



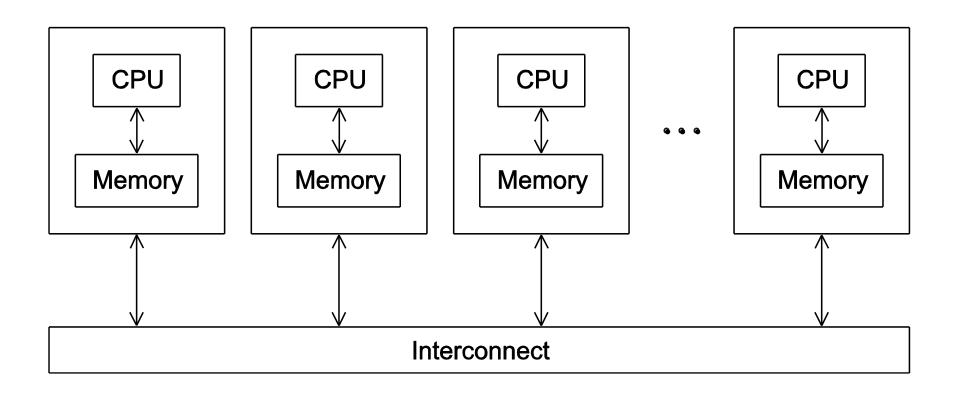
用MPI进行分布式内存编程

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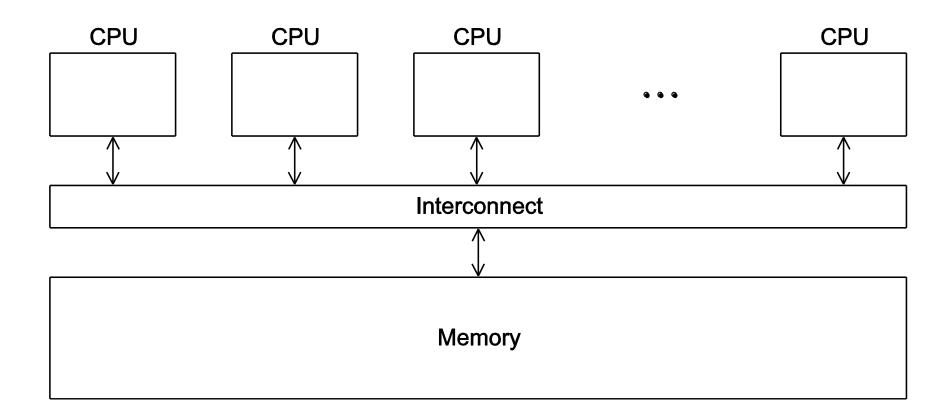
Roadmap

- Writing your first MPI program.
- Using the common MPI functions.
- The Trapezoidal Rule in MPI.
- Collective communication.
- MPI derived datatypes.
- Performance evaluation of MPI programs.
- Parallel sorting.
- Safety in MPI programs.

A distributed memory system



A shared memory system



Hello World!

```
#include <stdio.h>
int main(void) {
   printf("hello, world\n");
   return 0;
}
```

(a classic)



Identifying MPI processes

 Common practice to identify processes by nonnegative integer ranks.

• p processes are numbered 0, 1, 2, .. p-1

Our first MPI program

```
1 #include < stdio.h>
  #include <string.h> /* For strlen
3 #include <mpi.h> /* For MPI functions, etc */
   const int MAX_STRING = 100;
   int main(void) {
                 greeting[MAX_STRING];
      char
                 comm sz: /* Number of processes */
      int
10
                 my_rank; /* My process rank
      int
                                                                        Number of Processes
11
      MPI_Init(NULL, NULL);
12
      MPI_Comm_size(MPI_COMM_WORLD, &comm_sz);
13
14
      MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);
15
                                                                         My Process Rank
      if (my_rank != 0) {
16
         sprintf(greeting, "Greetings from process %d of %d!",
17
               my_rank, comm_sz);
18
         MPI_Send(greeting, strlen(greeting)+1, MPI_CHAR, 0, 0,
19
               MPI COMM WORLD);
20
21
      } else {
22
         printf("Greetings from process %d of %d!\n", my_rank, comm_sz);
23
         for (int q = 1; q < comm_sz; q++) {
            MPI_Recv(greeting, MAX_STRING, MPI_CHAR, q,
24
25
               0, MPI_COMM_WORLD, MPI_STATUS_IGNORE);
            printf("%s\n", greeting);
26
27
28
29
30
      MPI_Finalize();
      return 0:
31
32
      /* main */
```

Compilation

wrapper script to compile source file mpicc -g -Wall -o mpi_hello mpi_hello.c produce create this executable file name debugging (as opposed to default a.out) information turns on all warnings

Execution

mpiexec -n <number of processes> <executable>

```
mpiexec -n 1 ./mpi_hello

run with 1 process

mpiexec -n 4 ./mpi_hello

run with 4 processes
```

Execution

```
mpiexec -n 1 ./mpi_hello
```

Greetings from process 0 of 1!

```
mpiexec -n 4 ./mpi_hello
```

Greetings from process 0 of 4!

Greetings from process 1 of 4!

Greetings from process 2 of 4!

Greetings from process 3 of 4!

MPI Programs

- Written in C.
 - Has main.
 - Uses stdio.h, string.h, etc.
- Need to add mpi.h header file.
- Identifiers defined by MPI start with "MPI_".
- First letter following underscore is uppercase.
 - For function names and MPI-defined types.
 - Helps to avoid confusion.

MPI Components

- MPI_Init
 - Tells MPI to do all the necessary setup.

- MPI_Finalize
 - Tells MPI we're done, so clean up anything allocated for this program.

```
int MPI_Finalize(void);
```

Basic Outline

```
#include <mpi.h>
int main(int argc, char* argv[]) {
   /* No MPI calls before this */
   MPI_Init(&argc, &argv);
   MPI_Finalize();
   /* No MPI calls after this */
   return 0;
```

Communicators

- A collection of processes that can send messages to each other.
- MPI_Init defines a communicator that consists of all the processes created when the program is started.
- Called MPI_COMM_WORLD.





```
int MPI_Comm_size(
    MPI_Comm comm /* in */,
    int* comm_sz_p /* out */);
```

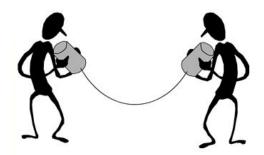
number of processes in the communicator

SPMD

- Single-Program Multiple-Data
- We compile one program.
- Process 0 does something different.
 - Receives messages and prints them while the other processes do the work.
- The if-else construct makes our program SPMD.

Communication

Tag is used to distinguish messages that are otherwise identical

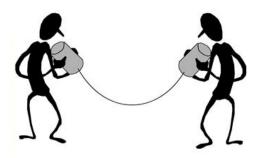


Data types

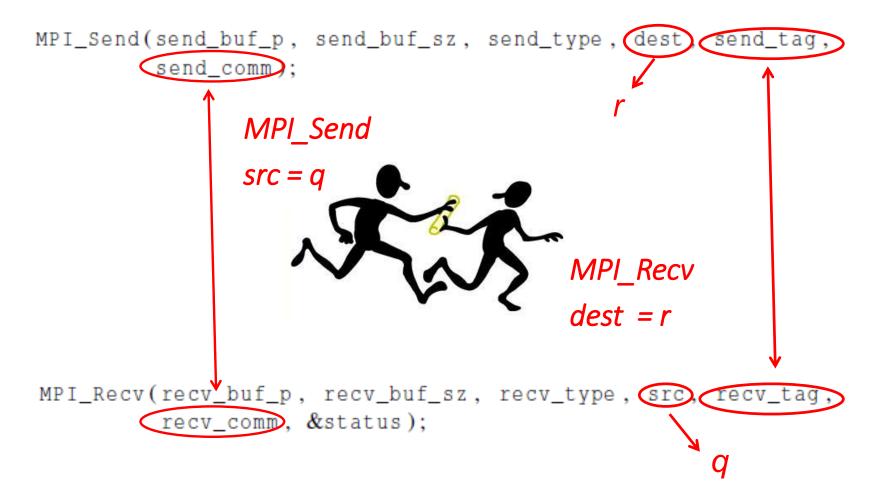
MPI datatype	C datatype
MPI_CHAR	signed char
MPI_SHORT	signed short int
MPI_INT	signed int
MPI_LONG	signed long int
MPI_LONG_LONG	signed long long int
MPI_UNSIGNED_CHAR	unsigned char
MPI_UNSIGNED_SHORT	unsigned short int
MPI_UNSIGNED	unsigned int
MPI_UNSIGNED_LONG	unsigned long int
MPI_FLOAT	float
MPI_DOUBLE	double
MPI_LONG_DOUBLE	long double
MPI_BYTE	
MPI_PACKED	

Communication

```
int MPI_Recv(
                   msg_buf_p
                                /* out
     void*
                                /* in
     int
                  buf_size
                                /* in */,
     MPI_Datatype
                  buf_type
     int
                                /* in */,
                   source
                                /* in */,
     int
                   tag
              communicator /* in */,
     MPI_Comm
     MPI_Status* status_p /* out */);
```

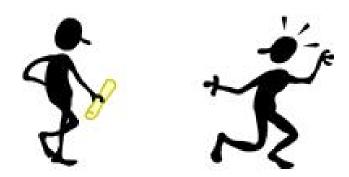


Message matching



Receiving messages

- A receiver can get a message without knowing:
 - the amount of data in the message,
 - the sender of the message,
 - or the tag of the message.



status_p argument

```
MPI_Recv(recv_buf_p, recv_buf_sz, recv_type, src, recv_tag,
          recv_comm, &status);
                             MPI_Status*
                                          MPI_SOURCE
MPI_Status* status;
                                          MPI_TAG
                                          MPI_ERROR
status.MPI_SOURCE
status.MPI TAG
```

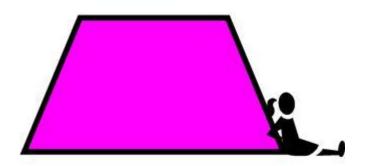
How much data am I receiving?



Issues with send and receive

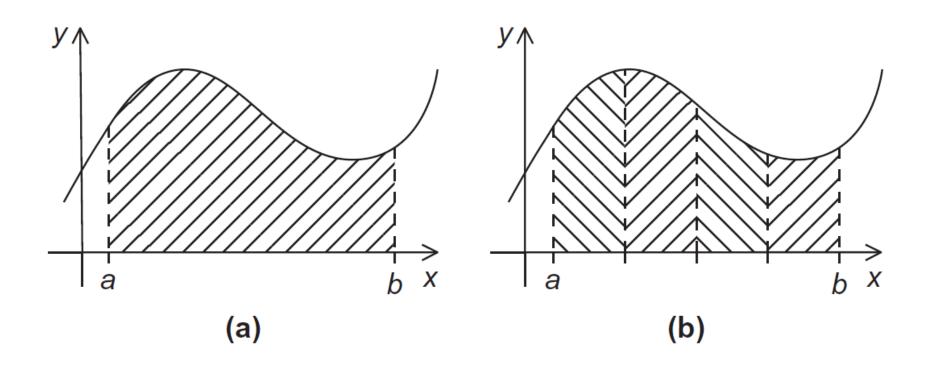
- Exact behavior is determined by the MPI implementation.
- MPI_Send may behave differently with regard to buffer size, cutoffs and blocking.
- MPI_Recv always blocks until a matching message is received.
- Know your implementation; don't make assumptions!



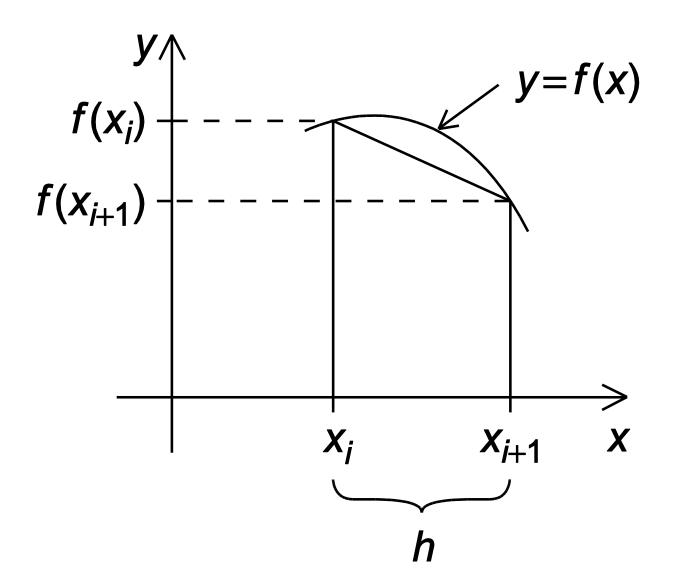


Trapezoidal rule in mpi

The Trapezoidal Rule



One trapezoid



The Trapezoidal Rule

Area of one trapezoid
$$=\frac{h}{2}[f(x_i)+f(x_{i+1})]$$

$$h = \frac{b-a}{n}$$

$$x_0 = a$$
, $x_1 = a + h$, $x_2 = a + 2h$, ..., $x_{n-1} = a + (n-1)h$, $x_n = b$

Sum of trapezoid areas =
$$h[f(x_0)/2 + f(x_1) + f(x_2) + \dots + f(x_{n-1}) + f(x_n)/2]$$

Pseudo-code for a serial program

```
/* Input: a, b, n */
h = (b-a)/n;
approx = (f(a) + f(b))/2.0;
for (i = x, i \le n-1; i++)
   x = a + i*h;
   approx += f(x_i);
                          Any error?
approx = h*approx;
```

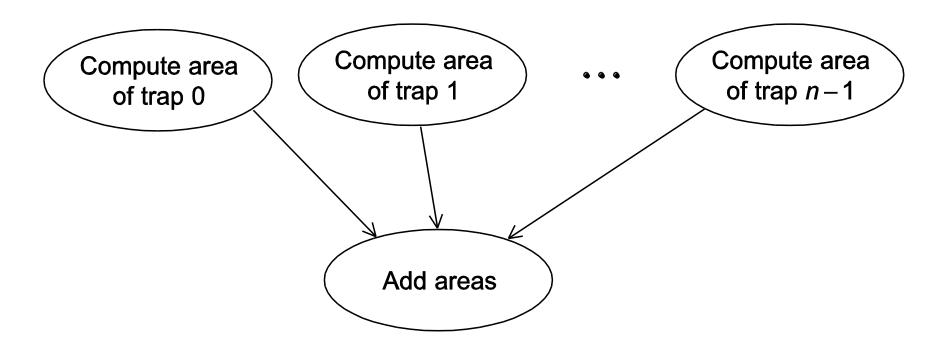
Parallelizing the Trapezoidal Rule

- 1. Partition problem solution into tasks.
- 2. Identify communication channels between tasks.
- Aggregate tasks into composite tasks.
- 4. Map composite tasks to cores.

Parallel pseudo-code

```
Get a, b, n;
      h = (b-a)/n;
      local_n = n/comm_sz;
4
      local_a = a + my_rank*local_n*h;
      local b = local a + local n*h;
6
      local_integral = Trap(local_a, local_b, local_n, h);
      if (my rank != 0)
         Send local_integral to process 0;
9
      else /* my\_rank == 0 */
10
         total_integral = local_integral;
11
         for (proc = 1; proc < comm_sz; proc++) {</pre>
12
             Receive local_integral from proc;
13
             total integral += local integral;
14
15
16
      if (my_rank == 0)
17
         print result;
```

Tasks and communications for Trapezoidal Rule



First version (1)

```
int main(void) {
      int my rank, comm sz, n = 1024, local n;
      double a = 0.0, b = 3.0, h, local_a, local_b;
      double local int, total int;
      int source:
6
      MPI Init(NULL, NULL);
      MPI Comm rank (MPI COMM WORLD, &my rank);
9
      MPI Comm size (MPI COMM WORLD, &comm sz);
10
11
      h = (b-a)/n; /* h is the same for all processes */
      local n = n/comm_sz; /* So is the number of trapezoids */
12
13
14
      local a = a + my rank*local n*h;
15
      local b = local a + local n*h;
16
      local int = Trap(local a, local b, local n, h);
17
      if (my_rank != 0) {
18
19
         MPI\_Send(\&local\_int, 1, MPI\_DOUBLE, 0, 0,
20
               MPI COMM WORLD):
```

First version (2)

```
21
        else
22
         total_int = local_int;
23
         for (source = 1; source < comm_sz; source++) {</pre>
24
            MPI_Recv(&local_int, 1, MPI_DOUBLE, source, 0,
25
                   MPI COMM WORLD, MPI STATUS IGNORE);
26
            total int += local int;
27
28
29
30
      if (my rank == 0) 
         printf("With n = %d trapezoids, our estimate \n", n);
31
32
         printf("of the integral from %f to %f = %.15e\n",
33
             a, b, total int);
34
35
      MPI_Finalize();
36
      return 0:
37
     /* main */
```

First version (3)

```
double Trap(
         double left endpt /* in */,
         double right_endpt /* in */,
         int trap_count /* in */,
5
         double base_len /* in */) {
6
      double estimate, x;
      int i;
9
      estimate = (f(left endpt) + f(right endpt))/2.0;
10
      for (i = 1; i \le trap_count - 1; i++)
11
         x = left endpt + i*base len;
12
        estimate += f(x);
13
14
      estimate = estimate * base len;
15
16
      return estimate;
17
   } /* Trap */
```

Dealing with I/O

```
Each process just
#include < stdio.h>
#include <mpi.h>
                                    prints a message.
int main(void) {
   int my_rank, comm_sz;
   MPI_Init(NULL, NULL);
   MPI Comm size (MPI COMM WORLD, &comm sz);
   MPI Comm rank (MPI COMM WORLD, &my rank);
   printf("Proc %d of %d > Does anyone have a toothpick?\n",
         my rank, comm sz);
   MPI_Finalize();
   return 0;
   /* main */
```

Running with 6 processes

```
Proc 0 of 6 > Does anyone have a toothpick?

Proc 1 of 6 > Does anyone have a toothpick?

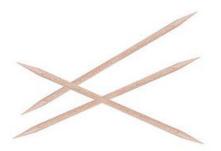
Proc 2 of 6 > Does anyone have a toothpick?

Proc 4 of 6 > Does anyone have a toothpick?

Proc 3 of 6 > Does anyone have a toothpick?

Proc 5 of 6 > Does anyone have a toothpick?
```

unpredictable output



Input

- Most MPI implementations only allow process 0 in MPI_COMM_WORLD access to stdin.
- Process 0 must read the data (scanf) and send to the other processes.

```
MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);
MPI_Comm_size(MPI_COMM_WORLD, &comm_sz);
Get_data(my_rank, comm_sz, &a, &b, &n);
h = (b-a)/n;
. . .
```

Function for reading user input

```
void Get_input(
              my_rank /* in */.
     int
           comm_sz /*in */.
     int
     double* a_p /* out */,
     double* b_p /* out */,
     int* np /* out */) {
  int dest:
  if (my rank == 0) {
     printf("Enter a, b, and n\n");
     scanf("%lf %lf %d", a_p, b_p, n_p);
     for (dest = 1; dest < comm sz; dest++) {
        MPI_Send(a_p, 1, MPI_DOUBLE, dest, 0, MPI_COMM_WORLD);
        MPI_Send(b_p, 1, MPI_DOUBLE, dest, 0, MPI_COMM_WORLD);
        MPI Send(n p, 1, MPI INT, dest, 0, MPI COMM WORLD);
   else { /* my\_rank != 0 */}
     MPI_Recv(a_p, 1, MPI_DOUBLE, 0, 0, MPI COMM WORLD,
           MPI STATUS IGNORE);
     MPI_Recv(b_p, 1, MPI_DOUBLE, 0, 0, MPI_COMM_WORLD,
           MPI_STATUS_IGNORE);
     MPI_Recv(n_p, 1, MPI_INT, 0, 0, MPI_COMM_WORLD,
           MPI_STATUS_IGNORE);
  /* Get_input */
```

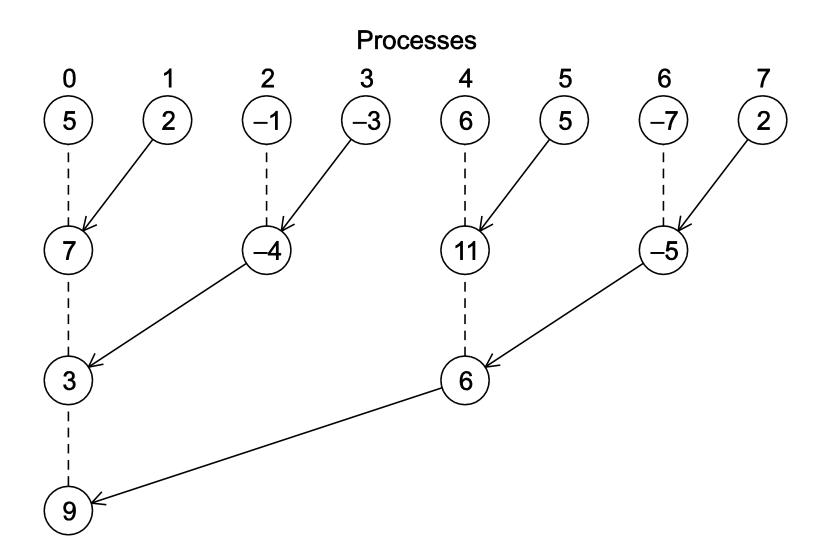


Collective communication

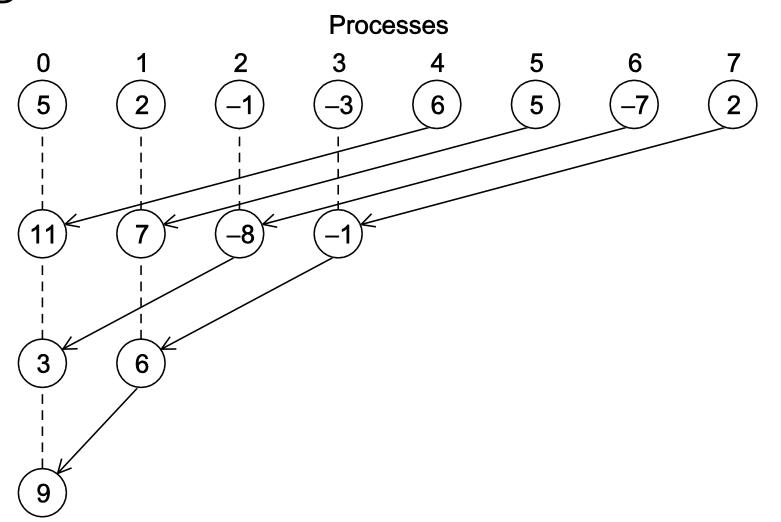
Tree-structured communication

- 1. In the first phase:
 - (a) Process 1 sends to 0, 3 sends to 2, 5 sends to 4, and 7 sends to 6.
 - (b) Processes 0, 2, 4, and 6 add in the received values.
 - (c) Processes 2 and 6 send their new values to processes 0 and 4, respectively.
 - (d) Processes 0 and 4 add the received values into their new values.
- 2. (a) Process 4 sends its newest value to process 0.
 - (b) Process 0 adds the received value to its newest value.

A tree-structured global sum



An alternative tree-structured global sum



Collective Communications

 Collective Communication: communication functions that involve all the processes in a communicator, like MPI_Reduce

Point-to-Point Communication: communication functions between point and point, like MPI_Send, MPI_Recv

MPI Reduce

```
int MPI_Reduce(
    void * input_data_p /* in */,
    void * output_data_p /* out */,
    int count /* in */,
    MPI_Datatype datatype /* in */,
    MPI_Op operator /* in */,
    int dest_process /* in */,
    MPI_Comm comm /* in */);
```

Predefined reduction operators in MPI

Operation Value	Meaning
MPI_MAX	Maximum
MPI_MIN	Minimum
MPI_SUM	Sum
MPI_PROD	Product
MPI_LAND	Logical and
MPI_BAND	Bitwise and
MPI_LOR	Logical or
MPI_BOR	Bitwise or
MPI_LXOR	Logical exclusive or
MPI_BXOR	Bitwise exclusive or
MPI_MAXLOC	Maximum and location of maximum
MPI_MINLOC	Minimum and location of minimum

- All the processes in the communicator must call the same collective function.
- For example, a program that attempts to match a call to MPI_Reduce on one process with a call to MPI_Recv on another process is erroneous, and, in all likelihood, the program will hang or crash.

- The arguments passed by each process to an MPI collective communication must be "compatible."
- For example, if one process passes in 0 as the dest_process and another passes in 1, then the outcome of a call to MPI_Reduce is erroneous, and, once again, the program is likely to hang or crash.

- The output_data_p argument is only used on dest_process.
- However, all of the processes still need to pass in an actual argument corresponding to output_data_p, even if it's just NULL.

- Point-to-point communications are matched on the basis of tags and communicators.
- Collective communications don't use tags.

 They're matched solely on the basis of the communicator and the order in which they're called.

Example (1)

Time	Process 0	Process 1	Process 2
0	a = 1; c = 2	a = 1; c = 2	a = 1; c = 2
1	MPI_Reduce(&a, &b,)	MPI_Reduce(&c, &d,)	MPI_Reduce(&a, &b,)
2	MPI_Reduce(&c, &d,)	MPI_Reduce(&a, &b,)	MPI_Reduce(&c, &d,)

Multiple calls to MPI_Reduce

Example (2)

- Suppose that each process calls MPI_Reduce with operator MPI_SUM, and destination process 0.
- At first glance, it might seem that after the two calls to MPI_Reduce, the value of b will be 3, and the value of d will be 6.

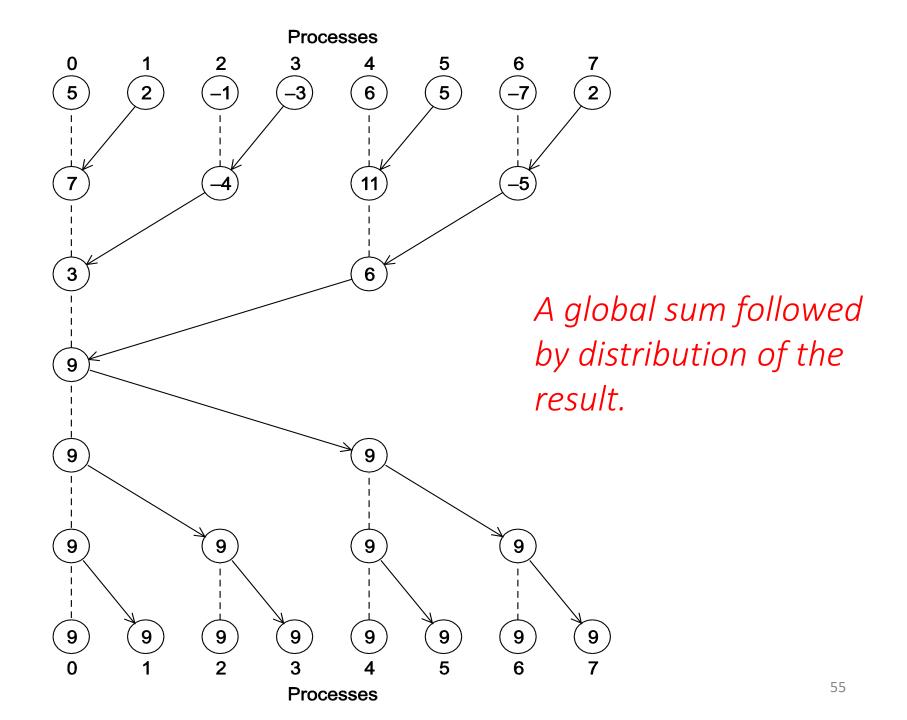
Example (3)

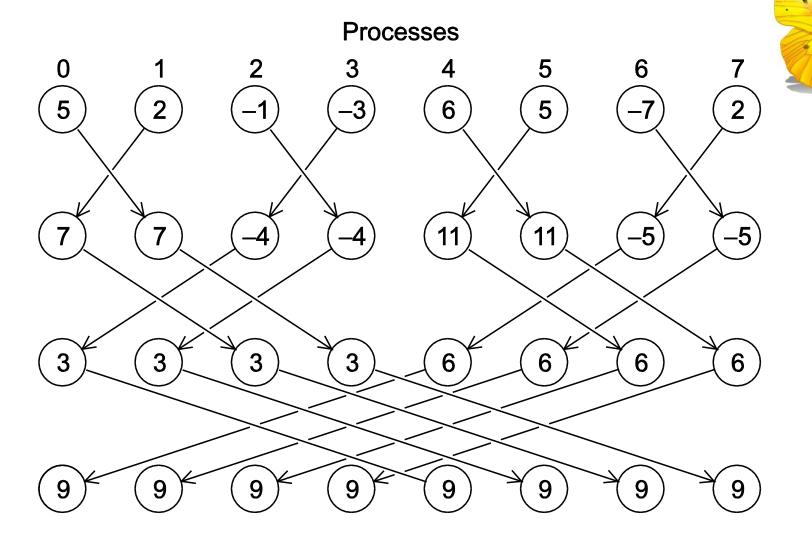
 However, the names of the memory locations are irrelevant to the matching of the calls to MPI_Reduce.

• The order of the calls will determine the matching so the value stored in b will be 1+2+1=4, and the value stored in d will be 2+1+2=5.

MPI_Allreduce

 Useful in a situation in which all of the processes need the result of a global sum in order to complete some larger computation.





A butterfly-structured global sum.

Broadcast

 Data belonging to a single process is sent to all of the processes in the communicator.

A tree-structured broadcast. 6 **Processes**

A version of Get_input that uses MPI Bcast

```
void Get_input(
     int my_rank /* in */,
     int comm_sz /*in */,
     double * a_p /* out */,
     double* b_p /* out */,
          n_p /* out */) {
     int*
  if (my_rank == 0) {
     printf("Enter a, b, and n\n");
     scanf("%lf %lf %d", a_p, b_p, n_p);
  MPI_Bcast(a_p, 1, MPI_DOUBLE, 0, MPI_COMM_WORLD);
  MPI_Bcast(b_p, 1, MPI_DOUBLE, 0, MPI_COMM_WORLD);
  MPI_Bcast(n_p, 1, MPI_INT, 0, MPI_COMM_WORLD);
  /* Get_input */
```

Data distributions

$$\mathbf{x} + \mathbf{y} = (x_0, x_1, \dots, x_{n-1}) + (y_0, y_1, \dots, y_{n-1})$$

$$= (x_0 + y_0, x_1 + y_1, \dots, x_{n-1} + y_{n-1})$$

$$= (z_0, z_1, \dots, z_{n-1})$$

$$= \mathbf{z}$$

Compute a vector sum.

Serial implementation of vector addition

```
void Vector_sum(double x[], double y[], double z[], int n) {
   int i;

for (i = 0; i < n; i++)
    z[i] = x[i] + y[i];
} /* Vector_sum */</pre>
```

Different partitions of a 12component vector among 3 processes

	Components											
									В	locl	k-cyc	lic
Process	Block			Cyclic			Blocksize = 2					
0	0	1	2	3	0	3	6	9	0	1	6	7
1	4	5	6	7	1	4	7	10	2	3	8	9
2	8	9	10	11	2	5	8	11	4	5	10	11

Partitioning options

- Block partitioning
 - Assign blocks of consecutive components to each process.
- Cyclic partitioning
 - Assign components in a round robin fashion.
- Block-cyclic partitioning
 - Use a cyclic distribution of blocks of components.

Parallel implementation of vector addition

```
void Parallel_vector_sum(
    double local_x[] /* in */,
    double local_y[] /* in */,
    double local_z[] /* out */,
    int local_n /* in */) {
    int local_i;

    for (local_i = 0; local_i < local_n; local_i++)
        local_z[local_i] = local_x[local_i] + local_y[local_i];
} /* Parallel_vector_sum */</pre>
```

Scatter

 MPI_Scatter can be used in a function that reads in an entire vector on process 0 but only sends the needed components to each of the other processes.

```
int MPI_Scatter(
                  send_buf_p /* in */.
     void*
                  send_count /* in */.
     int
                 send_type /*in */.
     MPI_Datatype
     void*
             recv_buf_p /* out */,
                  recv_count /* in */,
     int
                 recv_type /* in */,
     MPI_Datatype
     int
                  src_proc /* in */,
                  comm /* in */);
     MPI_Comm
```

Reading and distributing a vector

```
void Read vector(
     double local a[] /* out */,
          local n /*in */,
     int
             n /* in */,
     int
     char vec name [] /* in */,
     int     my_rank  /* in */.
     MPI_Comm comm /* in */) {
  double * a = NULL:
  int i:
  if (my rank == 0) {
     a = malloc(n*sizeof(double));
     printf("Enter the vector %s\n", vec_name);
     for (i = 0; i < n; i++)
        scanf("%lf", &a[i]);
     MPI_Scatter(a, local_n, MPI_DOUBLE, local_a, local_n, MPI_DOUBLE,
           0, comm);
     free(a);
    else
     MPI Scatter(a, local n, MPI DOUBLE, local a, local n, MPI DOUBLE,
           0, comm);
  /* Read_vector */
```

Gather

 Collect all of the components of the vector onto process 0, and then process 0 can process all of the components.

```
int MPI_Gather(
                  send_buf_p /* in */,
     void*
                  send_count /*in */,
     int
     MPI_Datatype send_type /*in */,
                  recv_buf_p /* out */,
     void*
     int
                  recv_count /* in
                                    */,
                  recv_type /*in */,
     MPI_Datatype
     int
                  dest_proc /* in */,
                             /* in */);
     MPI Comm
                  comm
```

Print a distributed vector (1)

```
void Print vector(
    double local_b[] /* in */,
    int local_n /* in */,
               /* in */.
    int
    char title[] /*in */,
        my_rank /* in */,
    int
                    /* in */) {
    MPI_Comm comm
  double*b = NULL;
  int i;
```

Print a distributed vector (2)

```
if (my_rank == 0) {
  b = malloc(n*sizeof(double));
  MPI_Gather(local_b, local_n, MPI_DOUBLE,
                                                local_n, MPI_DOUBLE
         0, comm);
  printf("%s\n", title);
  for (i = 0; i < n; i++)
     printf("%f ", b[i]);
  printf("\n");
  free(b);
 else
  MPI_Gather(local_b, local_n, MPI_DOUBLE,
                                                local_n, MPI_DOUBLE,
         0, comm);
  Print_vector */
```

Allgather

- Concatenates the contents of each process' send_buf_p and stores this in each process' recv_buf_p.
- As usual, recv_count is the amount of data being received from each process.

Matrix-vector multiplication

$$A = (a_{ij})$$
 is an $m \times n$ matrix

 \mathbf{x} is a vector with n components

y = Ax is a vector with m components

$$y_i = a_{i0}x_0 + a_{i1}x_1 + a_{i2}x_2 + \cdots + a_{i,n-1}x_{n-1}$$

i-th component of y

Dot product of the ith row of A with x.

Matrix-vector multiplication

<i>a</i> ₀₀	<i>a</i> ₀₁	• • •	$a_{0,n-1}$		уо
a_{10}	a_{11}		$a_{1,n-1}$	x_0	<i>y</i> ₁
:	:		::	<i>x</i> ₁	:
a_{i0}	a_{i1}		$a_{i,n-1}$: -	$y_i = a_{i0}x_0 + a_{i1}x_1 + \cdots + a_{i,n-1}x_{n-1}$
:	:		:	x_{n-1}	
$a_{m-1,0}$	$a_{m-1,1}$		$a_{m-1,n-1}$		<i>ym</i> −1

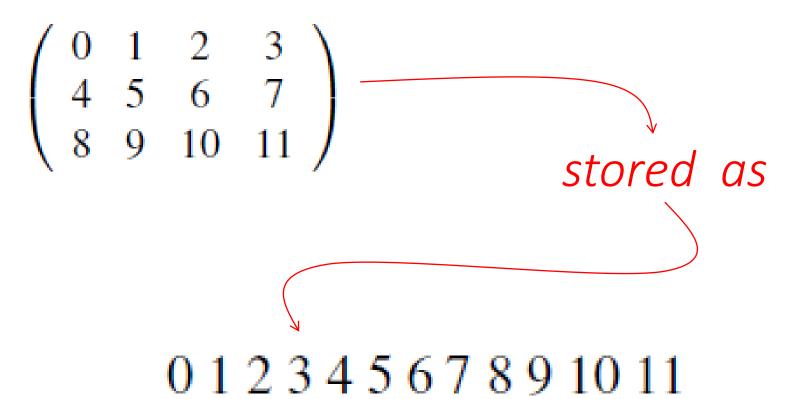
Multiply a matrix by a vector

```
/* For each row of A */
for (i = 0; i < m; i++) {
    /* Form dot product of ith row with x */
    y[i] = 0.0;

for (j = 0; j < n; j++)
    y[i] += A[i][j]*x[j];
}</pre>
```

Serial pseudo-code

C style arrays



Serial matrix-vector multiplication

```
void Mat_vect_mult(
     double A[] /* in */,
     double x[] /* in */,
     double y[] /* out */,
     int m /*in */,
     int n /* in */) {
  int i, j;
  for (i = 0; i < m; i++) {
     y[i] = 0.0;
     for (j = 0; j < n; j++)
       y[i] += A[i*n+j]*x[j];
 /* Mat_vect_mult */
```

An MPI matrix-vector multiplication function (1)

```
void Mat_vect_mult(
    double local_A[] /* in */,
    double local_x[] /* in */,
    double local_y[] /* out */,
    int local_m /* in */,
    int n
                 /* in */,
     int local_n /* in */,
                    /* in */) {
    MPI_Comm comm
  double * x;
  int local_i, j;
  int local_ok = 1;
```

An MPI matrix-vector multiplication function (2)



Mpi derived datatypes

Derived datatypes

- Used to represent any collection of data items in memory by storing both the types of the items and their relative locations in memory.
- The idea is that if a function that sends data knows this information about a collection of data items, it can collect the items from memory before they are sent.
- Similarly, a function that receives data can distribute the items into their correct destinations in memory when they're received.

Derived datatypes

- Formally, consists of a sequence of basic MPI data types together with a displacement for each of the data types.
- Trapezoidal Rule example:

Variable	Address
a	24
b	40
n	48

 $\{(MPI_DOUBLE, 0), (MPI_DOUBLE, 16), (MPI_INT, 24)\}$

MPI_Type_create_struct

 Builds a derived datatype that consists of individual elements that have different basic types.

MPI_Get_address

- Returns the address of the memory location referenced by location_p.
- The special type MPI_Aint is an integer type that is big enough to store an address on the system.

```
int MPI_Get_address(
    void* location_p /* in */,
    MPI_Aint* address_p /* out */);
```

MPI_Type_commit

 Allows the MPI implementation to optimize its internal representation of the datatype for use in communication functions.

```
int MPI_Type_commit(MPI_Datatype* new_mpi_t_p /* in/out */);
```

MPI_Type_free

 When we're finished with our new type, this frees any additional storage used.

```
int MPI_Type_free(MPI_Datatype* old_mpi_t_p /* in/out */);
```

Get input function with a derived datatype (1)

Get input function with a derived datatype (2)

Get input function with a derived datatype (3)

```
void Get_input(int my_rank, int comm_sz, double* a_p, double* b_p,
     int* n_p) {
  MPI Datatype input mpi t;
  Build_mpi_type(a_p, b_p, n_p, &input_mpi_t);
   if (my rank == 0) {
     printf("Enter a, b, and n\n");
     scanf("%lf %lf %d", a_p, b_p, n_p);
  MPI_Bcast(a_p, 1, input_mpi_t, 0, MPI_COMM_WORLD);
  MPI_Type_free(&input_mpi_t);
  /* Get_input */
```



Performance evaluation

Elapsed parallel time

 Returns the number of seconds that have elapsed since some time in the past.

Elapsed serial time

- In this case, you don't need to link in the MPI libraries.
- Returns time in microseconds elapsed from some point in the past.

```
#include "timer.h"
. . .
double now;
. . .
GET_TIME(now);
```



Elapsed serial time

```
#include "timer.h"
. . .
double start, finish;
. . .
GET_TIME(start);
/* Code to be timed */
. . .
GET_TIME(finish);
printf("Elapsed time = %e seconds\n", finish-start);
```

MPI_Barrier

• Ensures that no process will return from calling it until every process in the communicator has started calling it.



MPI_Barrier

```
double local_start, local_finish, local_elapsed, elapsed;
MPI Barrier(comm);
local start = MPI Wtime();
/* Code to be timed */
local finish = MPI Wtime();
local_elapsed = local_finish - local_start;
MPI_Reduce(&local_elapsed, &elapsed, 1, MPI_DOUBLE,
   MPI MAX, 0, comm);
if (my_rank == 0)
   printf("Elapsed time = %e seconds\n", elapsed);
```

Run-times of serial and parallel matrix-vector multiplication

	Order of Matrix				
comm_sz	1024	2048	4096	8192	16,384
1	4.1	16.0	64.0	270	1100
2	2.3	8.5	33.0	140	560
4	2.0	5.1	18.0	70	280
8	1.7	3.3	9.8	36	140
16	1.7	2.6	5.9	19	71

(Seconds)

Speedup

$$S(n, p) = \frac{T_{\text{serial}}(n)}{T_{\text{parallel}}(n, p)}$$

Efficiency

$$E(n,p) = \frac{S(n,p)}{p} = \frac{T_{\text{serial}}(n)}{p \times T_{\text{parallel}}(n,p)}$$

Speedups of Parallel Matrix-Vector Multiplication

	Order of Matrix				
comm_sz	1024	2048	4096	8192	16,384
1	1.0	1.0	1.0	1.0	1.0
2	1.8	1.9	1.9	1.9	2.0
4	2.1	3.1	3.6	3.9	3.9
8	2.4	4.8	6.5	7.5	7.9
16	2.4	6.2	10.8	14.2	15.5

Efficiencies of Parallel Matrix-Vector Multiplication

	Order of Matrix				
comm_sz	1024	2048	4096	8192	16,384
1	1.00	1.00	1.00	1.00	1.00
2	0.89	0.94	0.97	0.96	0.98
4	0.51	0.78	0.89	0.96	0.98
8	0.30	0.61	0.82	0.94	0.98
16	0.15	0.39	0.68	0.89	0.97

Scalability

• A program is scalable if the problem size can be increased at a rate so that the efficiency doesn't decrease as the number of processes increase.



Scalability

- Programs that can maintain a constant efficiency without increasing the problem size are sometimes said to be strongly scalable.
- Programs that can maintain a constant efficiency if the problem size increases at the same rate as the number of processes are sometimes said to be weakly scalable.

A parallel sorting algorithm

Sorting

- n keys and p = comm_sz processes.
- n/p keys assigned to each process.
- No restrictions on which keys are assigned to which processes.
- When the algorithm terminates:
 - The keys assigned to each process should be sorted in (say) increasing order.
 - If 0 ≤ q < r < p, then each key assigned to process q should be less than or equal to every key assigned to process r.

Serial bubble sort

```
void Bubble_sort(
     int a[] /* in/out */,
     int n /* in */) {
  int list_length, i, temp;
  for (list_length = n; list_length \geq 2; list_length--)
     for (i = 0; i < list_length-1; i++)
         if (a[i] > a[i+1]) {
           temp = a[i];
           a[i] = a[i+1];
           a[i+1] = temp;
  /* Bubble_sort */
```

Odd-even transposition sort

- A sequence of phases.
- Even phases, compare swaps:

$$(a[0], a[1]), (a[2], a[3]), (a[4], a[5]), \dots$$

Odd phases, compare swaps:

$$(a[1], a[2]), (a[3], a[4]), (a[5], a[6]), \dots$$

Example

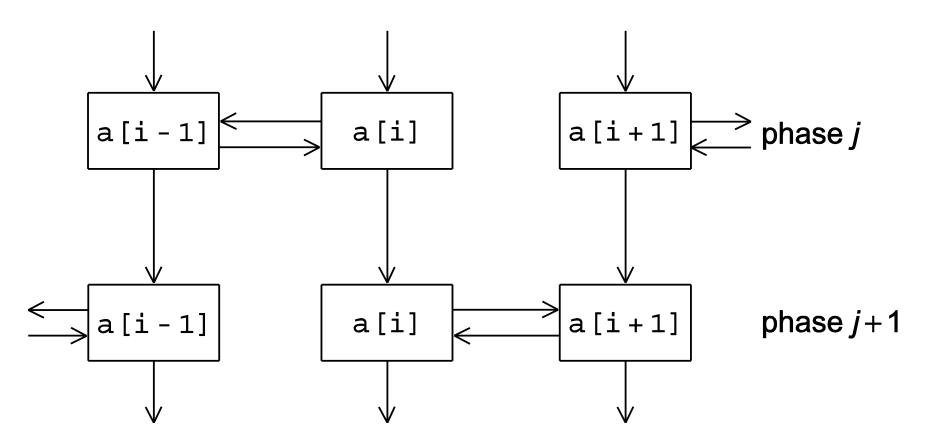
```
Start: 5, 9, 4, 3
Even phase: compare-swap (5,9) and (4,3)
  getting the list 5, 9, 3, 4
Odd phase: compare-swap (9,3)
 getting the list 5, 3, 9, 4
Even phase: compare-swap (5,3) and (9,4)
  getting the list 3, 5, 4, 9
Odd phase: compare-swap (5,4)
```

getting the list 3, 4, 5, 9

Serial odd-even transposition sort

```
void Odd even sort(
      int a [] /* in/out */,
      int n /* in */) {
   int phase, i, temp;
   for (phase = 0; phase < n; phase++)
      if (phase % 2 == 0) { /* Even phase */
         for (i = 1; i < n; i += 2)
            if (a[i-1] > a[i])
              temp = a[i];
               a[i] = a[i-1];
              a[i-1] = temp;
      } else { /* Odd phase */
        for (i = 1; i < n-1; i += 2)
            if (a[i] > a[i+1])
              temp = a[i];
               a[i] = a[i+1];
              a[i+1] = temp;
  /* Odd_even_sort */
```

Communications among tasks in odd-even sort



Tasks determining a[i] are labeled with a[i].

Parallel odd-even transposition sort

	Process				
Time	0	1	2	3	
Start	15, 11, 9, 16	3, 14, 8, 7	4, 6, 12, 10	5, 2, 13, 1	
After Local Sort	9, 11, 15, 16	3, 7, 8, 14	4, 6, 10, 12	1, 2, 5, 13	
After Phase 0	3, 7, 8, 9	11, 14, 15, 16	1, 2, 4, 5	6, 10, 12, 13	
After Phase 1	3, 7, 8, 9	1, 2, 4, 5	11, 14, 15, 16	6, 10, 12, 13	
After Phase 2	1, 2, 3, 4	5, 7, 8, 9	6, 10, 11, 12	13, 14, 15, 16	
After Phase 3	1, 2, 3, 4	5, 6, 7, 8	9, 10, 11, 12	13, 14, 15, 16	

Pseudo-code

```
Sort local keys;
for (phase = 0; phase < comm_sz; phase++) {
   partner = Compute_partner(phase, my_rank);
   if (I'm not idle) {
      Send my keys to partner;
      Receive keys from partner;
      if (my_rank < partner)</pre>
         Keep smaller keys;
      else
         Keep larger keys;
```

Compute_partner

```
if (phase % 2 == 0) /* Even phase */
  if (my_rank % 2 != 0) /* Odd rank */
     partner = my_rank - 1;
  else
                            /* Even rank */
     partner = my_rank + 1;
else
                       /* Odd phase */
  if (my_rank % 2 != 0)  /* Odd rank */
     partner = my_rank + 1;
  else
                            /* Even rank */
     partner = my_rank - 1;
if (partner == -1 || partner == comm_sz)
  partner = MPI_PROC_NULL;
```

- The MPI standard allows MPI_Send to behave in two different ways:
 - it can simply copy the message into an MPI managed buffer and return,
 - or it can block until the matching call to MPI_Recv starts.

- Many implementations of MPI set a threshold at which the system switches from buffering to blocking.
- Relatively small messages will be buffered by MPI_Send.
- Larger messages, will cause it to block.

- If the MPI_Send executed by each process blocks, no process will be able to start executing a call to MPI_Recv, and the program will hang or deadlock.
- Each process is blocked waiting for an event that will never happen.

(see pseudo-code)

 A program that relies on MPI provided buffering is said to be unsafe.

 Such a program may run without problems for various sets of input, but it may hang or crash with other sets.

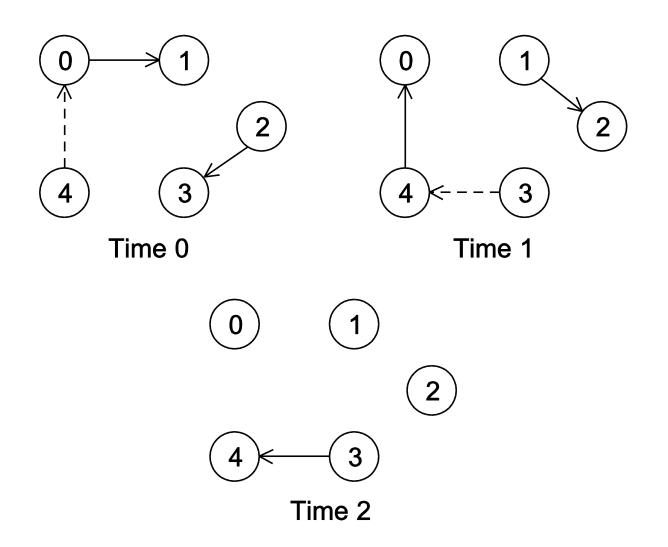
MPI_Ssend

- An alternative to MPI_Send defined by the MPI standard.
- The extra "s" stands for synchronous and MPI_Ssend is guaranteed to block until the matching receive starts.

Restructuring communication



Safe comm. with five processes



MPI_Sendrecv

- An alternative to scheduling the communications ourselves.
- Carries out a blocking send and a receive in a single call.
- The dest and the source can be the same or different.
- Especially useful because MPI schedules the communications so that the program won't hang or crash.

MPI Sendrecv

```
int MPI_Sendrecv(
     void*
                  send_buf_p /* in */,
                  send_buf_size /*in */,
     int
     MPI_Datatype send_buf_type /*in */,
     int
                                /* in */,
                  dest_
     int
                                /* in */,
                  send_tag
     void*
                  recv_buf_p /* out */,
                  recv_buf_size /*in */,
     int
                  recv_buf_type /*in */,
     MPI_Datatype
     int
                                 /* in */,
                   source
                                /* in */,
     int
                   recv_tag
                  communicator /*in */,
     MPI Comm
                                /* in */);
     MPI Status*
                  status_p
```

Parallel odd-even transposition sort

```
void Merge_low(
     int my_keys[], /* in/out */
     int recv_keys[], /* in */
     int temp_keys[], /* scratch */
     int local_n /* = n/p, in */) {
  int m_i, r_i, t_i;
  m i = r i = t i = 0;
  while (t_i < local_n) {
     if (my_keys[m_i] <= recv_keys[r_i]) {</pre>
        temp_keys[t_i] = my_keys[m_i];
        t i++; m i++;
     } else {
        temp_keys[t_i] = recv_keys[r_i];
        t i++; r i++;
  for (m i = 0; m i < local n; m i++)
     my keys[m i] = temp keys[m i];
  /* Merge_low */
```

Run-times of parallel odd-even sort

	Number of Keys (in thousands)				
Processes	200	400	800	1600	3200
1	88	190	390	830	1800
2	43	91	190	410	860
4	22	46	96	200	430
8	12	24	51	110	220
16	7.5	14	29	60	130

(times are in milliseconds)

Concluding Remarks (1)

- MPI or the Message-Passing Interface is a library of functions that can be called from C, C++, or Fortran programs.
- A communicator is a collection of processes that can send messages to each other.
- Many parallel programs use the single-program multiple data or SPMD approach.

Concluding Remarks (2)

- Most serial programs are deterministic: if we run the same program with the same input we'll get the same output.
- Parallel programs often don't possess this property.
- Collective communications involve all the processes in a communicator.

Concluding Remarks (3)

- When we time parallel programs, we're usually interested in elapsed time or "wall clock time".
- Speedup is the ratio of the serial run-time to the parallel run-time.
- Efficiency is the speedup divided by the number of parallel processes.

Concluding Remarks (4)

- If it's possible to increase the problem size (n) so that the efficiency doesn't decrease as p is increased, a parallel program is said to be scalable.
- An MPI program is unsafe if its correct behavior depends on the fact that MPI_Send is buffering its input.