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$$G = (V, E) \text{ --- , } k \text{ ---}$$
$$f : V \longrightarrow N_k, \quad N_k = \{1, 2, \dots, k\},$$
$$\left(u, v \right) \in E \qquad f\left(u \right) \neq f\left(v \right).$$
$$k_-$$

$$f\qquad\qquad\qquad,$$

$$\begin{array}{l} |V|=k \\ k \end{array}.$$

$$-$$

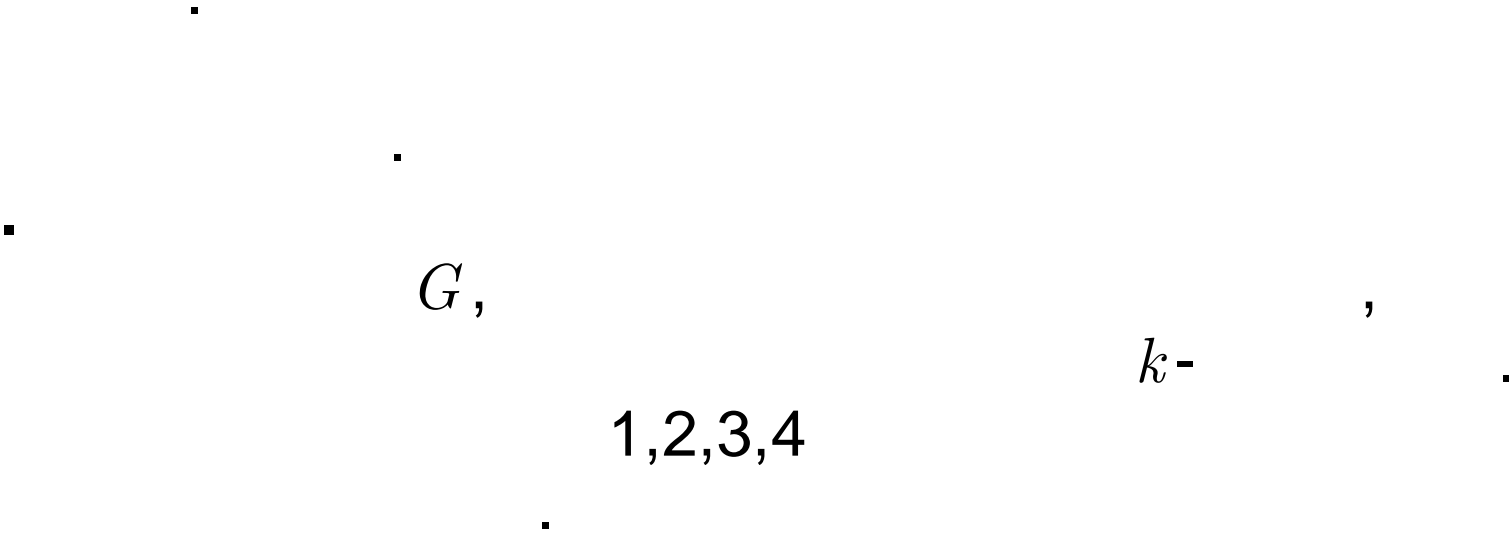
$$k-$$

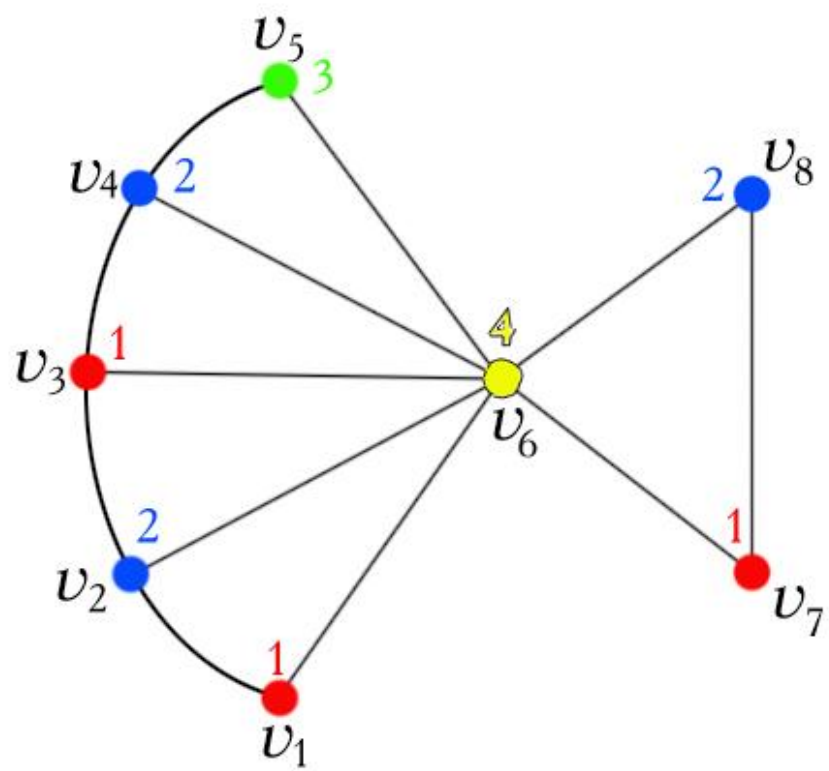
$$V_1\cup V_2\cup...\cup V_l=V,\qquad l\leq k,\;V_i\neq\emptyset,\;i=1,2,...,l.$$

$$V_i\text{ ---},$$

$$.$$

$$\begin{array}{ccccccc}
& & & & & k, & \\
& & & & k - & & G, \\
& & & & & & \\
& & X_p(G). & & & & \\
& & \cdot & X_p(G) = k, & & G & \\
k - & & \cdot & \cdot & \cdot & & \\
& k & & & & , & \\
& & & & \cdot & & \\
& & & & & & \\
& & & k - & & G & \\
& \cdot & & & & & \\
k = X_p(G) & & & & & \cdot &
\end{array}$$





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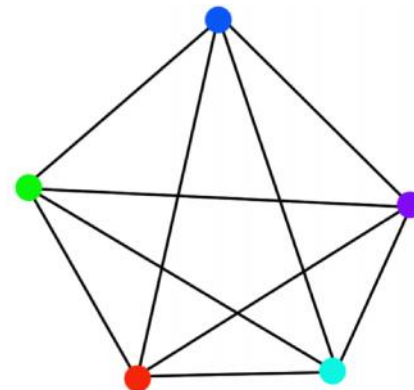
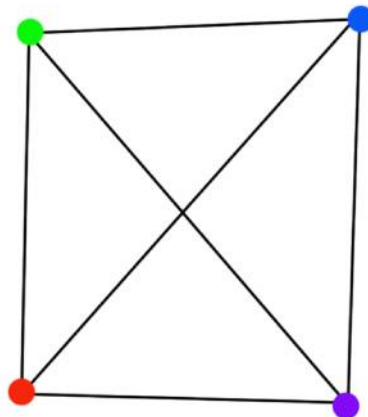
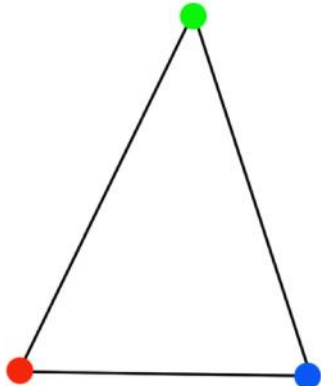
1.

K_n ,

n

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$$X_p(K_n) = n$$



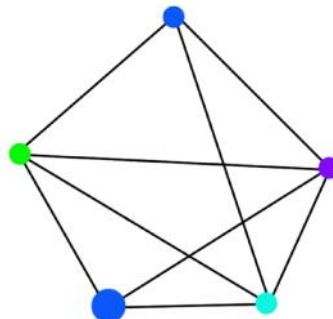
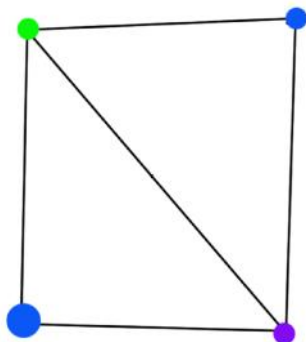
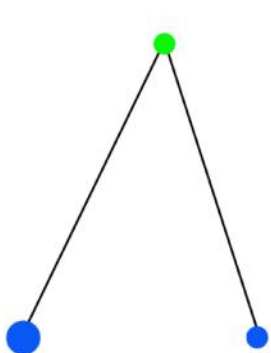
2.

$K_n - e$,

n

,

$$X_p(K_n - e) = n - 1$$

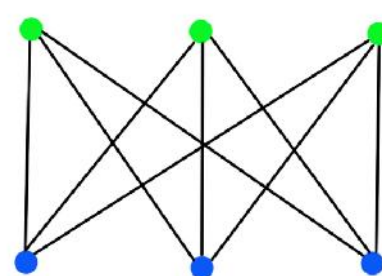
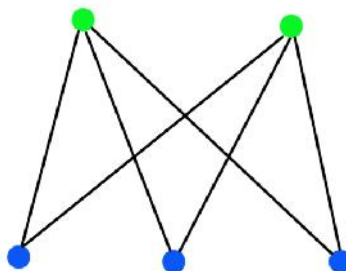
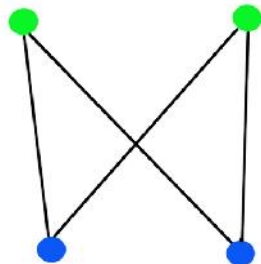
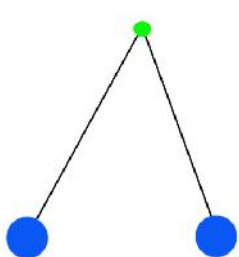


3.

$$|A| = m \quad |B| = n,$$

$$K_{m,n},$$

$$X_p(K_{m,n}) = 2$$



▪

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▪

1-

2-

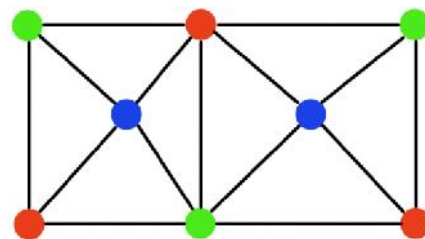
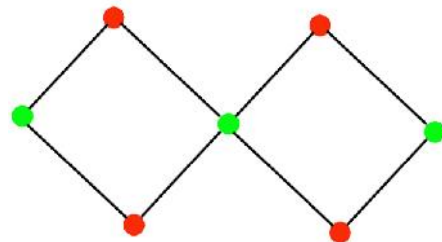
, 2-

3-

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n

n

K_m ,

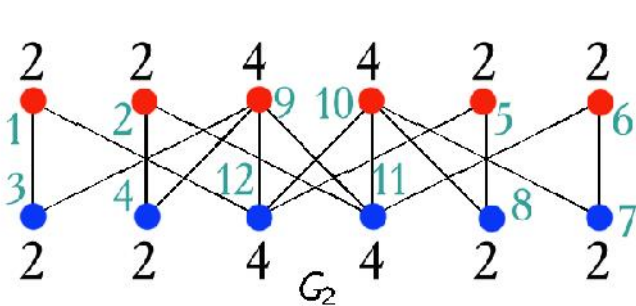
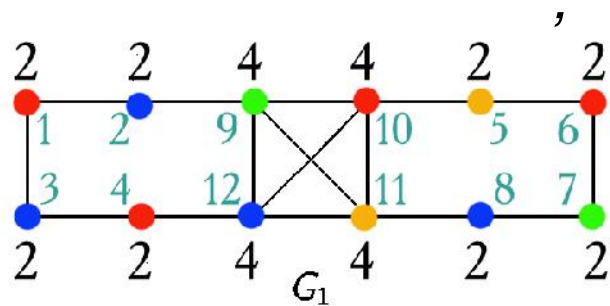
m .

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G_1

G_2

12

4

4

2,

, $x(G_1) = 4$, $x(G_2) = 2$,

G_1

K_4 .

G_2 —

, $x(G_2) = 2$.

$$X(G) \geq c, \quad c \text{ — } G.$$

$$, \quad X(G) \leq c, \quad c \text{ — } .$$

$$\cdot \quad , \quad G \quad , \quad G$$

$$\check{S}(G).$$

$$\cdot \quad G \text{ — } ,$$

$$\cdot \quad G$$

$$X(G) \geq \check{S}(G).$$

▪ G .

▪

G $s(G)$.

— ,

▪

G — , a \bar{G} — ,
 $s(G) = \check{S}(\bar{G})$.

$$X(G) \geq \frac{n(G)}{s(G)}$$

,

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G –

$n = n(G) -$

$G,$

$m = m(G) -$

$G,$

$$X(G) \geq \frac{n^2}{n^2 - 2m}$$

,

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)

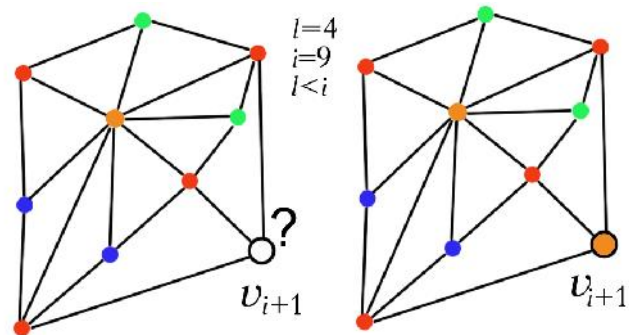
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1. v_1, v_2, \dots, v_i l
 $1, 2, \dots, l; \quad l \leq i,$ v_{i+1}



1.

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2.

1.

3.

1.

4.

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.4.1.–4.2.:

4.1.

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4.2.

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5.

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1.

2.

3.

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```
procedure visit(i: integer);
```

begin

```
if i = n + 1 then Print else
```

begin

```
for  $c := \text{color}[i] + 1$  to  $k$  do //  $k -$ 
```

if () **then**

```
begin color[i] := c; visit(i + 1); end else
```

```
visit(i);
```

end ;

end ;

« »

$G(V, E).$

1. $monochrom := \emptyset,$

, .

2.

« »

Procedure Greedy

For ($v \in V$) **do**

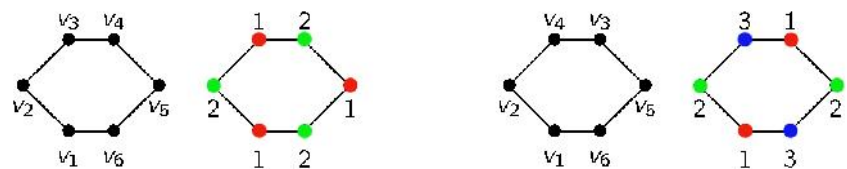
If $v \in monochrom$ **then**

begin

$color(v) :=$;

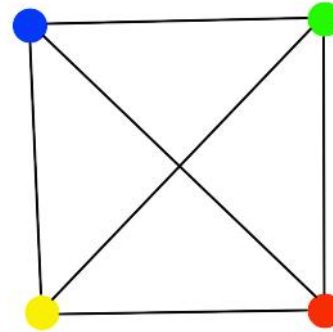
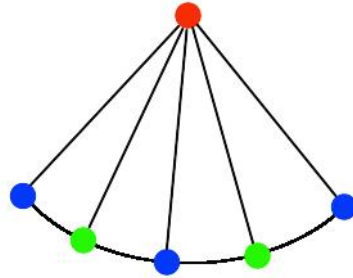
$monochrom := monochrom \cup \{v\}$

end.

$$(2 \quad \quad),$$


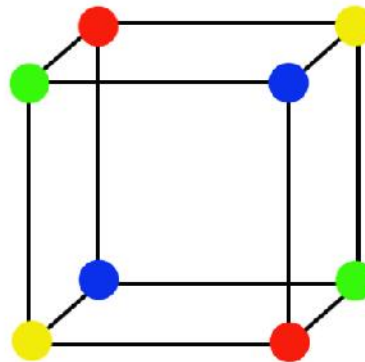
2.

$$X_p(G) \leq r + 1, \quad r = \max_{v \in V} (\deg(v)) .$$



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$r \geq 3,$

$X_p(G) \leq r$.

G —

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▪

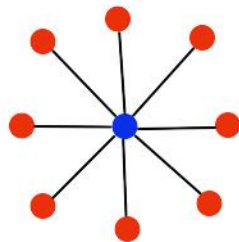
,

$$K_{1n},$$

$$n$$

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▪



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▪

($\chi_p(G) \leq 6$)

($\chi_p(G) \leq 5$)

4-

1976 (Kenneth Appel and Wolfgang Haken. Every Planar Map is Four Colorable. Contemporary Mathematics 98, American Mathematical Society, 1980).

8 v_1, v_2, \dots, v_8 .

a_1, a_2, \dots, a_6 .

:

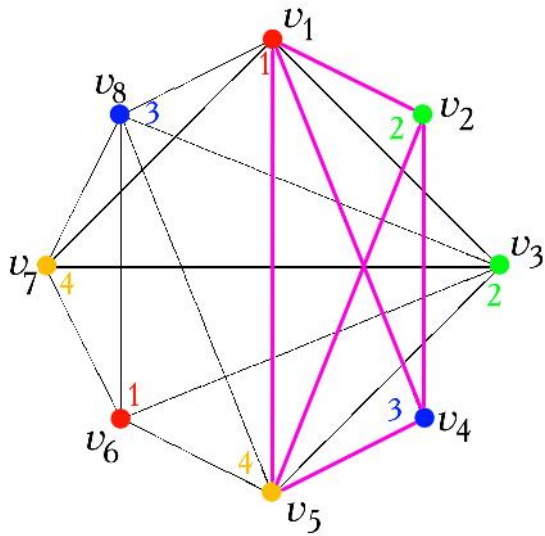
	v_1	v_2	v_3	v_4	v_5	v_6	v_7	v_8
a_1	+		+				+	+
a_2		+		+				
a_3			+			+	+	
a_4	+	+		+	+			
a_5			+		+			+
a_6					+	+		+

. 1 .

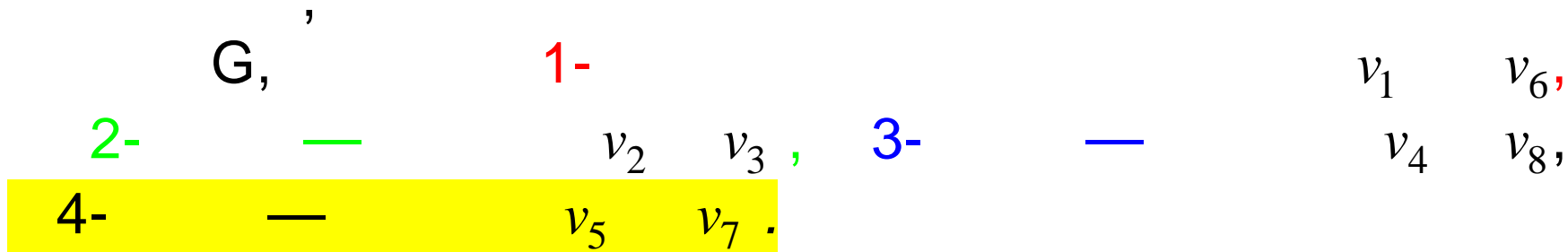
,

?

$G,$
 $v_1, v_2, \dots, v_8,$
 $($
 $).$



$K_4.$
 $v_1, v_2, v_4, v_5,$
 $X\{G\} \geq 4.$
 $G,$
 $X(G).$
 $4.$



	v_1	v_2	v_3	v_4	v_5	v_6	v_7	v_8
a_1	+		+				+	+
a_2		+		+				
a_3			+			+	+	
a_4	+	+		+	+			
a_5			+		+			+
a_6					+	+		+

1.

2.

3.

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1. : 1 2.

2.

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· Y,

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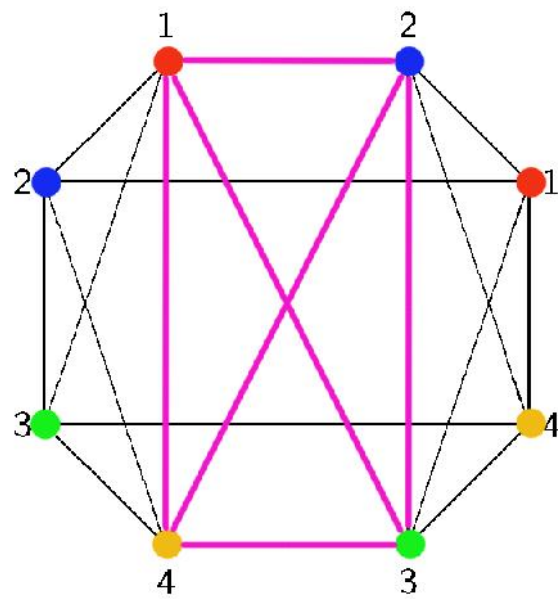
»

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1, 2, 1 2

K_4 .







4.
4



4,

4

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	1	2
1		
2		
3		
4	