

PWDFT.jl Documentation

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This document is a work in progress

In this part I will describe my design choices in implementing PWDFT.jl. This design is by no means perfect and it might change in the future to accomodate more complex use cases.

1 Overview

The design of PWDFT.jl is intended to be rather simple. One constraint that is set to the code is that it should be possible to perform application of Hamiltonian operator to wave function as simple as:

```
Hpsi = Ham*psi # or  
Hpsi = op_H(Ham, psi)
```

where `psi` is, currently, of type `Array{ComplexF64, 2}`¹. This comes with an important consequences: all other pieces of information about how this operation is done should be present in the type of `Ham`.² In PWDFT.jl, the type of `Ham` is `Hamiltonian`. Several important fields of `Hamiltonian` are instances of the following types (please refer to the source code for more details about this):

- `Atoms`: contains information about atomic structure: cell vectors, atomic species and atomic coordinates.
- `PSPot_GTH`: contains information about atomic pseudopotentials.
- `Electrons`: contains information about electronic states.
- `PWGrid`: contains information about plane wave basis set.
- `Potentials`: contains information about local potentials such as local pseudopotential, Hartree and exchange-correlation potential.
- `PSPotNL`: contains information about nonlocal pseudopotential terms.
- `Energies`: contains information about components of Kohn-Sham energy.
- `SymmetryInfo`: contains information about symmetry operations.

2 Atomic structure

The type `Atoms` contains the following information:

- Number of atoms: `Natoms::Int64`
- Number of atomic species: `Nspecies::Int64`
- Atomic coordinates: `positions::Array{Float64, 2}`
- Unit cell vectors (lattice vectors): `LatVecs::Array{Float64, 2}`

¹This function may be extended take other types other than plain Julia array for more complex case.

²We will also see some quirks related to this design choice later, such as applying Hamiltonian to several k-points or spin-polarized case

Atoms also contains several other fields such as `Zvals` which will be set according to the pseudopotentials assigned to the instance of `Atoms`.³

Atoms struct definition

```
mutable struct Atoms
    Natoms::Int64
    Nspecies::Int64
    positions::Array{Float64,2}
    atm2species::Array{Int64,1}
    atsyms::Array{String,1}
    SpeciesSymbols::Array{String,1}
    LatVecs::Array{Float64,2}
    Zvals::Array{Float64,1}
end
```

Figure 1: Definition of `Atoms`.

`LatVecs` is a 3×3 matrix. The vectors are stored column-wise which is opposite to the PWSCF input convention. Convenience functions to calculate lattice vectors for several types of Bravais lattice are provided in `PWDFT.jl`. These functions adopt PWSCF definition. Several of these functions are listed below:

- `gen_lattice_sc` or `gen_lattice_cubic` for generating simple cubic lattice vectors.
- `gen_lattice_fcc`: for fcc structure
- `gen_lattice_bcc`: for bcc structure
- `gen_lattice_hcp`: for hcp structure

Please see file `gen_lattice.jl` for more information.

There are several ways to initialize an instance of `Atoms`. The following are typical cases.

- From xyz file. We need to supply the path to xyz file as string and set the lattice vectors:

```
atoms = Atoms(xyz_file="file.xyz", LatVecs=gen_lattice_sc(16.0))
```

- For crystalline systems, using keyword argument `xyz_string_frac` is sometimes convenient:

```
atoms = Atoms(xyz_string_frac=
    """
    2

    Si  0.0  0.0  0.0
    Si  0.25 0.25 0.25
    """, in_bohr=true,
    LatVecs=gen_lattice_fcc(10.2631))
```

IMPORTANT We need to be careful to also specify `in_bohr` keyword to get the correct coordinates in bohr (which is used internally in `PWDFT.jl`).

- From extended xyz file, the lattice vectors information is included along with several others information, if any, however they are ignored):

³Maybe we should include pseudopotential information under the `Atoms` type. However this would make `Atoms` "heavier".

```
atoms = Atoms(ext_xyz_file="file.xyz")
```

3 Plane wave basis set, real space grid, and k-points

The type PWGrid wraps various variables related to plane wave basis set. This has two fields of type GVectors and GVectorsW for storing information about **G**-vectors that are used in potential and wave functions, respectively.

PWGrid struct definition

```
struct PWGrid
  ecutwfc::Float64
  ecutrho::Float64
  Ns::Tuple{Int64, Int64, Int64}
  LatVecs::Array{Float64, 2}
  RecVecs::Array{Float64, 2}
  CellVolume::Float64
  r::Array{Float64, 2}
  gvec::GVectors
  gvecw::GVectorsW
  planfw
  planbw
end
```

Figure 2: Definition of PWGrid. The type annotation of planfw and planbw is omitted because they are too long.

We can define grid points over unit cell as:

$$\mathbf{r} = \frac{i}{N_{s1}}\mathbf{a}_1 + \frac{j}{N_{s2}}\mathbf{a}_2 + \frac{k}{N_{s3}}\mathbf{a}_3$$

where $i = 0, 1, \dots, N_{s1} - 1$, $j = 0, 1, \dots, N_{s2} - 1$, $k = 0, 1, \dots, N_{s3} - 1$

GVectors struct definition

```
struct GVectors
  Ng::Int64
  G::Array{Float64, 2}
  G2::Array{Float64, 1}
  idx_g2r::Array{Int64, 1}
  G2_shells::Array{Float64, 1}
  idx_g2shells::Array{Int64, 1}
end
```

Figure 3: Definition of GVectors.

GVectorsW struct definition

```

struct GVectorsW
  Ngwx::Int64
  Ngw::Array{Int64, 1}
  idx_gw2g::Array{Array{Int64, 1}, 1}
  idx_gw2r::Array{Array{Int64, 1}, 1}
  kpoints::KPoints
end

```

Figure 4: Definition of GVectorsW.

The \mathbf{G} -vectors can be defined as:

$$\mathbf{G} = n_1 \mathbf{b}_1 + n_2 \mathbf{b}_2 + n_3 \mathbf{b}_3 \quad (1)$$

where n_1, n_2, n_3 are integer numbers and $\mathbf{b}_1, \mathbf{b}_2, \mathbf{b}_3$ are three vectors describing unit cell of reciprocal lattice or *unit reciprocal lattice vectors*. They satisfy the following relations:

$$\mathbf{a}_1 = 2\pi \frac{\mathbf{a}_2 \times \mathbf{a}_3}{\Omega} \mathbf{a}_2 = 2\pi \frac{\mathbf{a}_3 \times \mathbf{a}_1}{\Omega} \mathbf{a}_3 = 2\pi \frac{\mathbf{a}_1 \times \mathbf{a}_2}{\Omega} \quad (2)$$

A periodic function

$$f(\mathbf{r}) = f(\mathbf{r} + \mathbf{L}), \quad \mathbf{L} = n_1 \mathbf{a}_1 + n_2 \mathbf{a}_2 + n_3 \mathbf{a}_3 \quad (3)$$

can be expanded using plane wave basis functions as:

$$f(\mathbf{r}) = \frac{1}{\sqrt{\Omega}} \sum_{\mathbf{G}} C_{\mathbf{G}} \exp(i\mathbf{G} \cdot \mathbf{r}) \quad (4)$$

where $C_{\mathbf{G}}$ are expansion coefficients. This sum is usually truncated at a certain maximum value of \mathbf{G} -vector, \mathbf{G}_{\max} .

Kohn-Sham wave function:

$$\psi_{i,\mathbf{k}}(\mathbf{r}) = u_{i,\mathbf{k}}(\mathbf{r}) \exp[i\mathbf{k} \cdot \mathbf{r}] \quad (5)$$

where $u_{i,\mathbf{k}}(\mathbf{r}) = u_{i,\mathbf{k}}(\mathbf{r} + \mathbf{L})$

Using plane wave expansion:

$$u_{i,\mathbf{k}}(\mathbf{r}) = \frac{1}{\sqrt{\Omega}} \sum_{\mathbf{G}} C_{i,\mathbf{k},\mathbf{G}} \exp(i\mathbf{G} \cdot \mathbf{r}), \quad (6)$$

we have:

$$\psi_{i,\mathbf{k}}(\mathbf{r}) = \frac{1}{\sqrt{\Omega}} \sum_{\mathbf{G}} C_{i,\mathbf{G}+\mathbf{k}} \exp[i(\mathbf{G} + \mathbf{k}) \cdot \mathbf{r}] \quad (7)$$

With this expression we can expand electronic density in plane wave basis:

$$\begin{aligned}
\rho(\mathbf{r}) &= \sum_i \int f_{i,\mathbf{k}} \psi_{i,\mathbf{k}}^*(\mathbf{r}) \psi_{i,\mathbf{k}}(\mathbf{r}) d\mathbf{k} \\
&= \frac{1}{\Omega} \sum_i \int f_{i,\mathbf{k}} \left(\sum_{\mathbf{G}'} C_{i,\mathbf{G}'+\mathbf{k}} \exp[-i(\mathbf{G}' + \mathbf{k}) \cdot \mathbf{r}] \right) \left(\sum_{\mathbf{G}} C_{i,\mathbf{G}+\mathbf{k}} \exp[i(\mathbf{G} + \mathbf{k}) \cdot \mathbf{r}] \right) d\mathbf{k} \\
&= \frac{1}{\Omega} \sum_i \int f_{i,\mathbf{k}} \sum_{\mathbf{G}} \sum_{\mathbf{G}'} C_{i,\mathbf{G}+\mathbf{k}} C_{i,\mathbf{G}'+\mathbf{k}} \exp[i(\mathbf{G} - \mathbf{G}') \cdot \mathbf{r}] d\mathbf{k} \\
&= \frac{1}{\Omega} \sum_{\mathbf{G}''} C_{\mathbf{G}''} \exp[i\mathbf{G}'' \cdot \mathbf{r}] d\mathbf{k}
\end{aligned}$$

The sum over \mathbf{G}'' extends twice the range over the range needed by the wave function expansion.

For wave function expansion we use plane wave expansion over \mathbf{G} vectors defined by:

$$\frac{1}{2} |\mathbf{G} + \mathbf{k}|^2 \leq E_{\text{cut}} \quad (8)$$

where E_{cut} is a given cutoff energy which corresponds to `ecutwfc` field of `PWGrid`. For electronic density (and potentials) we have:

$$\frac{1}{2} \mathbf{G}^2 \leq 4E_{\text{cut}} \quad (9)$$

The value of $4E_{\text{cut}}$ corresponds to `ecutrho` field of `PWGrid`.

In the implementation, we first generate a set of \mathbf{G} -vectors which satisfy Equation (9) and derives several subsets from it which satisfy Equation (??) for a given \mathbf{k} -points.

An instance of `PWGrid` can be initialized by using its constructor which has the following signature:

```
function PWGrid( ecutwfc::Float64, LatVecs::Array{Float64,2};
    kpoints=nothing, Ns_=(0,0,0) )
```

There are two mandatory arguments: `ecutwfc` and `LatVecs`. `ecutwfc` is cutoff energy for kinetic energy (in Hartree) and `LatVecs` is usually correspond to the one used in an instance of `Atoms`.

Structure factor

FFT

operators op nabla op nabla 2

KPoints struct definition

```
struct KPoints
    Nkpt::Int64
    mesh::Tuple{Int64,Int64,Int64}
    k::Array{Float64,2}
    wk::Array{Float64,1}
    RecVecs::Array{Float64,2}
end
```

Figure 5: Definition of `KPoints`.

4 Electronic states

Electrons struct definition

```
mutable struct Electrons
    Nelectrons::Float64
    Nstates::Int64
    Nstates_occ::Int64
    Focc::Array{Float64,2}
    ebands::Array{Float64,2}
    Nspin::Int64
end
```

Figure 6: Definition of `Electrons`.

5 Potentials and energies

In KSDFT approach [1, 2], total energy per unit cell system $E_{\text{total}}^{\text{KS}}$ can be written as

$$E_{\text{total}}^{\text{KS}} = E_{\text{kin}} + E_{\text{ele-nuc}} + E_{\text{Ha}} + E_{\text{xc}} + E_{\text{nuc-nuc}} \quad (10)$$

Kohn-Sham equations:

$$H_{\text{KS}}\psi_{i\mathbf{k}}(\mathbf{r}) = \epsilon_{i\mathbf{k}}\psi_{i\mathbf{k}}(\mathbf{r}) \quad (11)$$

Potentials struct definition

```
mutable struct Potentials
  Ps_loc::Array{Float64, 1}
  Hartree::Array{Float64, 1}
  XC::Array{Float64, 2}
  Total::Array{Float64, 2}
end
```

Figure 7: Definition of Potentials.

Energies struct definition

```
mutable struct Energies
  Kinetic::Float64
  Ps_loc::Float64
  Ps_nloc::Float64
  Hartree::Float64
  XC::Float64
  NN::Float64
  PspCore::Float64
  mTS::Float64
end
```

Figure 8: Definition of Energies.

Calculation of electron density and total energy

Using Libxc.jl

Equations for E_{xc} and V_{xc} (LDA and GGA, nonspin and spinpol cases)

6 Pseudopotentials

Currently, PWDFT.jl supports a subset of GTH (Goedecker-Teter-Hutter) pseudopotentials. This type of pseudopotential is analytic and thus is somewhat easier to program. PWDFT.jl distribution contains several parameters of GTH pseudopotentials for LDA and GGA functionals.

These pseudopotentials can be written in terms of local $V_{\text{loc}}^{\text{PS}}$ and angular momentum l dependent nonlocal components ΔV_l^{PS} :

$$V_{\text{ene-nuc}}(\mathbf{r}) = \sum_I \left[V_{\text{loc}}^{\text{PS}}(\mathbf{r} - \mathbf{R}_I) + \sum_{l=0}^{l_{\text{max}}} V_l^{\text{PS}}(\mathbf{r} - \mathbf{R}_I, \mathbf{r}' - \mathbf{R}_I) \right] \quad (12)$$

PsPot_GTH struct definition

```

struct PsPot_GTH
  pspfile::String
  atsyb::String
  zval::Int64
  rlocal::Float64
  rc::Array{Float64, 1}
  c::Array{Float64, 1}
  h::Array{Float64, 3}
  lmax::Int64
  Nproj_l::Array{Int64, 1}
  rcut_NL::Array{Float64, 1}
end

```

Figure 9: Definition of PsPot_GTH.

6.1 Local pseudopotential

The local pseudopotential for I -th atom, $V_{\text{loc}}^{\text{PS}}(\mathbf{r} - \mathbf{R}_I)$, is radially symmetric function with the following radial form

$$V_{\text{loc}}^{\text{PS}}(r) = -\frac{Z_{\text{val}}}{r} \text{erf}\left[\frac{\bar{r}}{\sqrt{2}}\right] + \exp\left[-\frac{1}{2}\bar{r}^2\right] (C_1 + C_2\bar{r}^2 + C_3\bar{r}^4 + C_4\bar{r}^6) \quad (13)$$

with $\bar{r} = r/r_{\text{loc}}$ and r_{loc} , Z_{val} , C_1 , C_2 , C_3 and C_4 are the corresponding pseudopotential parameters. In \mathbf{G} -space, the GTH local pseudopotential can be written as

$$V_{\text{loc}}^{\text{PS}}(G) = -\frac{4\pi}{\Omega} \frac{Z_{\text{val}}}{G^2} \exp\left[-\frac{x^2}{2}\right] + \sqrt{8\pi^3} \frac{r_{\text{loc}}^3}{\Omega} \exp\left[-\frac{x^2}{2}\right] \times \\ (C_1 + C_2(3 - x^2) + C_3(15 - 10x^2 + x^4) + C_4(105 - 105x^2 + 21x^4 - x^6)) \quad (14)$$

where $x = Gr_{\text{loc}}$.

6.2 Nonlocal pseudopotential

PsPotNL struct definition

```

struct PsPotNL
  NbetaNL::Int64
  prj2beta::Array{Int64, 4}
  betaNL::Array{ComplexF64, 3}
end

```

Figure 10: Definition of PsPotNL.

The nonlocal component of GTH pseudopotential can be written in real space as

$$V_l^{\text{PS}}(\mathbf{r} - \mathbf{R}_I, \mathbf{r}' - \mathbf{R}_I) = \sum_{\mu=1}^{N_l} \sum_{\nu=1}^{N_l} \sum_{m=-l}^l \beta_{\mu lm}(\mathbf{r} - \mathbf{R}_I) h_{\mu\nu}^l \beta_{\nu lm}^*(\mathbf{r}' - \mathbf{R}_I) \quad (15)$$

where $\beta_{\mu lm}(\mathbf{r})$ are atomic-centered projector functions

$$\beta_{\mu lm}(\mathbf{r}) = p_{\mu}^l(r) Y_{lm}(\hat{\mathbf{r}}) \quad (16)$$

and $h_{\mu\nu}^l$ are the pseudopotential parameters and Y_{lm} are the spherical harmonics. Number of projectors per angular momentum N_l may take value up to 3 projectors. In \mathbf{G} -space, the nonlocal part of GTH pseudopotential can be described by the following equation.

$$V_l^{\text{PS}}(\mathbf{G}, \mathbf{G}') = (-1)^l \sum_{\mu}^3 \sum_{\nu}^3 \sum_{m=-l}^l \beta_{\mu lm}(\mathbf{G}) h_{\mu\nu}^l \beta_{\nu lm}^*(\mathbf{G}') \quad (17)$$

with the projector functions

$$\beta_{\mu lm}(\mathbf{G}) = p_{\mu}^l(G) Y_{lm}(\hat{\mathbf{G}}) \quad (18)$$

The radial part of projector functions take the following form

$$p_{\mu}^l(G) = q_{\mu}^l(G r_l) \frac{\pi^{5/4} G^l \sqrt{r_l^{2l+3}}}{\sqrt{\Omega}} \exp \left[-\frac{1}{2} G^2 r_l^2 \right] \quad (19)$$

For $l = 0$, we consider up to $N_l = 3$ projectors:

$$q_1^0(x) = 4\sqrt{2} \quad (20)$$

$$q_2^0(x) = 8\sqrt{\frac{2}{15}}(3 - x^2) \quad (21)$$

$$q_3^0(x) = \frac{16}{3}\sqrt{\frac{2}{105}}(15 - 20x^2 + 4x^4) \quad (22)$$

For $l = 1$, we consider up to $N_l = 3$ projectors:

$$q_1^1(x) = 8\sqrt{\frac{1}{3}} \quad (23)$$

$$q_2^1(x) = 16\sqrt{\frac{1}{105}}(5 - x^2) \quad (24)$$

$$q_3^1(x) = 8\sqrt{\frac{1}{1155}}(35 - 28x^2 + 4x^4) \quad (25)$$

For $l = 2$, we consider up to $N_l = 2$ projectors:

$$q_1^2(x) = 8\sqrt{\frac{2}{15}} \quad (26)$$

$$q_2^2(x) = \frac{16}{3}\sqrt{\frac{2}{105}}(7 - x^2) \quad (27)$$

For $l = 3$, we only consider up to $N_l = 1$ projector:

$$q_1^3(x) = 16\sqrt{\frac{1}{105}} \quad (28)$$

In the present implementation, we construct the local and nonlocal components of pseudopotential in the \mathbf{G} -space using their Fourier-transformed expressions and transformed them back to real space if needed. We refer the readers to the original reference [3] and the book [4] for more information about GTH pseudopotentials.

Due to the separation of local and non-local components of electrons-nuclei interaction, Equation (??) can be written as

$$E_{\text{ele-nuc}} = E_{\text{loc}}^{\text{PS}} + E_{\text{nloc}}^{\text{PS}} \quad (29)$$

The local pseudopotential contribution is

$$E_{\text{loc}}^{\text{PS}} = \int_{\Omega} \rho(\mathbf{r}) V_{\text{loc}}^{\text{PS}}(\mathbf{r}) d\mathbf{r} \quad (30)$$

and the non-local contribution is

$$E_{\text{nloc}}^{\text{PS}} = \sum_{\mathbf{k}} \sum_i w_{\mathbf{k}} f_{i\mathbf{k}} \int_{\Omega} \psi_{i\mathbf{k}}^*(\mathbf{r}) \left[\sum_I \sum_{l=0}^{l_{\text{max}}} V_l^{\text{PS}}(\mathbf{r} - \mathbf{R}_I, \mathbf{r}' - \mathbf{R}_I) \right] \psi_{i\mathbf{k}}(\mathbf{r}) d\mathbf{r}. \quad (31)$$

7 Hamiltonian operators

Hamiltonian struct definition

```
mutable struct Hamiltonian
  pw::PWGrid
  potentials::Potentials
  energies::Energies
  rhoe::Array{Float64,2}
  electrons::Electrons
  atoms::Atoms
  sym_info::SymmetryInfo
  rhoe_symmetrizer::RhoeSymmetrizer
  pspots::Array{PsPot_GTH,1}
  pspotNL::PsPotNL
  xcfunc::String
  ik::Int64
  ispin::Int64
end
```

Figure 11: Definition of Hamiltonian.

Operators:

- op_H
- op_K
- op_V_loc
- op_V_Ps_loc
- op_V_Ps_nloc

7.1 Iterative diagonalization of Hamiltonian

8 Self-consistent field

Density vs potential mix

KS_solve_SCF

KS_solve_SCF_potmix

In the mean time, they are separated. They might be combined into one function in the future development.

Mixing algorithms:

- Simple or linear mixing
- Adaptive linear mixing
- Anderson mixing
- Broyden mixing
- Pulay mixing
- Restarted Pulay mixing
- Periodic Pulay mixing

9 Direct minimization

KS_solve_Emin_PCG

A Howtos

This part contains miscellaneous info.

A.1 Referring or including files in **sandbox** (or other dirs in **PWDFT.jl**)

```
using PWDFT
const DIR_PWDFT = joinpath(dirname(pathof(PWDFT)), "..")
const DIR_PSP = joinpath(DIR_PWDFT, "pseudopotentials", "pade_gth")
const DIR_STRUCTURES = joinpath(DIR_PWDFT, "structures")

pspfiles = [joinpath(DIR_PSP, "Ag-q11.gth")]
```

A.2 Using Babel to generate xyz file from SMILES

```
babel file.smi file.sdf
babel file.sdf file.xyz
```

Use `babel -h` to autogenerate hydrogens.

A.3 Setting up pseudopotentials

One can use the function `get_default_psp(::Atoms)` to get default pseudopotentials set for a given instance of `Atoms`.

Currently, it is not part of main `PWDFT.jl` package. It is located under `sandbox` subdirectory of `PWDFT.jl` distribution.

```
using PWDFT

DIR_PWDFT = joinpath(dirname(pathof(PWDFT)), "..")
include(joinpath(DIR_PWDFT, "sandbox", "get_default_psp.jl"))

atoms = Atoms(ext_xyz_file="atoms.xyz")
pspfiles = get_default_psp(atoms)
```

Alternatively, one can set `pspfiles` manually because it is simply an array of `String`:

```
pspfiles = ["Al-q3.gth", "O-q6.gth"]
```

IMPORTANT Be careful to set the order of species to be same as `atoms.SpeciesSymbols`. For example, if

```
atoms.SpeciesSymbols = ["Al", "O", "H"]
```

then

```
pspfiles = ["Al-q3.gth", "O-q6.gth", "H-q1.gth"]
```

A.4 Initializing Hamiltonian

For molecular systems:

```
Ham = Hamiltonian( atoms, pspfiles, ecutwfc )
```

For insulator and semiconductor solids:

```
Ham = Hamiltonian( atoms, pspfiles, ecutwfc, meshk=[3,3,3] )
```

For metallic systems:

```
Ham = Hamiltonian( atoms, pspfiles, ecutwfc, meshk=[3,3,3],
↳ extra_states=4 )
```

Empty extra states can be specified by using `extra_states` keyword.

For spin-polarized systems, `Nspin` keyword can be used.

A.5 Iterative diagonalization of Hamiltonian

```
evals = diag_LOBPCG!( Ham, psiks, verbose=false, verbose_last=false,
Nstates_conv=Nstates_occ )
```

A.6 Calculating electron density

Several ways:

```
Rhoe = calc_rhoe( Nelectrons, pw, Focc, psiks, Nspin )
# or
Rhoe = calc_rhoe( Ham, psiks )
# or
calc_rhoe!( Ham, psiks, Rhoe )
```

A.7 Read and write array (binary file)

Write to binary files:

```
for ikspin = 1:Nkpt*Nspin
    wfc_file = open("WFC_ikspin_"*string(ikspin)*".data", "w")
    write( wfc_file, psiks[ikspin] )
    close( wfc_file )
end
```

Read from binary files:

```
psiks = BlochWavefunc(undef, Nkpt)
for ispin = 1:Nspin, ik = 1:Nkpt
    ikspin = ik + (ispin-1)*Nkpt
    # Don't forget to use read mode
    wfc_file = open("WFC_ikspin_"*string(ikspin)*".data", "r")
    psiks[ikspin] = Array{ComplexF64}(undef, Ngw[ik], Nstates)
    psiks[ikspin] = read!( wfc_file, psiks[ikspin] )
    close( wfc_file )
end
```

Subspace rotation

In case need sorting:

```

Hr = psiks[ikspin]' * op_H( Ham, psiks[ikspin] )
evals, evecs = eigen(Hr)
evals = real(evals[:])

# Sort in ascending order based on evals
idx_sorted = sortperm(evals)

# Copy to Hamiltonian
Ham.electrons.ebands[:,ikspin] = evals[idx_sorted]

# and rotate
psiks[ikspin] = psiks[ikspin]*evecs[:,idx_sorted]

```

Usually we don't need to sort the eigenvalues if we use Hermitian matrix. We can calculate the subspace Hamiltonian by:

```

evals, evecs = eigen(Hermitian(Hr))

```

Status

29 July 2019 Total energy results are now similar to ABINIT and Quantum ESPRESSO. A rather comprehensive test has been added for SCF and Emin PCG for several simple systems.

28 May 2018 The following features are working now:

- LDA and GGA, spin-paired and spin polarized calculations
- Calculation with k-points (for periodic solids). SPGLIB is used to reduce the Monkhorst-Pack grid points for integration over Brillouin zone.

Band structure calculation is possible in principle as this can be done by simply solving Schrodinger equation with converged Kohn-Sham potentials, however there is currently no tidy script or function to do that.

Total energy result for isolated systems (atoms and molecules) agrees quite well with ABINIT and PWSCF results.

~~Total energy result for periodic solid is quite different from ABINIT and PWSCF. I suspect that this is related to treatment of electrostatic terms in periodic system.~~

These discrepancies have been minimized. For several systems the agreement is very good even though I did not use the same algorithm as ABINIT.

~~SCF is rather shaky for several systems, however it is working in quite well in nonmetallic system.~~

SCF stability has been improved with Pulay mixing and its variants.

References

- [1] P. Hohenberg and W. Kohn. Inhomogenous electron gas. *Phys. Rev.*, 136:B864–871, 1964.
- [2] W Kohn and L.J. Sham. Self-consistent equations including exchange and correlation effects. *Phys. Rev.*, 140(4A):A1333–1138, 1965.
- [3] S. Goedecker, M. Teter, and J. Hutter. Separable dual-space Gaussian pseudopotentials. *Phys. Rev. B*, 54:1703–1710, 1996.
- [4] Dominik Marx and Jürg Hutter. *Ab Initio Molecular Dynamics: Basic Theory and Advanced Methods*. Cambridge University Press, 2009.