

1.

2.

3.

4.

5.

5.1.

5.2.

5.3. ()

6.

6.1. , , ,

6.2.

7.

7.1.

7.2. ()

7.2.1.

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- X (), Y ,- X (), Y ,- X Y ,- X (), Y ,- X () Y ,- X () Y ,- X () Y ,- X Y ,- X () Y . .

R X Y
 $X \times Y$. $(x, y) \in R$, xRy ;
 x y R , x

$$y. \qquad X=Y, \qquad X\times X. \qquad X.$$

$$\begin{array}{l} 1. \qquad X\times Y \\ 2. \qquad X \text{ --- } \end{array} \qquad X \text{ --- } Y.$$

$$\left\{ \left(a,b \right) \in X \times X \Big| a^2 + b^2 = 4 \right\}$$

$$X.$$

$$\begin{array}{l} 3. \qquad X \text{ --- } \qquad \qquad \qquad Y \text{ --- } \\ \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \left\{ \left(a,b \right) \in X \times Y \Big| a \text{ price } b \right\} \text{ ---} \end{array}$$

$$\begin{array}{l} 4. \qquad X \text{ --- } Y. \\ \left\{ \left(a,b \right) \Big| b \right. \qquad \qquad \qquad \left. a \right\} \qquad \qquad \qquad X \text{ --- } Y. \end{array}$$

$$\begin{array}{l} 5. \qquad A \text{ --- } \\ \qquad \qquad \qquad \left\{ \left(a,b \right) \in A^2 \Big| b \right. \qquad \qquad \qquad \left. a \right\} \\ \qquad \qquad \qquad A. \end{array}$$

$$\begin{array}{l} x \in X \qquad \qquad \qquad , \qquad \qquad \qquad R \qquad X \qquad Y \\ \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad y \in Y \qquad \qquad \qquad \left(x,y \right) \in R. \end{array}$$

$$\begin{array}{l} \qquad \qquad \qquad R. \\ y \in Y \qquad \qquad \qquad \left(x,y \right) \in R \qquad \qquad \qquad R \qquad X \qquad Y \\ \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad x \in X. \qquad \qquad \qquad , \\ \qquad \qquad \qquad R \\ \qquad \qquad \qquad R. \end{array}$$

$$Y \times X. \qquad \qquad \qquad R \qquad X \times Y \qquad \qquad \qquad R^{-1}$$

$$\begin{array}{l} 1. \qquad \qquad \qquad , \qquad \qquad \qquad \\ (\qquad \qquad \qquad) \qquad \qquad \qquad , \\ \qquad \qquad \qquad , \dots \qquad \qquad \qquad (\qquad \qquad \qquad) \qquad \qquad \qquad , \\ \qquad \qquad \qquad). \end{array}$$

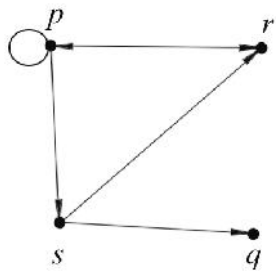
$$\begin{array}{l} \qquad \qquad \qquad X = \left\{ p,r,s,q \right\}. \\ R \subseteq X \times X \qquad \qquad \qquad R = \left\{ \left(p,r \right), \left(s,q \right), \left(r,p \right), \left(p,p \right), \left(s,r \right), \left(p,s \right) \right\} \\ \qquad \qquad \qquad N \text{ --- } \qquad \qquad \qquad . \\ \qquad \qquad \qquad , \qquad \qquad \qquad : \end{array}$$

$$R_1 = \{ (n,m) \in N \times N \mid n \leq m \}$$

2. $X = \{ x_i \mid i \in \mathbb{N} \}$. $R = \{ (x_i, x_j) \mid i \leq j \}$.

$(x_i, x_j) \in R \iff (x_j, x_i) \in R$.

$$R = \{ (p,r), (s,q), (r,p), (p,p), (s,r), (p,s) \}.$$



3. $R \subseteq X \times Y$, $X = \{ x_1, x_2, x_3, \dots, x_n \}$; $Y = \{ y_1, y_2, y_3, \dots, y_m \}$.

$n \times m$ -matrix $R = (r_{ij})$, where $r_{ij} = 1$ if $(x_i, y_j) \in R$, and 0 otherwise.

$R = \{ (p,r), (s,q), (r,p), (p,p), (s,r), (p,s) \}$:

R	p	q	r	s
p	1	0	1	1
q	0	0	0	0
r	1	0	0	0
s	0	1	1	0

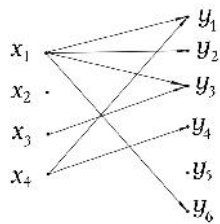
$R = \{ (x, y) \mid x \in X, y \in Y, (x, y) \in R \}$.

$R(x) = \{ y \in Y \mid (x, y) \in R \}$.

$R(y) = \{ x \in X \mid (x, y) \in R \}$.

$R = \{ (x, y) \mid (x, y) \in R \}$.

$$R \subset X \times Y, \quad X = \{x_1, x_2, x_3, x_4\} \quad Y = \{y_1, y_2, y_3, y_4, y_5, y_6\}$$



$$x_1: R(x_1) = \{y_1, y_2, y_3, y_6\}$$

$$x_2: R(x_2) = \{\emptyset\}$$

$$x_3: R(x_3) = y_4$$

$$x_4: R(x_4) = \{y_1, y_4\}$$

(),

, , ,

$$R \subseteq S$$

$$R \subseteq S, \quad R, \quad S.$$

$$R = S, \quad R \subseteq S$$

$$R \cup S, \quad R \subseteq S,$$

$$R \cap S, \quad R \subseteq S,$$

$$R - S, \quad R \subseteq S,$$

$$Y, \quad R - (X \times Y) \quad (X \times Y) - R \quad X$$

$$\begin{aligned} (R_i)_{i \in I} &= \bigcup_{i \in I} R_i, \\ &R_i. \end{aligned}$$

$$= \bigcap_{i \in I} R_i,$$

1.

$$\begin{aligned} &R \\ &R^{-1} \\ &R = \{(p,r),(s,q),(r,p),(p,p),(s,r),(p,s)\} \\ &R^{-1} = \{(r,p),(q,s),(p,r),(p,p),(r,s),(s,p)\} \\ &R^{-1} \\ &R \\ &R^{-1} \\ &R \subseteq X \times Y \\ &X \times Y \\ &R^{-1} \\ &R^{-1} = \{(y,x) | (x,y) \in R\}. \\ &(y,x) \in R^{-1}, \quad (x,y) \in R \\ &yR^{-1}x, \quad xRy. \\ &R^{-1} \\ &R. \\ &R = \{(1,r),(1,s),(3,s)\}, \\ &R^{-1} = \{(r,1),(s,1),(s,3)\}. \end{aligned}$$

$$R = \{ (a,b) \mid b \in a \}, \quad R^{-1} = \{ (b,a) \mid a \in b \}$$

$$R = \{ (a,b) \mid b \in a \}, \quad R = R^{-1}$$

$$2. \quad R = \{ (a,b) \mid a^2 + b^2 = 4 \}, \quad R^{-1} = R.$$

$$R \subseteq X \times Y \implies R^{-1} \subseteq Y \times X, \\ S \subseteq Y \times Z \implies S^{-1} \subseteq Z \times Y.$$

$$T = \{ (x,z) \mid \exists y \in Y, (x,y) \in R, (y,z) \in S \}.$$

$$T = S \circ R.$$

$$X = \{1,2,3\}, \quad Y = \{a,b\}, \quad Z = \{r,s,\}, \sim\}.$$

$$R = X \times Y \quad S = Y \times Z. \quad R = \{(1,a), (2,b), (3,b)\},$$

$$S = \{(a,r), (a,s), (b,\}, (b,\sim)\},$$

$$S \circ R = \{(1,r), (1,s), (2,\}, (2,\sim), (3,\}, (3,\sim)\}$$

$$(1,a) \in R \quad (a,r) \in S \quad , \quad (1,r) \in S \circ R,$$

$$(1,a) \in R \quad (a,s) \in S \quad , \quad (1,s) \in S \circ R,$$

.....

$$(3,b) \in R \quad (b,\sim) \in S \quad , \quad (3,\sim) \in S \circ R.$$

$$R \subseteq X \times Y, \quad S \subseteq Y \times Z \implies S^{-1} \subseteq Z \times Y, \quad T \subseteq X \times Z \implies T^{-1} \subseteq Z \times X$$

$$T \circ (S \circ R) = (T \circ S) \circ R.$$