# **Hidden Markov Models**

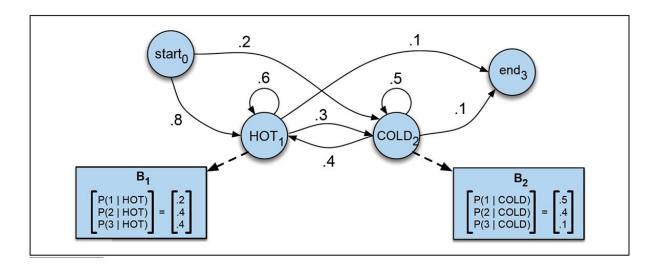
**Assignment 3** 

# **Assignment: The Forward & Viterbi Algorithm**

- 1. Implement the Forward Algorithm for the Hidden Markov Model (shown on the next slide) to compute the probability of the observation sequence 3 1 3.
- 2. Implement the Viterbi Algorithm to compute the most likely weather sequence for the observation sequence 3 1 3.

Use the file hmm\_template.py, it contains the incomplete functions compute\_forward and compute viterbi.

# **Assignment: The Forward & Viterbi Algorithm**



The Hidden Markov Model above shows the number of ice creams eaten by Jason (the observations) related to the weather (HOT or COLD, the hidden variables).

Visit <a href="https://web.stanford.edu/~jurafsky/slp3/A.pdf">https://web.stanford.edu/~jurafsky/slp3/A.pdf</a> for further details.

### Pseudocode for the Forward Algorithm

```
function FORWARD(observations of len T, state-graph of len N) returns forward-prob create a probability matrix forward[N+2,T] for each state s from 1 to N do ; initialization step forward[s,1] \leftarrow a_{0,s} * b_s(o_1) for each time step t from 2 to T do ; recursion step for each state s from 1 to N do forward[s,t] \leftarrow \sum_{s'=1}^{N} forward[s',t-1] * a_{s',s} * b_s(o_t) forward[q_F, T] \leftarrow \sum_{s=1}^{N} forward[s,T] * a_{s,q_F} ; termination step return forward[q_F,T]
```

Note that in the code, the transition matrix corresponds to a, whereas the emissions matrix corresponds to b.

### Pseudocode for the Viterbi Algorithm

```
function VITERBI(observations of len T, state-graph of len N) returns best-path
 create a path probability matrix viterbi[N+2,T]
 for each state s from 1 to N do
                                                             ; initialization step
       viterbi[s,1] \leftarrow a_{0,s} * b_s(o_1)
      backpointer[s,1] \leftarrow 0
 for each time step t from 2 to T do
                                                             ; recursion step
    for each state s from 1 to N do
      viterbi[s,t] \leftarrow \max_{s'=1}^{N} viterbi[s',t-1] * a_{s',s} * b_s(o_t)
      backpointer[s,t] \leftarrow \underset{\sim}{\operatorname{argmax}} viterbi[s',t-1] * a_{s',s}
viterbi[q_F,T] \leftarrow \max_{s}^{N} viterbi[s,T] * a_{s,q_F}; termination step
 backpointer[q_F,T] \leftarrow \underset{s}{\operatorname{argmax}} viterbi[s,T] * a_{s,q_F}; termination step
return the backtrace path by following backpointers to states back in
          time from backpointer [q_F, T]
```

Note that in the code, the transition matrix corresponds to a, whereas the emissions matrix corresponds to b.