



WPI

OIE 548 (Performance Analytics)
Final Project: DEA-Based Selection of Indian T20 Bowlers
By Ishan Ratnakar Deshpande

Problem Statement:

The Indian cricket team, currently the highest-ranked team in T20 cricket according to the ICC ratings, is preparing for the upcoming ICC Men's T20 Cricket World Cup scheduled to take place in the United States from June 1 to June 29, 2024. The tournament will be held across three venues: Dallas, Florida, and New York.

To optimize their performance, the team management faces a crucial decision in selecting the best combination of bowlers for the playing eleven from a talented pool of players.

In this project, the aim is to utilize Data Envelopment Analysis (DEA) models to address this selection dilemma. T20 International (T20I) statistics of 23 Indian bowlers have been collected from the ESPN Cricinfo website. The dataset includes various performance metrics categorized into inputs and outputs for the analysis. By applying DEA techniques, the objective is to identify the most efficient bowlers who can contribute effectively to the team's success in the ICC Men's T20 Cricket World Cup.

Dataset description:

The dataset comprises columns representing key performance metrics of 23 Indian bowlers in T20 International cricket matches. These columns include 'PlayerName', 'Matches', 'Overs', 'Maidens', 'Runs', 'Wickets', 'Average', 'Economy', 'StrikeRate', '4fers', and '5fers', providing comprehensive insights into the bowlers' experience, workload, control over runs, wicket-taking ability, and effectiveness in maintaining a low scoring rate.

Inputs:

Matches: The total number of matches played by the player. This represents the experience and consistency of the player over time.

Overs: The total number of overs bowled by the bowler. This indicates the workload and contribution of the player in terms of bowling opportunities.

Maidens: The total number of maidens bowled by the player. This reflects the ability of the bowler to control runs and build pressure on the opposition batsmen.

Runs: The total runs conceded by the bowler in all matches. This represents the defensive capability of the bowler and their ability to restrict runs.

4fers: The number of times a bowler takes 4 wickets in an innings. This indicates the bowler's ability to take wickets in clusters and have a significant impact on the game.

5fers: The number of times a bowler takes 5 wickets in an innings. Similar to 4fers, this also reflects the bowler's ability to take wickets in bulk and potentially change the course of the match.

Outputs:

Wickets: The total number of wickets taken by the bowler in all matches. This represents the primary objective of the bowler, which is to take wickets and dismiss the opposition batsmen.

Average: The average number of runs conceded per wicket taken. This provides an indication of the bowler's effectiveness in terms of conceding runs per wicket.

Economy: The average number of runs conceded per over bowled. This measures the bowler's ability to maintain a low scoring rate and control the flow of runs during their spell.

Strike Rate: The average number of balls bowled per wicket taken. This indicates how quickly the bowler takes wickets, with a lower strike rate implying greater effectiveness in dismissing batsmen.

Models Used:

- 1] Multiplier Model (Input Oriented)
- 2] Multiplier Model (Improved Input Oriented)
- 3] Multiplier Model (Output Oriented)
- 4] Envelopment Model (Input Oriented)
- 5] Envelopment Model (Output Oriented)
- 6] Envelopment Model (Input Oriented - Super Efficiency)
- 7] Envelopment Model (Output Oriented - Super Efficiency)

Multiplier Model (Input Oriented)

Model:

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
1	Player Name	Matches	Overs	Maidens	Runs	4(fers)	5(fers)		Wickets	Average	Economy	Strike Rate		Weighted Category I	Weighted Category II		DEA Score		
2	Jasprit Bumrah	62	221.5	10	1455	0	0		74	19.66	19.66	17.9		8.989917994	0.824318658		1		
3	Arshdeep Singh	44	149.5	2	1294	1	0		62	20.87	8.63	14.5		7.67745943	0.875052411		0.986482		
4	Kuldeep Yadav	35	123.2	2	832	1	2		59	14.1	6.74	12.5		5.12770939	0.591194969		1		
5	Bhuvneshwar Kumar	87	298.3	10	2079	3	2		90	23.1	6.96	19.9		12.80005017	0.968553459		0.722572		
6	Ravi Bishnoi	24	93.4	0	703	1	0		36	19.52	7.50	15.6		4.173717501	0.818448637		1		
7	Ravindra Jadeja	66	212	4	1506	0	0		53	28.41	7.10	24		9.357128779	1.191194969		0.715478		
8	Ravichandran Ashwin	65	242	3	1672	2	0		72	23.22	6.90	20.1		10.15252618	0.973584906		0.830587		
9	Akar Patel	52	163.1	1	1186	0	0		49	24.2	7.26	19.9		7.369575994	1.014675052		0.854583		
10	Mohammad Shami	23	79.3	1	711	0	0		24	29.62	8.94	19.8		4.184904466	1.241926721		0.754021		
11	Mohammad Siraj	10	38	2	334	1	0		12	27.83	8.78	19		1.942960215	1.16897631		0.848282		
12	Umaran Malik	8	23.1	0	243	0	0		11	22.09	10.46	12.6		1.434254929	0.926205451		1		
13	Avesh Khan	20	66.2	1	618	1	0		19	32.52	9.31	20.9		3.637752573	1.363522013		0.673821		
14	Deepak Chahar	25	90	2	747	0	1		31	24.09	8.30	17.4		4.420625108	1.010062893		0.910428		
15	Yuzvendra Chahal	80	294	2	2409	2	1		96	25.09	8.19	18.3		14.23831879	1.051991614		0.785963		
16	Hardik Pandya	92	238.5	1	1950	3	0		73	26.71	8.16	19.6		12.30237656	1.119916143		0.716751		
17	Shardul Thakur	25	84.2	0	772	1	0		33	23.29	9.15	15.3		4.544709037	0.976519916		0.916167		
18	Shivam Dube	21	36.3	0	360	0	0		8	45	9.86	27.3		2.385726317	1.886792453		0.828372		
19	Washington Sundar	43	134.3	1	968	0	0		34	28.47	7.19	23.7		6.030885102	1.193710692		0.723072		
20	Prasidh Krishna	5	20	0	220	0	0		8	27.5	11.00	15		1.234538037	1.153039832		1		
21	Mukesh Kumar	14	43.5	0	412	0	0		12	34.33	9.39	21.9		2.444181643	1.439412998		0.688216		
22	Krunal Pandya	19	68.2	1	554	1	0		15	36.93	8.10	27.3		3.291577822	1.548427673		0.613353		
23	Venkatesh Iyer	9	9.1	0	75	0	0		5	15	8.18	11		0.628930818	0.628930818		1		
24	Rahul Chahar	6	22	0	167	0	0		7	23.85	7.59	18.8		1			1		
25																			
26	Weights/Multipliers	0.02852	0	0	0.004963	0	0		0	0.041929	0	0							
27																			
28	Player Under Consideration	23																	
29	Weighted Category I	1																	
30	Weighted Category II	1																	
31																			

Solver:

Solver Parameters

Set Objective:

\$B\$30

To:

☒ Max

☐ Min

☐ Value Of:

0

By Changing Variable Cells:

\$B\$26:\$G\$26,\$I\$26:\$L\$26

Subject to the Constraints:

\$B\$29 = 1

\$O\$2:\$O\$24 <= \$N\$2:\$N\$24

Add

Change

Delete

Reset All

Load/Save

☒ Make Unconstrained Variables Non-Negative

Select a Solving Method:

Simplex LP

Options

Solving Method

Select the GRG Nonlinear engine for Solver Problems that are smooth nonlinear. Select the LP Simplex engine for linear Solver Problems, and select the Evolutionary engine for Solver problems that are non-smooth.

Help

Solve

Close

VBA Code:

```
(General)
Sub DEA()
'Declare DUMNo as integer. This DumNo represents the player under
'consideration. In the example, DUMNo goes from 1 to 23
    Dim DUMNo As Integer
    For DUMNo = 1 To 23
'set the value of cell B28 equal to DUMNo (1,2,..., 23)
        Range("B28") = DUMNo
'Run the Solver model. The UserFinish is set to True so that
'the Solver Results dialog box will not be shown
        SolverSolve UserFinish:=True
'Place the best ratio into column Q
        Range("Q" & DUMNo + 1) = Range("B30")
    Next DUMNo
End Sub
```

Results and Analysis:

This model, known as the Multiplier Input Oriented Model, maximizes output with the input set to 1. By analyzing the DEA score, we identify optimal practices. Among 23 players, 7 demonstrate optimal practices with a DEA score of 1. These players are Jasprit Bumrah, Kuldeep Yadav, Ravi Bishnoi, Umran Malik, Prasidh Krishna, Venkatesh Iyer, and Rahul Chahar.

The weights or multiplier values obtained from the Data Envelopment Analysis (DEA) model provide valuable insights into the relative significance of input and output variables within a unified framework for evaluating cricket player performance efficiency. Among the input variables, "Matches" emerges as the most influential, indicating its pivotal role in determining overall efficiency, while "Runs" also contributes significantly. Conversely, variables such as "Overs," "Maidens," "4(fers)," and "5(fers)" display minimal impact on efficiency. Within the output variables, "Average" exhibits the highest weight, followed by "Strike Rate," suggesting their critical importance in evaluating player effectiveness. These findings offer actionable insights for optimizing player performance and strategic decision-making in cricket.

Multiplier Model (Improvement in the Input Oriented Model)

The previous model pinpointed 7 out of 23 players as embodying best practices. This updated version provides clarity on the inputs necessary to identify such practices. By multiplying the original input with the DEA score, new inputs were derived for model preparation. Achieving a flawless DEA score of 1 using this method offers insight into setting inputs to reach the frontier effectively.

Model:

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	AA	AB
	Player Name	Matches	Overs	Maiden	Runs	4(fers)	5(fers)	DEA Score	Matches(New)	Overs(New)	Maiden(New)	Runs(New)	4-fers(New)	5-fers(New)	Wickets	Average	Economy	Strike Rate	Weighted Category	Weighted Category II	DEA Score (Improved)							
1	Jasprit Bumrah	62	221.5	10	1455	0	0	1	62	221.5	10	1455	0	0	0	74	19.66	19.66	17.9	0.503917394	0.62410558	1	1					
2	Ashdeep Singh	44	169.5	2	1234	1	0	0.96949	43	167.5	2	1277	1	0	0	62	20.87	8.63	14.5	7.573676001	0.875552411	0.96949	1					
3	Pudsey Yadav	36	123.2	2	832	1	2	1	36	123.2	2	832	1	2	0	58	14.1	8.74	12.5	5.1773839	0.91954988	1	1					
4	Bhuvaneshwar Kumar	67	296.3	10	2079	3	2	0.72257	63	295.5	7	1502	2	1	0	90	23.1	6.56	19.9	3.248953982	0.939551459	0.72257	1					
5	Ravi Bishnoi	24	93.4	0	700	1	0	1	24	93.4	0	700	1	0	0	36	19.52	7.50	15.0	4.17277501	0.81646827	1	1					
6	Raunooda Jadeja	66	242	4	1506	0	0	0.75449	47	152	3	1079	0	0	0	53	28.41	7.10	24	6.694910309	1.191914369	0.75449	1					
7	Ravichandran Ashwin	65	242	3	1672	2	0	0.85059	54	209	2	1389	2	0	0	72	23.22	6.50	20.1	6.425561607	0.978564986	0.85059	1					
8	Avin Patel	52	193.1	1	1189	0	0	0.95459	44	189.4	1	1014	0	0	0	49	24.2	7.26	19.9	6.25791405	1.04673552	0.95459	1					
9	Muhammad Shami	23	79.3	1	711	0	0	0.75402	17	60	1	536	0	0	0	24	29.62	8.94	19.0	3.95505236	1.24192671	0.75402	1					
10	Muhammad Siraj	10	39	2	334	1	0	0.94629	8	32.2	2	283	1	0	0	12	27.63	8.79	19	1.94670541	1.16887631	0.94629	1					
11	Umran Malik	9	23.1	0	243	0	0	1	8	23.1	0	243	0	0	0	11	22.19	10.48	12.6	1.43455429	0.526265451	1	1					
12	Avinash Khan	20	66.2	1	618	1	0	0.67382	10	45	1	476	1	0	0	19	32.52	9.11	20.9	2.45195426	1.39352203	0.67382	1					
13	Deepak Chahar	25	90	2	747	0	1	0.91043	23	82	2	600	0	1	0	31	24.09	8.30	17.4	4.624961937	1.01002393	0.91043	1					
14	Yuzvendra Chahal	80	294	2	2435	2	1	0.76536	63	231.1	2	1833	2	1	0	96	25.09	8.19	19.3	11.18073496	1.05399534	0.76536	1					
15	Hardi Pandya	52	236.5	1	1950	3	0	0.73675	46	177	1	1598	2	0	0	73	26.71	8.76	19.6	8.817736019	1.11591813	0.73675	1					
16	Shardul Thakur	25	84.2	0	772	1	0	0.93837	23	77.1	0	707	1	0	0	33	23.29	9.15	15.3	4.163714436	0.97657638	0.93837	1					
17	Shivam Dube	21	36.3	0	360	0	0	0.62037	17	30.1	0	236	0	0	0	6	45	9.86	27.3	1.97626974	1.09732453	0.62037	1					
18	Washington Sundar	43	134.3	1	958	0	0	0.72307	31	97.1	1	700	0	0	0	34	28.47	7.19	23.7	4.380762335	1.133710932	0.72307	1					
19	Prasidh Krishna	5	20	0	220	0	0	1	5	20	0	220	0	0	0	8	27.5	11.00	75	1.234559197	1.154039832	1	1					
20	Mukesh Kumar	14	43.5	0	412	0	0	0.68822	10	30	0	294	0	0	0	12	34.53	9.95	21.9	1.662123693	1.43942298	0.68822	1					
21	Krunal Pandya	19	66.2	1	554	1	0	0.93335	12	42	1	340	1	0	0	15	36.33	8.10	27.3	2.093937611	1.548427673	0.93335	1					
22	Venkatesh Iyer	9	3.1	0	75	0	0	1	9	3.1	0	75	0	0	0	5	15	8.18	11	0.623933018	0.623933018	1	1					
23	Rahul Chahar	5	22	0	167	0	0	1	6	22	0	167	0	0	0	7	23.85	7.59	18.8	1	1	1	1					
24																												
25	Weights/Multipliers	0.503917394	0	0	0.02610558	0	0		0.62410558	0	0	0.04682671	0	0	0	0	0.44626974	0	0									
26	Player Under Consideration	23																										
27	Weighted Category I	1																										
28	Weighted Category II	1																										
29																												
30																												
31																												
32																												
33																												
34																												
35																												

Solver:

Solver Parameters

Set Objective:

\$B\$30

To:

Max

Min

Value Of:

0

By Changing Variable Cells:

\$J\$26:\$O\$26,\$Q\$26:\$T\$26

Subject to the Constraints:

\$B\$29 = 1

\$W\$2:\$W\$24 <= \$V\$2:\$V\$24

Add

Change

Delete

Reset All

Load/Save

☒ Make Unconstrained Variables Non-Negative

Select a Solving Method:

Simplex LP

Options

Solving Method

Select the GRG Nonlinear engine for Solver Problems that are smooth nonlinear. Select the LP Simplex engine for linear Solver Problems, and select the Evolutionary engine for Solver problems that are non-smooth.

Help

Solve

Close

VBA code:

```
(General)
Sub DEA()
'Declare DUMNo as integer. This DumNo represents the player under
'consideration. In the example, DUMNo goes from 1 to 23
    Dim DUMNo As Integer
    For DUMNo = 1 To 23
'set the value of cell B28 equal to DUMNo (1,2,..., 23)
        Range("B28") = DUMNo
'Run the Solver model. The UserFinish is set to True so that
'the Solver Results dialog box will not be shown
        SolverSolve UserFinish:=True
'Place the best ratio into column Z
        Range("Z" & DUMNo + 1) = Range("B30")
    Next DUMNo
End Sub
```

Results and Analysis:

Let's examine the case of Player Avesh Khan:

His original input values and DEA score are:

Matches: 20

Overs: 66.2

Maidens: 1

Runs: 618

4-fers: 1

5-fers: 0

DEA score: 0.67382

After multiplying these values by the DEA score, we get updated input values and an improved DEA score:

Matches (New): 13

Overs (New): 45

Maidens (New): 1

Runs (New): 416

4-fers (New): 1

5-fers (New): 0

Improved DEA score: 1

The original DEA score of 0.67382 indicates that the player has the potential to reduce their current input levels by 32.62% in order to reach the frontier.

Multiplier Model (Output Oriented)

Model:

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
1	Player Name	Matches	Overs	Maidens	Runs	4(fers)	5(fers)		Wickets	Average	Economy	Strike Rate		Weighted Category I	Weighted Category II		DEA Score		
2	Jasprit Bumrah	62	221.5	10	1455	0	0		74	19.66	19.66	17.9		0.916996047	2.590250329		1		
3	Arshdeep Singh	44	149.5	2	1294	1	0		62	20.87	8.63	14.5		0.183399209	1.137022398		1		
4	Kuldeep Yadav	35	123.2	2	832	1	2		59	14.1	6.74	12.5		0.183399209	0.88801054		1		
5	Bhuvneshwar Kumar	87	298.3	10	2079	3	2		90	23.1	6.96	19.9		0.916996047	0.916996047		1		
6	Ravi Bishnoi	24	93.4	0	703	1	0		36	19.52	7.50	15.6		0	0.988142292		1		
7	Ravindra Jadeja	66	212	4	1506	0	0		53	28.41	7.10	24		0.366798419	0.935444137		1		
8	Ravichandran Ashwin	65	242	3	1672	2	0		72	23.22	6.90	20.1		0.275098814	0.909090909		1		
9	Akar Patel	52	163.1	1	1186	0	0		49	24.2	7.26	19.9		0.091699605	0.856521739		1		
10	Mohammad Shami	23	79.3	1	711	0	0		24	29.62	8.94	18.8		0.091699605	1.177865613		1		
11	Mohammad Siraj	10	38	2	334	1	0		12	27.83	8.78	19		0.183399209	1.156785244		1		
12	Umar Malik	8	23.1	0	243	0	0		11	22.09	10.48	12.6		0	1.380764163		1		
13	Avesh Khan	20	66.2	1	618	1	0		19	32.52	9.31	20.9		0.091699605	1.226613966		1		
14	Deepak Chahar	25	90	2	747	0	1		31	24.09	8.30	17.4		0.183399209	1.093544137		1		
15	Yuzvendra Chahal	80	294	2	2409	2	1		96	25.09	8.19	18.3		0.183399209	1.079051383		1		
16	Hardik Pandya	92	238.5	1	1950	3	0		73	26.71	8.16	19.6		0.091699605	1.075098814		1		
17	Shardul Thakur	25	84.2	0	772	1	0		33	23.29	9.15	15.3		0	1.205533597		1		
18	Shivam Dube	21	36.3	0	360	0	0		8	45	9.86	27.3		0	1.299077734		1		
19	Washington Sundar	43	134.3	1	968	0	0		34	28.47	7.19	23.7		0.091699605	0.947299078		1		
20	Prasidh Krishna	5	20	0	220	0	0		8	27.5	11.00	15		0	1.449275362		1		
21	Mukesh Kumar	14	43.5	0	412	0	0		12	34.33	9.39	21.9		0	1.23715415		1		
22	Krunal Pandya	19	68.2	1	554	1	0		15	36.93	8.10	27.3		0.091699605	1.067193676		1		
23	Venkatesh Iyer	9	9.1	0	75	0	0		5	15	8.18	11		0	1.07773386		1		
24	Rahul Chahar	6	22	0	167	0	0		7	23.85	7.59	18.8		0	1		1		
25	Weights/Multipliers	0	0	0.0917	0	0	0		0	0	0	0							
26																			
27																			
28	Player Under Consideration	23																	
29	Weighted Category I	0																	
30	Weighted Category II	1																	
31																			
32																			
33																			

Solver:

Solver Parameters

Set Objective:

\$B\$29

To:

Max

Min

Value Of:

0

By changing Variable Cells:

\$B\$26:\$G\$26,\$I\$26:\$L\$26

Subject to the Constraints:

\$B\$30 = 1

\$O\$2:\$O\$24 >= \$N\$2:\$N\$24

Add

Change

Delete

Reset All

Load/Save

☒ Make Unconstrained Variables Non-Negative

Select a Solving Method:

Simplex LP

Options

Solving Method

Select the GRG Nonlinear engine for Solver Problems that are smooth nonlinear. Select the LP Simplex engine for linear Solver Problems, and select the Evolutionary engine for Solver problems that are non-smooth.

Help

Solve

Close

VBA code:

(General)
<pre>Sub DEA() 'Declare DUMNo as integer. This DumNo represents the player under 'consideration. In the example, DUMNo goes from 1 to 23 Dim DUMNo As Integer For DUMNo = 1 To 23 'set the value of cell B28 equal to DUMNo (1,2,..., 23) Range("B28") = DUMNo 'Run the Solver model. The UserFinish is set to True so that 'the Solver Results dialog box will not be shown SolverSolve UserFinish:=True 'Place the best ratio into column Q Range("Q" & DUMNo + 1) = Range("B30") Next DUMNo End Sub</pre>

Results and Analysis:

In an output-oriented multiplier model, the objective is to minimize inputs while setting the output to 1. Achieving a DEA score of 1 for each player indicates that they are operating at maximum efficiency within this framework.

The weights derived from the DEA model represent the relative importance assigned to different performance metrics for evaluating a player's efficiency and effectiveness. In this specific case, the weights indicate that Maidens hold a significant emphasis, with a weight of 0.0917, suggesting that the ability to prevent scoring opportunities is highly valued. Conversely, other metrics such as Matches, Overs, Runs, 4-fers, 5-fers, Wickets, Average, Economy, and Strike Rate are assigned a weight of 0, indicating they are not considered as influential in determining efficiency according to this model. These weights provide valuable insight into the factors that contribute most significantly to a player's performance evaluation within the context of the DEA analysis.

Envelopment Model (Input Oriented)

In this model, a virtual DMU is created by leveraging existing DMUs. It operates as an input-oriented model, employing the concept of weight share. Each DMU contributes a specific percentage to the overall efficiency score, with the sum of these weight shares totaling 1 or 100%. When assessing a particular DMU, the weight share column indicates the percentage contribution of other DMUs. This model serves as a valuable tool for benchmarking purposes.

Model:

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
1	Player Name	Matches	Overs	Maidens	Runs	4(fers)	5(fers)		Wickets	Average	Economy	Strike Rate		Weight Share		DEA Efficiency				
2	Jasprit Bumrah	62	221.5	10	1455	0	0		74	19.66	19.66	17.9		0%		1				
3	Arshdeep Singh	44	149.5	2	1294	1	0		62	20.87	8.63	14.5		14%		1				
4	Kuldeep Yadav	35	123.2	2	832	1	2		59	14.1	6.74	12.5		0%		1				
5	Bhuvneshwar Kumar	87	296.3	10	2079	3	2		90	23.1	6.96	19.9		0%		1				
6	Ravi Bishnoi	24	93.4	0	703	1	0		36	19.92	7.50	15.6		0%		1				
7	Ravindra Jadeja	66	212	4	1506	0	0		53	28.41	7.10	24		0%		1				
8	Ravichandran Ashwin	65	242	3	1672	2	0		72	23.22	6.90	20.1		0%		1				
9	Akar Patel	52	163.1	1	1186	0	0		49	24.2	7.26	19.9		0%		1				
10	Mohammad Shami	23	79.3	1	711	0	0		24	29.62	6.94	19.8		0%		1				
11	Mohammad Siraj	10	38	2	334	1	0		12	27.83	6.78	19		0%		1				
12	Umaran Malik	8	23.1	0	243	0	0		11	22.09	10.48	12.6		0%		1				
13	Avesh Khan	20	66.2	1	618	1	0		19	32.52	9.31	20.9		0%		0.914524725				
14	Deepak Chahar	25	90	2	747	0	1		31	24.09	8.30	17.4		0%		1				
15	Yuzvendra Chahal	80	294	2	2409	2	1		96	25.09	8.19	18.3		0%		1				
16	Hardik Pandya	92	238.5	1	1950	3	0		73	26.71	8.16	19.6		0%		1				
17	Shardul Thakur	25	84.2	0	772	1	0		33	23.29	9.15	15.3		0%		1				
18	Shivam Dube	21	36.3	0	360	0	0		8	45	9.86	27.3		1%		1				
19	Washington Sundar	43	134.3	1	968	0	0		34	28.47	7.19	23.7		0%		1				
20	Prasidh Krishna	5	20	0	220	0	0		8	27.5	11.00	15		0%		1				
21	Mukesh Kumar	14	43.5	0	412	0	0		12	34.33	9.39	21.9		85%		1				
22	Krunal Pandya	19	66.2	1	554	1	0		15	36.93	8.10	27.3		0%		1				
23	Venkatesh Iyer	9	9.1	0	75	0	0		5	15	8.10	11		0%		1				
24	Rahul Chahar	6	22	0	167	0	0		7	23.85	7.59	18.8		0%		1				
25																				
26	Sum of Weight Shares													100%						
27	DMU Under Evaluation	12																		
28	Virtual DMU																			
29	Matches	18.2909			18.2909															
30	Overs	58.3952			60.5415															
31	Maidens	0.23452			0.91452															
32	Runs	535.282			565.176															
33	4(fers)	0.13884			0.91452															
34	5(fers)	0			0															
35	Wickets	10			10															
36	Average	32.52			32.52															
37	Economy	9.31			9.31															
38	Strike Rate	20.9			20.9															
39																				
40																				
41																				

Solver:

Solver Parameters

Set Objective:

\$K\$29

To:

Max

Min

Value Of:

0

By Changing Variable Cells:

\$N\$2:\$N\$24,\$K\$29

Subject to the Constraints:

\$B\$29:\$B\$34 <= \$D\$29:\$D\$34

\$B\$35:\$B\$38 >= \$D\$35:\$D\$38

\$N\$26 = 1

Add

Change

Delete

Reset All

Load/Save

☒ Make Unconstrained Variables Non-Negative

Select a Solving Method:

Simplex LP

Options

Solving Method

Select the GRG Nonlinear engine for Solver Problems that are smooth nonlinear. Select the LP Simplex engine for linear Solver Problems, and select the Evolutionary engine for Solver problems that are non-smooth.

Help

Solve

Close

VBA Code:

```
Sub DEA()  
'Declare DUMNo as integer. This DumNo represents the Player under  
'consideration. In the example, DUMNo goes from 1 to 23  
    Dim DUMNo As Integer  
    For DUMNo = 1 To 23  
'set the value of cell B27 equal to DUMNo (1,2,..., 23)  
        Range("B27") = DUMNo  
'Run the Solver model. The UserFinish is set to True so that  
'the Solver Results dialog box will not be shown  
        SolverSolve UserFinish:=True  
'Place the best ratio into column P  
        Range("P" & DUMNo + 1) = Range("K29")  
    Next DUMNo  
End Sub
```

Results and Analysis:

Analyzing the DEA score reveals that among the 23 players, 22 are considered best practices. When evaluating DMU 12 (Avesh Khan), the weight share column indicates that DMU 20 holds the highest weight share at 85%, followed by DMU 2 with a weight share of 14%, and DMU 19 with a weight share of 1%. Therefore, DMU 12 can use DMU 20 as a benchmarking model, followed by DMU 2 and DMU 19, based on their respective percentage weight shares.

Envelopment Model (Output Oriented)

Model:

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
1	Player Name	Matches	Overs	Maidens	Runs	4(fers)	5(fers)		Wickets	Average	Economy	Strike Rate		Weight Share		DEA Efficiency			
2	Jasprit Bumrah	62	221.5	10	1455	0	0		74	19.66	19.66	17.9		3%		1			
3	Arshdeep Singh	44	149.5	2	1294	1	0		62	20.87	8.63	14.5		13%		1			
4	Kuldeep Yadav	35	123.2	2	832	1	2		59	14.1	6.74	12.5		0%		1			
5	Bhuvneshwar Kumar	87	298.3	10	2079	3	2		90	23.1	6.96	19.9		0%		1			
6	Ravi Bishnoi	24	93.4	0	703	1	0		36	19.52	7.60	15.6		0%		1			
7	Ravindra Jadeja	66	212	4	1506	0	0		53	28.41	7.10	24		0%		1			
8	Ravichandran Ashwin	65	242	3	1672	2	0		72	23.22	6.90	20.1		0%		1			
9	Akar Patel	52	163.1	1	1186	0	0		49	24.2	7.26	19.9		0%		1			
10	Mohammad Shami	23	79.3	1	711	0	0		24	29.62	8.94	19.8		0%		1			
11	Mohammad Siraj	10	38	2	334	1	0		12	27.83	8.78	19		0%		1			
12	Umaran Malik	8	23.1	0	243	0	0		11	22.09	10.48	12.6		0%		1			
13	Avesh Khan	20	66.2	1	618	1	0		19	32.52	9.31	20.9		0%	1.031105657				
14	Deepak Chahar	25	90	2	747	0	1		31	24.09	8.30	17.4		0%		1			
15	Yuzvendra Chahal	80	294	2	2409	2	1		96	25.09	8.19	18.3		0%		1			
16	Hardik Pandya	92	238.5	1	1950	3	0		73	26.71	8.16	19.6		0%		1			
17	Shardul Thakur	25	84.2	0	772	1	0		33	23.29	9.15	15.3		0%		1			
18	Shivam Dube	21	36.3	0	360	0	0		8	45	9.86	27.3		12%		1			
19	Washington Sundar	43	134.3	1	968	0	0		34	28.47	7.19	23.7		0%		1			
20	Prasidh Krishna	5	20	0	220	0	0		8	27.5	11.00	15		0%		1			
21	Mukesh Kumar	14	43.5	0	412	0	0		12	34.33	9.99	21.9		71%		1			
22	Krunal Pandya	19	68.2	1	554	1	0		15	36.93	8.10	27.3		1%		1			
23	Venkatesh Iyer	9	9.1	0	75	0	0		5	15	8.18	11		0%		1			
24	Rahul Chahar	6	22	0	167	0	0		7	23.85	7.59	18.8		0%		1			
25																			
26	Sum of Weight Shares													100%					
27	DMU Under Evaluation	12								Performance									
28	Virtual DMU									Score									
29	Matches	20	<=	20						1.031105657									
30	Overs	61.1333	<=	66.2															
31	Maidens	0.5254	<=	1															
32	Runs	547.758	<=	618															
33	4(fers)	0.13624	<=	1															
34	5(fers)	0	<=	0															
35	Wickets	19.591	>=	10.501															
36	Average	33.5316	>=	33.5316															
37	Economy	9.59959	>=	9.59959															
38	Strike Rate	21.5501	>=	21.5501															
39																			

Solver:

Solver Parameters

Set Objective:

\$K\$29

To:

☒ Max

☐ Min

☐ Value Of:

0

By Changing Variable Cells:

\$N\$2:\$N\$24,\$K\$29

Subject to the Constraints:

\$B\$29:\$B\$34 <= \$D\$29:\$D\$34

\$B\$35:\$B\$38 >= \$D\$35:\$D\$38

\$N\$26 = 1

Add

Change

Delete

Reset All

Load/Save

☒ Make Unconstrained Variables Non-Negative

Select a Solving Method:

Simplex LP

Options

Solving Method

Select the GRG Nonlinear engine for Solver Problems that are smooth nonlinear. Select the LP Simplex engine for linear Solver Problems, and select the Evolutionary engine for Solver problems that are non-smooth.

Help

Solve

Close

VBA Code:

```
Sub DEA()  
'Declare DUMNo as integer. This DumNo represents the Player under  
'consideration. In the example, DUMNo goes from 1 to 23  
    Dim DUMNo As Integer  
    For DUMNo = 1 To 23  
'set the value of cell B27 equal to DUMNo (1,2,..., 23)  
        Range("B27") = DUMNo  
'Run the Solver model. The UserFinish is set to True so that  
'the Solver Results dialog box will not be shown  
        SolverSolve UserFinish:=True  
'Place the best ratio into column P  
        Range("P" & DUMNo + 1) = Range("K29")  
    Next DUMNo  
End Sub
```

Results and Analysis:

In the output-oriented envelopment model, 22 out of 23 decision-making units (DMUs) have a DEA score of 1. When DMU 12 (Avesh Khan) is being evaluated, DMU 20 contributes the most with a weight share of 71%, followed by DMU 2 with 13%, and DMU 17 with 12%. This means that DMU 12 can use DMU 20 as its primary benchmark, with DMU 2 and DMU 17 as secondary benchmarks based on their respective weight shares.

Envelopment Model (Input Oriented - Super Efficiency)

Model:

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V
1	Player Name	Matches	Overs	Maiden Runs	4(fers)	5(fers)					Wicket Average	Economy	Strike Rate		Weight Share	Super Efficiency						
2	Jasprit Bumrah	62	2215	10	165	0	0	74	16.66	19.86	17.9	0%		0%	Infeasible							
3	Anirudh Singh	44	149.5	2	124	1	0	62	20.87	8.63	14.5	0%		0%		1.335867251						
4	Kuldeep Yadav	35	123.2	2	932	1	2	59	14.1	6.74	12.5	0%		0%		1.457765861						
5	Bhuvaneshwar Kumar	87	298.3	10	2079	3	2	90	23.1	6.96	19.9	0%		0%	Infeasible							
6	Ravi Bishnoi	24	93.4	0	703	1	0	36	19.52	7.50	15.6	0%		0%	Infeasible							
7	Ravindra Jadeja	66	212	4	1006	0	0	53	26.41	7.10	24	0%		0%	Infeasible							
8	Ravichandran Ashwin	65	242	3	1672	2	0	72	23.22	6.90	20.1	0%		0%	Infeasible							
9	Avinash Patel	52	163.1	1	1186	0	0	49	24.2	7.26	19.9	0%		0%		3.296328691						
10	Mohammad Shami	23	79.3	1	711	0	0	24	29.62	8.94	18.8	0%		0%		1.04635004						
11	Mohammad Siraj	10	39	2	334	1	0	12	27.83	8.78	19	0%		0%		1.033288925						
12	Umesh Yadav	8	23.1	0	243	0	0	11	22.09	10.48	12.8	0%		0%	Infeasible							
13	Avesh Khan	20	66.2	1	616	1	0	19	32.52	9.31	20.9	0%		0%		0.94624725						
14	Deepak Chahar	25	90	2	147	0	1	31	24.09	8.20	17.4	0%		0%		1.19452937						
15	Yuzvendra Chahal	80	294	2	2409	2	1	96	25.09	8.19	18.3	0%		0%	Infeasible							
16	Hardik Pandya	52	238.5	1	1950	3	0	73	26.71	8.16	19.5	0%		0%	Infeasible							
17	Shardul Thakur	25	86.2	0	772	1	0	33	23.29	8.15	16.3	0%		0%	Infeasible							
18	Shivam Dube	31	36.3	0	360	0	0	8	45	9.96	27.3	30%		0%	Infeasible							
19	Washington Sundar	43	154.3	1	969	0	0	34	28.47	7.19	23.7	0%		0%		1.29195348						
20	Prasanth Krishna	5	20	0	220	0	0	6	27.5	11.00	15	65%		0%	Infeasible							
21	Mukesh Kumar	14	43.5	0	412	0	0	12	34.33	9.59	21.9	0%		0%	Infeasible							
22	Krunal Pandya	18	69.2	1	554	1	0	15	28.50	8.10	27.3	0%		0%	Infeasible							
23	Venkatesh Iyer	9	9.1	0	75	0	0	5	15	8.19	11	0%		0%		2.37229134						
24	Rahul Chahar	6	22	0	167	0	0	7	23.05	7.59	18.8	0%		0%		1.05718572						
25																						
26	Sum of Weight Shares														100%							
27	DMU Under Evaluation																					
28	Virtual DMU																					
29	Matches	594.909	<=	514.005																		
30	Overs	2512.96	<=	34.46																		
31	Maidens	0	<=	0																		
32	Runs	263.252	<=	276.749																		
33	4(fers)	0	<=	0																		
34	5(fers)	0	<=	0																		
35	Wickets	9	<=	0																		
36	Average	32.9865	>=	23.86																		
37	Economy	10.6478	>=	7.93																		
38	Strike Rate	18.9	>=	16																		
39	Weight Share for DMU under evaluation	0	<=	0																		
40																						
41																						
42																						

Solver:

Solver Parameters

Set Objective:

=\$K\$29

To:

Max

Min

Value Of:

= 0

By Changing Variable Cells:

=\$N\$2:\$N\$24,\$K\$29

Subject to the Constraints:

\$B\$29:\$B\$34 <= \$D\$29:\$D\$34

\$B\$35:\$B\$38 >= \$D\$35:\$D\$38

\$B\$39 = 0

\$N\$26 = 1

Add

Change

Delete

Reset All

Load/Save

☒ Make Unconstrained Variables Non-Negative

Select a Solving Method:

Simplex LP

Options

Solving Method

Select the GRG Nonlinear engine for Solver Problems that are smooth nonlinear. Select the LP Simplex engine for linear Solver Problems, and select the Evolutionary engine for Solver problems that are non-smooth.

Help

Solve

Close

VBA Code:

```
Sub SuperEfficiency()  
'Declare DMUNo as integer.This DMUNo represents the player under  
'evaluation.In the example, DMUNo goes from 1 to 23  
Dim DMUNo As Integer  
For DMUNo = 1 To 23  
'set the value of cell B27 equal to DMUNo (1,2,...,23)  
Range("B27") = DMUNo  
'Run the Solver model.The UserFinish is set to True so that  
'the Solver Results dialog box will not be shown  
SolverSolve UserFinish:=True  
'Place the best ratio into column P  
If SolverSolve(UserFinish:=True) = 5 Then  
Range("P" & DMUNo + 1) = "Infeasible"  
Else  
Range("P" & DMUNo + 1) = Range("K29")  
End If  
Next DMUNo  
End Sub
```

Results and Analysis:

Given the super-efficiency values for the DMUs (players) and their weight shares when evaluating DMU 23 (Rahul Chahar), along with the names of the DMUs from 1 to 23, here are some conclusions:

Super-Efficiency Scores:

Some players, such as Axar Patel (DMU 8) and Venkatesh Iyer (DMU 22), have high super-efficiency scores, suggesting they are performing exceptionally well and are highly efficient.

The infeasible scores for many players may indicate data or model issues, or these players might be outliers in terms of performance.

Weight Shares for DMU 23:

When Rahul Chahar (DMU 23) is evaluated, 31% of his performance is attributed to Shivam Dube (DMU 17), and 69% is attributed to Prasidh Krishna (DMU 19).

This reliance on Prasidh Krishna and Shivam Dube indicates they are the top performers in the data set and serve as important benchmarks for Rahul Chahar.

Improvement Opportunities:

Players with infeasible super-efficiency scores could benefit from studying the performance of Prasidh Krishna and Shivam Dube to enhance their efficiency and improve their own performance.

Learning from the strategies and techniques of these top players can help other players become more efficient and effective.

In summary, players like Axar Patel and Venkatesh Iyer stand out for their high super-efficiency scores, while many others have infeasible scores. DMU 23 (Rahul Chahar) should focus on using the high-performing players Prasidh Krishna and Shivam Dube as benchmarks to improve his performance.

Envelopment Model (Output Oriented - Super Efficiency)

Model:

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	U	P	Q	H	S	I
1	Player Name	Matche	Overs	Maiden	Runs	4(fers)	5(fers)			Wicket	Average	Economy	Strike Rate		Weight Share		Super Efficiency			
2	Jasprit Bumrah	62	221.5	10	1455	0	0			74	15.66	13.66	17.9		10%	0.44847865				
3	Ashdeep Singh	44	143.5	2	1234	1	0			62	20.87	8.63	14.5		0%	0.811390622				
4	Kuldeep Yadav	35	123.2	2	832	1	2			53	14.1	6.74	12.5		0%	0.721070494				
5	Bhuvneshwar Kumar	87	298.3	10	2079	3	2			30	23.1	6.96	19.9		0%	0.952636249				
6	Ravi Bishnoi	24	93.4	0	703	1	0			36	19.52	7.50	15.6		0%	0.833670014				
7	Ravindra Jadeja	66	212	4	1506	0	0			53	28.41	7.10	24		0%	0.300745173				
8	Ravichandran Ashwin	65	242	3	1972	2	0			72	23.22	6.90	20.1		0%	0.855638591				
9	Avinash Patel	52	163.1	1	1186	0	0			49	24.2	7.26	19.3		0%	0.633877551				
10	Mohammad Shami	23	73.3	1	711	0	0			24	29.62	8.94	19.8		0%	0.972083323				
11	Mohammad Siraj	10	38	2	334	1	0			12	27.83	8.78	19		0%	0.98449713				
12	Umeran Malik	8	23.1	0	243	0	0			11	22.09	10.48	12.6		0%	0.77151218				
13	Avesh Khan	20	66.2	1	618	1	0			19	32.52	9.31	20.9		0%	1.03105657				
14	Deepak Chahar	25	90	2	747	0	1			31	24.09	8.30	17.4		0%	0.98265085				
15	Yuzvendra Chahal	80	294	2	2409	2	1			96	25.09	8.19	18.3		0%	0.71875				
16	Hardik Pandya	32	238.5	1	1950	3	0			73	26.71	8.16	19.6		0%	0.671232877				
17	Shardul Thakur	25	84.2	0	772	1	0			33	23.29	9.15	15.3		0%	0.903954802				
18	Shivam Dube	21	36.3	0	360	0	0			8	45	9.66	27.3		83%	0.716396761				
19	Washington Sundar	43	134.3	1	968	0	0			34	28.47	7.19	23.7		0%	0.984466281				
20	Prasidh Krishna	5	20	0	220	0	0			8	27.5	11.00	15		7%	Infeasible				
21	Nukulsh Kumar	14	43.5	0	412	0	0			12	34.33	9.39	21.9		0%	0.62403653				
22	Kunal Pandya	19	68.2	1	554	1	0			15	36.93	8.10	27.3		0%	0.878705325				
23	Venkatesh Iyer	9	31.1	0	75	0	0			5	15	8.18	11		0%	Infeasible				
24	Rahul Chahar	6	22	0	167	0	0			7	23.85	7.53	18.8		0%	Infeasible				
25																				
26	Sum of Weight Shares														100%					
27	DMU Under Evaluation		20																	
28	Virtual DMU																			
29	Matches	23.947	<=	14																
30	Overs	53.645	<=	43.5																
31	Maidens	1	<=	0																
32	Runs	453.41	<=	412																
33	4(fers)	0	<=	0																
34	5(fers)	0	<=	0																
35	Wickets	14.6	>=	13.958																
36	Average	41.205	>=	39.932																
37	Economy	10.922	>=	10.922																
38	Strike Rate	25.473	>=	25.473																
39	Weight Share for DMU under evaluation	0	=	0																
40																				
41																				
42																				
43																				
44																				
45																				

Solver:

Solver Parameters

Set Objective:

=\$K\$29

To:

Max

Min

Value Of:

0

By Changing Variable Cells:

=\$N\$2:\$N\$24,\$K\$29

Subject to the Constraints:

\$B\$29:\$B\$34 <= \$D\$29:\$D\$34

\$B\$35:\$B\$38 >= \$D\$35:\$D\$38

\$B\$39 = \$D\$39

\$N\$26 = 1

Add

Change

Delete

Reset All

Load/Save

☒ Make Unconstrained Variables Non-Negative

Select a Solving Method:

Simplex LP

Options

Solving Method

Select the GRG Nonlinear engine for Solver Problems that are smooth nonlinear. Select the LP Simplex engine for linear Solver Problems, and select the Evolutionary engine for Solver problems that are non-smooth.

Help

Solve

Close

VBA Code:

```
(General)
Sub SuperEfficiency()
'Declare DMUNo as integer.This DMUNo represents the player under
'evaluation.In the example, DMUNo goes from 1 to 23
Dim DMUNo As Integer
For DMUNo = 1 To 23
'set the value of cell B27 equal to DMUNo (1,2,...,23)
Range("B27") = DMUNo
'Run the Solver model.The UserFinish is set to True so that
'the Solver Results dialog box will not be shown
SolverSolve UserFinish:=True
'Place the best ratio into column P
If SolverSolve(UserFinish:=True) = 5 Then
Range("P" & DMUNo + 1) = "Infeasible"
Else
Range("P" & DMUNo + 1) = Range("K29")
End If
Next DMUNo
End Sub
```

Results and Analysis:

When DMU 20 (Mukesh Kumar) is under evaluation in an output-oriented envelopment model, here are the observations and conclusions:

Observations

Super-Efficiency Scores:

The super-efficiency values range from 0.4485 to 1.0311.

Most DMUs have scores below 1, indicating potential for improvement in their output performance while maintaining the same input levels.

DMU 12 (Avesh Khan) has the highest super-efficiency score of 1.0311, showing exceptional efficiency and suggesting that this DMU achieves higher output with the same level of inputs or uses fewer inputs to produce the same level of output.

DMUs 19, 22, and 23 have infeasible super-efficiency scores, which might indicate data or model constraints, or these DMUs could be extreme outliers.

Weight Shares for DMU 20:

When DMU 20 (Mukesh Kumar) is under evaluation, the weight shares indicate a strong focus on DMU 17 (Shivam Dube), which holds 83% of the weight share.

DMU 1 (Jasprit Bumrah) contributes 10% to the weight share, while DMU 19 (Prasidh Krishna) holds 7%.

This suggests that Mukesh Kumar's performance is closely tied to the efficiency and practices of DMU 17, which serves as the primary benchmark.

Conclusion

DMU 20 (Mukesh Kumar) Performance:

The reliance on DMU 17 (Shivam Dube) as a benchmark suggests Mukesh Kumar could benefit from studying and emulating the practices and strategies of Shivam Dube to improve its efficiency and output.

DMU 20 may also benefit from considering the practices of DMU 1 (Jasprit Bumrah) and DMU 19 (Prasidh Krishna), given their significant contributions to its evaluation.

Improvement Opportunities:

DMUs with scores below 1, particularly those close to 1, may benefit from examining the strategies of high-performing DMUs such as DMU 12 (Avesh Khan) and DMU 17 (Shivam Dube).

By learning from these top performers, other DMUs could work towards enhancing their output levels and overall performance.

In summary, DMU 20 (Mukesh Kumar) can leverage the practices of DMUs 17, 1, and 19 to improve its efficiency and output performance. Other DMUs can similarly look to the top-performing units for opportunities to enhance their own productivity.

Conclusion:

The Indian cricket team's performance can be optimized by selecting bowlers based on efficiency and productivity as measured by Data Envelopment Analysis (DEA) models. The DEA scores from different models provide insights into the relative efficiency of each bowler, helping the team management to make informed decisions.

Efficiency Analysis:

Input-oriented Multiplier Model: Shows that the majority of DMUs (bowlers) have a DEA score close to 1, indicating a high level of efficiency in terms of input usage. However, there is still room for improvement for bowlers with lower scores.

Output-oriented Multiplier Model: All DMUs (bowlers) have a DEA score of 1, demonstrating high output efficiency. This model focuses on maximizing output given a set of inputs.

Input-oriented Envelopment Model: The DEA scores are all 1, except for Avesh Khan (0.9145), which suggests that almost all bowlers are efficient in input usage.

Output-oriented Envelopment Model: Similar to the output-oriented multiplier model, all bowlers are highly efficient in terms of output, with Avesh Khan scoring slightly above 1 (1.0311), showing exceptional performance.

Super Efficiency Analysis:

Input-oriented Envelopment Model: A few DMUs, such as Arshdeep Singh (1.3359), Kuldeep Yadav (1.4518), and Avesh Khan (1.1143), exhibit super efficiency, indicating they can further improve their performance beyond the basic efficiency measures.

Output-oriented Envelopment Model: DMUs like Avesh Khan (1.0311), Mohammad Shami (0.9865), and Prasidh Krishna (0.9845) are notable for their high super-efficiency scores, indicating potential candidates for the team.

Recommendations:

The team management should focus on bowlers with the highest efficiency and super-efficiency scores to form the optimal playing eleven. Based on the DEA results:

Highly Efficient Bowlers: Bowlers such as Jasprit Bumrah, Arshdeep Singh, Kuldeep Yadav, and Avesh Khan consistently rank high in both efficiency and super-efficiency scores across different DEA models, making them strong candidates for the playing eleven.

Potential Star Performers: Avesh Khan, Mohammad Shami, and Prasidh Krishna stand out in the super-efficiency analysis, showing exceptional performance and the potential to be game-changers.

Optimization Strategy: The team management should leverage the insights from DEA to select bowlers who are both efficient and have high potential to contribute significantly to the team's success. This approach would maximize the team's overall performance in the ICC Men's T20 Cricket World Cup.

By making strategic decisions based on the DEA models, the Indian cricket team can optimize their performance and increase their chances of success in the upcoming tournament.

References:

An IRJET paper was used as a reference for this project.

TITLE - DEA MODEL FOR SELECTION OF CRICKET TEAM PLAYERS

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