



SRM INSTITUTE OF SCIENCE & TECHNOLOGY

DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING

18CSC305J-ARTIFICIAL INTELLIGENCE

SEMESTER – 6

BATCH-2

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Exercise: 1

Date : 21-01-2021

TOY PROBLEM

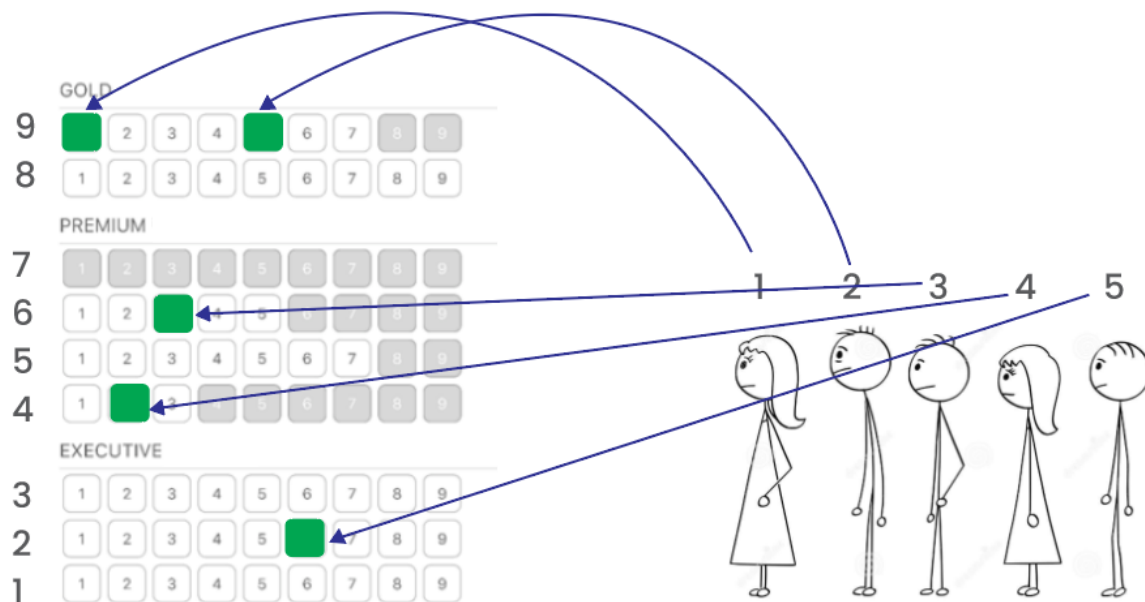
Problem Statement : Given an integer N and an array of seats[] where N is the number of people standing in a line to buy a movie ticket and seat[i] is the number of empty seats in the i th row of the movie theater. The task is to find the maximum amount a theater owner can make by selling movie tickets to N people. Price of a ticket is equal to the maximum number of empty seats among all the rows.

Algorithm :

1. Initialize queue q insert all seats array elements to the queue.
2. Tickets sold and the amount generated to be set to 0.
3. If tickets sold $< N$ (People in the queue) and q top > 0
4. Then remove top element from queue and update total amount
5. Repeat step 3 and 4 until tickets sold = number of people in the queue.

Optimization technique : This problem can be solved by using a priority queue that will store the count of empty seats for every row and the maximum among them will be available at the top.

1. Create an empty priority_queue q and traverse the seats[] array and insert all elements into the priority_queue.
2. Initialize two integer variable ticketSold = 0 and ans = 0 that will store the number of tickets sold and the total collection of the amount so far.
3. Now check while ticketSold $< N$ and $q.top() > 0$ then remove the top element from the priority_queue and update ans by adding top element of the priority queue. Also store this top value in a variable temp and insert temp - 1 back to the priority_queue.
4. Repeat these steps until all the people have been sold the tickets and print the final result.



Priority Queue

[2, 6, 9, 4, 9] ← Filling in Queue
 5 3 2 4 1 ← Actual Priority

■ = Available Seats

Normal Queue

[1, 2, 3, 4, 5]

Simple FIFO approach

Tool : VS Code and Python 3.9.0

Programming code :

```
def maxAmount(M, N, seats):
```

```
    q = []
```

```
    for i in range(M):
```

```
        q.append(seats[i])
```

```
ticketSold = 0
```

```
ans = 0
```

```
q.sort(reverse = True)
```

```
while (ticketSold < N and q[0] > 0):
```

```
    ans = ans + q[0]
```

```
    temp = q[0]
```

```
    q = q[1:]
```

```
    q.append(temp - 1)
```

```
    q.sort(reverse = True)
```

```
    ticketSold += 1
```

```
return ans
```

```
if __name__ == '__main__':
```

```
    seats = []
```

```
    rows = int(input("Enter number of rows available : "))
```

```
    for i in range(0, rows):
```

```
        empty = int(input())
```

```
seats.append(empty)

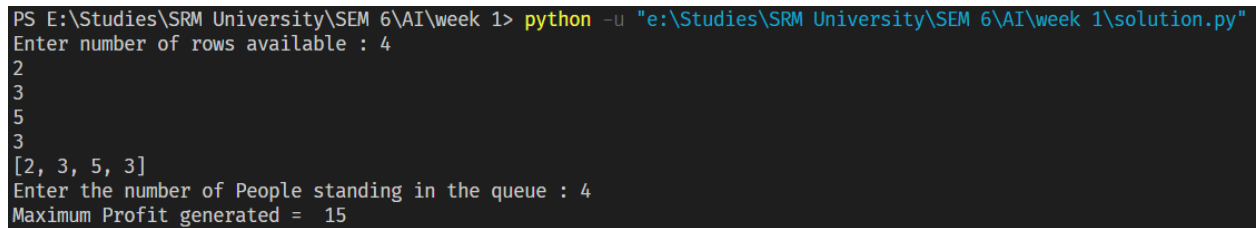
print(seats)

M = len(seats)

N = int(input("Enter the number of People standing in the queue : "))

print("Maximum Profit generated = ", maxAmount(N, M, seats))
```

Output screen shots :



```
PS E:\Studies\SRM University\SEM 6\AI\week 1> python -u "e:\Studies\SRM University\SEM 6\AI\week 1\solution.py"
Enter number of rows available : 4
2
3
5
3
[2, 3, 5, 3]
Enter the number of People standing in the queue : 4
Maximum Profit generated = 15
```

Result : Successfully found out the maximum amount the theater owner can make by selling movie tickets to N people for a movie.

Exercise: 2

Date : 29-01-2021

GRAPH COLORING PROBLEM

PROBLEM STATEMENT : Given a graph color its edges such that no two adjacent have the same color using minimum number of colors and return the Chromatic number.

ALGORITHM :

Initialize:

1. Color first vertex with first color.

Loop for remaining $V-1$ vertices.:

1. Consider the currently picked vertex and color it with the lowest numbered color that has not been used on any previously colored vertices adjacent to it.

2. If all previously used colors appear on vertices adjacent to v , assign a new color to it.

3. Repeat the following for all edges.

4. Index of color used is the chromatic number.

OPTIMIZATION TECHNIQUE:

Graph coloring problem is to assign colors to certain elements of a graph subject to certain constraints.

Vertex coloring is the most common graph coloring problem. The problem is, given m colors, find a way of coloring the vertices of a graph such that no two adjacent vertices are colored using

the same color. The other graph coloring problems like Edge Coloring (No vertex is incident to two edges of same color) and Face Coloring (Geographical Map Coloring) can be transformed into vertex coloring.

Chromatic Number: The smallest number of colors needed to color a graph G is called its chromatic number. For example, the following can be colored at least 2 colors.

TOOLS : VS Code, Python 3.9.0

CODE - EDGE COLORING :

```
import matplotlib.pyplot as plt

import networkx as nx

from matplotlib.patches import Polygon

import numpy as np


G = nx.Graph()


colors = {0:"red", 1:"green", 2:"blue", 3:"yellow"}


G.add_nodes_from([1,2,3,4,5])

G.add_edges_from([(1,2), (1,3), (2,4), (3,5), (4,5)])


nodes = list(G.nodes)

edges = list(G.edges)


color_lists = []
```



```

color_of_edge = []

some_colors = ['red','green','blue','yellow']


for i in range(len(nodes) + 1):

    color_lists.append([])

    color_of_edge.append(-1)


def getSmallestColor(ls1,ls2):

    i = 1

    while(i in ls1 or i in ls2):

        i = i + 1

    return i


#iterate over edges

i = 0

for ed in edges:

    newColor = getSmallestColor(color_lists[ed[0]],color_lists[ed[1]])

    color_lists[ed[0]].append(newColor)

    color_lists[ed[1]].append(newColor)

    color_of_edge[i] = newColor

    i = i + 1


# Makin graph again

```

```
G = nx.Graph()
```

```
for i in range(len(edges)):
```

```
    G.add_edge(edges[i][0],edges[i][1],color=some_colors[color_of_edge[i]-1])
```

```
colors = nx.get_edge_attributes(G,'color').values()
```

```
nx.draw(G, edge_color=colors, with_labels=True, width=2)
```

```
plt.show()
```

OUTPUT :

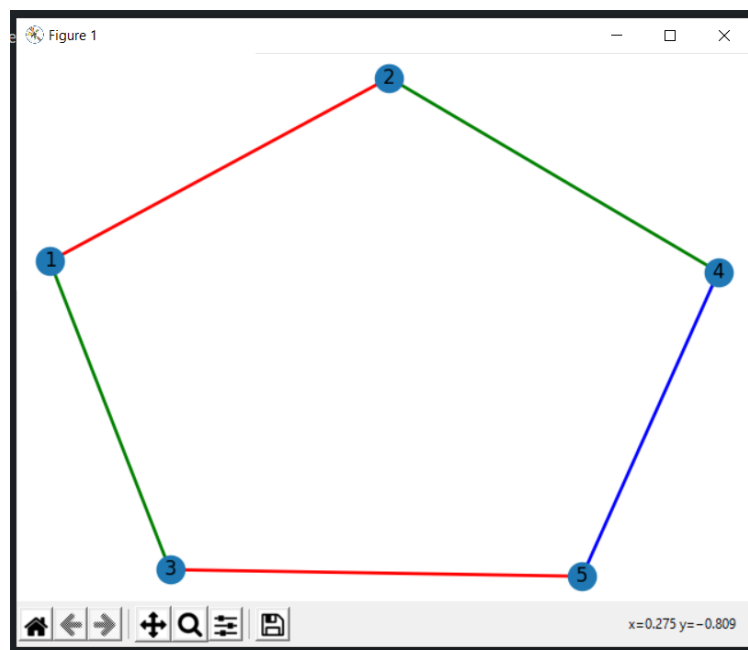


Fig: Edge Coloring

CODE - VERTEX COLORING :

```
import matplotlib.pyplot as plt
```

```
import networkx as nx
```

```
G = nx.Graph()
```

```
colors = {0:"red", 1:"green", 2:"blue"}
```

```
G.add_nodes_from([1,2,3,4,5])
```

```
G.add_edges_from([(1,2), (1,3), (2,4), (3,5), (4,5)])
```

```
d = nx.coloring.greedy_color(G, strategy = "largest_first")
```

```
node_colors = []
```

```
for i in sorted (d.keys()):
```

```
    node_colors.append(colors[d[i]])
```

```
nx.draw(G, node_color = node_colors, with_labels = True, width = 5)
```

```
plt.show()
```

OUTPUT :

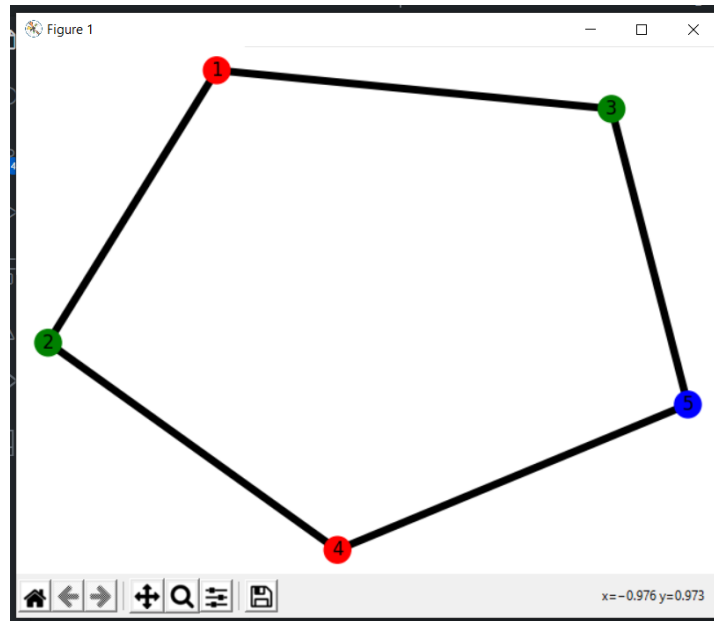


Fig : Vertex Coloring

CODE - FACE COLORING :

```
import networkx as nx

G = nx.Graph()

colors = {0:"red", 1:"green", 2:"blue", 3:"yellow"}

G.add_nodes_from([1,2,3,4,5])

G.add_edges_from([(1,2), (1,3), (2,4), (3,4), (4,5)])

nodes = list(G.nodes)

edges = list(G.edges)

some_colors = ['red','green','blue','yellow']

no_of_faces = len(edges)+2-len(nodes)-1

def regionColour(regions):
```

```

print("NO OF FACES : "+str(regions))

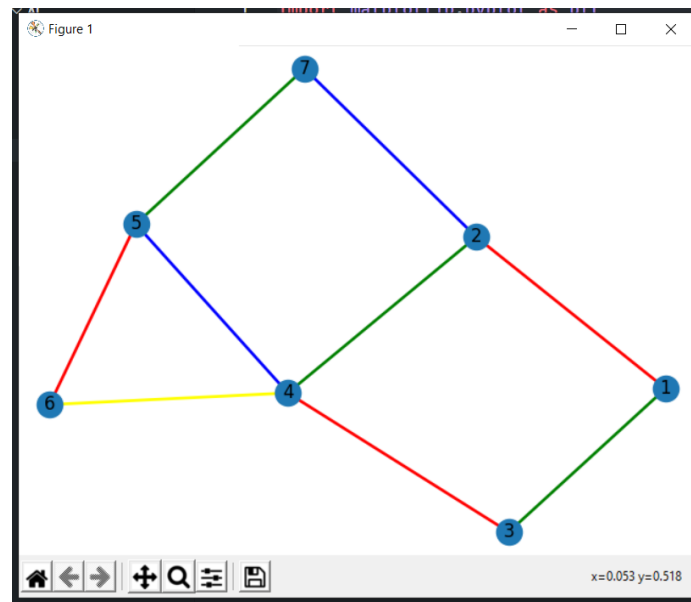
for i in range(1,regions+1):

    print("FACE 1 : "+some_colors[i%4])

regionColour(no_of_faces)

```

OUTPUT :



```

NO OF FACES : 3
FACE 1 : green
FACE 2 : blue
FACE 3 : yellow
PS E:\Studies\SRM University\SEM 6\AI> 

```

fig: Face Coloring

RESULT :

Edge, vertex and face coloring problem which are together known as graph coloring problem solved and visualized in an optimized way using greedy approach.

Date : 05-02-2021

1) SEND + MORE = MONEY

1. From Column 5, $M=1$, since it is only carry-over possible from sum of 2 single digit number in column 4.
2. To produce a carry from column 4 to column 5 ' $S + M$ ' is at least 9 so ' $S=8 \text{ or } 9$ ' so ' $S+M=9 \text{ or } 10$ ' & so ' $O = 0 \text{ or } 1$ '. But ' $M=1$ ', so ' $O = 0$ '.
3. If there is carry from Column 3 to 4 then ' $E=9$ ' & so ' $N=0$ '. But ' $O = 0$ ' so there is no carry & ' $S=9$ ' & ' $c_3=0$ '.
4. If there is no carry from column 2 to 3 then ' $E=N$ ' which is impossible, therefore there is carry & ' $N=E+1$ ' & ' $c_2=1$ '.
5. If there is carry from column 1 to 2 then ' $N+R=E \bmod 10$ ' & ' $N=E+1$ ' so ' $E+1+R=E \bmod 10$ ', so ' $R=9$ ' but ' $S=9$ ', so there must be carry from column 1 to 2. Therefore ' $c_1=1$ ' & ' $R=8$ '.
6. To produce carry ' $c_1=1$ ' from column 1 to 2, we must have ' $D+E=10+Y$ '

as Y cannot be 0/1 so D+E is at least 12. As D is at most 7 & E is

At least 5 (D cannot be 8 or 9 as it is already assigned). N is at most 7

& 'N=E+1' so 'E=5or6'.

7. If E were 6 & D+E at least 12 then D would be 7, but 'N=E+1' & N would also be 7 which is impossible. Therefore 'E=5' & 'N=6'.

8. D+E is at least 12 for that we get 'D=7' & 'Y=2'.

SOLUTION:

$$\begin{array}{r} 9 \ 5 \ 6 \ 7 \\ + \ 1 \ 0 \ 8 \ 5 \\ \hline 1 \ 0 \ 6 \ 5 \ 2 \end{array}$$

VALUES:

$$S=9$$

$$E=5$$

$$N=6$$

$$D=7$$

$$M=1$$

$$O=0$$

$$R=8$$

$$Y=2$$

2. BASE + BALL = GAMES

Assuming numbers can't start with 0, G is 1 because two four-digit numbers can't sum to 20000 or more.

$SE + LL = ES$ or $1ES$.

If it is ES , then LL must be a multiple of 9 because SE and ES are always congruent mod 9. But LL is a multiple of 11, so it would have to be 99, which is impossible.

So $SE + LL = 1ES$. LL must be congruent to 100 mod 9. The only multiple of 11 that work is 55, so L is 5.

$SE + 55 = 1ES$. This is possible when $E + 5 = S$. The possibilities for ES are 27, 38, or 49.

$BA + BA + 1 = 1AM$. B must be at least 5 because $B + B$ (possibly +1 from a carry) is at least 10.

If A is less than 5, then $A + A + 1$ does not carry, and A must be even. Inversely, if A is greater than 5, it must be odd. The possibilities for A are 0, 2, 4, 7, or 9.

0 does not work because M would have to be 1.

2 and 7 don't work because M would have to be 5.

9 doesn't work because M would also have to be 9.

So A is 4, M is 9, and B is 7. This leaves 38 as the only possibility for ES . The

full equation is:

7483

+ 7455

14938

3. TWO + TWO = FOUR

$F = 1$ for carry over $T \geq 5$.

'O' can't be 0 as R will be 0. So T can't be 5 so let $T \geq 6$

If $T = 6$, $O = 2$ and $R = 4$ and $W + W = U$ for W can't be 1,2,6,4. $W < 4$ to avoid carry over. W can't be 3 as U will be 6.

So $T = 7$, so, O can be 4 or 5 depending on whether or $W + W > 10$. If O is 4 then

$R = 8$. W can't be 1, 2. So $W = 3$

If $W = 3$ then $U = 6$ hence

Here is one + answer:

7 3 4

+ 7 3 4

1 4 6 8

4. CROSS + ROADS= DANGER

Solution:

C5C4C3C2C1

CROSS

+ROADS

DANGER

Since it is already mentioned that the carry value of resultaint cannot be 0 then

let's presume that the carry value of D is 1

We know that the sum of two similar values is even, hence R will have an even

value

Hence $S+S=R$ So R is an even number for sure.

So the value of R can be (0, 2, 4, 6, 8)

Value of R cannot be 0 as two different values cannot be allotted the same

Digit, (if $S=10$ then their sum = 20 carry forward 2, then the value of $R=0$)

which is not possible.

IF $S=1$:

Not possible since D has the same value.

IF $S=2$

Then $R=4$ which is possible Hence $S=2$ and $R=4$

$$C4+C+R=A+10$$

$$C4+C+4=A+10$$

$C4+C>5$ (Being the value of carry will be generated when the value of C is

greater than 5

$$C=9$$

$$C1+S+D=E$$

$$C1+2+1=E$$

$$\text{Therefore } E=3$$

$$C4+C+R=A+10$$

$$C4+9+4=A+10$$

Therefore $A=3$ but it cannot be possible as $E=3$

Now let's Consider $S+D+C1=E$

$$2+1+0=3$$

Therefore $E = 3$ making $C_2 = 0$ since $2+1=3$

Now let's consider the equation again:

$$C + R + C_4 = A + 10$$

$$9 + 4 + 0 = A + 10$$

$$13 = A + 10$$

Therefore $A = 3$ but $E = 3$

So A is not equal to 3

Again considering $R = 6$ So $S = 3$ $C_4 = 0$

$$C + R + C_4 = A + 10$$

$$9 + 6 + 0 = A + 10$$

$$15 = A + 10$$

Therefore $A = 5$

And $S + D + C_1 = E$

$$3 + 1 + 0 = E \text{ therefore } E = 4 \text{ and } C_2 = 0$$

Now considering the equation

$$R + O + C_3 = N$$

$$6 + 0 + C_3 = N$$

So $6 + 0 + C_3 < \text{or equal to } 3$

$$\text{Let } C_3 = 1$$

Then $O < \text{or equal to } 2$

That is $O = 0, 1, 2$

$$\text{Let } O = 2$$

Again considering $R + O + C_3 = N$

$$6+2+1=N$$

Hence $N=9$ but $C=9$ so N cannot be equal to 9.

Now let $N=8$ and $C_3=0$

Let us consider equation

$$O+A+C_2=G$$

Therefore $G=7$

Hence $D=1$ $S=3$ $A=5$ $G=7$ $C=9$ $O=2$ $E=4$ $R=6$ $N=8$

And $C_1=0$ $C_2=0$ $C_3=0$ $C_4=0$ $C_5=1$

Now verifying the above values in the equation we get:

$$C_5C_4C_3C_2C_1$$

CROSS

96233

ROADS

62513

Shape

DANGER

158746

5. If $AA + BB = ABC$

Explanation:

$$\begin{array}{r} AA \\ BB + \\ CC \\ \hline \end{array}$$

$$\begin{array}{r} ABC \\ \hline \end{array}$$

The digits are distinct and positive. Let's first focus on the value A, when we add three 2 digit numbers the most you get is in the 200's (ex: $AA + BB + CC = ABC$ u $99 + 88 + 77 = 264$). From this, we can tell that the largest value of A can be 2. So Either $A = 1$ or $A = 2$.

Now focus on value B, let's take the unit digit of the given question: $A + B + C = C$ (units). This can happen only if $A + B = 0$ (in the units) u A and B add up to 10.

Two possibilities: $11 + 99 + CC = 19C$ u (1) or $22 + 88 + CC = 28C$ u (2)

Take equation (2), $110 + CC = 28C$

Focus on ten's place, $1 + C = 8$, here $C = 7$. Then $22 + 88 + 77 = 187$

Thus, Equation (2) is not possible.

From Equation (1), $11 + 99 + CC = 19C$ u $110 + CC = 19C$ u $1 + C = 9$, then $C = 8$.

$11 + 99 + 88 = 198$ u hence solved $A = 1, B = 9$ and $C = 8$

$A + B + C = 18$

$$6. \text{NO} + \text{GUN} + \text{NO} = \text{HUNT}$$

Solution:

$$\begin{array}{r} \text{N O} \\ + \text{G U N} \\ \text{N O} \\ \hline \text{H U N T} \\ \hline \end{array}$$

Here $H = 1$, from the NUNN column we must have “carry 1,” so $G = 9$, $U = \text{zero}$.

Since we have “carry” zero or 1 or 2 from the ONOT column, correspondingly

we have $N + U = 10$ or 9 or 8 . But duplication is not allowed, so $N = 8$ with

“carry 2” from ONOT. Hence, $O + O = T + 20 - 8 = T + 12$. Testing for $T = 2, 4$

or 6 , we find only $T = 2$ +acceptable, $O = 7$. So we have $87 + 908 + 87 = 1082$.

HUNT = 1082

TOOLS : VS Code, Python 3.9.0

CODE :

```
def solutions():

    # letters = ('s', 'e', 'n', 'd', 'm', 'o', 'r', 'y')

    all_solutions = list()

    for s in range(9, -1, -1):

        for e in range(9, -1, -1):

            for n in range(9, -1, -1):

                for d in range(9, -1, -1):

                    for m in range(9, 0, -1):

                        for o in range(9, -1, -1):

                            for r in range(9, -1, -1):

                                for y in range(9, -1, -1):

                                    if len(set([s, e, n, d, m, o, r, y])) == 8:

                                        send = 1000 * s + 100 * e + 10 * n + d

                                        more = 1000 * m + 100 * o + 10 * r + e

                                        money = 10000 * m + 1000 * o + 100 * n + 10 * e + y

                                    if send + more == money:

                                        all_solutions.append((send, more, money))

    return all_solutions

print(solutions())
```

OUTPUT :

```
PS E:\Studies\SRM University\SEM 6\AI> python -u  
[(9567, 1085, 10652)]  
PS E:\Studies\SRM University\SEM 6\AI> 
```

RESULT :

The constraint satisfying problem $SEND + MORE = MONEY$ solved using the carry over technique and values for the alphabets obtained successfully.

Exercise: 4

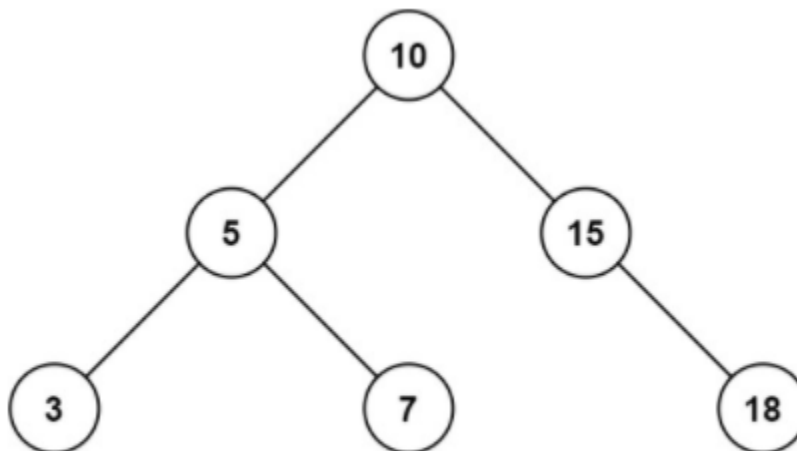
Date : 12-02-2021

RANGE SUM OF BINARY SEARCH TREE (Implementation and Analysis of DFS and BFS for an application)

AIM : Given the root node of a binary search tree, return the sum of values of all nodes with a value in the range [low, high] using depth first and then breadth first search.

While :

- The number of nodes in the tree is in the range $[1, 2 * 10^4]$.
- $1 \leq \text{Node.val} \leq 10^5$
- $1 \leq \text{low} \leq \text{high} \leq 10^5$
- All Node.value are unique.



Input: root = [10,5,15,3,7,null,18], low = 7, high = 15
Output: 32

ALGORITHM #1 DFS :

1. Traverse the tree using a depth first search.
2. Create a stack to store accessed nodes.
3. If `node.value` falls outside the range $[L, R]$
4. Then only the right branch could have nodes with value inside $[L, R]$.
5. If $Left \leq node.value \leq Right$ then `Result[0] += node.value`
6. Else, recursively call the function until all nodes are visited.

ALGORITHM #2 BFS :

1. Traverse the tree using the breadth first search approach.
2. Maintain a queue and ptr to point toward the current node.
3. If `node == None` then continue.
4. If $Left \leq node.value \leq Right$ the result `+= node.value`
5. If $Left > node.value$ then `queue.append(node.right)`
6. If $R < node.value$ then `queue.append(node.left)`
7. Repeat till all nodes are visited.

OPTIMIZATION TECHNIQUE:

Time Complexity: $O(N)$, where N is the number of nodes in the tree.

Space Complexity: $O(N)$. For the recursive implementation, the recursion will consume additional space in the function call stack. In the worst case, the tree is of chain shape, and we will reach all the way down to the leaf node.

For the iterative implementation, essentially we are doing a BFS (Breadth-First Search) traversal, where the stack will contain no more than two levels of the nodes. The maximal number of nodes in a binary tree is $N/2$

Therefore, the maximal space needed for the stack would be $O(N)$.

TOOLS : VS Code and Python 3.9.0

DEPTH FIRST SEARCH (DFS) CODE :

ITERATIVE APPROACH

```
class Solution(object):

    def rangeSumBST(self, root, L, R):

        def dfs(node):

            if node:

                if L <= node.val <= R:

                    self.ans += node.val

                if L < node.val:

                    dfs(node.left)

                if node.val < R:

                    dfs(node.right)

        self.ans = 0

        dfs(root)

        return self.ans
```

RECURSIVE APPROACH

```
class Solution(object):

    def rangeSumBST(self, root, L, R):

        ans = 0

        stack = [root]
```

```

while stack:

    node = stack.pop()

    if node:

        if L <= node.val <= R:

            ans += node.val

        if L < node.val:

            stack.append(node.left)

        if node.val < R:

            stack.append(node.right)

return ans

```

```

bst = TreeNode(10)

bst.left = TreeNode(5)

bst.right = TreeNode(15)

bst.left.left = TreeNode(3)

bst.left.right = TreeNode(7)

bst.right.right = TreeNode(18)

```

```

min = int(input("Enter the Lower value of the range : "))

```

```

max = int(input("Enter the Higher value of the range : "))

```

```

sol = rangeSumBST(bst, min, max)

```

```

print(f"The sum of the nodes in the range {min} and {max} is {sol}")

```

DEPTH FIRST SEARCH OUTPUT :

```
PS E:\Studies\SRM University\SEM 6\AI> python -u
Enter the Lower value of the range : 7
Enter the Higher value of the range : 15
The sum of the nodes in the range 7 and 15 is 32
PS E:\Studies\SRM University\SEM 6\AI> █
```

BREATH FIRST (BFS) CODE:

```
class Solution(object):

    def rangeSumBST(self, root, L, R):

        if root == None:

            return 0

        res = 0

        q = [root]

        while q:

            next = []

            for node in q:

                if L <= node.val <= R:

                    res += node.val

                if node.left:

                    next.append(node.left)

                if node.right:

                    next.append(node.right)

            q = next
```

```

        return res

bst = TreeNode(10)

bst.left = TreeNode(5)

bst.right = TreeNode(15)

bst.left.left = TreeNode(3)

bst.left.right = TreeNode(7)

bst.right.right = TreeNode(18)


min = int(input("Enter the Lower value of the range : "))

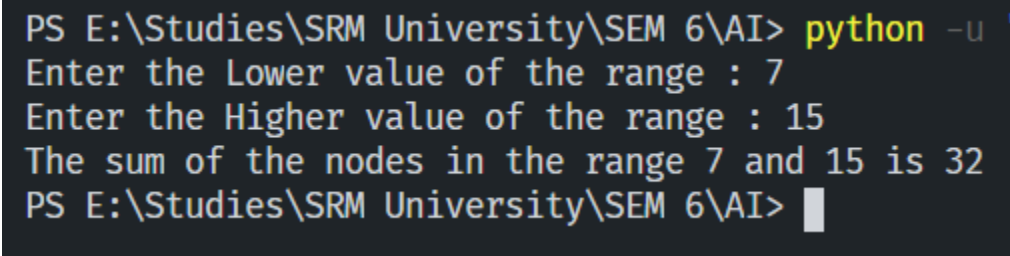
max = int(input("Enter the Higher value of the range : "))


sol = rangeSumBST(bst, min, max)

print(f"The sum of the nodes in the range {min} and {max} is {sol}")

```

BREADTH FIRST OUTPUT:



```

PS E:\Studies\SRM University\SEM 6\AI> python -u
Enter the Lower value of the range : 7
Enter the Higher value of the range : 15
The sum of the nodes in the range 7 and 15 is 32
PS E:\Studies\SRM University\SEM 6\AI>

```

RESULT : Successfully found the sum of nodes in a binary search tree between any given range (min, max) using both depth first search and breadth first search approach.

Exercise: 5

Date : 26-02-2021

CUT OF TREE FOR GOLF EVENT (Implementation and Analysis of BFS and A* Search)

AIM : You are asked to cut off all the trees in a forest for a golf event. The forest is represented as an $m \times n$ matrix. In this matrix:

- 0 means the cell cannot be walked through.
- 1 represents an empty cell that can be walked through.
- A number greater than 1 represents a tree in a cell that can be walked through, and this number is the tree's height.

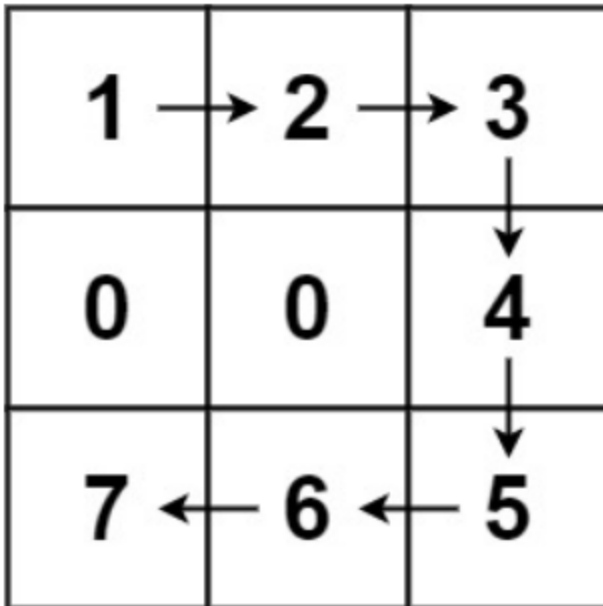
In one step, you can walk in any of the four directions: north, east, south, and west. If you are standing in a cell with a tree, you can choose whether to cut it off.

You must cut off the trees in order from shortest to tallest. When you cut off a tree, the value at its cell becomes 1 (an empty cell).

Starting from the point (0, 0), return the minimum steps you need to walk to cut off all the trees. If you cannot cut off all the trees, return -1.

You are guaranteed that no two trees have the same height, and there is at least one tree that needs to be cut off.

Example 1:



Input: forest = [[1,2,3],[0,0,4],[7,6,5]]

Output: 6

Explanation: Following the path above allows you to cut off the trees from shortest to tallest in 6 steps.

ALGORITHM #1 BFS :

1. Perform best-first-search, processing nodes (grid positions) in a queue.
2. Seen keeps track of nodes that have already been added to the queue at some point.
3. Those nodes will be already processed or are in the queue awaiting processing.
4. For each node that is next to be processed, look at it's neighbors. If they are in the forest (grid), they haven't been enqueued, and they aren't an obstacle, we will enqueue that neighbor.
5. Keep a side count of the distance travelled for each node. If the node we are processing is our destination 'target' (tr, tc), we'll return the answer.

ALGORITHM #1 A* SEARCH :

1. The A* star algorithm is another path-finding algorithm
2. For every node at position (r, c), have some estimated cost $\text{node.f} = \text{node.g} + \text{node.h}$
3. node.g is the actual distance from (sr, sc) to (r, c).
4. node.h is our heuristic (guess) of the distance from (r, c) to (tr, tc).
5. The taxicab distance, $\text{node.h} = \text{abs}(r - \text{tr}) + \text{abs}(c - \text{tc})$.
6. Keep a priority queue to decide what node to search in (expand) next.

OPTIMIZATION TECHNIQUE:

We frame the problem as providing some distance function $\text{dist}(\text{forest}, \text{sr}, \text{sc}, \text{tr}, \text{tc})$ that calculates the path distance from source (sr, sc) to target (tr, tc) through obstacles $\text{dist}[i][j] == 0$. (This distance function will return -1 if the path is impossible.)

What follows is code and complexity analysis that is common to all three approaches. After, the algorithms presented in our approaches will focus on only providing our dist function.

All three algorithms have similar worst case complexities, but in practice each successive algorithm presented performs faster on random data.

Time Complexity: $O((RC)^2)$ where there are R rows and C columns in the given forest. We walk to $R*C$ trees, and each walk could spend $O(R*C)$ time searching for the tree.

Space Complexity: $O(R*C)$, the maximum size of the data structures used.

TOOLS : Python 3.9.0 and VS Code.

CODE #1 BFS :

```
def bfs(forest, sr, sc, tr, tc):  
  
    R, C = len(forest), len(forest[0])  
  
    queue = collections.deque([(sr, sc, 0)])  
  
    seen = {(sr, sc)}  
  
    while queue:  
  
        r, c, d = queue.popleft()  
  
        if r == tr and c == tc:  
  
            return d  
  
        for nr, nc in ((r-1, c), (r+1, c), (r, c-1), (r, c+1)):  
  
            if (0 <= nr < R and 0 <= nc < C and  
  
                (nr, nc) not in seen and forest[nr][nc]):  
  
                seen.add((nr, nc))  
  
                queue.append((nr, nc, d+1))  
  
    return -1
```

OUTPUT #1 BFS :

```
PS E:\Studies\SRM University\SEM 6\AI> Input: forest = [[1,2,3],[0,0,4],[7,6,5]]  
>> Output: 6
```

CODE #2 A* SEARCH :

```
def astar(forest, sr, sc, tr, tc):

    R, C = len(forest), len(forest[0])

    heap = [(0, 0, sr, sc)]

    cost = {(sr, sc): 0}

    while heap:

        f, g, r, c = heapq.heappop(heap)

        if r == tr and c == tc: return g

        for nr, nc in ((r-1,c), (r+1,c), (r,c-1), (r,c+1)):

            if 0 <= nr < R and 0 <= nc < C and forest[nr][nc]:

                ncost = g + 1 + abs(nr - tr) + abs(nc - tc)

                if ncost < cost.get((nr, nc), 9999):

                    cost[nr, nc] = ncost

                    heapq.heappush(heap, (ncost, g+1, nr, nc))

    return -1
```

OUTPUT #2 A* SEARCH :

```
PS E:\Studies\SRM University\SEM 6\AI> Input: forest = [[1,2,3],[0,0,4],[7,6,5]]
>> Output: 6
```

RESULT : The cutting off of tree problem for a golf event successfully solved with 2 different approaches : Best first search and A* search algorithm.

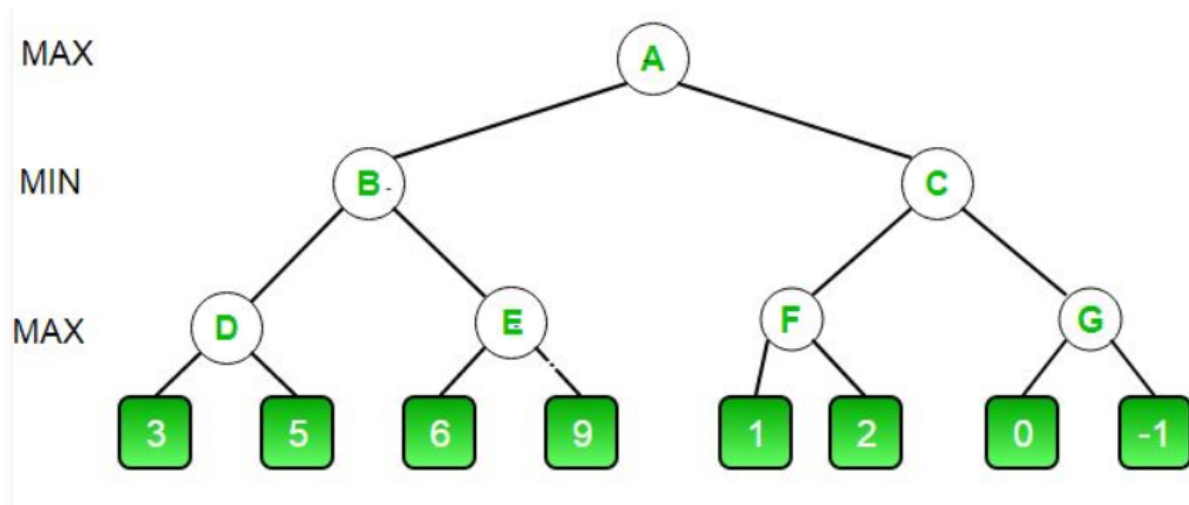
Exercise: 5

Date : 26-02-2021

MINIMAX ALGORITHM IN ALPHA BETA PRUNING

AIM : Developing a mini max algorithm for real world problems.

PROBLEM : Find the optimal value in the given tree of integer values in the most optimal way possible under the time complexity $O(n+m) = O(N)$.



ALGORITHM MINIMAX APPROACH :

1. Start traversing the given tree in top to bottom manner.
2. If node is a leaf node then return the value of the node.
3. If isMaximizingPlayer exist then $bestVal = -INFINITY$
4. For each child node, $value = minimax(node, depth+1, false, alpha, beta)$
5. $bestVal = \max(bestVal, value)$ and $alpha = \max(alpha, bestVal)$
6. If $beta \leq alpha$ then stop traversing and return $bestVal$
7. Else, $bestVal = +INFINITY$
8. For each child node, $value = minimax(node, depth+1, true, alpha, beta)$
9. $bestVal = \min(bestVal, value)$ and $beta = \min(beta, bestVal)$
10. if $beta \leq alpha$ the stop traversing and return $bestVal$

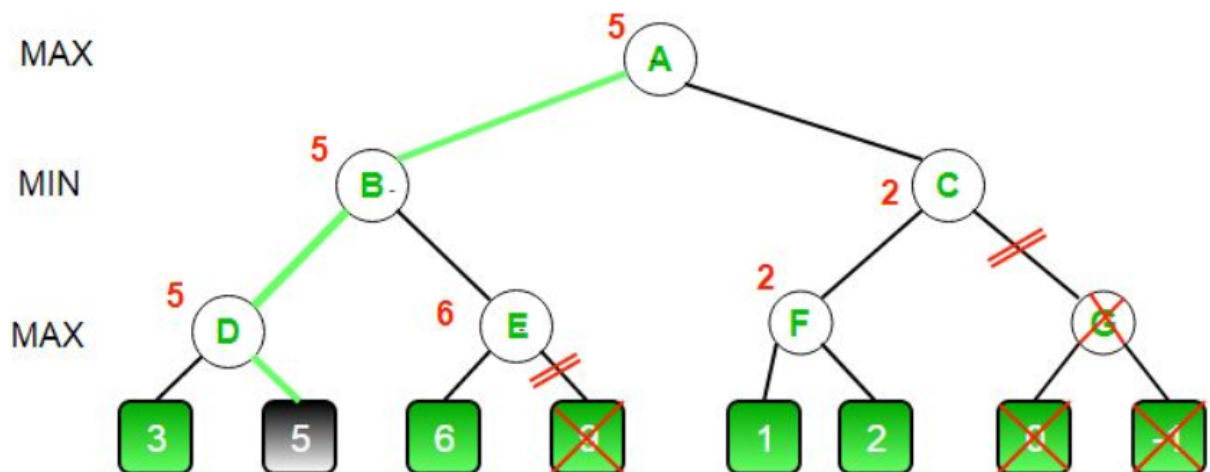
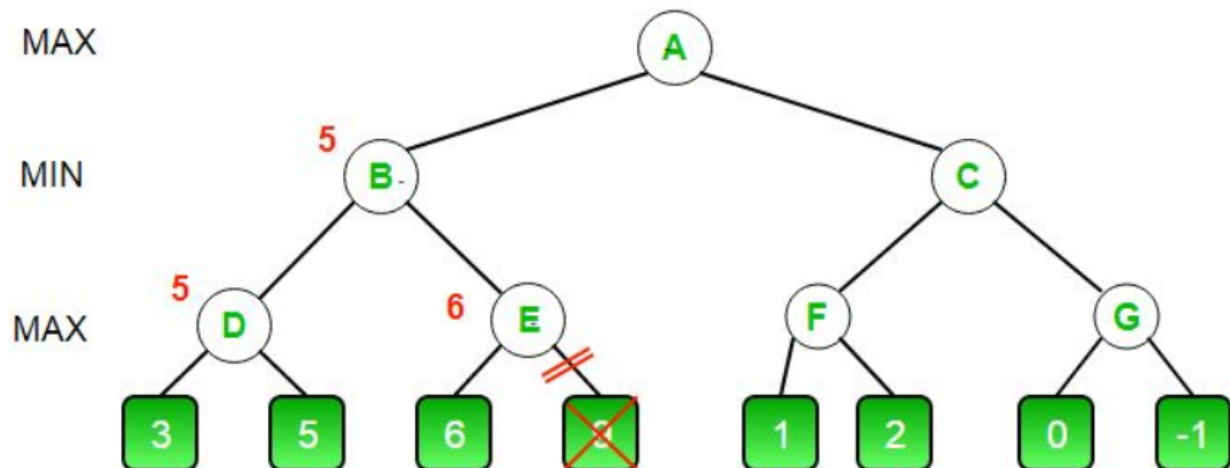
OPTIMIZATION TECHNIQUE :

Alpha-Beta pruning is not actually a new algorithm, rather an optimization technique for minimax algorithms. It reduces the computation time by a huge factor. This allows us to search much faster and even go into deeper levels in the game tree. It cuts off branches in the game tree which need not be searched because there already exists a better move available. It is called Alpha-Beta pruning because it passes 2 extra parameters in the minimax function, namely alpha and beta.

Let's define the parameters alpha and beta.

Alpha is the best value that the **maximizer** currently can guarantee at that level or above.

Beta is the best value that the **minimizer** currently can guarantee at that level or above.



CODE (MINIMAX ALGORITHM) :

MAX, MIN = 1000, -1000

```
def minimax(depth, nodeIndex, maximizingPlayer,  
            values, alpha, beta):
```

```
    if depth == 3:
```

```
        return values[nodeIndex]
```

```
    if maximizingPlayer:
```

```
        best = MIN
```

```
        for i in range(0, 2):
```

```
            val = minimax(depth + 1, nodeIndex * 2 + i,  
                           False, values, alpha, beta)
```

```
            best = max(best, val)
```

```
            alpha = max(alpha, best)
```

```
            if beta <= alpha:
```

```
                break
```

```
        return best
```

```
    else:
```

```
        best = MAX
```

```
        for i in range(0, 2):
```

```
            val = minimax(depth + 1, nodeIndex * 2 + i,  
                           True, values, alpha, beta)
```

```

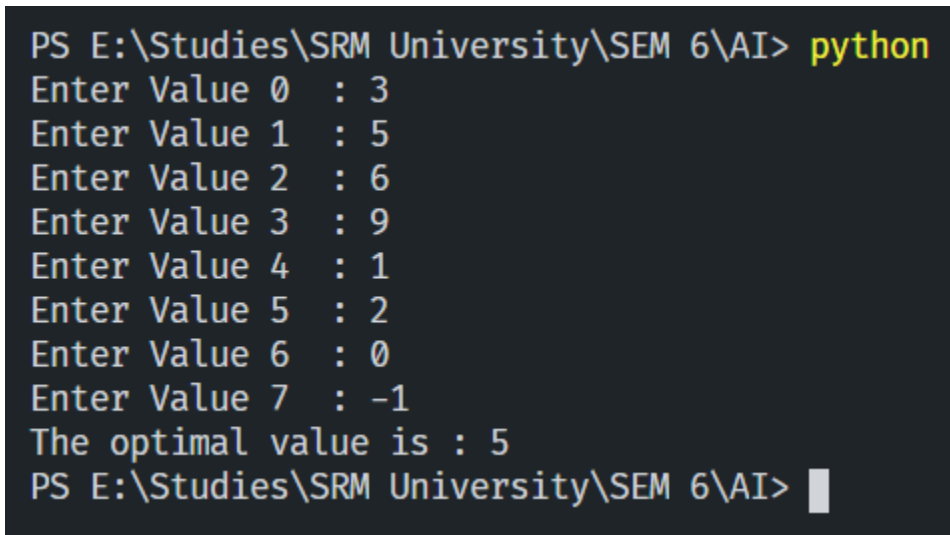
        best = min(best, val)
        beta = min(beta, best)
        if beta <= alpha:
            break

    return best

if __name__ == "__main__":
    values = []
    for i in range(0, 8):
        x = int(input(f"Enter Value {i} : "))
        values.append(x)
    print ("The optimal value is :", minimax(0, 0, True, values, MIN, MAX))

```

OUTPUT :



```

PS E:\Studies\SRM University\SEM 6\AI> python
Enter Value 0 : 3
Enter Value 1 : 5
Enter Value 2 : 6
Enter Value 3 : 9
Enter Value 4 : 1
Enter Value 5 : 2
Enter Value 6 : 0
Enter Value 7 : -1
The optimal value is : 5
PS E:\Studies\SRM University\SEM 6\AI>

```

RESULT : The Optimal value of the given tree successfully found using Minimax Algorithm with Alpha Beta Pruning in time complexity $O(N)$.