

- 1.
- 2.
- 3.
- 4.
- 5.
- 6.
- 7.
- 8.
- 9.

- 10.
- 11.
12. « »
- 13.
- 14.
15. ,
- 16.
- 17.

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 • , , ;
 • , — ;
 • ;
 • .

$G = (V, E)$ — , k — .

$N_k = \{1, 2, \dots, k\}$, k - G . $f: V \rightarrow N_k$, k - ,

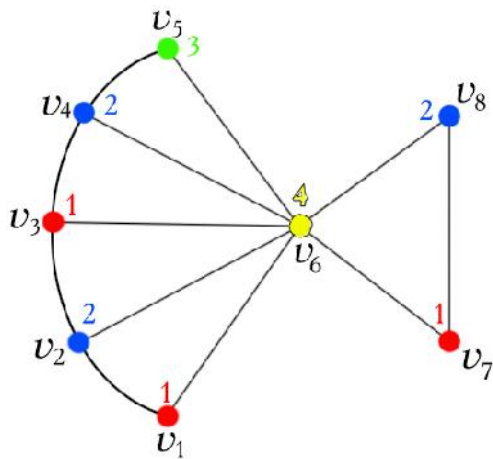
$f(u) \neq f(v)$.
 $(u,v) \in E$

k -
 $|V| = k$

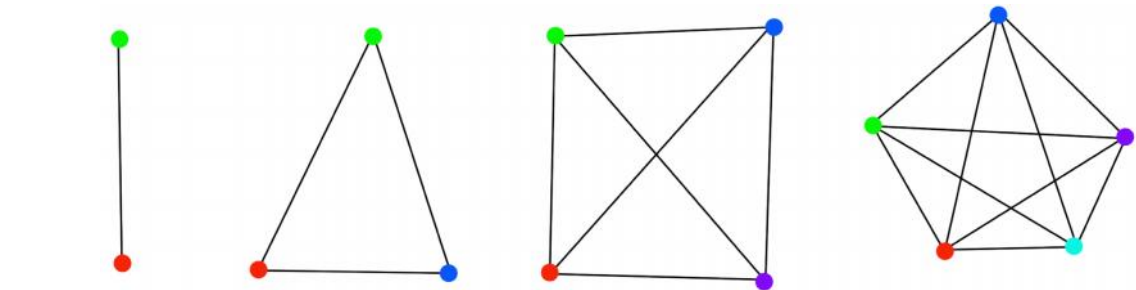
V
 G
 $V_1 \cup V_2 \cup \dots \cup V_l = V, \quad l \leq k, \quad V_i \neq \emptyset,$
 $i = 1, 2, \dots, l.$
 V_i —

k -
 G ,
 $X_p(G).$
 $X_p(G) = k,$
 k -
 $k = X_p(G)$

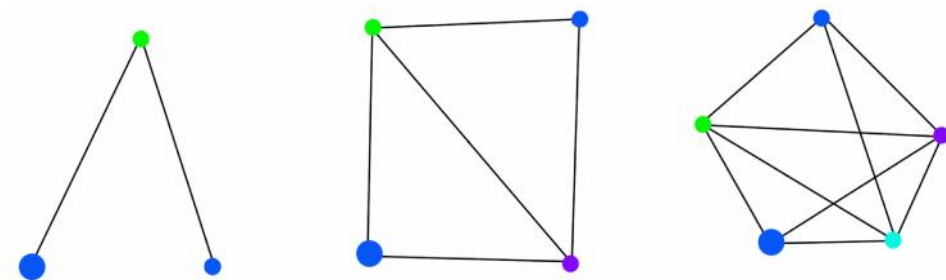
G ,
 $1, 2, 3, 4$



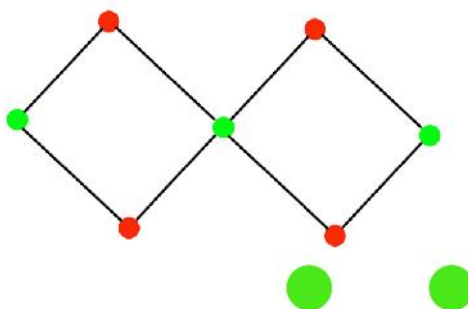
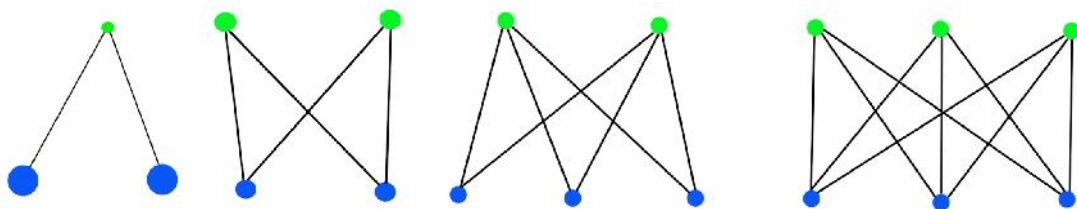
1. K_n , n ,
 $X_p(K_n) = n$



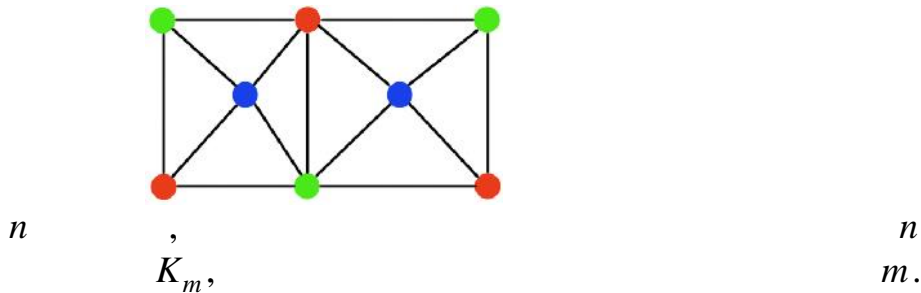
2. $K_n - e$, n
 $X_p(K_n - e) = n - 1$



3. $K_{m,n}$, $|A| = m$ $|B| = n$,
 $X_p(K_{m,n}) = 2$

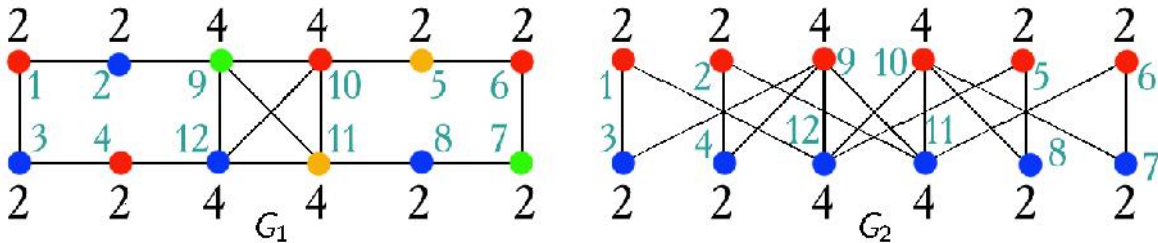


2-
3-
3-



$$r = \max_{v \in V} (\deg(v))$$

$G = (V, E)$.

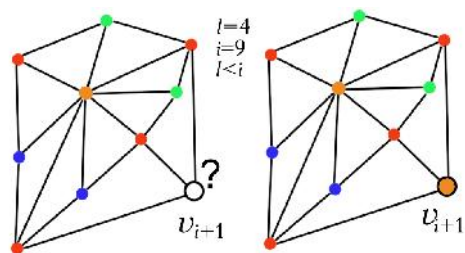


$$x(G_1) = 4, \quad x(G_2) = 2, \quad x(G_1) = 4, \quad x(G_2) = 2.$$

G_1 G_2 K_4 .

$$X(G) \geq c, \quad c = \dots, \quad X(G) \leq c,$$

G .



1.

2.

1.

3.

1.

4.

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.4.1.–4.2.:

4.1.

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4.2.

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5.

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1. .
2. , ,
3. , « » ,

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procedure visit(i: integer);
begin
  if i = n + 1 then Print else
    begin
      for c := color[i]+1 to k do // k -
        if ( ) then
          begin color[i] := c; visit(i + 1); end else
            visit(i);
          end;
    end;

```

« »
 $G(V, E)$.

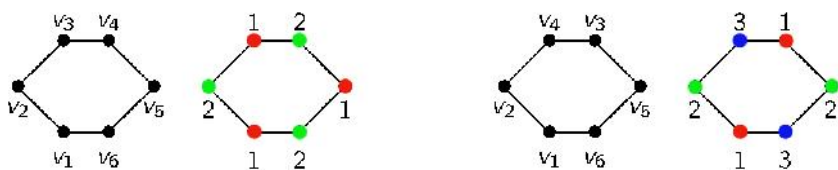
1. $monochrom := \emptyset$,
2. « »

Procedure Greedy

```

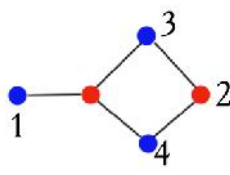
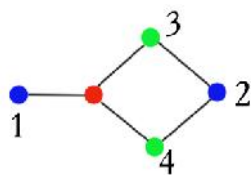
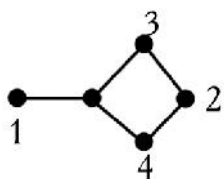
For (  $v \in V$  ) do
  If  $v \in monochrom$  then
    begin
      color(v) := ;
       $monochrom := monochrom \cup \{v\}$ 
    end

```



(2) ,

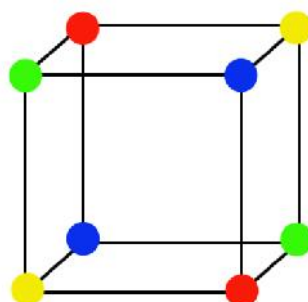
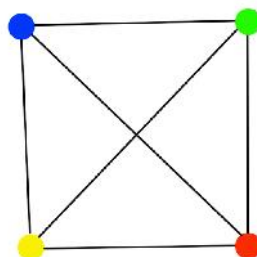
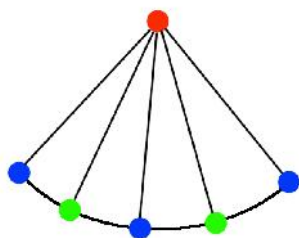
1 3 4, , , 2 . " 2, " ,
 1 2, 4' .



2.

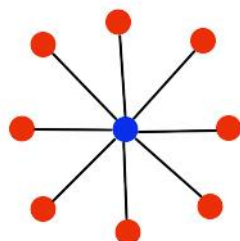
G

$$X_p(G) \leq r+1.$$



, , .
 . G — $r \geq 3$, $X_p(G) \leq r$.

, , K_{1n} ,
 n , .



($\frac{1}{2} - \frac{1}{2n}$)).

$X_p(G) \leq 6$.

$X_p(G) \leq 5$.

1976 (Kenneth Appel and Wolfgang Haken. Every Planar Map is Four Colorable. Contemporary Mathematics 98, American Mathematical Society, 1980).

v_1, v_2, \dots, v_8 .
 a_1, a_2, \dots, a_6 .

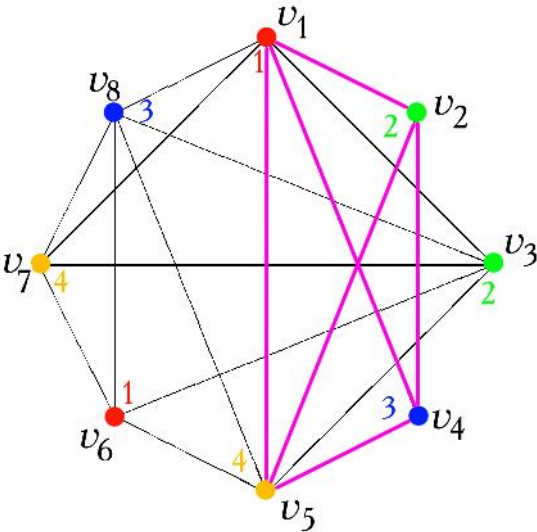
:

	v_1	v_2	v_3	v_4	v_5	v_6	v_7	v_8
a_1	+		+				+	+
a_2		+		+				
a_3			+			+	+	
a_4	+	+		+	+			
a_5			+		+			+
a_6					+	+		+

1

?

G ,
 v_1, v_2, \dots, v_8 ,
 $($,
 $)$.



v_1, v_2, v_4, v_5
 $X\{G\} \geq 4$.
 G ,
 K_4 .
 $X(G)$.
 4 .
 G ,

- 1- v_1 v_6 ,
- 2- v_2 v_3 ,
- 3- v_4 v_8 ,
- 4- v_5 v_7 .

	v_1	v_2	v_3	v_4	v_5	v_6	v_7	v_8
a_1	+		+				+	+
a_2		+		+				
a_3			+			+	+	
a_4	+	+		+	+			
a_5			+		+			+
a_6					+	+		+

1. , :
2. .
3. .

(, « »).

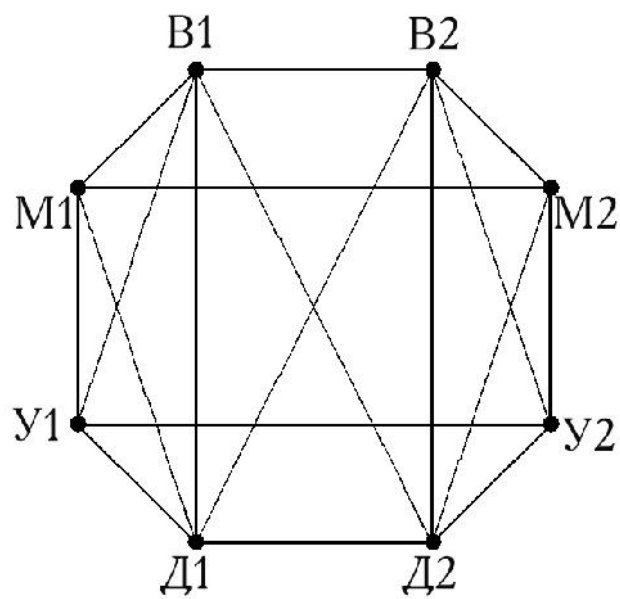
1. : 1 2.

2. :
 - — . ,
 - — . ,
 - — . Y,
 - — . Z.

, « » ,

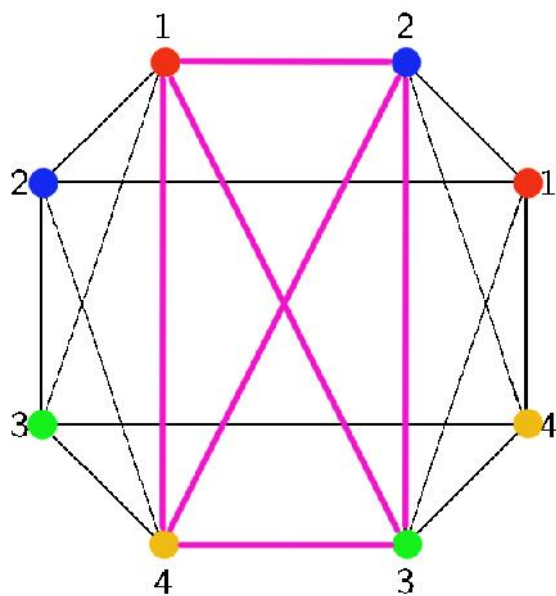
(. 1, 2, 1, 2, M1, 2, 1 2
 (, —).
 , ,

, :



1, 2, 1 2 ,
 K_4 .

4. 4 .



, 4, . . .
 4 .

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	1	2
1	.	.
2	.	.
3	.	.
4	.	.

