronic entropy contribution (with minus sign). This is used for calculation with partial occupations such as metals.

9 Local potentials

Various local potentials are stored in the type Potentials. Currently its fields are as follows.

- Ps_loc local pseudopotential components. Its shape is (Npoints,).
- Hartree: classical electrostatic potential. Its shape is (Npoints,).
- xc: exchange-correlation potential. This potential can be spin dependent so its shape is (Npoints, Nspin).

All of these potentials are stored in the real space representation.

10 Pseudopotentials

Currently, only GTH pseudopotentials with no core-correction are supported. The type for handling GTH pseudopotential for a species is PsPot_GTH. It is declared as follows.

```
struct PsPot_GTH
    pspfile::String
    atsymb::String
    zval::Int64
    rlocal::Float64
    rc::Array{Float64,1}
    c::Array{Float64,1}
    h::Array{Float64,3}
    lmax::Int64
    Nproj_l::Array{Int64,1}
    rcut_NL::Array{Float64,1}
```

11 Hamiltonian operator

Apply Hamiltonian operator to wave function

12 Eigensolver 10

```
for ispin = 1:Nspin
    for ik = 1:Nkpt
        # Important: need to set internal variables within ::Hamiltonian
        Ham.ispin = ispin
        Ham.ik = ik
        Hpsiks = op_H(Ham, psiks)
    end
end
```

12 Eigensolver

Three methods are available:

- LOBPCG method
- blocked Davidson method
- preconditioned conjugate gradient by minizing trace of Hamiltonian

These eigensolvers can be used to find eigenvalues and eigenvectors of Hamiltonian at fixed potential.

13 Solving Kohn-Sham problems

Two main algorithms are available:

- self-consistent field (SCF)
- direct minimization of Kohn-Sham total energy functional

The solvers of Kohn-Sham problems start with prefix KS_solve_. Currently implemented solvers are

```
• KS_solve_SCF
```

- KS solve Emin PCG
- KS_solve_DCM
- KS_solve_TRDCM

13.1 Self-consistent field

```
KS_solve_SCF
```

13.2 Direct energy minimization via nonlinear conjugate gradient method

```
KS_solve_Emin_PCG
```

This method is described by Ismail-Beigi and Arias

Presently only working for systems with band gap (insulators and semiconductors).

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13.3 Direct constrained minimization method of Yang (experimental feature)

KS_solve_DCM

13.4 Chebyshev filtered subspace iteration SCF (experimental feature)

update_psi="CheFSI"

14 Status

28 May 2018 The following features are working now:

- LDA and GGA, spin-paired and spin polarized calculations
- Calculation with k-points (for periodic solids). SPGLIB is used to reduce the Monkhorst-Pack grid points for integration over Brillouin zone.

Band structure calculation is possible in principle as this can be done by simply solving Schrodinger equation with converged Kohn-Sham potentials, however there is currently no tidy script or function to do that.

Total energy result for isolated systems (atoms and molecules) agrees quite well with ABINIT and PWSCF results.

Total energy result for periodic solid is quite different from ABINIT and PWSCF. I suspect that this is related to treatment of electrostatic terms in periodic system.

These discrepancies have been minimized. For several systems the agreement is very good even though I did not use the same algorithm as ABINIT.

SCF is rather shaky for several systems, however it is working in quite well in nonmetallic system.

SCF stability has been improved with Pulay mixing and its variants.