

RAE6-9CK Airfoil simulation using Spalart Allmaras model

By Computational Domain

Introduction

- Simulation of a supercritical airfoil RAE6-9CK is performed using Spalart Allmaras in openFOAM
- Spalart Allmaras turbulence model:
 - Uses one transport equation

$$\nu_t = \tilde{\nu} f_{v1}, \quad f_{v1} = \frac{\chi^3}{\chi^3 + C_{v1}^3}, \quad \chi := \frac{\tilde{\nu}}{\nu}$$

Conditions

- Standard Sea-level conditions:
 - Temperature: 298.15 K
 - Pressure: 101 325 Pa
 - Density: 1.225 kg/m³
 - Reynold's numer: 6.5e6
 - Mach numer: 0.7
 - Angle of attack: 5°

Sutherland's viscous law

$$\mu = \mu_0 \left(\frac{T}{T_0} \right)^{\frac{3}{2}} \frac{T_0 + T_s}{T + T_s}$$

$$\mu = A_s \frac{T^{\frac{3}{2}}}{T + T_s}$$

$$A_s = \mu_0 \frac{(T_0 + T_s)}{T_0^{\frac{3}{2}}}, \quad \frac{T_s}{T_0} = \frac{110.4}{273.15}$$

Sutherland's viscous law

$$\mu_0 = \frac{\rho \cdot M \sqrt{\gamma R T} \cdot c}{Re} = \frac{1.225 \cdot 0.7 \sqrt{1.4 \cdot 287 \cdot 298.15}}{6.5 \cdot 10^6} = 4.56607 \cdot 10^{-5} [Pa \cdot s]$$

$$T_s = \frac{110.4}{273.15} \cdot 298.15 = 120.5043383 [K]$$

$$A_s = 4.56607 \cdot 10^{-5} \cdot \frac{298.15 + 120.5043383}{298.15^{\frac{3}{2}}} = 3.71318 \cdot 10^{-6}$$

Equation of State

- Molar mass of air: $M = 28.97 \text{ g/mol}$
- Number of moles: $n = 1$

$$p = \frac{\rho RT}{M}$$

Initial turbulent viscosity

- Initial turbulent viscosity: $\mu_t = 3-5\mu$
- Source: https://www.iccfd.org/iccfd7/assets/pdf/papers/ICCFD7-1902_paper.pdf