2018/19 Semester 1

Object Oriented Programming with Applications

Problem Sheet 3 - Wednesday 10th October 2018¹

Exercise 3.1. You might have noticed that the following code for computing the Fibonacci sequence fails (or takes very long to run) for n > 100.

```
static ulong NumberWithoutHashtable(ulong n)
{
   if (n == 0)
      return 0;
   else if (n == 1)
      return 1;
   else
      return NumberWithoutHashtable(n - 1) + NumberWithoutHashtable(n - 2);
}
```

Use either a Hashtable or another data structure to store already computed values so that you can calculate the Fibonacci numbers even for large n.

Exercise 3.2. The linear least squares problem consists of finding

$$\hat{\beta} = \operatorname*{arg\,min}_{\beta \in \mathbb{R}^n} |y - X\beta|^2,$$

where X is a given $m \times n$ matrix such that $X_{i1} = 1, i = 1, ..., m$ and y is a column vector in \mathbb{R}^m . It can be shown (using calculus) that the solution is given by solving the linear system

$$(X^T X)\hat{\beta} = X^T y.$$

Use MathNet.Numerics linear algebra methods to complete the class below which is suggested for solving the problem

Here you need to write code to solve $(X^TX)\hat{\beta} = X^Ty$ and return $\hat{\beta}$.

[}]

¹Last updated 1st October 2018

Now test it by adding the following.

```
class MainClass
{
    public static void Main (string[] args)
    {
        double[,] x = {{ 1.0} , {2.0}, {3.0}, {4.0} };
        Matrix<double> dataX = Matrix<double>.Build.DenseOfArray (x);

        double[] y = {6, 5, 7, 10};
        Vector<double> dataY = Vector<double>.Build.DenseOfArray (y);

        LinearLeastSquares lls = new LinearLeastSquares (dataX, dataY);
        Vector<double> beta = lls.CalculateCoefficients ();
        Console.WriteLine (beta);
    }
}
```

Exercise 3.3. Use the lecture slides on System. Numerics and Excel integration with ExcelDNA to create two new Excel functions:

- 1. public static double ComplexLogarithmRealPart (double realPart, double imaginaryPart) which returns, for $z \in \mathbb{C}$, $\Re(\ln(z))$ i.e. the real part of complex logarithm,
- 2. public static double ComplexLogarithmImaginaryPart (double realPart, double imaginaryPart) which returns, for $z \in \mathbb{C}$, $\Im(\ln(z))$ i.e. the imaginary part of complex logarithm.

For a real number $z = \exp(i\theta)$ use these functions to plot the real and imaginary parts of the complex logarithm for $\theta \in [0, 2\pi]$.