

1.
2.
3.
4.
5.

5.1.
5.2.
5.3.

6.

6.1.
6.2.
6.3.
6.4.
6.5.

3.

3.1.
3.2.

4.

4.1. -
4.2. -
4.3. -
4.4. -

X

X_j :

-

X_j

X :

$$X = \bigcup_{j \in J} X_j$$

-

$j \in J \quad i \neq j$

, . . .

$i \in J$

: $X_i \cap X_j = \emptyset$.

1.

X_1

X

$X_2 = X \setminus X_1$

,

$X_1 \cup X_2 = X$

$X_1 \cap X_2 = \emptyset$.

2.

$X = \{10, 11, 12, \dots, 98, 99\}$

4:

,

0 - $X_0 = \{12, 16, 20, \dots, 96\}$;

,

1 - $X_1 = \{13, 17, 21, \dots, 97\}$;

,

2 - $X_2 = \{10, 14, 18, \dots, 98\}$;

$$, \qquad 3\text{-}X_3=\{11,15,19,...,99\}.$$

$$C=\left\{Y_j\right\}_{j\in J}, \qquad X: \qquad$$

$$C\text{ --- }X, \qquad D\subset C, \\ X,$$

$$C.$$

$$X=\left\{i\big| i=2n+1,n=0,1,2,...\right\}, \\ J=\left\{1,2\right\},\,C=\left\{Y_1,Y_2\right\},\,Y_1=\left\{-k\big|k=1,2,...\right\},\,Y_2=\left\{k\big|k=0,1,2,...\right\}. \\ X\subset Y_1\cup Y_2, \qquad C \\ X.$$

$$(\hspace{1.5cm})$$

$$,$$

$$.$$

$$\hspace{1.5cm}:1)\hspace{1.5cm},\hspace{1.5cm};2)\hspace{1.5cm}; \\ 3)\hspace{1.5cm},\hspace{1.5cm};4)\hspace{1.5cm}; \\ (\hspace{1.5cm})$$

$$\boldsymbol{n}\text{-}(\hspace{1.5cm}\boldsymbol{n}\text{-})\text{---} \\ \boldsymbol{n}(\hspace{1.5cm}\boldsymbol{n}\text{---}0). \\ x_i,1\leq i\leq n\hspace{1.5cm}X.$$

$$(\hspace{1.5cm})$$

$$(\hspace{1.5cm}):$$

$$X=\left(x_1,x_2,x_3,...,x_n\right)$$

$$\hspace{1.5cm}2 \\ \hspace{1.5cm}3\text{-}\hspace{1.5cm},4\text{-}\hspace{1.5cm}.$$

$$:$$

$$1)\left(x_1\right)\hspace{1.5cm};$$

$$2)\left(\hspace{1.5cm}\right)\hspace{1.5cm},\hspace{1.5cm}\dots\hspace{1.5cm}0.$$

$$.$$

$$.$$

$$.$$


```

(*                                     Quicksort *)
if (g<j) then Quicksort(g,j);
if (i<r) then Quicksort(i,r);
end;
begin
  writeln('          ',N, '          ':'') ;
  for k:=1 to N do readln(a[k]);
  Quicksort(1,N); (*
                    *)
  writeln('          ':'');
  for :=1 to N do write(a[k], ' ');
end.

```

$$C = A \times B, \quad A = \{a, b\}, \quad B = \{1, 2\},$$

$$a \in A, b \in B,$$

$$C = A \times B = \{(a, b) \mid a \in A, b \in B\}.$$

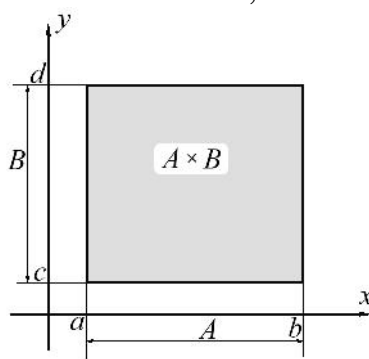
$$A = \{x, y, z\}, B = \{1, 2\}.$$

$$C = \{(x, 1), (x, 2), (y, 1), (y, 2), (z, 1), (z, 2)\}.$$

$$A = \{x \mid a \leq x \leq b\}$$

$$B = \{y \mid c \leq y \leq d\}$$

$$A \times B$$



$$, C = A \times B = \{(x, y) \mid x \in A, y \in B\}.$$

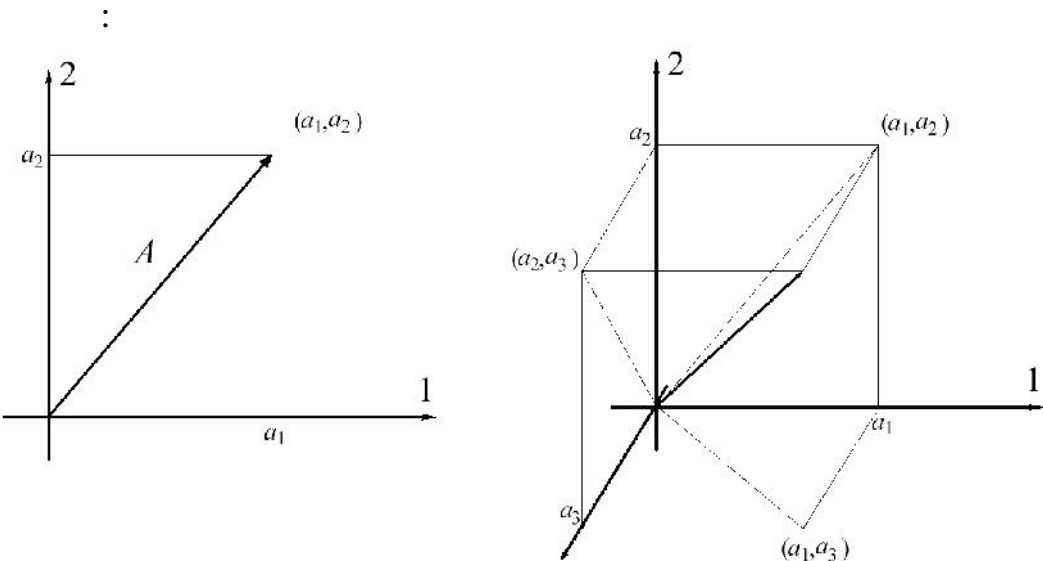
$$A \times A = A^2, A \times A \times A = A^3, \underbrace{A \times A \times A \times \dots \times A}_n = A^n.$$

$$, n=2,3,\dots$$

$$A^1 = A, A^0 = \{ \Lambda \}, \quad \Lambda - \qquad \qquad \qquad , \dots$$

$$\begin{aligned} C &= A \times B - \\ C^{-1} &= B \times A \\ C. \end{aligned}$$

$$\begin{aligned} R^2 &= R \times R & R^3 &= R \times R \times R \end{aligned}$$



$$\begin{aligned} (a_1, a_2) - & \\ a_1 & a_2 - \end{aligned}$$

$$\bar{A} = (a_1, a_2) \qquad 1 \quad 2. \qquad \qquad \qquad :$$

$$\begin{aligned} proj_1 \bar{A} &= proj_1 (a_1, a_2) = a_1, \\ proj_2 \bar{A} &= proj_2 (a_1, a_2) = a_2. \end{aligned}$$

$$\begin{aligned} (a_1, a_2, a_3) - & \\ & (a_1, a_2, a_3). \end{aligned}$$

$$\begin{aligned} proj_1 \bar{A} &= proj_1 (a_1, a_2, a_3) = a_1, \\ proj_2 \bar{A} &= proj_2 (a_1, a_2, a_3) = a_2, \\ proj_3 \bar{A} &= proj_3 (a_1, a_2, a_3) = a_3. \end{aligned}$$

:

$$\begin{aligned}
proj_{1,2}\bar{A} &= proj_{1,2}(a_1, a_2, a_3) = (a_1, a_2), \\
proj_{1,3}\bar{A} &= proj_{1,3}(a_1, a_2, a_3) = (a_1, a_3), \\
proj_{2,3}\bar{A} &= proj_{2,3}(a_1, a_2, a_3) = (a_2, a_3).
\end{aligned}$$

$$\begin{aligned}
& \qquad \qquad \qquad n - \qquad \qquad \qquad , \qquad \qquad \qquad n - \\
& \qquad \qquad \qquad (a_1, a_2, a_3, \dots, a_n) \\
& n - \qquad \qquad \qquad .
\end{aligned}$$

$$\begin{aligned}
proj_i\bar{A} &= proj_i(a_1, a_2, a_3, \dots, a_i, \dots, a_n) = a_i, \\
proj_{i,j}\bar{A} &= proj_{i,j}(a_1, a_2, a_3, \dots, a_i, \dots, a_j, \dots, a_n) = (a_i, a_j),
\end{aligned}$$

$$proj_{i,j,k}\bar{A} = proj_{i,j,k}(a_1, a_2, a_3, \dots, a_i, \dots, a_j, \dots, a_k, \dots, a_n) = (a_i, a_j, a_k),$$

.....

$$\begin{aligned}
& , \qquad \qquad \qquad , \\
& , \qquad \qquad \qquad n - 1 .
\end{aligned}$$

$$\begin{aligned}
& D \qquad \qquad \qquad D \qquad \qquad \qquad m . \\
& D \qquad \qquad \qquad D . \\
& : D = \{(1, 2, 3, 4, 5), (3, 2, 1, 5, 4), (2, 3, 6, 7, 1), (8, 1, 1, 4, 6)\}.
\end{aligned}$$

:

$$\begin{aligned}
proj_1D &= \{(1), (3), (2), (8)\}, \\
proj_2D &= \{(2), (2), (3), (1)\}, \\
proj_3D &= \{(3), (1), (6), (1)\}, \\
proj_4D &= \{(4), (5), (7), (4)\}, \\
proj_5D &= \{(5), (4), (7), (6)\}.
\end{aligned}$$

:

$$\begin{aligned}
proj_{1,2}D &= \{(1, 2), (3, 2), (2, 3), (8, 1)\}, \\
proj_{1,3}D &= \{(1, 3), (3, 1), (2, 6), (8, 1)\},
\end{aligned}$$

.....

$$proj_{2,3}D=\left\{ (2,3),(2,1),(3,6),(1,1)\right\} ,$$

$$proj_{1,3}D=\left\{ (1,3),(3,1),(2,6),(8,1)\right\} ,$$

$$\dots\dots\dots$$

$$\vdots$$

$$proj_{1,2,3}D=\left\{ (1,2,3),(3,2,1),(2,3,6),(8,1,1)\right\}$$

$$\dots\dots\dots$$

$$proj_{3,4,5}D=\left\{ (3,4,5),(1,5,4),(6,7,7),(1,4,6)\right\}$$

$$\dots\dots\dots$$

$$,$$

$$\cdot$$

$$\cdot$$

$$X\quad Y.$$

$$-$$

$$,$$

$$(x,y).$$

$$,\quad \cdot \quad \cdot$$

$$x\in X$$

$$y\in Y,\\ X\quad Y$$

$$x,$$

$$,$$

$$\cdot$$

$$\vdots$$

$$1)$$

$$X,$$

$$;$$

$$2)$$

$$Y,$$

$$;$$

$$3)$$

$$Q\subseteq X\times Y,$$

$$(\quad),$$

$$,\quad \cdot \quad \cdot$$

$$(x,y),$$

$$\cdot$$

$$,$$

$$(\quad$$

$$q)$$

$$q=\left\langle X,Y,Q\right\rangle$$

$$Q\subseteq X\times Y-$$

$$X\quad Y,$$

$$;$$

$$X-$$

$$;$$

$$Y-$$

$$;$$

$$,$$

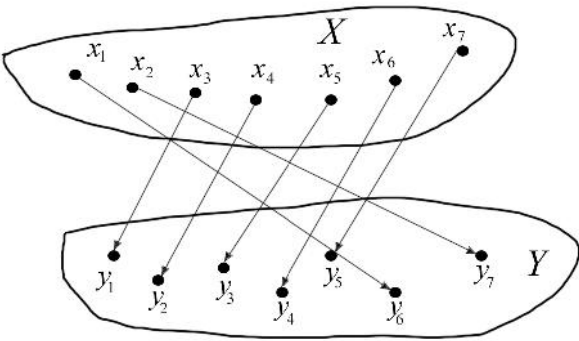
$$\vdots$$

$$1. \qquad \qquad \qquad \textit{proj}_x Q, \qquad \qquad \qquad , \qquad \qquad \qquad X, \qquad \qquad \qquad ;$$

$$2. \qquad \qquad \qquad \textit{proj}_y Q \qquad \qquad \qquad , \qquad \qquad \qquad ,$$

$$\begin{aligned} & \qquad \qquad \qquad Y, \qquad \qquad \qquad . \\ & (x,y) \in Q, \qquad \qquad \qquad , \qquad \qquad \qquad y \qquad \qquad \qquad x. \\ & \qquad \qquad \qquad , \qquad \qquad \qquad x \qquad y: \\ & \qquad \qquad \qquad X \qquad \qquad Y \end{aligned}$$

$$Q = \left\{ (x_1,y_6), (x_2,y_7), (x_3,y_1), (x_4,y_2), (x_5,y_3), (x_6,y_4), (x_7,y_5) \right\}$$



$$q = \langle X,Y,Q \rangle, \, Q \subseteq X \times Y$$

$$\begin{aligned} & , \qquad \qquad \qquad , \\ & , \qquad \qquad \qquad , \qquad \qquad \qquad x \in X, \\ & \qquad \qquad \qquad y \in Y. \end{aligned}$$

$$: \, q^{-1} = \langle X,Y,Q^{-1} \rangle, \qquad Q^{-1} = Y \times X.$$

$$\begin{aligned} & . \\ & . \\ & : \qquad - \qquad \qquad , \qquad \qquad - \end{aligned}$$

$$\begin{aligned} &) \qquad - \qquad \qquad (\qquad \qquad - \qquad \qquad) \qquad \qquad - \\ & X \qquad \qquad \qquad Y \qquad \qquad X \qquad Y, \\ & \qquad \qquad \qquad Z \end{aligned}$$

$$P.$$

$$\begin{aligned} & - \\ & . \qquad \qquad \qquad Z \qquad P \qquad \qquad - \end{aligned}$$

$$\begin{aligned} &) \qquad - \\ & X \qquad Y, \qquad \qquad \qquad - \qquad \qquad \qquad X \\ & \qquad \qquad \qquad Y, \end{aligned}$$

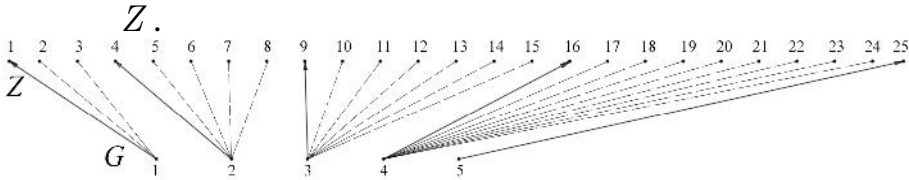
$$G = \{1,2,3,4,5\}$$

$$Z = \{1,2,3,4,5,6,7,8,9,10,11,12,13,15,16,...,25\}.$$

$$G$$

$$Z.$$

$$,$$



$$)$$

$$-$$

$$X$$

$$Y,$$

$$,$$

$$.$$

$$.$$

$$X = \{1,2,3,...,25\}$$

$$,$$

$$Y = \{2,3,4,5\}$$

$$-$$

$$,$$

$$)$$

$$-$$

$$X$$

$$Y,$$

$$.$$

$$X-$$

$$,$$

$$Y-$$

$$.$$

$$,$$

$$.$$