

1.

2.

3.

 n

4.

5.

 k -

6.

7.

8.

8.1.

8.2.

8.3.

.

1.

.

 n -

$$A = \{a_1, a_2, \dots, a_n\}.$$

,

:

•

,

•

,

.

,

 n - A 2^n

.

.

$$B \subset A$$

$$b_1 b_2 \dots b_j \dots b_n,$$

:

$$b_j = \begin{cases} 0, & a_j \notin B, \\ 1, & a_j \in B. \end{cases}$$

 n B .

2.

$$n - A, \quad , \\ n .$$

,

2.

$$i = 1, 2, \dots, 2^{|M|} \quad , \quad M = \{a_0, a_1, a_2\} \\ i - M \quad B_i,$$

$$b_0 b_1 b_2 \quad B_i \\ b_j = \begin{cases} 0, & a_j \notin B, \\ 1, & a_j \in B. \end{cases} :$$

i	$b_0 b_1 b_2$	B_i
0	000	\emptyset
1	001	a_2
2	010	a_1
3	011	a_1, a_2
4	100	a_0
5	101	a_0, a_2
6	110	a_0, a_1
7	111	a_0, a_1, a_2

$$2^M = \{\emptyset, a_0, a_1, a_2, \{a_0, a_1\}, \{a_0, a_2\}, \{a_1, a_2\}, \{a_0, a_1, a_2\}\}$$

$$3. \quad n$$

$$b = (b_{n-1}, b_{n-1}, \dots, b_1, b_0)$$

$$n, \quad , \quad b[n], b[n-1], \quad \dots, b[1], b[0], \quad .$$

$$1. \quad b[n] := 0. \quad b[n], b[n-1], \quad \dots, b[1], b[0],$$

$$2. \quad , \quad b[i] \quad ,$$

$$3. \quad b[i] := 0. \quad b[i] := 1, \quad b[j], j < i,$$

$$4. \quad b[i], \quad 0. \quad b[n]$$

,

(1,1,...,1), $i=n$.

$b[n]=1$

n

```
For i:=0 to n do b[i]:=0; [
While b[n] ≠ 1 do [
begin
Write(b[n-1], b[n-2],..., b[0]);
i:=0;
While b[i]=1 do
begin
b[i]:=0;
i:=i+1;
end;
b[i]:=1;
end;
```

$A = \{a_0, a_1, \dots, a_{n-1}\}.$

$a_n \notin A.$

b

$n=3$

B

$A = \{a_0, a_1, a_2\}.$

```
B := ∅ ;
While  $a_n \notin B$  do
begin
Write( B ) ;
i := 0 ;
While  $a_i \in B$  do
begin
B := B \ { $a_i$ } ;
i := i + 1 ;
end ;
B := B ∪ { $a_i$ } ;
end ;
```

$b^1 = (0,0,0), B^1 = \emptyset, i = 1;$

$b^2 = (0,0,1), B^2 = \{a_2\}, i = 2;$

$b^3 = (0,1,0), B^3 = \{a_1\}, i = 0;$

$b^4 = (0,1,1), B^4 = \{a_1, a_2\}, i = 2;$

$b^5 = (1,0,0), B^5 = \{a_0\}, i = 0;$

$b^6 = (1,0,1), B^6 = \{a_0, a_2\}, i = 1;$

$b^7 = (1,1,0), B^7 = \{a_0, a_1\}, i = 0;$

$b^8 = (1,1,1), B^8 = \{a_0, a_1, a_2\}, i = 3.$

4.

$b_1b_2...b_n$ — $(n-1)$ -разрядное двоичное число,

$$\begin{array}{r}
 b_1b_2b_3...b_{n-1}b_n \\
 \oplus b_1b_2b_3...b_{n-1}b_n \\
 \hline
 c_1c_2c_3...c_{n-1}c_n
 \end{array}$$

$c_i = b_i \oplus b_{i-1}, \quad b_0 = 0.$

i			
0	000	$000 \oplus 00 = 000$	000
1	001	$001 \oplus 00 = 001$	001
2	010	$010 \oplus 01 = 011$	011
3	011	$011 \oplus 01 = 010$	010
4	100	$100 \oplus 10 = 110$	110
5	101	$101 \oplus 10 = 111$	111
6	110	$110 \oplus 11 = 101$	101
7	111	$111 \oplus 11 = 100$	100

1. $(b_1b_2b_3b_4b_5b_6b_7b_8)_{10} = (00,01,11,10)_{2,2}$.
2. $(b_1b_2b_3b_4b_5b_6b_7b_8)_{10} = (00,01,11,10)_{2,2}$:
 $00,01,11,10$:
 $000,010,110,100$.
 $00,01,11,10$:
 $10,11,01,00$.
 $10,11,01,00$:
 $101,111,011,001$.
 $000, 010,110,100,101,111,011,001$.

3.

.1 , . 2 .

4. $n - 2$, $n -$.

$$c_1, c_2, c_3, \dots, c_k$$

, ,

, ,

$k + 1$,

.

.

$$A = \{a_1, a_2, a_3\}$$

.

.

:

i	$b_1b_2b_3$	B_i
0	000	\emptyset
1	001	a_3
2	011	a_2, a_3
3	010	a_2
4	110	a_1, a_2
5	111	a_1, a_2, a_3
6	101	a_1, a_3
7	100	a_1

,

Program Gray;

Var

i,M,N:byte;

{N- , $=2^N$ - }

G:array[1..M] of byte;

function BinToGray(b:byte):byte;

begin

BinToGray:=b xor (b shr 1)

end;

```

begin (*)
  For i:=1 to M do G[i]:=BinToGray(i);
end; (*)

```

5. $k -$

$X .$ $X = \{1, 2, \dots, n\} .$ $k -$ $n -$
 $k ,$
 $X .$

1. $(a_1, a_2, \dots, a_k) .$
 2. $:$
 $(b_1, b_2, \dots, b_k) = (a_1, \dots, a_{p-1}, a_p + 1, a_p + 2, \dots, a_p + k - p + 1) ,$
 $p = \max \{i | a_i < n - k + 1\}$
 3. $(b_1, b_2, \dots, b_k) :$
 $(c_1, \dots, c_k) = (b_1, \dots, b_{p'-1}, b_{p'} + 1, b_{p'} + 2, \dots, b_{p'} + k - p' + 1) ,$
 $p' = \begin{cases} p - 1, & b_k = n, \\ k, & b_k < n \end{cases}$
 $k -$
 $n -$

```

begin
  For i:=0 to k do A[i]:=i;
  p:=k;
  while p ≥ 1 do
    begin
      write (A[1], ..., A[k]);
      if A[k]=n then p:=p-1
      else p:=k;
      If p ≥ 1 then
        For i:=k downto p do
          A[i]:=A[p]+i-p+1;
        end;
    end;
end;

```

4-
 $\{1, \dots, 6\} ,$

1234
1235
1236
1245
1246
1256
1345
1346
1356
1456
2345
2546
2356
2456
3456

$$P[1], P[2], \dots, P[n].$$
$$X \stackrel{\bullet}{\rightarrow} \{x_1, x_2, x_3, \dots, x_n\}, \{y_1, y_2, y_3, \dots, y_n\}, \dots$$
$$X \cdot \{x_1, x_2, x_3, \dots, x_n\}, \{y_1, y_2, y_3, \dots, y_n\}, \dots$$
$$\begin{array}{c} (1, 2, \dots, n). \\ (n, n-1, \dots, 1). \\ (x_1, x_2, \dots, x_n) \quad (y_1, y_2, \dots, y_n) \\ (y_1, y_2, \dots, y_n)? \end{array}$$

$$x = \overset{\leftarrow}{(x_1, x_2, \dots, x_i, x_{i+1}, \dots, x_n)}$$

$$i, \quad x_i < x_{i+1}.$$

$$2. \quad , \quad x_1 > x_2 > \dots > x_n, \quad x = (n, n-1, \dots, 1).$$

$$3. \quad i, \quad x_i < x_{i+1} > x_{i+2} > \dots > x_n.$$

$$4. \quad j \quad n \quad i, \\ x_i < x_j. \quad i < j.$$

$$x = \overset{\leftarrow}{(x_1, x_2, \dots, x_i, x_{i+1}, \dots, x_j, \dots, x_n)}$$

$$5. \quad x_i \quad x_j$$

$$x = \overset{\leftarrow}{(x_1, x_2, \dots, x_i, x_{i+1}, \dots, x_j, \dots, x_n)}$$

$$6. \quad x_{i+1}, \dots, x_{n-1}, x_n, \quad ,$$

$$7. \quad y = (y_1, y_2, \dots, y_n).$$

$$. \quad x = (2, 6, 5, 8, 7, 4, 3, 1).$$

$$1. \quad , \quad x_i = 5, \quad x_j = 7.$$

$$2. \quad i = 3 \quad j = 5 : \\ \tilde{x} = (2, 6, 7, 8, 5, 4, 3, 2, 1)$$

$$3. \quad x_3, \dots, x_8 \rightarrow x_8, \dots, x_3 : \\ (8, 5, 4, 3, 1) \rightarrow (1, 3, 2, 5, 8).$$

$$y = (2, 6, 7, 1, 3, 4, 5, 8)$$

$$a[0]=0$$

$$\textbf{For } j:=0 \textbf{ to } n \textbf{ do } a[j]:=j; \{ \quad . \quad . \}$$


```

i:=1;
while i ≠ 0 do
begin
write(a[1],a[2],...,a[n]);
i:=n-1;           {      a[i]}
while a[i]>a[i+1] do i:=i-1;
j:=n;             {      a[j]}
while a[j]<a[i] do j:=j-1;
Swap(a[i],a[j]);

{                                     }
k:=i+1;
m:=i+trunc $\left(\frac{n-1}{2}\right)$ ;
while k≤m do
begin
Swap(a[k],a[n-k+i+1]);
k:=k+1;
end;
end;

```

. $n = 3$

a^k .

$a^1=\{123\}$, $a^1[i]=2$, $a^1[j]=3$;
 $a^2=\{132\}$, $a^2[i]=1$, $a^2[j]=2$;
 $a^3=\{213\}$, $a^3[i]=1$, $a^3[j]=3$;
 $a^4=\{231\}$, $a^4[i]=1$, $a^4[j]=3$;
 $a^5=\{312\}$, $a^5[i]=1$, $a^5[j]=2$;
 $a^6=\{321\}$, $i=0$;

$$X = \{1,2,3\} \qquad ()$$

()

	()	()
1	1 2 3	1 2 3
2	1 3 2	2 1 3
3	2 1 3	1 3 2
4	2 3 1	3 1 2
5	3 1 2	2 3 1
6	3 2 1	3 2 1

7.

$$\begin{array}{ccccc}
 n & & k & & k \\
 & n & & & \\
 k - & & n - & & A = \{1,2,...,n\} .
 \end{array}$$

: $\{1, 2, \dots, k\}$.

: $(n - k + 1, n - k + 2, \dots, n - 1, n)$.

$a = (a_1, a_2, \dots, a_k)$

:

$b = (a_1, \dots, a_{m-1}, a_m + 1, a_m + 2, \dots, a_m + k - m + 1),$

$m = \max \{i | a_i < n - k + i, 1 \leq i \leq k\}.$ b $a,$

$b_i = \begin{cases} a_i, & 1 \leq i < m, \\ a_m + i - m + 1, & m \leq i \leq k, \end{cases} \quad m = \begin{cases} m - 1, & b_k = n, \\ k, & b_k < n. \end{cases}$

n k

123

124

125

134

135

145

234

235

245

345

```
Var p,i,k,n,m:integer;
    a: Array [0..19] of Integer;
begin
  For i:=1 to k do a[i]:=i;
  If k=n then p:=1 else p:=k;
  while p>=1 do
    begin
      For m:=1 to k do write(a[m]);
      writeln(' ');
      if a[k]=n then p:=p-1 else p:=k;
      if p>=1 then
        for i:=k downto p do
          a[i]:=a[p]+i-p+1;
        end;
    end;
end.
```

5 3,

.

7

(7.1) = (1, 1, 1, 1, 1, 1, 1),
 (1.2, 5.1) = (2, 1, 1, 1, 1, 1),
 (2.2, 3.1) = (2, 2, 1, 1, 1),
 (3.2, 1.1) = (2, 2, 2, 1),
 (1.3, 4.1) = (3, 1, 1, 1, 1),
 (1.3, 1.2, 2.1) = (3, 2, 1, 1),
 (1.3, 2.2) = (3, 2, 2),
 (2.3, 1.1) = (3, 3, 1),
 (1.4, 3.1) = (4, 1, 1, 1),
 (1.4, 1.2, 1.1) = (4, 2, 1),
 (1.4, 1.3) = (4, 3),

8.

2.

(. Quick Sort) -

2. : ,


```

while A[j]>X do j:=j-1;
  if i<=j then
    begin
      y:=A[i]; A[i]:=A[j]; A[j]:=y;
      i:=i+1; j:=j-1;
    end;
  end;
  if L<j then QSort(L,j);
  if i<R then QSort(i,R);
end;
begin
  write(' ');
  read(N);
  for i:=1 to n do read(A[i]);
  QSort(1,n); { n- }
  { }
  for i:=1 to n do write(A[i], ' ');
end.

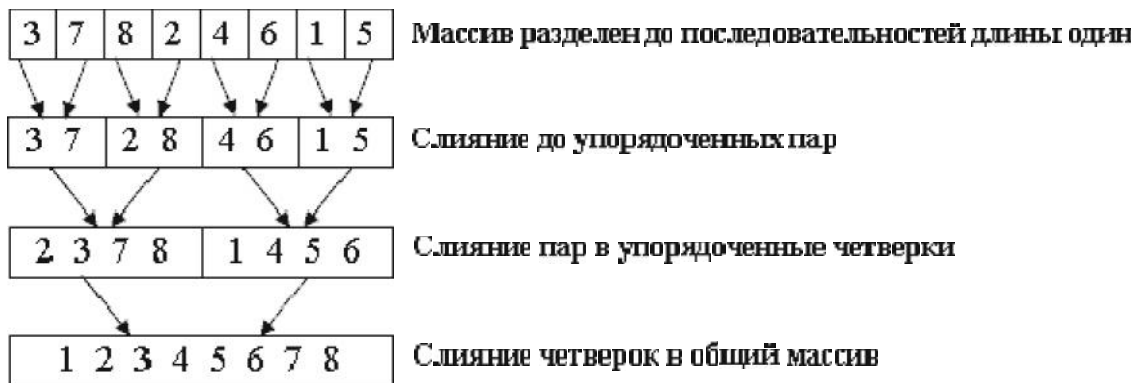
```

8.2.

" - - ",
quickSort. ,
.

Merge A[mid+1]...A[right] A[left]...A[mid]
A[left]...A[right].

3 7 8 2 4 6 1 5..



merge.

```

Program MrgeSort;
Var A,B : array[1..1000] of integer;
      N : integer;
{
Procedure Merge(left,right : integer);
Var mid,i,j,k : integer;
Begin
  mid:=(left+right) div 2;
  i:=left;
  j:=mid+1;
  for k:=left to right do
    if (i<=mid) and ((j>right) or (A[i]<A[j])) then
      begin
        B[k]:=A[i];
        i:=i+1;
      end else
        begin
          B[k]:=A[j];
          j:=j+1;
        end ;
      for k:=left to right do A[k]:=B[k];
End;
{left,right -
  }
Procedure Sort(left,right : integer);
Begin
  {
  if left<right then
    begin
      mid:=(left+right) div 2
      Sort(left,mid);
      Sort((mid + 1,right);
      Merge(left,right);
    end;
End;
Begin
  {
    A - N)
  ...
  {
    }
  Sort(1,N);
  {
    A}
  ...
End.

```

merge (A, B, C)
{
A B { A B
}
}

буфер $\begin{Bmatrix} 2367 \\ 145 \end{Bmatrix}$ 1 $\begin{Bmatrix} 2367 \\ 45 \end{Bmatrix}$ 12 $\begin{Bmatrix} 367 \\ 45 \end{Bmatrix}$ 123 $\begin{Bmatrix} 67 \\ 45 \end{Bmatrix}$
1234 $\begin{Bmatrix} 67 \\ 5 \end{Bmatrix}$ 12345 $\begin{Bmatrix} 67 \\ \text{пусто} \end{Bmatrix}$ дописываем 67 в буфер: 1234567
}

:
 $T(n) = 2T(n/2) + \Theta(n)$.
: $T(n) = n \log n -$
" ".
: $\Theta(n)$.
MergeSort
().

8.3. ()

,
,
,
(-),

1023,

- 255.
10

1,

511

1023

