

Section for Applied Statistics and Data Analysis

TA: Cong Mu

Office Hour: Wednesday 10:00AM - 12:00PM

October 11, 2019

1 Some Statistics

- Checking Error Assumptions
 - Constant Variance
 - Normality
 - Correlated Errors

2 Some Programming

- Examples in Faraway

- Recall

$$\epsilon \sim \mathcal{N}(0, \sigma^2 \mathbf{I}) .$$

- Checking Error Assumptions

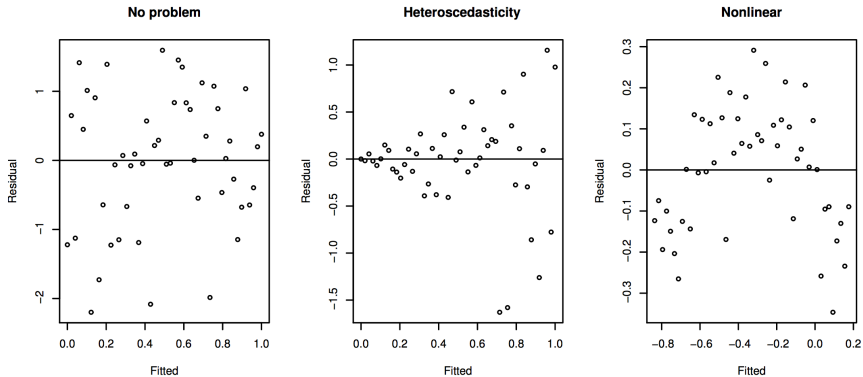
- Constant Variance
- Normality
- Correlated Errors

- Finding Unusual Observations

- Leverage
- Outliers
- Influential Observations

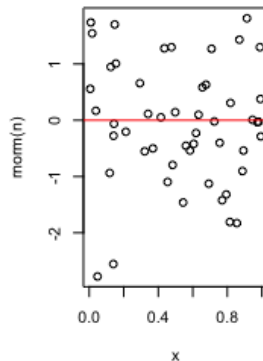
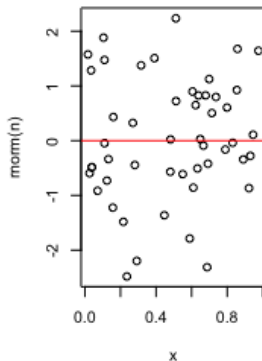
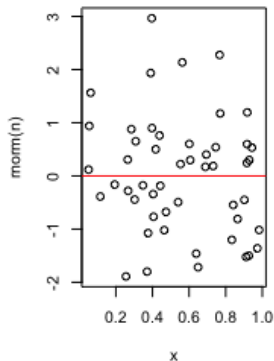
- Checking the Structure of the Model

Constant Variance - Overview

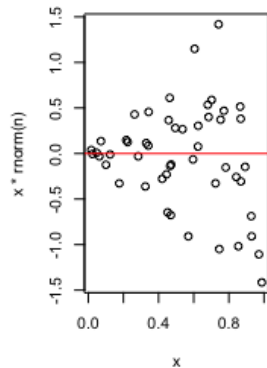
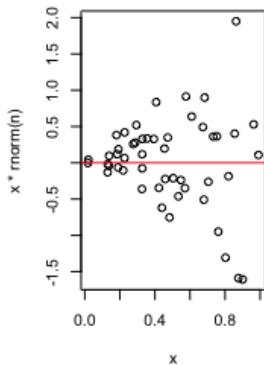
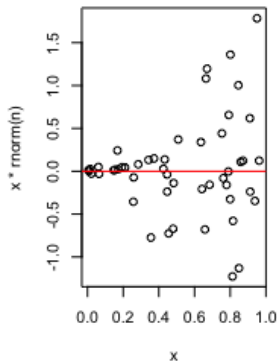


(Figure from Linear Models with R)

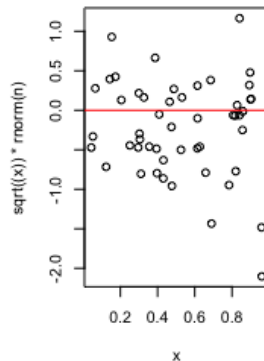
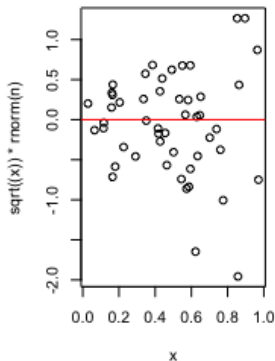
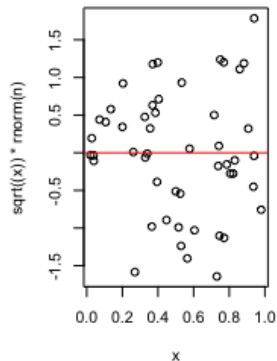
Example - Constant Variance



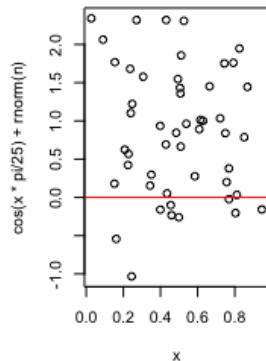
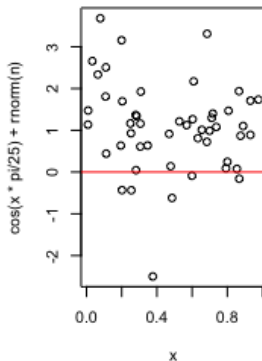
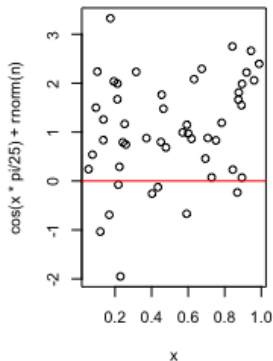
Example - Strong Nonconstant Variance



Example - Mild Nonconstant Variance



Example - Nonlinearity

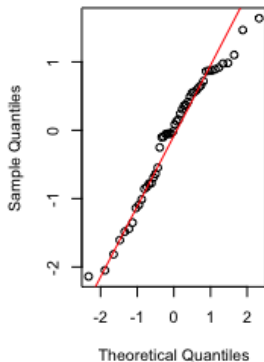


Normality - Overview

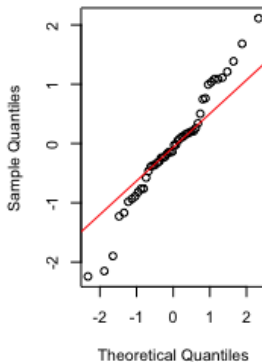
- Q-Q Plot
- Tests
 - Shapiro-Wilk test
 - Anderson-Darling test
 - etc
- Some R Packages
 - `nortest`
 - `normtest`
 - etc

Example - Normal

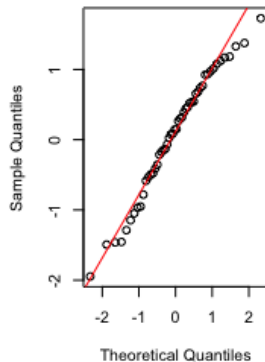
Normal Q-Q Plot



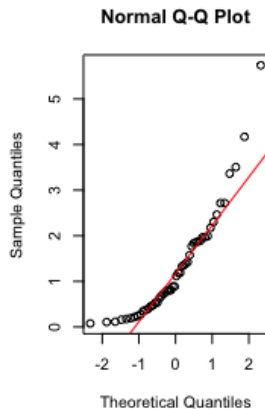
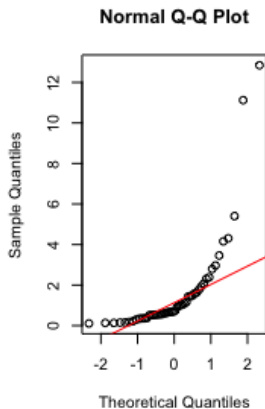
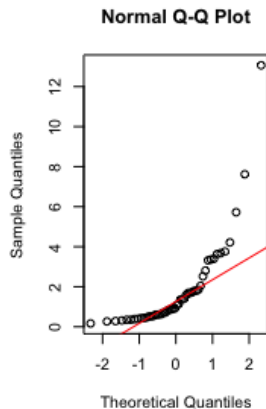
Normal Q-Q Plot



Normal Q-Q Plot

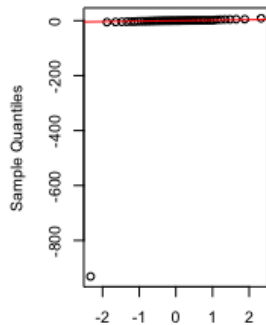


Example - Lognormal (a skewed distribution)



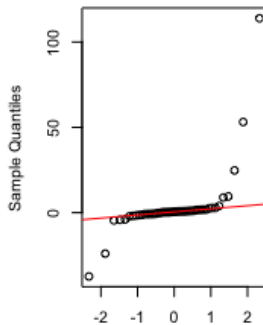
Example - Cauchy (a long-tailed distribution)

Normal Q-Q Plot



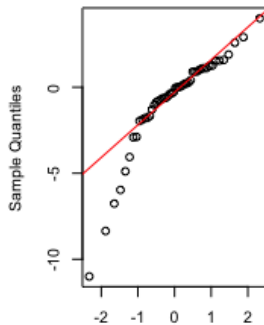
Theoretical Quantiles

Normal Q-Q Plot



Theoretical Quantiles

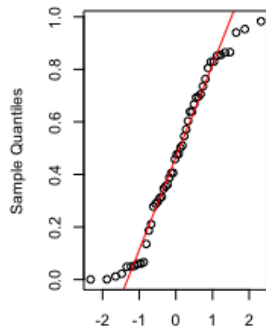
Normal Q-Q Plot



Theoretical Quantiles

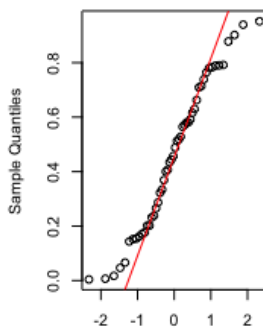
Example - Uniform (a short-tailed distribution)

Normal Q-Q Plot



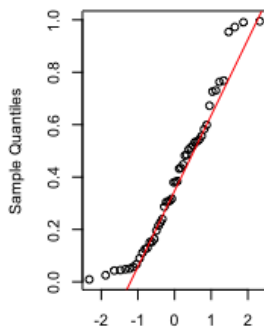
Theoretical Quantiles

Normal Q-Q Plot



Theoretical Quantiles

Normal Q-Q Plot



Theoretical Quantiles

Correlated Errors - Overview

- Plot Successive Pairs of Residuals
- Tests
 - Durbin-Watson test
 - etc
- Some R Packages
 - lmtest
 - etc

Examples in Faraway Chapter 6

- **Example:** savings dataset
- **Example:** gala dataset
- **Example:** globwarm dataset

Thanks for listening!