

$$y' = M(W, b, x) = 20 \cdot \sigma(\text{Linear}(W, b, x)) \quad (1)$$

$$\mathcal{L}_{MSE} = \frac{1}{N} \sum^N (y - y')^2 \quad (2)$$

$$\frac{\partial \mathcal{L}}{\partial W} = \frac{(y - y')^2}{\partial W} \quad (3)$$

$$\frac{(y - y')^2}{\partial W} = -2 \cdot (y - y') \cdot \frac{y'}{\partial W} \quad (4)$$

$$-2 \cdot (y - y') \cdot \frac{y'}{\partial W} = -2 \cdot (y - y') \cdot \frac{M(W, b, x)}{\partial W} \quad (5)$$

$$-2 \cdot (y - y') \cdot \frac{M(W, b, x)}{\partial W} = -2 \cdot (y - y') \cdot \frac{20 \cdot \sigma(a)}{\partial(\sigma(a))} \cdot \frac{\sigma(a)}{\partial W} \quad (6)$$

$$-2 \cdot (y - y') \cdot \frac{20 \cdot \sigma(a)}{\partial(\sigma(a))} \cdot \frac{\sigma(a)}{\partial W} = -2 \cdot (y - y') \cdot 20 \cdot \frac{\sigma(a)}{\partial a} \cdot \frac{\text{Linear}(W, b, x)}{\partial W} \quad (7)$$

$$-2 \cdot (y - y') \cdot 20 \cdot \frac{\sigma(a)}{\partial a} \cdot \frac{\text{Linear}(W, b, x)}{\partial W} = -2 \cdot (y - y') \cdot 20 \cdot \frac{e^{-x}}{(1 + e^{-x})^2} \cdot \frac{W \cdot x + b}{\partial W} \quad (8)$$

$$-2 \cdot (y - y') \cdot 20 \cdot \frac{e^{-x}}{(1 + e^{-x})^2} \cdot \frac{W \cdot x + b}{\partial W} = -2 \cdot (y - y') \cdot 20 \cdot \frac{e^{-x}}{(1 + e^{-x})^2} \cdot x \quad (9)$$

For b the sequence of steps is similar, however the last derivative is:

$$\frac{\partial W \cdot x + b}{\partial b} = 1 \quad (10)$$

Therefore:

$$\frac{\partial \mathcal{L}}{\partial b} = -2 \cdot (y - y') \cdot 20 \cdot \frac{e^{-x}}{(1 + e^{-x})^2} \quad (11)$$