

- 1. .
- 2.
- 3.
- 4.
- 5.
- 6.
- 7.
- 8.
- 9.
- 10.
- 11.

- 12.
- 13.
- 14. « »
- 15.
- 16.
- 17. ,
- 18.
- 19.

$G(V,\Gamma)$. $S\subset V$,
 S ,
 ,
 $\Gamma^+(S)\cap S=\emptyset$.
 Φ

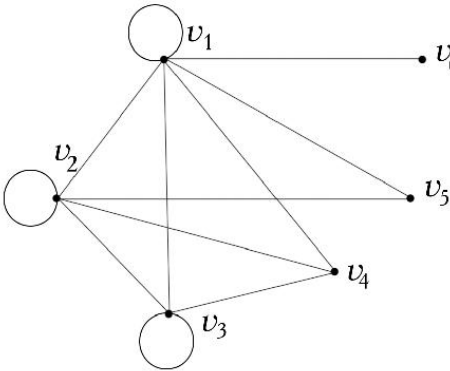
- 1. $\emptyset\in\Phi$, $S\in\Phi$.
- 2. $A\subset S$ $A\in\Phi$.

G ,

:

$a=\max_{S\in\Phi}|S|$.

.



$$S=\{v_4,v_5,v_6\}\text{ (}\quad\quad\quad\text{)},\quad\quad\quad G$$

$$a=3.$$

$$G(V,\Gamma).$$

$$,\quad\quad\quad T\subset V,\quad\quad\quad,$$

$$v\notin T\quad\quad\quad\Gamma^+(v)\cap T\neq\emptyset,$$

$$V\backslash T\subset\Gamma^{-1}(T).$$

$$\Psi\text{ --}\quad\quad\quad,$$

$$\quad\quad\quad:$$

$$1.\quad T\in\Psi.$$

$$2.\quad\quad T\subset A\quad\quad A\in\Psi.$$

$$\quad\quad\quad G,\quad\quad\quad,$$

$$\quad\quad\quad:$$

$$b=\min_{T\in\Psi}|T|.$$

$$\quad\quad\quad.$$

$$T=\{v_1\}\text{ (}\quad\quad\quad\text{)}\quad\quad\quad(\quad\quad\quad$$

$$T)\quad\quad\quad v_1\quad\quad T).$$

$$G\quad\quad\quad b=1.$$

$$i=1,2,\dots,l.$$
 V_i — $k -$
$$X_p(G).$$
$$X_p(G) = k,$$

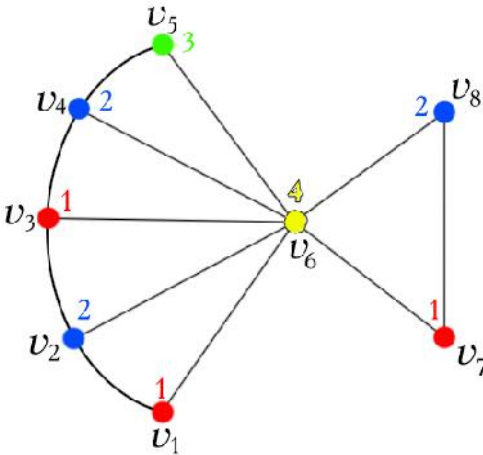
G

 k k $k -$

G

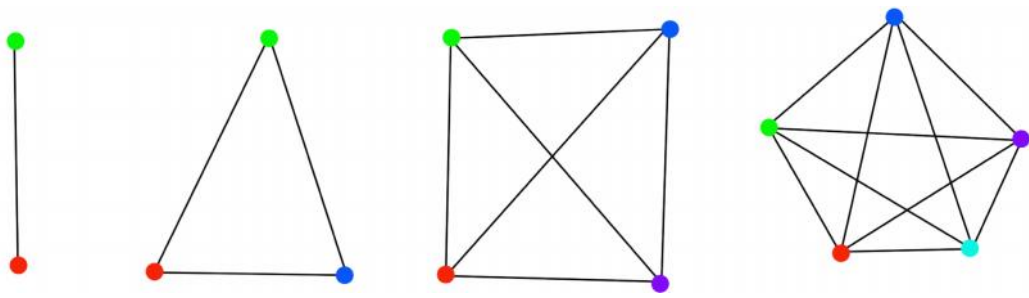
$$k = X_p(G)$$

G

 $k -$
$$1, 2, 3, 4,$$


1.

 K_n
$$n$$
$$X_p(K_n) = n$$

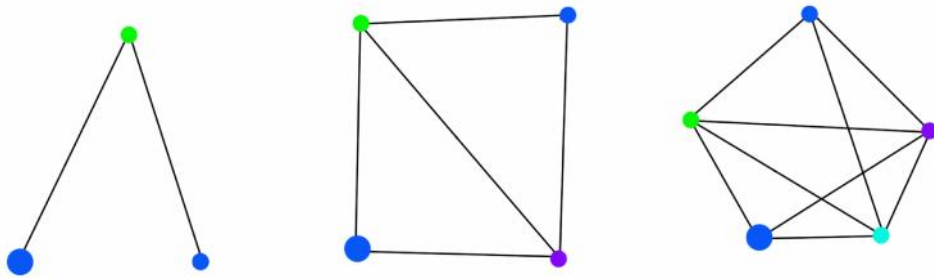


2.

$$K_n - e,$$

n

$$X_p(K_n - e) = n - 1$$

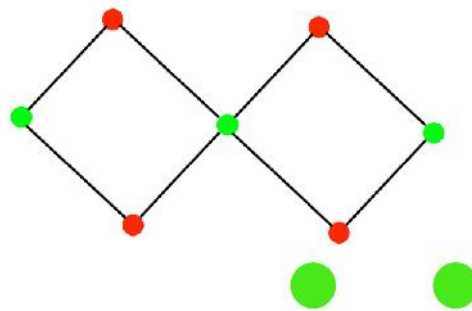
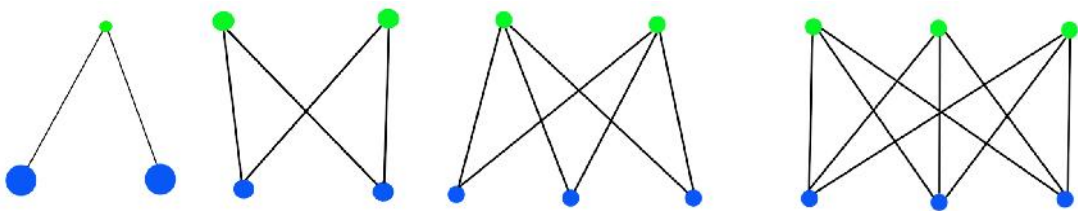


3.

$$K_{m,n},$$

$$|A| = m \quad |B| = n,$$

$$X_p(K_{m,n}) = 2$$



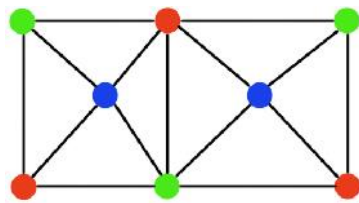
1-

2-

3-

3-

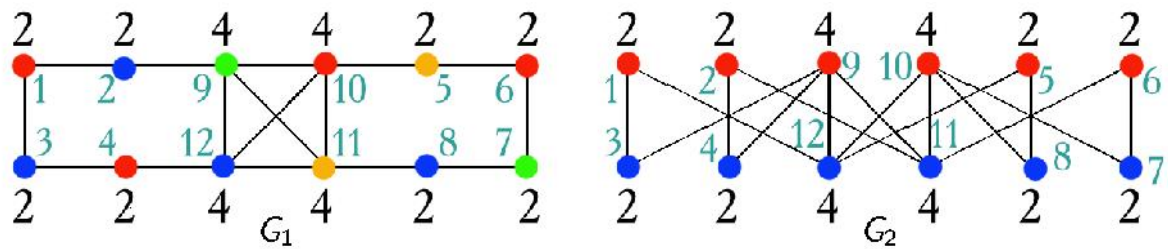
, 2-



n , K_m , n
 m .

$$r = \max_{v \in V} (\deg(v))$$

$$G=(V,E).$$



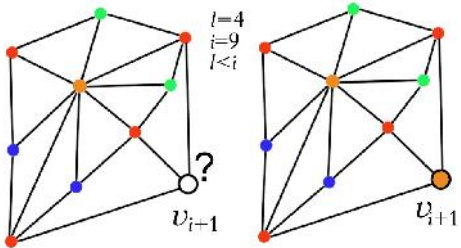
G_1 G_2 .
4 4 12 2,

$x(G_2) = 2$, G_1 $x(G_1) = 4$,
 G_2 — K_4 .
 $x(G_2) = 2$.

$$X(G) \geq c, \quad c \text{ —}$$

$$G. \quad X(G) \leq c,$$

c .
 G , G , $\check{S}(G)$.
 G -



- 1.
2. 1.
3. 1.
4. , 4.1.–4.2.:
- 4.1. ,
- 4.2. .
5. .

.
 —
 .
 . —
 .
 .
 ,
 ,
 .
 .
 .

1. .
2. , ,
3. , « » ,

```

procedure visit(i: integer);
begin
  if i = n + 1 then Print else
    begin
      for c := color[i]+1 to k do // k -
        if ( ) then
          begin color[i] := c; visit(i + 1); end else
            visit(i);
          end;
    end;
end;

```

« »
 $G(V, E)$.

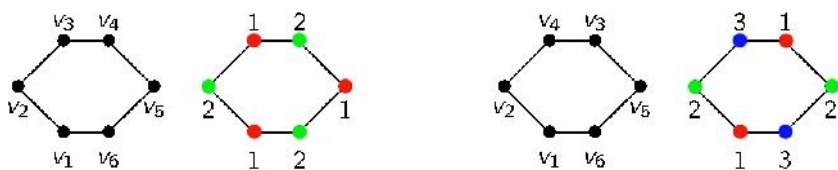
1. $monochrom := \emptyset$,
2. « »

Procedure Greedy

```

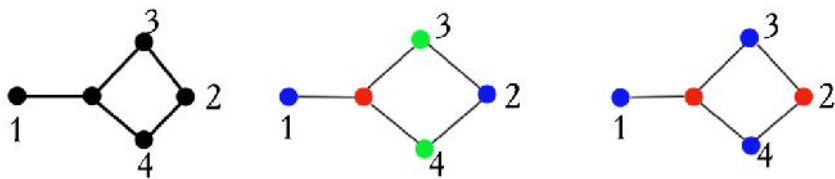
For (  $v \in V$  ) do
  If  $v \in monochrom$  then
    begin
      color(v) := ;
       $monochrom := monochrom \cup \{v\}$ 
    end

```



(2) ,

1 3 4, , , 2 . " 2, " ,
 1 2, 4' .



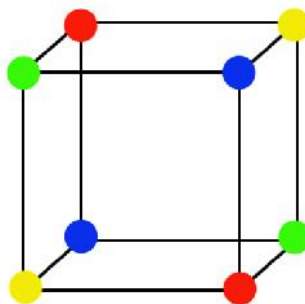
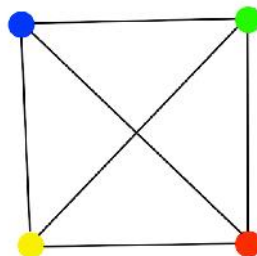
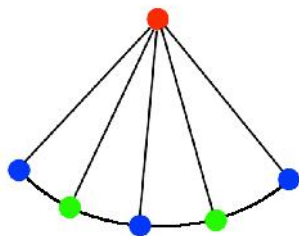
2.

$$r = \max_{v \in V} (\deg(v))$$

G

$$X_p(G) \leq r + 1,$$

$$G = (V, E).$$

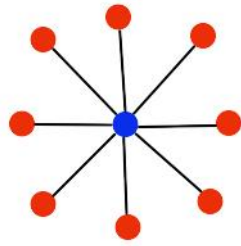


, , .

$$G — r \geq 3, \quad X_p(G) \leq r .$$

, , K_{1n} ,

$$n$$
 , .



(\dots), (\dots)).
 \cdot

$X_p(G) \leq 6$.

$X_p(G) \leq 5$.

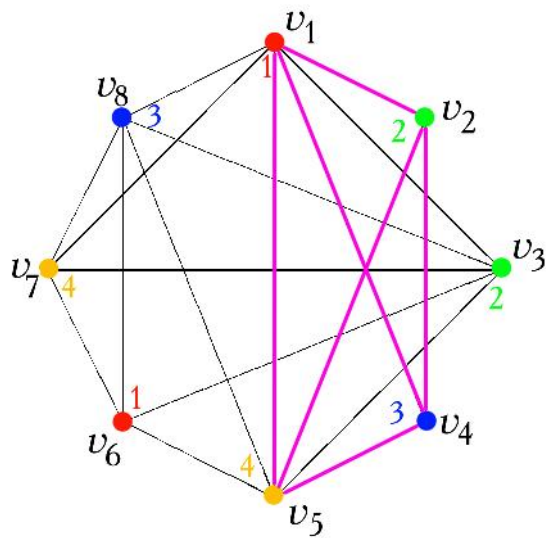
1976 (Kenneth Appel and Wolfgang Haken. Every Planar Map is Four Colorable. Contemporary Mathematics 98, American Mathematical Society, 1980).

8 v_1, v_2, \dots, v_8 .
 a_1, a_2, \dots, a_6 .

:

	v_1	v_2	v_3	v_4	v_5	v_6	v_7	v_8
a_1	+		+				+	+
a_2		+		+				
a_3			+			+	+	
a_4	+	+		+	+			
a_5			+		+			+
a_6					+	+		+

. 1 .
 ,
 ?
 . G ,
 v_1, v_2, \dots, v_8 ,
 (, ,
).



v_1, v_2, v_4, v_5 G , K_4 .
 $X\{G\} \geq 4$. $X(G)$.
 4 .
 G ,

1- v_1 v_6 ,
 2- v_2 v_3 ,
 3- v_4 v_8 ,
 4- v_5 v_7 .

	v_1	v_2	v_3	v_4	v_5	v_6	v_7	v_8
a_1	+		+				+	+
a_2		+		+				
a_3			+			+	+	
a_4	+	+		+	+			
a_5			+		+			+
a_6					+	+		+

1. , : .
2. .
3. .

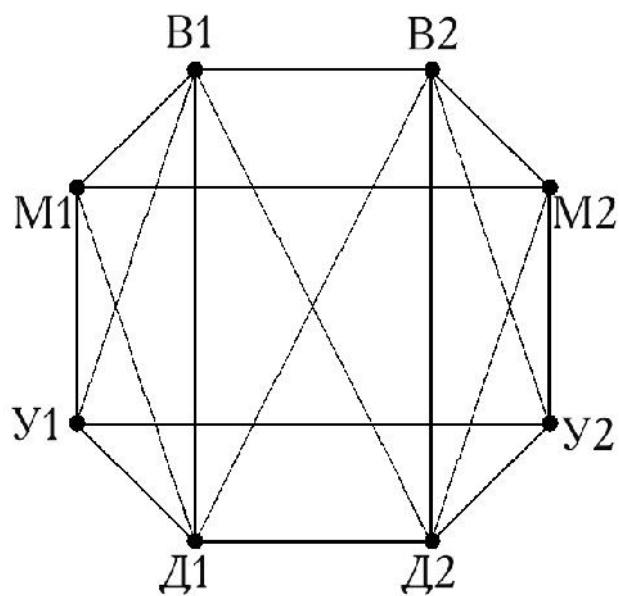
(, « »).

1. : 1 2.

2. :
 - — . ,
 - — . ,
 - — . Y,
 - — . Z.

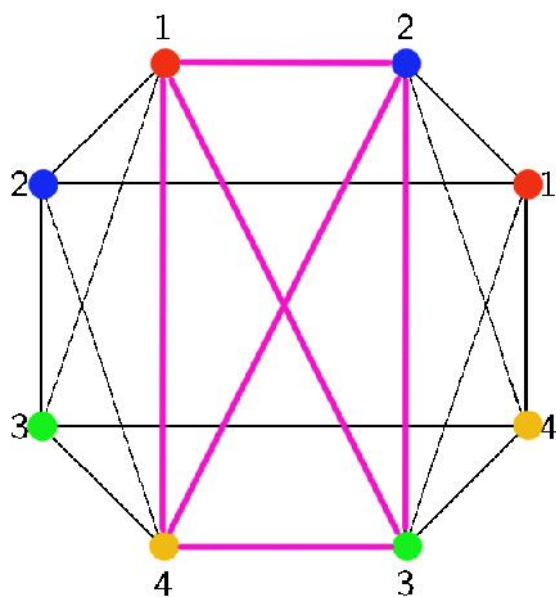
, « » ,

(. 1, 2, 1, 2, M1, 2, 1 2
 (, —).
 , ,
 . :
 ,



1, 2, 1 2 ,
 K_4 .

4. 4 .



, 4, . . .
 4 .

.

	1	2
1	.	.
2	.	.
3	.	.
4	.	.

