## 2018/19 Semester 1

## **Object Oriented Programming with Applications**

Problem Sheet 3 - Wednesday 17th October 2018<sup>1</sup>

**Exercise 3.1.** You might have noticed that the following code for computing the Fibonacci sequence fails (or takes very long to run) for n > 100.

```
static ulong NumberWithoutHashtable(ulong n)
{
   if (n == 0)
      return 0;
   else if (n == 1)
      return 1;
   else
      return NumberWithoutHashtable(n - 1) + NumberWithoutHashtable(n - 2);
}
```

Use either a Hashtable or another data structure to store already computed values so that you can calculate the Fibonacci numbers even for large n.

**Exercise 3.2.** The linear least squares problem consists of finding

$$\hat{\beta} = \operatorname*{arg\,min}_{\beta \in \mathbb{R}^n} |y - X\beta|^2,$$

where X is a given  $m \times n$  matrix such that  $X_{i1} = 1, i = 1, ..., m$  and y is a column vector in  $\mathbb{R}^m$ . It can be shown (using calculus) that the solution is given by solving the linear system

$$(X^T X)\hat{\beta} = X^T y.$$

Use MathNet.Numerics linear algebra methods to complete the class below which is suggested for solving the problem

Here you need to write code to solve  $(X^TX)\hat{\beta} = X^Ty$  and return  $\hat{\beta}$ .

<sup>}</sup> 

<sup>&</sup>lt;sup>1</sup>Last updated 9th October 2018

## Now test it by adding the following.

```
class MainClass
{
    public static void Main (string[] args)
    {
        double[,] x = {{ 1.0} , {2.0}, {3.0}, {4.0} };
        Matrix<double> dataX = Matrix<double>.Build.DenseOfArray (x);

        double[] y = {6, 5, 7, 10};
        Vector<double> dataY = Vector<double>.Build.DenseOfArray (y);

        LinearLeastSquares lls = new LinearLeastSquares (dataX, dataY);
        Vector<double> beta = lls.CalculateCoefficients ();
        Console.WriteLine (beta);
    }
}
```

## **Exercise 3.3.** Use the lecture slides on System. Numerics and Excel integration with ExcelDNA to create two new Excel functions:

- 1. public static double ComplexLogarithmRealPart (double realPart, double imaginaryPart) which returns, for  $z \in \mathbb{C}$ ,  $\Re(\ln(z))$  i.e. the real part of complex logarithm,
- 2. public static double ComplexLogarithmImaginaryPart (double realPart, double imaginaryPart) which returns, for  $z \in \mathbb{C}$ ,  $\Im(\ln(z))$  i.e. the imaginary part of complex logarithm.

For a real number  $z = \exp(i\theta)$  use these functions to plot the real and imaginary parts of the complex logarithm for  $\theta \in [0, 2\pi]$ .