

## 2.1

2.  $\mathbf{A} = \begin{bmatrix} E & R & S & T & A \\ N & P & O & C & W \\ H & B & U & I & L \\ M & G & Y & F & K \end{bmatrix}$
- (a)  $a_{31}, a_{11}, a_{35}, a_{22}$   
HELU
- (b)  $a_{35}, a_{34}, a_{21}, a_{11}, a_{15}, a_{15}$   
LINEAR
- (c)  $a_{11}, a_{35}, a_{32}, a_{23}, a_{25}$   
ELBOW
- (d)  $a_{25}, a_{15}, a_{14}, a_{24}, a_{31}, a_{23}, a_{33}, a_{14}$   
WATCHOUT

12.  $\mathbf{A} = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 2 & 4 & 6 & 8 \\ 3 & 5 & 7 & 9 \end{bmatrix}$  and  $\mathbf{B} = \begin{bmatrix} -1 & 0 & 2 & 1 \\ 2 & -1 & -1 & 0 \\ 2 & 0 & 0 & 2 \end{bmatrix}$

(b)  $2\mathbf{B} = \begin{bmatrix} -2 & 0 & 4 & 2 \\ 4 & -2 & -2 & 0 \\ 4 & 0 & 0 & 4 \end{bmatrix}$

(d)  $\mathbf{A} + \mathbf{B} = \begin{bmatrix} 0 & 2 & 5 & 5 \\ 4 & 3 & 5 & 8 \\ 5 & 5 & 7 & 11 \end{bmatrix}$

## 2.2

10.

$$2x_1 + 3x_2 - 2x_3 = 5y_1 + 2y_2 - 3y_3 + 200$$

$$x_1 + 4x_2 + 3x_3 = 6y_1 - 4y_2 + 4y_3 - 120$$

$$5x_1 + 2x_2 - x_3 = 2y_1 - 2y_3 + 350$$

(a)  $\mathbf{A} = \begin{bmatrix} 2 & 3 & -2 \\ 1 & 4 & 3 \\ 5 & 2 & -1 \end{bmatrix}, \mathbf{x} = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$

$$\mathbf{B} = \begin{bmatrix} 5 & 2 & -3 & 200 \\ 6 & -4 & 4 & -120 \\ 2 & 0 & -2 & 350 \end{bmatrix}, \mathbf{y} = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ 1 \end{bmatrix}$$

$$\mathbf{Ax} = \mathbf{By}$$

(b)  $\mathbf{A} = \begin{bmatrix} 2 & 3 & -2 & -5 & -2 & 3 \\ 1 & 4 & 3 & -6 & 4 & -4 \\ 5 & 2 & -1 & -2 & 0 & 2 \end{bmatrix}, \mathbf{n} = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ y_1 \\ y_2 \\ y_3 \end{bmatrix}, \mathbf{b} = \begin{bmatrix} 200 \\ -120 \\ 350 \end{bmatrix}$

$$\mathbf{An} = \mathbf{b}$$

18.  $\mathbf{A} = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 2 & 4 & 6 & 8 \\ 3 & 6 & 7 & 9 \end{bmatrix}, \mathbf{B} = \begin{bmatrix} 1 & 0 & -1 \\ 2 & -2 & 0 \\ 0 & 1 & -1 \end{bmatrix}, \mathbf{C} = \begin{bmatrix} 5 & 4 & 1 \\ 1 & 0 & 2 \\ 3 & 2 & 1 \\ 0 & 1 & 3 \end{bmatrix}$

(a)  $\mathbf{AB}$  does not exist.

$$(b) \mathbf{BA} = \begin{bmatrix} -2 & -4 & -4 & -5 \\ -2 & -4 & -6 & -8 \\ -1 & -2 & -1 & -1 \end{bmatrix}$$

$$(c) \mathbf{AC} = \begin{bmatrix} 16 & 14 & 20 \\ 32 & 28 & 40 \\ 42 & 35 & 49 \end{bmatrix}$$

$$(d) \mathbf{CA} = \begin{bmatrix} 16 & 32 & 46 & 61 \\ 7 & 14 & 17 & 22 \\ 10 & 20 & 28 & 37 \\ 11 & 22 & 27 & 35 \end{bmatrix}$$

$$(e) \mathbf{CB} = \begin{bmatrix} 13 & -7 & -6 \\ 1 & 2 & -3 \\ 7 & -3 & -4 \\ 2 & 1 & -3 \end{bmatrix}$$

$$22. \begin{array}{cc} & \begin{array}{cc} \text{Store } A & \text{Store } B \end{array} \\ \begin{array}{c} \text{Apple} \\ \text{Orange} \\ \text{Pear} \end{array} & \begin{bmatrix} .10 & .15 \\ .15 & .20 \\ .10 & .10 \end{bmatrix} \end{array} \quad \begin{array}{cc} & \begin{array}{ccc} \text{Apple} & \text{Orange} & \text{Pear} \end{array} \\ \begin{array}{c} \text{Person } A \\ \text{Person } B \end{array} & \begin{bmatrix} 5 & 10 & 3 \\ 4 & 5 & 5 \end{bmatrix} \end{array}$$

$$\begin{array}{cc} & \begin{array}{cc} \text{Person } A & \text{Person } B \end{array} \\ \begin{array}{c} \text{Town } 2 \\ \text{Town } 1 \end{array} & \begin{bmatrix} 1000 & 500 \\ 2000 & 1000 \end{bmatrix} \end{array}$$

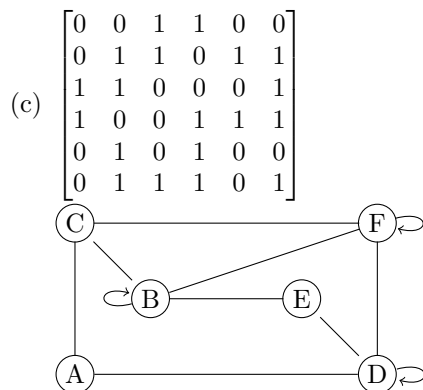
$$(a) \begin{bmatrix} 5 & 10 & 3 \\ 4 & 5 & 5 \end{bmatrix} \begin{bmatrix} .10 & .15 \\ .15 & .20 \\ .10 & .10 \end{bmatrix} = \begin{array}{cc} & \begin{array}{cc} \text{Store } A & \text{Store } B \end{array} \\ \begin{array}{c} \text{Person } A \\ \text{Person } B \end{array} & \begin{bmatrix} 2.30 & 3.05 \\ 1.65 & 2.10 \end{bmatrix} \end{array}$$

$$(b) \begin{bmatrix} 1000 & 500 \\ 2000 & 1000 \end{bmatrix} \begin{bmatrix} 5 & 10 & 3 \\ 4 & 5 & 5 \end{bmatrix} = \begin{array}{cc} & \begin{array}{ccc} \text{Apple} & \text{Orange} & \text{Pear} \end{array} \\ \begin{array}{c} \text{Town } 1 \\ \text{Town } 2 \end{array} & \begin{bmatrix} 7000 & 12500 & 5500 \\ 14000 & 25000 & 11000 \end{bmatrix} \end{array}$$

$$(c) \begin{bmatrix} 7000 & 12500 & 5500 \\ 14000 & 25000 & 11000 \end{bmatrix} \begin{bmatrix} .10 & .15 \\ .15 & .20 \\ .10 & .10 \end{bmatrix} = \begin{array}{cc} & \begin{array}{cc} \text{Store } A & \text{Store } B \end{array} \\ \begin{array}{c} \text{Town } 1 \\ \text{Town } 2 \end{array} & \begin{bmatrix} 3125 & 4100 \\ 6250 & 8200 \end{bmatrix} \end{array}$$

## 2.3

1.



2.

$$(e) \begin{bmatrix} 0 & 1 & 1 & 1 & 1 & 1 \\ 1 & 0 & 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

3.

$$(e) \ G_5^2 = \begin{bmatrix} 5 & 2 & 2 & 2 & 0 & 0 \\ 2 & 3 & 2 & 2 & 1 & 1 \\ 2 & 2 & 3 & 2 & 1 & 1 \\ 2 & 2 & 2 & 3 & 1 & 1 \\ 0 & 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 & 1 & 1 \end{bmatrix}$$

There are 2 paths of length 2 between  $a$  and  $d$ .