

# CSULA PROGFEST 2014

## Problem 3 Lazy Days

Eddie is a sophomore studying computer science, and is failing his discrete mathematics course. It's not that he doesn't understand the concepts: it's just that he's too lazy, or too smart(so he claims), to do homework. Staring at the chapter homework for functions and relations, he realized that he could write a program to do the homework for him. He learned the following definitions in class:

**Definition 1.** A **relation** from a set  $A$  to a set  $B$  is a set of ordered pairs  $(a, b)$  where  $a$  is an element of  $A$  and  $b$  is an element of  $B$ . i.e.  $\{(-4, 1), (-2, 3), (0, -5)\}$ , set  $A$  is  $\{-4, -2, 0\}$  and set  $B$  is  $\{1, 3, -5\}$  The set  $A$  is the **domain** of the relation and set  $B$  is its **codomain**.

**Definition 2.** A **function** is a relation that satisfies:

- for each element  $a$  in the domain, there is an element  $b$  in its codomain such that  $(a, b)$  is in the relation, and
- if  $(a, b)$  and  $(a, c)$  are in the relation, then  $b = c$ .

**Definition 3. one-to-one:** A function is said to be one-to-one, if and only if each element in the codomain corresponds to no more than one element in the domain.

**Definition 4. onto:** A function is said to be onto, if and only if each element of the codomain of the function has a corresponding element in the domain.

**Definition 5. bijective:** A function is said to be bijective if and only if it is both one-to-one and onto.

Your job is to design a program that, given a domain and codomain and a list of relations using them, determine what type of functions the relations are, if they are functions at all.

### Input

The first line will contain a list of  $D$  integers separated by commas, denoting the domain for all relations to be tested,  $1 \leq D \leq 100$ . The second line will contain a list of  $C$  integers separated by commas, denoting the codomain for all relations to be tested,  $1 \leq C \leq 100$ . The third line will contain a single integer, denoting the number of relations to be tested. Each relation consists of one line, denoting the relation in set notation.

### Output

For each relation, print, on a single line whether it's "not a function" or "function". If it is a function, print a single comma after "function", followed by either "one-to-one", "onto", "bijective", or nothing at all if it doesn't fall into any of the categories.

### Sample Input

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```
1,2,6,7,8,9
1,2,3,4,5
4
{(1 1),(1 2),(2 3),(6 5),(7 4)}
{(1 1),(2 2),(6 3),(7 4),(8 5)}
{(1 4),(2 4),(6 4),(7 4),(8 4)}
{(1 1),(2 2),(6 3),(7 5),(8 5),(9 4)}
```

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### Sample Output

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```
not a function
function,bijective
function
function,onto
```

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