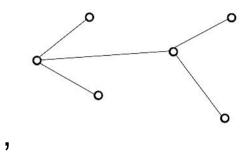
12

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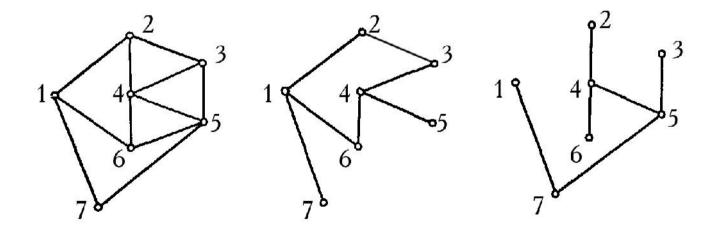
,

deg(b)=1 b deg(d)=1 deg(f)=1 deg(e)=1 deg(

,

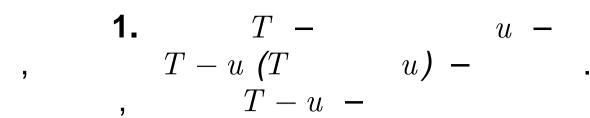
0

G,



,

, ЦИКЛ о ПЕЦР Неориентированный граф с циклом Неориентированное дерево



T,

- 1.
- 2. —
- 1, 0.
 3. , 0.
 1.

$$e=\left(u,v
ight)$$
 , v . v

,

u v,

T-e

3.

T

n .

1.

2.

n-1 .

3.

n-1

T

5.

6. *T*

 η -

G n n n-k . $\mathbf{2}$ (n_i-1)

 $\left(n_{1}-1\right)+\left(n_{2}-1\right)+\ldots+\left(n_{k}-1\right)=n_{1}+n_{2}+\ldots+n_{k}-k=n-k$,

G ,

G.

G.

G.

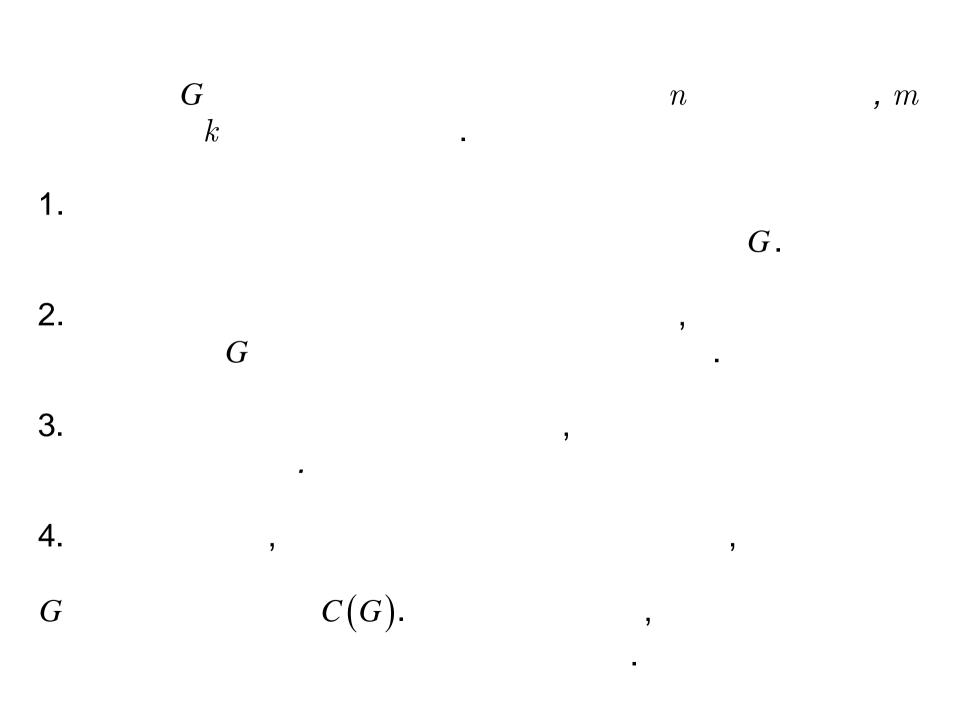
4.

$$G.$$

$$G.$$

$$1 + \sqrt{\frac{2}{4}} + \sqrt{\frac{2}{5}} + \sqrt{\frac{2}{6}} + \sqrt{\frac{2}{6}} + \sqrt{\frac{2}{5}} + \sqrt{\frac{2}{6}} + \sqrt{$$

 $T = T_{-}(3,5)$ $T_{2}=T_{1}-(2,3)$ $T_{3}=T_{2}-(1,6)$ $T_{4}=T_{3}-(1,2)$

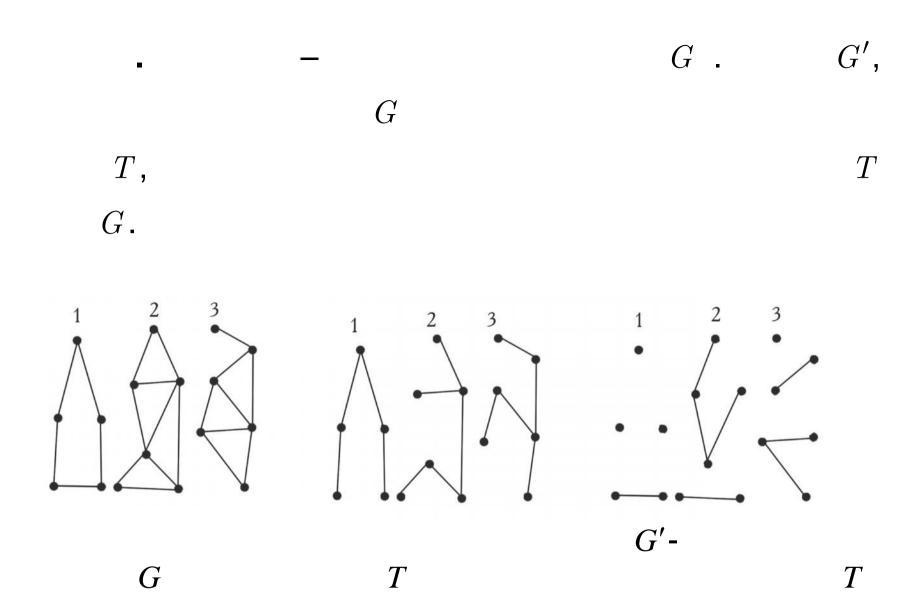


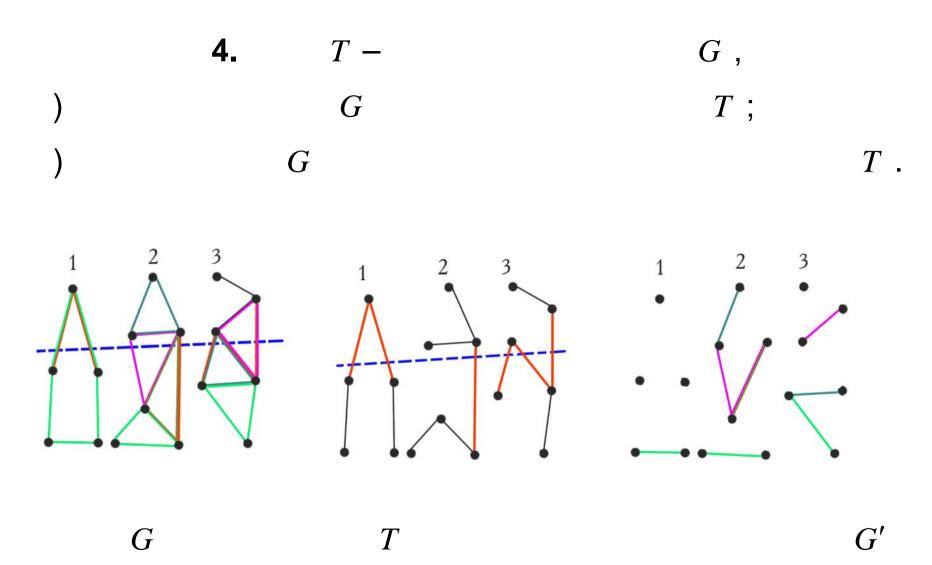
1. 2.

2,

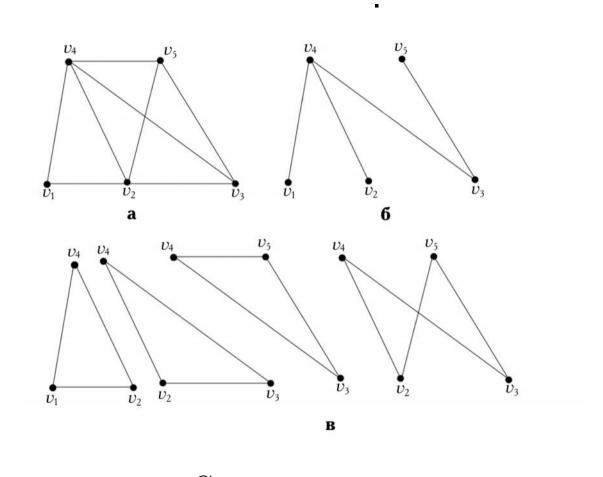
 $\begin{pmatrix}
8 & 1 & 2 \\
7 & & 3 \\
6 & 5 & 4
\end{pmatrix}$

,





G.



,

G; G.

G;

$$G = (V, E) - G$$

$$C(G) = |E| - |V| + k,$$
 $k - G.$

,
$$C(G) = 0$$
.

,
$$C(G)=1$$
 .

$$n \geq 2$$

$$G = (V, E)$$

$$d_i = d(e_i), \quad e_i \in E, \quad i = 1, 2, ..., |E|.$$

 d_i

$$S = \min \sum_{e_i \in E} \left(d\left(e_i\right) \right)$$

 $e_i^{}$,

,





,



1.

G n .

n , n^{n-2} .

2.

3.

• •

 n^{n-2} n

.

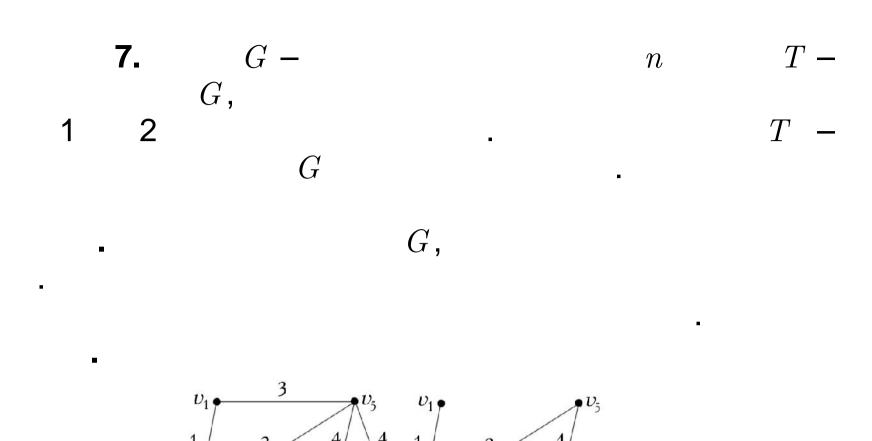
1. – ,

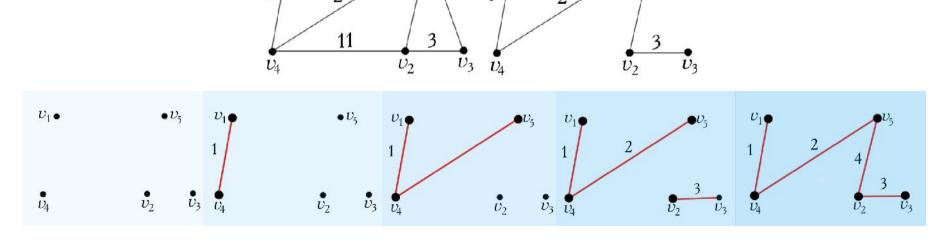
2. — , 0.

1. $O \qquad T_1 = O + e_1, \\ e_1 - \qquad G = \left(V, E\right)$

2. $T_k \qquad \qquad k < n-1,$ $T_{k+1} = T_k + e_{k+1}, \qquad e_{k+1} -$

 $G, \qquad T_k, \qquad T_k, \qquad T_k, \qquad T_k$





1

2.

3.

 $O(e \cdot \log e)$, e -

1. *O*

2. e_1 $T_1 = O + e_1$,.

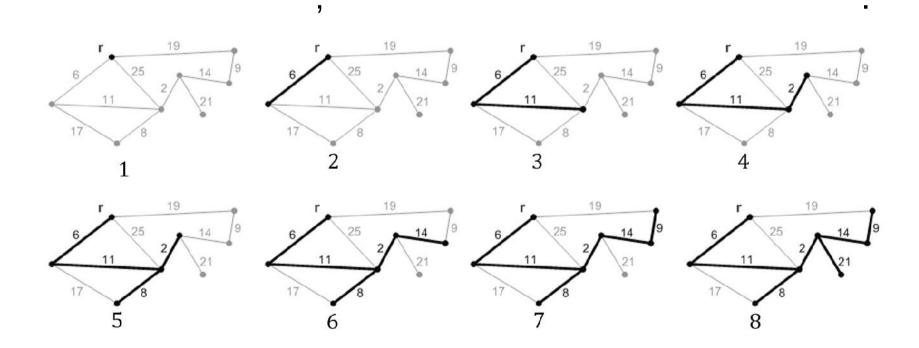
 $3. T_k k < n-1,$

 $T_{k+1} = T_k + e_{k+1}, \qquad e_{k+1} -$

 T_k .

. 1.

2. ,



1.

2.

n –

3.

,

,

e

1

 $O(n^2)$,

2

 n^2 ,

 n^2 ,

```
G(V,E),
                                               V = \{1, 2, ..., i, ..., n\}
U = \varnothing -
T = \emptyset-
procedure Prim (G:
                          ; var T:
var U:
  u, v:
begin
 T := \emptyset; U := \{i\};
 while U V do
 begin
                           (u, v)
           , u \in U v \in V \setminus U
  T := \bigcup \{(u,v)\};
  U := U \cup \{v\}
 end
end.
```

-

1. :

1.3.

1.3.

2.

-:-

-

x, , zzy, , z, y. 11 " , ,

1. *N*

 $N \times N$ A[N,N].

,

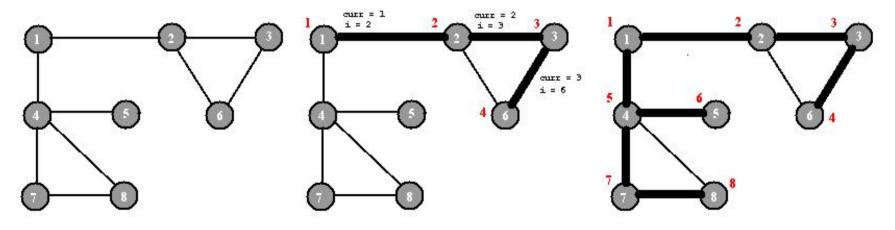
,

2.Visited[N]

,

3.

Begin Go(Start) end.



3.

a . ,

,

a

a .

,

,

1. Visited[N]

Queue[N].

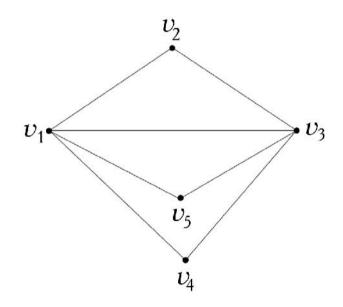
3. *r* ,

4. *w* ,

5.

```
r := 0, w := 1;
While (r < w) do
begin
  r := r+1;
  Curr = queue[r]; {
  For i:= 1 to N do {
  begin
   if ( (Visited[i]=0) AND (A[curr,i]=1) do
   begin
    Visited[i]:= 1; {
    w := w+1;
    queue[w]:= i; {
   end;
  end;
end;
```

G=ig(V,Eig) . , G ,



:
$$(v_1, v_2, v_3, v_4, v_1, v_5, v_3, v_1)$$
,

$$(v_4, v_3, v_2, v_1, v_3, v_5, v_1, v_4)$$

,

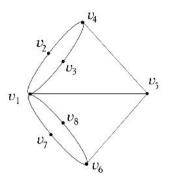
7

- ,

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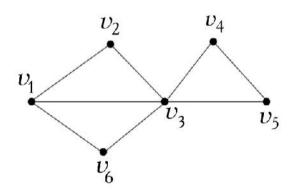
 v_1 v_2

,



$$G(V,E)$$
 — .

G



 $\vdots \ v_1, v_2, v_3, v_1, v_6, v_3, v_4, v_5, v_3.$

$$G = (V, E)$$
 —

$$G = (V, E)$$
 —

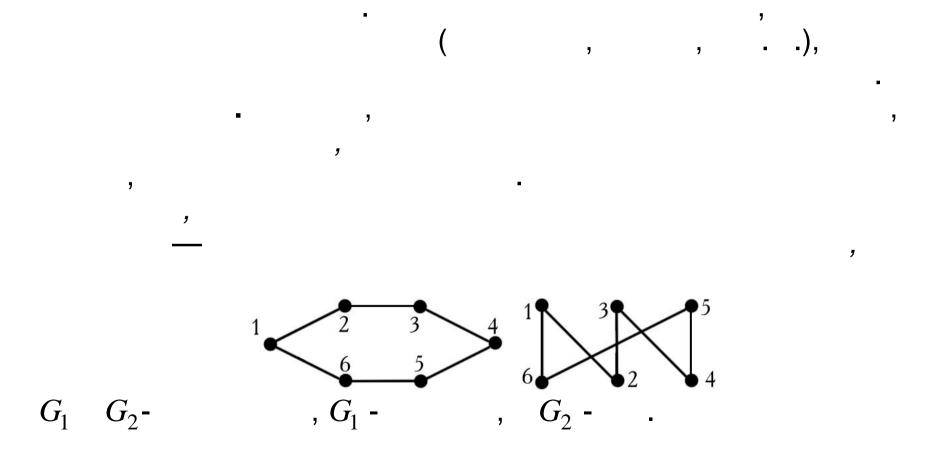
G,

,

G

1. ve, • 2. , , ,). 3. v , , .

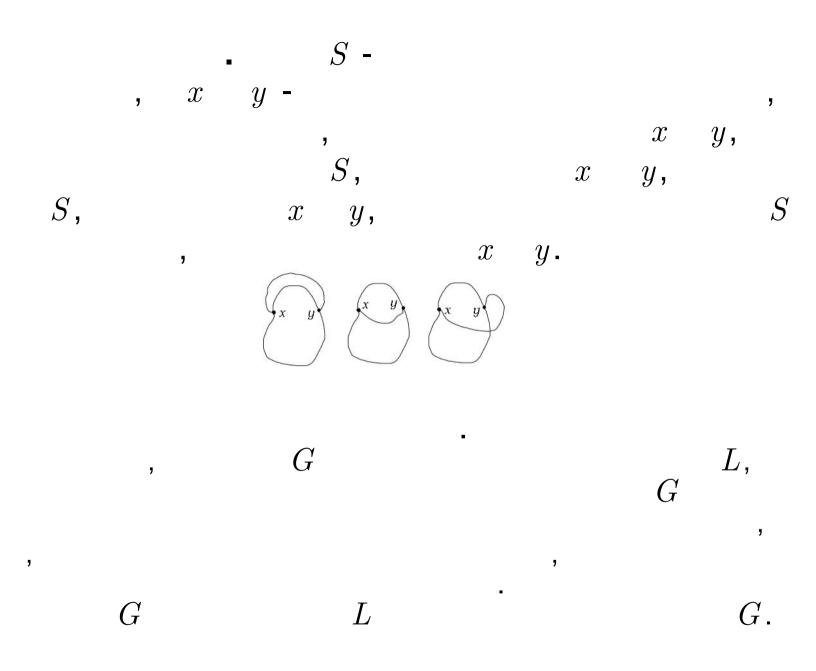
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(**>> «** , , **«** ,

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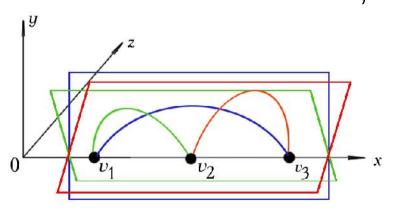
,

G = (V, E)

$$\begin{array}{c} OX. \\ |E| \\ (u,v) \in E \end{array}$$

$$u$$
 v .

.



$$K_5$$
 $K_{3,3}$

, K_{ξ} , K_{ξ} , V_1,v_2,v_3,v_4,v_5 , S_{ξ}

 $\begin{pmatrix} v_1,v_3 \end{pmatrix}$

 \mathcal{V}_3

1.

,
$$\begin{pmatrix} v_1,v_3 \end{pmatrix} \\ \begin{pmatrix} v_2,v_4 \end{pmatrix} & \begin{pmatrix} v_2,v_5 \end{pmatrix} \\ \begin{pmatrix} v_1,v_3 \end{pmatrix}, \end{pmatrix}$$

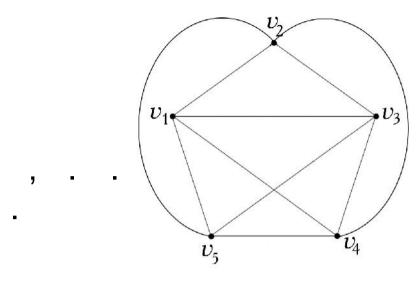
$$\left(\begin{array}{c} v_1, v_4 \\ \left(\begin{array}{c} v_2, v_5 \end{array} \right) \end{array} \right.$$

 $\left(\,v_3^{},v_5^{}\,\right)$

 (v_1,v_4)

$$\left(\left. v_{2},v_{4}\right) .\right.$$
 $\left(\left. v_{3},v_{5}\right) \right.$

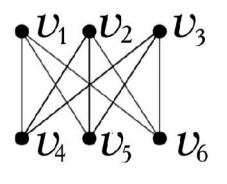
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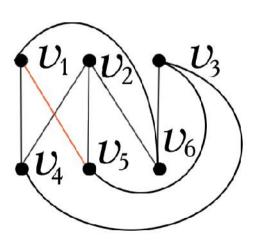


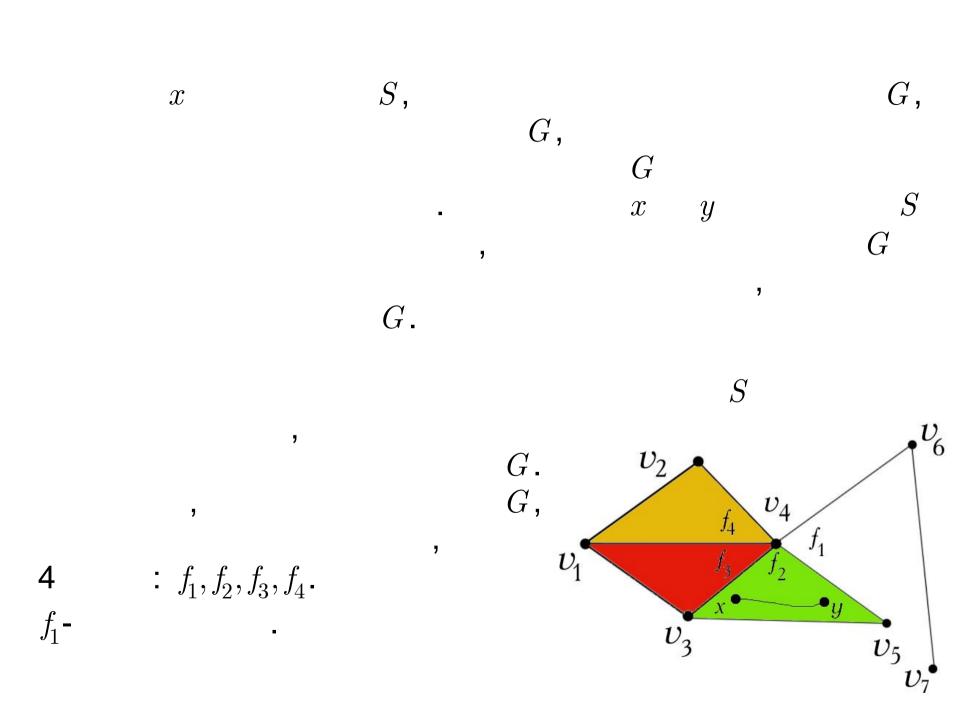
 K_5

 $K_{3,3}$.

,







G –

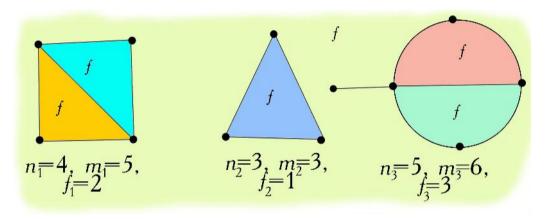
n -

m -

f -

n + f = m + 2.

, G - n , m , f k ; n+f=m+k+1.



$$n = n_1 + n_2 + n_3 = 4 + 3 + 5 = 12$$

$$m = m_1 + m_2 + m_3 = 5 + 3 + 6 = 14$$

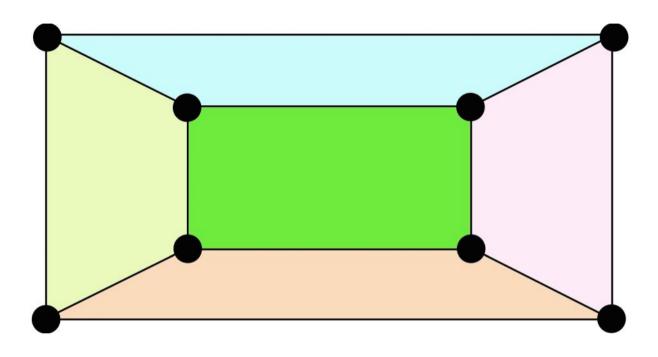
$$f = f_1 + f_2 + f_3 = 2 + 1 + 3 = 6$$

$$n + f = 12 + 6 = 18$$

$$m + k + 1 = 14 + 3 + 1 = 18$$

 $\begin{array}{ccc} & & & G & \text{-} \\ n \geq 3 & & & \end{array}$

 $m \le 3n - 6.$



$$n = 8 > 3$$
 $m = 12$

m < 3n - 6, $m < 3 \cdot 8 - 6$, m < 24 - 6, 12 < 18

7 8

•

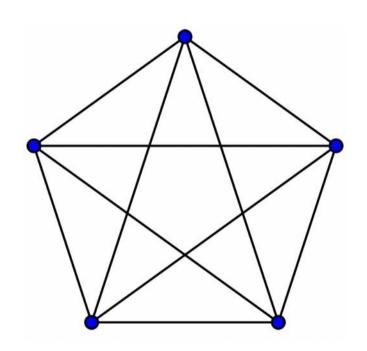
7

$$K_5$$

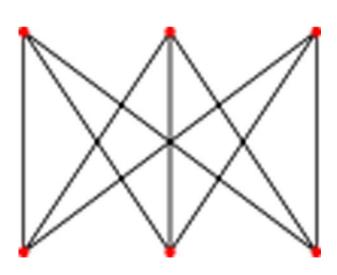
 $K_{3,3}$

 $K_5 K_{3,3} -$

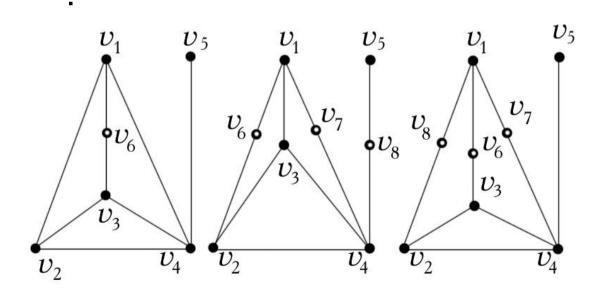
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2

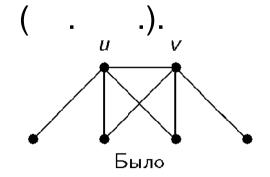


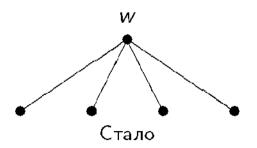
-

$$K_{5}$$
 $K_{3,3}$.

,

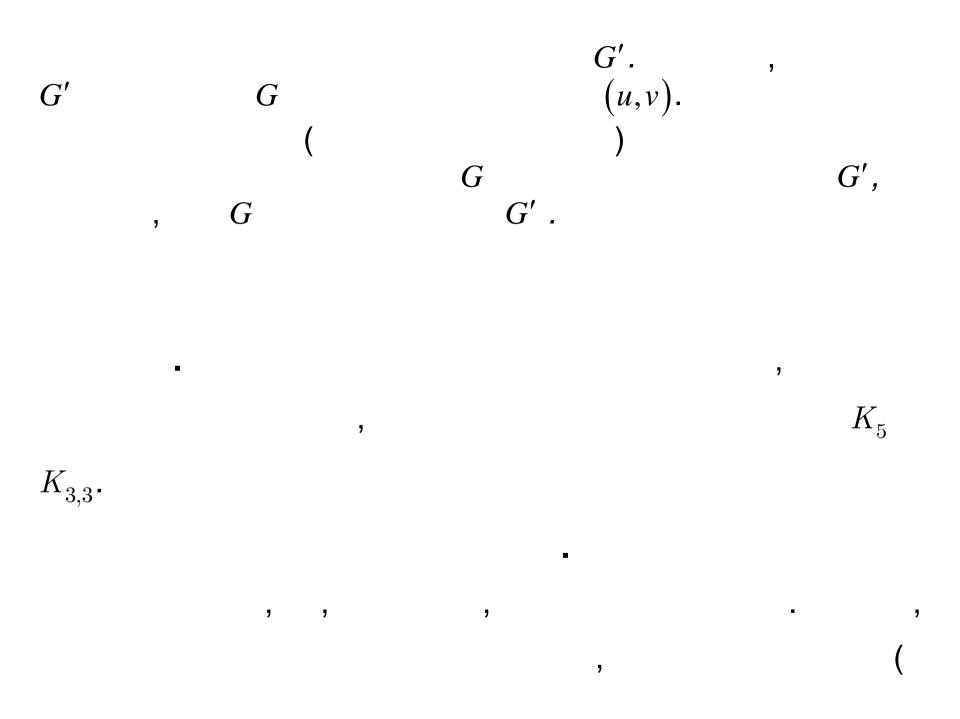
$$(u,v)$$
 — G .
 u v .
 w





G

u



, $K_{3,3}$. K_5 ,

