

Model Selection to Find a Sufficient Model Fitting to Thermal Performance of Metabolic Traits*

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Abstract

Determining thermal dependence of biological traits provides understanding in distribution patterns of species and is helpful in assessing the impact of climate change on biological systems. Here, I fitted four plausible models to observed data of metabolic traits under different temperatures to calculate thermal performance curves. Model selection by either AIC or BIC were conducted to find one most sufficient model fitting to empirical data of each curve. In most curves, AIC and BIC give support to the same model and Ratkowsky model has the highest frequency of being selected. However, for some thermal performance curves in the dataset, the selected model fails in describing thermal dependence of metabolic traits, indicating that the four plausible models are not suitable and more models need to be involved. Overall, the results show that Ratkowsky model is sufficient for most thermal performance curves involved in this study.

1 Introduction

Temperature is an important abiotic factor that influences the functioning of organisms, especially for ectotherms whose body temperatures reflect that of their environments to different extent. It affects the rates of biochemical reactions and consequently has profound influence on different biological activities like metabolism, growth, development and reproduction [1]. And this can lead to further consequences in abundance and distribution of organisms [2]. Besides, interactions among species are also affected by thermal environment [3].

Thermal performance curve describes the dependence of performance (usually, the rate of a physiological activities or fitness) on temperature quanti-

tatively [1]. Generally, organisms response to temperature fluctuation in a similar manner. The value of performance peaks at some temperature point and decreases when temperature deviates from the maximum point, while extremely high or low temperatures are lethal [1, 4]. The mathematical modelling of thermal performance curve provides a framework for the estimation of physiological characters like the optimum temperature at which performance peaks, upper and lower thermal limits of performance, and thermal tolerance range [4]. Besides, it is also helpful in predicting performance of organisms when temperature fluctuates. Thus, thermal performance curve is helpful in better understanding distribution patterns of species. There is evidence that the thermal tolerance range of a species is often corresponded to the temperature fluctuation of its habitat, indicating the importance of temperature as a selective force in shaping distribution pattern [5, 6]. There is also evidence showing that thermal sensitivity plays a role in the dynamics of biodiversity [7]. Furthermore, investigations in thermal performance curve help better predict the impact of current climate change on biological process [4, 8].

Currently, there are numerous mathematical models with different properties that are used to illustrate thermal performance curves of different clades [4, 9]. Which model, or models are sufficient in describing thermal dependence of performance is the main concern of this study. Using a dataset of observed data from 841 thermal performance curves of different metabolic traits, I calculated these curves by fitting four plausible models to them. Then I conducted model selection to find one model that is most sufficient to describe the observed data. Akaike information criterion (AIC) or Bayesian information criterion (BIC) was used as model selection criterion [10]. Besides, whether metabolic trait or habitat type is corresponded to

54 models that get most support from empirical data was assessed.

55 **2 Materials and Methods**

56 **2.1 Original Data**

57 The original dataset used here is named as ThermRespData.csv and its field
58 names are defined in another file called BiotraitsTemplateDescription.pdf.
59 Both files are accessible in

60 <https://github.com/mhasoba/TheMulQuaBio/tree/master/content/data>.

61 The main fields of interest are OriginalTraitValue (trait values) and Con-
62 Temp (temperatures in Celsius scale). Each thermal performance curve is
63 corresponded to a unique ID from 1 to 903. Among them 62 curves contain
64 negative trait values and were removed. So a total of 841 thermal perfor-
65 mance curves was used in following analysis.

66 **2.2 Plausible Models**

67 Denote by B the trait value and T the temperature. The function that
68 describes the relationship between temperature and trait value is

$$B = B(T) \tag{1}$$

69 Plausible models are: (1) quadratic polynomial model with constants B_0 ,
70 B_1 and B_2 :

$$B(T) = B_0 + B_1T + B_2T^2 \tag{2}$$

71 (2) cubic polynomial model with constants B_0 , B_1 , B_2 and B_3 :

$$B(T) = B_0 + B_1T + B_2T^2 + B_3T^3 \tag{3}$$

72 (3) Briere model with constants B_0 , T_0 and T_m [11]:

$$B(T) = B_0 T(T - T_0) \sqrt{T_m - T} \quad (4)$$

73 T_0 and T_m are lower and upper thermal limits of performance.

74 (4) Ratkowsky model with constants T_0 , T_m , a and b [12]:

$$B(T) = \{a(T - T_0)(1 - e^{b(T - T_m)})\}^2 \quad (5)$$

75 T_0 and T_m are lower and higher thermal limits of performance.

76 2.3 Model Fitting

77 To conduct model fitting, least square method was used, and non-linear
78 models were fitted using Levenberg-Marquardt algorithm [13, 14]. Maximum
79 iteration number was 200.

80 For fitting of Briere model, start values of T_0 and T_m were the lowest and
81 highest sampled temperatures of each curve and they are denoted by T_{0st}
82 and T_{mst} respectively. From Eq. (4),

$$B_0 = \frac{B(T)}{T(T - T_0) \sqrt{T_m - T}} \quad (6)$$

83 For each curve, remove samples with lowest and highest temperatures and
84 denote the rest as $\{(T_i, B_i), i = 1, 2, \dots, n - 2\}$, where n is sample size. So
85 from Eq. (6), a rough estimation of B_0 , denoted by B_{0est} can be given by

$$B_{0est} = \frac{\sum_{i=1}^{n-2} \frac{B_i}{T_i(T_i - T_{0st}) \sqrt{T_{mst} - T_i}}}{n - 2} \quad (7)$$

86 The start values of B_0 was taken from a uniform distribution between 0 and
87 $2B_{0est}$. Each curve was fitted 100 times with different start values of B_0 .
88 As for fitting of Ratkowsky model, start values of T_0 and T_m were the lowest
89 and highest sampled temperatures of each curve. Start values of a and b
90 were taken from set $\{10^i : i = -5, -4, -3, -2, -1, 0, 1, 2, 3, 4\}$ iteratively. So
91 for each curve, there are ten start values of a and b , and 100 combinations
92 of them. Hence, each curve was fitted 100 times with different start values.

93 2.4 Model Selection

94 After model fitting, AIC and BIC of all models were calculated using fol-
95 lowing equations [10]:

$$AIC = -2L + 2k \quad (8)$$

96

$$BIC = -2L + k \ln n \quad (9)$$

97 where n is sample size, k is number of parameters in the model, and L is
98 maximized log-likelihood value of the model. L is given by the following
99 equation [10]:

$$L = -\frac{n}{2} \ln \frac{RSS}{n} \quad (10)$$

100 where RSS is residual sum of squares of the model.

101 2.5 Model Averaging

102 In non-linear model fitting, dataset for each thermal performance curve was
103 fitted 100 times and multiple solutions with similar AIC or BIC could be
104 obtained. To find one most sufficient model supported by observed data, I
105 conducted model averaging. Among all solutions obtained through dataset
106 of one thermal performance curve, those with lowest AIC or BIC values were

selected and averaged. For one thermal performance curve, denote by l the number of optimal solutions with lowest AIC or BIC among all solutions obtained by non-linear model fitting, and θ_i the i th solution, then the parameters of averaged model, denoted by θ , is given by following equation [10, 15]:

$$\theta = \sum_{i=1}^l \omega_i \theta_i \quad (11)$$

The weight ω_i is given by smoothed AIC or BIC method [15]:

$$\omega_i = \frac{e^{-xIC_i/2}}{\sum_{i=1}^l e^{-xIC_i/2}} \quad (12)$$

where xIC_i is the AIC or BIC of i th solution. Here, model averaging was conducted to solutions with equal AIC or BIC values, so

$$\omega_i = \frac{1}{l} \quad (13)$$

Then I calculated AIC and BIC of the averaged model and conducted model selection among linear and non-linear models.

2.6 Computing Tools

Most scripts are written in R 4.0.3, taking advantage of its powerful packages in model fitting and visualization, and of in-built functions for form processing. R package minpack.lm was used for model fitting, while visualization was conducted by R packages ggplot2, gridExtra and cowplot. The report was written using LaTeX because it is efficient in typesetting. A bash script was used to compile LaTeX source code. Finally, a python3 script was written to run all scripts using os module.

125 **3 Results**

126 **3.1 Model Fitting and Selection**

127 For each curve, models with lowest AIC or BIC were selected and they are
128 either quadratic, cubic, of Briere or of Ratkowsky. No curve has multiple
129 models equally supported by AIC or BIC. Among 841 thermal performance
130 curves, 639 (76.0%) of them can be fitted by Briere model, and 649 (77.2%)
131 of them can be fitted by Ratkowsky model. After model fitting, Briere or
132 Ratkowsky models with lowest AIC or BIC values among all solutions were
133 selected and averaged before further model selection. Figure. 1 provides
134 examples of models that were used in selection among linear and non-linear
135 models, and Figure 2 illustrates the distributions of AIC and BIC for each
136 curve.

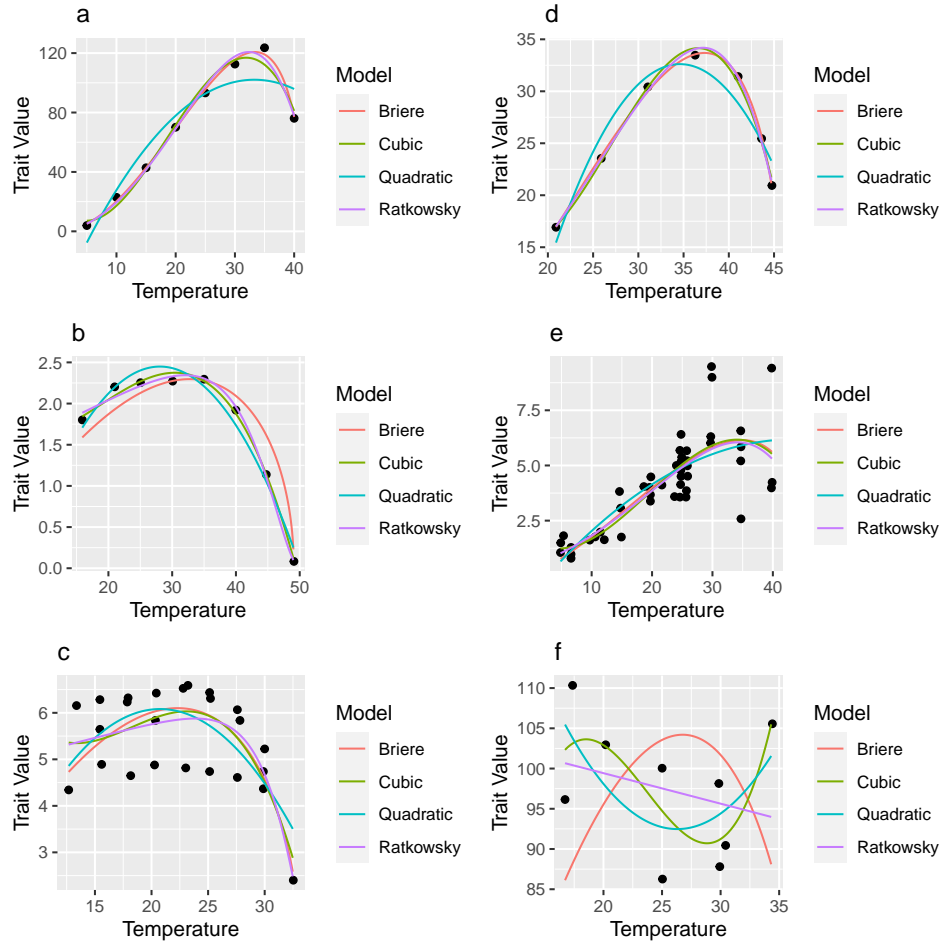


Figure 1: Examples of models used for model selection. Criterion of selection within non-linear models is AIC for subfigure **a**, **b** and **c**; and BIC for subfigure **d**, **e** and **f**. The IDs of thermal performance curves are: 148 (**a**), 204 (**b**), 322 (**c**), 138 (**d**), 237 (**e**), 519 (**f**).

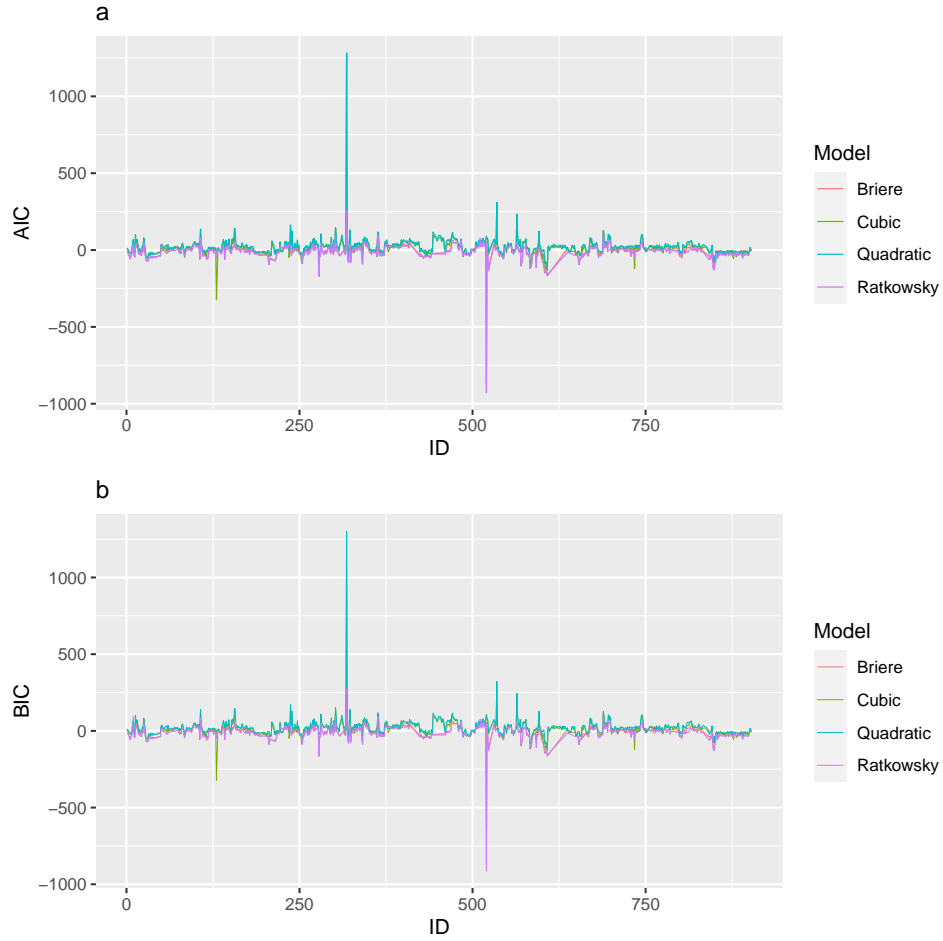


Figure 2: The distribution of AIC and BIC. The lateral axis represents the IDs of curves, and the vertical axis represents values of AIC (a) or BIC (b). The colours of lines represent different plausible models.

137 When AIC is used as criterion for model selection, 57 (6.78%) curves
 138 are fitted by quadratic polynomial function and 160 (19.02%) curves for
 139 cubic polynomial function. As for non-linear models, 190 (22.59%) curves
 140 are fitted by Briere model, and the rest 434 (51.61%) curves are fitted by
 141 Ratkowsky model. When BIC is used for model selection, 218 (25.92%)

142 curves are fitted by linear models (55 quadratic polynomial model and 163
 143 cubic polynomial model). 191 (22.71%) curves are fitted by Briere model,
 144 while the rest 432 (51.37%) curves are fitted by Ratkowsky model. 18 curves
 145 are sufficiently fitted by different models under different criteria for model
 146 selection as shown in Table 1.

Table 1: Curves That AIC and BIC Support Different Models

ID	AIC-supported	BIC-supported
99	Briere	Ratkowsky
105	Ratkowsky	cubic
232	Ratkowsky	Briere
318	Ratkowsky	Briere
330	Briere	Ratkowsky
351	Briere	Ratkowsky
426	Ratkowsky	Briere
496	Briere	Ratkowsky
569	Ratkowsky	Briere
635	quadratic	cubic
644	quadratic	cubic
669	Ratkowsky	Briere
681	Ratkowsky	Briere
737	Briere	Ratkowsky
745	Ratkowsky	Briere
765	Briere	Ratkowsky
827	Ratkowsky	Briere
879	Briere	Ratkowsky

147 **3.2 Selected Models for Curves of Different Metabolic or** 148 **Habitat Types**

149 To assess preferred models for thermal performance curves of different metabolic
150 traits or species living in different habitat types, 18 curves were removed be-
151 cause AIC and BIC supported different models. So a total of 823 curves were
152 involved.

153 In the original dataset, the metabolic trait of each curve is defined in the
154 field of StandardisedTraitName (trait name for comparison), which contains
155 three categories: gross photosynthesis rate, net photosynthesis rate and res-
156 piration rate. Another field relevant to trait name is OriginalTraitName
157 (trait name as it found in source). It should be noted there are four curves
158 have no StandardisedTraitName, while their OriginalTraitName are oxy-
159 gen evolution rate in thylakoid membranes (IDs: 698, 699) and cell specific
160 photosynthesis rate (IDs: 441, 442). They were not involved in assessing
161 which model is suitable for different metabolic traits. As for habit type
162 of each curve, it is defined in another field (Habitat), which is composed
163 of four types: aquatic, freshwater, freshwater/terrestrial, marine and ter-
164 restrial. Here I assessed which model is suitable for determining thermal
165 performance of species living in terrestrial or non-terrestrial (aquatic, fresh-
166 water, freshwater/terrestrial and marine) habitats.

167 Table 2 illustrates the sufficient models for thermal performance curves of
168 different metabolic traits. A total of 819 thermal performance curves of
169 three metabolic traits are involved. For models of each metabolic trait, non-
170 linear model occupies a larger proportion (75.0% in gross photosynthesis
171 rate, 78.8% in net photosynthesis rate, and 66.2% in respiration rate) than
172 linear models. Besides, Ratkowsky model takes a bigger amount than Briere

173 model in all metabolic traits except gross photosynthesis rate.
174 Then I classified thermal performance curves according to whether the species
175 studied is specific in terrestrial habitats (Table 3). Non-linear model takes
176 the biggest amount of sufficient models for both two kinds of habitat type
177 (82.1% for terrestrial habitat and 55.2% of non-terrestrial habitat), and
178 Ratkowsky model occupies biggest proportion among four plausible models.

Table 2: Selected Models for Thermal Performance Curves of Different Metabolic Traits

Model	Gross photosynthesis rate	Net photosynthesis rate	Respiration rate	Total
Quadratic	0	19	36	55
Cubic	9	80	71	160
Briere	16	73	94	183
Ratkowsky	11	294	116	421
Total	36	466	317	819

Table 3: Selected Models for Thermal Performance Curves from Species in Different Habitat Types

Model	Terrestrial	Non-terrestrial	Total
Quadratic	21	34	55
Cubic	81	79	160
Briere	134	49	183
Ratkowsky	335	90	425
Total	571	252	823

179 **3.3 Preferred Models May not Describe the Observed Data** 180 **Sufficiently**

181 Through model selection, I selected one model for each curve and it is the
182 most sufficient one in terms of describing the thermal performance curve
183 among four plausible models. However, the preferred models of some curves
184 still fail in describing thermal performance throughout the temperature
185 range between lower and upper thermal limits of performance. As the growth
186 of temperature in this range, performance is supposed to increase, peaks
187 at some point, and then drops [1, 4]. The preferred models of some curves
188 are not bell-shaped (Figure. 3). Furthermore, ecologically unrealistic esti-
189 mations of thermal limits of performance are also given by some selected
190 models (Figure 4).

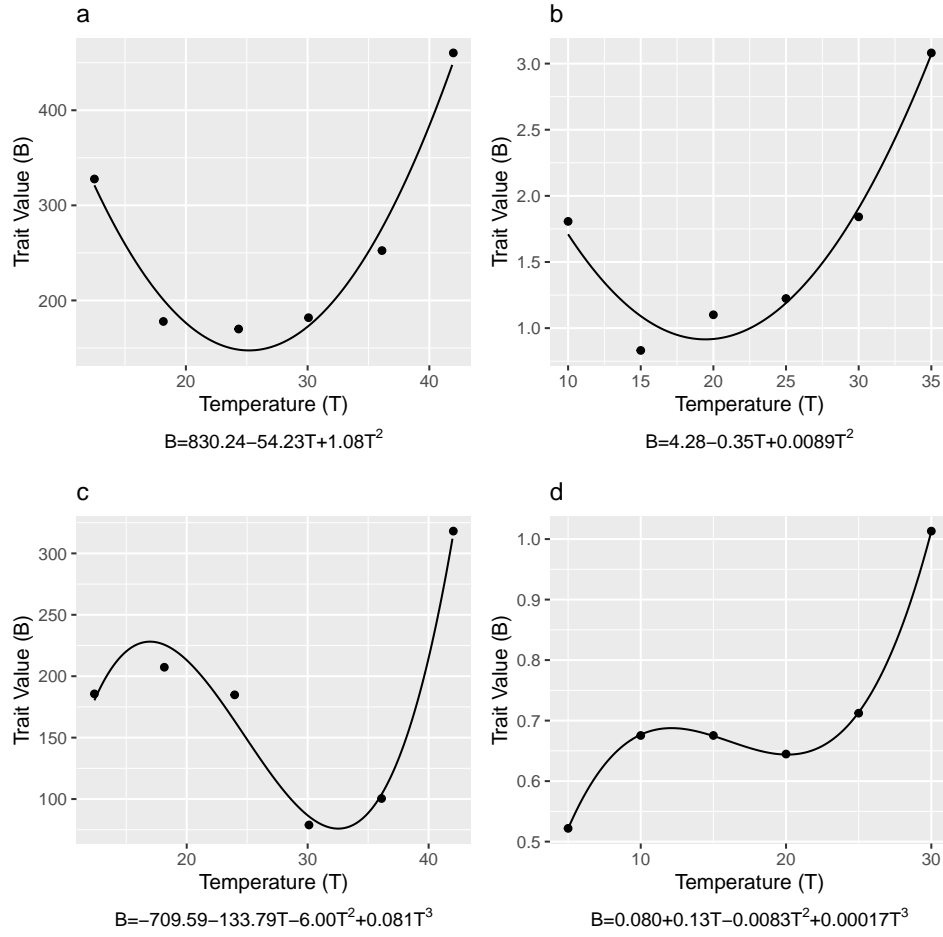


Figure 3: Examples of preferred models that are not bell-shaped curves. IDs of thermal performance curves are: 456 (a), 841 (b), 455 (c), 600 (d).

Mathematical expression of each model is given at the bottom of each subplot. For these datasets, AIC and BIC support the same models with equal parameters.

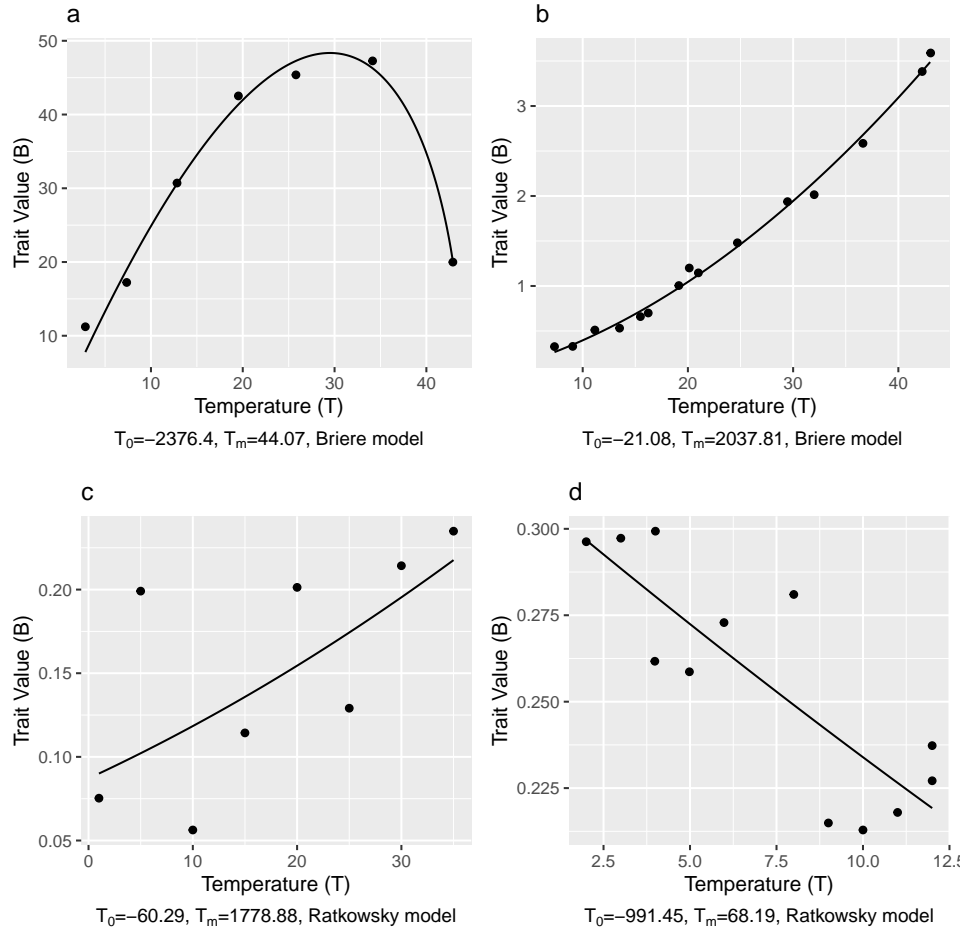


Figure 4: Examples of preferred models that give unrealistic estimations of thermal limits of performance. IDs of thermal performance curves are: 81 (a), 215 (b), 46 (c), 254 (d). Criterion of model selection is AIC, and estimations of lower and upper thermal limits of performance, denoted as T_0 and T_m , are given at the bottom of each subfigure.

191 4 Discussion

192 Investigations in how organisms response to temperature fulctuation are
 193 helpful in better understanding the impact of recent and future climate

194 change on biological systems [16, 17]. In assessment of thermal performance,
 195 it is important to choose an appropriate mathematical model that is best
 196 supported by empirical data and is able to provide relatively precise esti-
 197 mations of dependent variable using given values of independent variable.
 198 Currently, there are plenty of mathematical models used in fitting thermal
 199 performance curves, and model selection criteria can be used to explicate
 200 how sufficient a model is in describing thermal performance curves [4, 9, 10].
 201 In order to find which model is best supported by observed data of thermal
 202 performance, I fitted four plausible models to a dataset composed of 841
 203 thermal performance curves and conducted model averaging and selection
 204 using either AIC or BIC as criterion. In most cases, AIC and BIC prefer
 205 the same model. The results also showed that under both selection criteria,
 206 Ratkowsky model is sufficient in quantifying thermal performance for about
 207 51% of curves in the dataset.

208 In model selection, a set of plausible models are ranked by some criterion
 209 and the most appropriate one is selected. AIC and BIC are two criterion for
 210 model selection. They take both fit and model complexity into consideration
 211 to balance under- and over-fitting to observed data [10, 18]. Although AIC
 212 and BIC are quite similar in forms, they are divergent in theoretical motiva-
 213 tions. BIC is based on Bayesian statistical analysis and is an approximation
 214 reflecting the probability that the plausible model is the true model that
 215 generated the empirical data [19]. Minimized BIC is corresponded to max-
 216 imized posterior probability among all plausibilities and can be thought as
 217 a criterion for model selection [20]. However, whether there is such a "true
 218 model" is controversial [21], and the theoretical basis of BIC is disputed
 219 [19]. As for AIC, it measures the predictive performance of each candidate
 220 model by estimating Kullback-Leibler information loss [19, 22, 23], and is

221 thus well-founded in information theory. Here, I conducted model selection
222 using AIC and BIC as criterion respectively. In most cases, they prefer the
223 same model. However, I tend to use AIC as model selection criterion be-
224 cause of its solid theoretical foundation.

225 In non-linear model fitting, an iterative algorithm is employed to gain a
226 numerical local optimal solution, which is sensitive to start values [13, 14].
227 Here, I fitted each non-linear model 100 times with different start values
228 before model selection, attempting to find the global optimal solution. For
229 one thermal performance dataset, multiple solutions can be obtained by dif-
230 ferent start values while they have equal and lowest AIC or BIC. This is
231 because of limited accuracy in numerical calculation of AIC and BIC by R
232 scripts. To deal with this, I conducted model averaging using smoothed AIC
233 or BIC method. When multiple plausible models get nearly equivalent sup-
234 port from observed data (*e.g.* similar AIC or BIC values), model averaging
235 is a good method to give estimations of model parameters or predict values
236 of response variables [10].

237 Generally, thermal performance curve is supposed to be a bell-shaped curve
238 with ecologically realistic lower and upper thermal limits of performance
239 [1, 4]. However, some models supported by AIC or BIC are not bell-shaped
240 curves, as exemplified in Figure 3. Others may give estimations of thermal
241 limits of performance that are too low or too high to be realistic, as ex-
242 emplified in Figure 4. Such models may fit to the observed data well (*e.g.*
243 Figure 3d and Figure 4a), but fail in describing the whole thermal perfor-
244 mance curve. A possible reason is that there are not enough samples from a
245 wide enough temperature range to allow the models to capture the change
246 of performance over temperature in different ranges. For example, curve 215
247 only contains samples of relatively low temperature (*i.e.* temperatures of all

248 samples are no greater than the optimum temperature where performance
249 peaks) as it is shown in Figure 4b. An alternative explanation is that none of
250 the four plausible models are suitable for describing the observed data. AIC
251 and BIC can only explicate the relative goodness of each model in a given
252 set of models [10, 15, 18] and it is possible that no model in the given set
253 can fit to the observed data sufficiently. Under these circumstances, more
254 models are needed to be used in fitting and selection.

255 Overall, I conducted model fitting, averaging and selection using ob-
256 served data of 841 thermal performance curves. Plausible models include
257 quadratic polynomial model, cubic polynomial model, Briere model and
258 Ratkowsky model. AIC and BIC were used as model selection criterion.
259 For most curves, AIC and BIC give support to the same model. The results
260 shows that for more than a half of thermal performance curves involved here,
261 Ratkowsky model is the most sufficient one among four plausibilities. When
262 curves are classified according to metabolic trait or habitat type of species,
263 Ratkowsky model is most sufficient one for a majority of curves in most cat-
264 egories. However, some selected models cannot describe the whole thermal
265 performance curves or contain unrealistic parameters, indicating that none
266 of the four models is suitable for fitting to the observed data.

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