

# JMcDM: A Julia package for multiple-criteria decision making tools

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## Abstract

Ca. 100 words

*Keywords:* keyword 1, keyword 2, keyword 3

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## Required Metadata

### Current code version

Ancillary data table required for subversion of the codebase. Kindly replace examples in right column with the correct information about your current code, and leave the left column as it is.

Nr.	Code metadata description	Please fill in this column
C1	Current code version	v0.1.5
C2	Permanent link to code/repository used for this code version	<a href="https://github.com/jbytecode/JMcDM">https://github.com/jbytecode/JMcDM</a>
C3	Code Ocean compute capsule	
C4	Legal Code License	MIT
C5	Code versioning system used	git
C6	Software code languages, tools, and services used	Julia
C7	Compilation requirements, operating environments & dependencies	Julia 1.4
C8	If available Link to developer documentation/manual	<a href="https://jbytecode.github.io/JMcDM/docs/build">https://jbytecode.github.io/JMcDM/docs/build</a>
C9	Support email for questions	mhsatman@istanbul.edu.tr

Table 1: Code metadata (mandatory)

## 1. Motivation and significance

Introduce the scientific background and the motivation for developing the software. Explain why the software is important, and describe the exact (scientific) problem(s) it Indicates in what way the software has contributed (or how it will contribute in the future) to Provide a description of the experimental setting (how does the user use the software?). Introduce related work in literature (cite or list algorithms used, other software etc.).

The one-dimensional array  $a$  is in ascending order if and only if  $a_i \leq a_{i+1}$

where  $i = 1, 2, \dots, n - 1$ , and  $n$  is the length of array. In other terms, the process of ordering numbers requires the logical  $\leq$  operator to be perfectly defined. Since the operator  $\leq$  is not defined for any set of points in higher dimensions,  $\mathbb{R}^p$  for  $p \geq 2$ , there is not a unique ordering of points.

In multi-dimensional case, the binary domination operator  $\succ$  applied on points  $a$  and  $b$ ,  $a \succ b$ , is true iif each item in  $a$  is not worse than the corresponding item in  $b$  and at least one item is better than the corresponding item in  $b$  (1). On the other hand, the more relaxed operator  $\succeq$  returns true if each item in  $a$  is as good as the corresponding item in  $b$  (2). Several outranking methods in MCDA (Multiple-Criteria Decision Analysis) define a unique ranking mechanism to select the best alternative among others.

Suppose a decision process has  $n$  alternatives and  $m$  criteria which are either to be maximized or minimized. Each single criterion has a weight  $0 \leq w_i \leq 1$  where  $\sum_i^m w_i = 1$ .  $f_i$  is either maximum or minimum.  $g_j(\cdot)$  is evolution function and it is taken as  $g_j(x) = x$  in many methods. A multiple criteria decision problem can be represented using the decision table

Criteria	$C_1$	$C_2$	$\dots$	$C_m$
Weights	$w_1$	$w_2$	$\dots$	$w_m$
Functions	$f_1$	$f_2$	$\dots$	$f_m$
$A_1$	$g_1(A_1)$	$g_2(A_1)$	$\dots$	$g_m(S_A)$
$A_2$	$g_1(A_2)$	$g_2(A_2)$	$\dots$	$g_m(A_2)$
$\vdots$	$\vdots$	$\vdots$	$\ddots$	$\vdots$
$A_n$	$g_1(A_n)$	$g_2(A_n)$	$\dots$	$g_m(A_n)$

Table 2: Sample decision matrix

without loss of generality. When  $A_1, A_2, \dots, A_n$  are alternatives and  $C_1, C_2, \dots, C_m$  are different situations of a single criterion then the decision problem is said to be single criterion decision problem. If  $A_i$  and  $C_j$  are strategies of two game players then  $g_j(A_i)$  is the gain of the row player when she selects the strategy  $i$  and the column player selects the strategy  $C_j$ .

We must put here some text here like: MCDA is used in location selection of facilities (Ref), selection of suppliers (Ref).... .

Multiple-criteria decision-making (MCDM) tools provide several algorithms for ordering or selecting alternatives and/or determining the weights when there is uncertainty. Although some algorithms are suitable for hand calculations, a computer software is often required. *PyTOPS* is a Python tool for TOPSIS (3). *Super Decisions* is a software package which is mainly focused on AHP (Analytic Hierarchy Process) and ANP (Analytic Network Process) (4). *Visual Promethee* implements Promethee method on Windows platforms (5). *M-BACBETH* is an other commercial software product that implements MACBETH with a easy to use GUI. (6). *Sanna* is a standard MS Excel add-in application that supports several basic methods for multi-criteria evaluation of alternatives (WSA, TOPSIS, ELECTRE I and III, PROMETHEE I and II, MAPPAC and ORESTE) (7). *DEA Frontier* software requires Excel add-in that can solve up to 50 DMUs with unlimited number of inputs and outputs (subject to the capacity of the standard MS Excel Solver) (8).

*JMcDM* is designed to provide a developer-friendly library for solving multiple-criteria decision problems in Julia (9). Since Julia is a dynamic language, it is also useful for researchers that familiar with REPL environments.

50 The package includes multi-criteria decision methods as well as a game solver  
51 for zero-sum games and methods for single criterion methods.

## 52 **2. Software description**

### 53 *2.1. Software Architecture*

54 Give a short overview of the overall software architecture; provide a pic-  
55 torial component overview or similar (if possible). If necessary provide im-  
56 plementation details.

57 *JMcDM* provides a framework for performing multi-criteria decision anal-  
58 ysis as well as it includes utility functions for development of new methods.  
59 Each single MCDM method returns an object in subtype of `MCDMResult`  
60 which is defined as

```
61 abstract type MCDMResult end
```

62 and it is used to derive new return types. For instance, the `topsis()` function  
63 always returns a `TopsisResult` object which is defined as

```
64 struct TopsisResult <: MCDMResult
65     decisionMatrix::DataFrame
66     weights::Array{Float64,1}
67     normalizedDecisionMatrix::DataFrame
68     normalizedWeightedDecisionMatrix::DataFrame
69     bestIndex::Int64
70     scores::Array{Float64,1}
71 end
```

72 and holds many outputs in a single `struct`. Function definitions are also  
73 similar but they may differ depending on the requirements of algorithms.  
74 For instance the function `topsis` is defined as

```
75 function topsis(  
76     decisionMat::DataFrame,  
77     weights::Array{Float64,1},  
78     fns::Array{Function,1})::TopsisResult
```

79 where `decisionMat` is the decision matrix, `weights` are weights of criteria,  
80 and `fns` is an array of functions (either `minimum` or `maximum`) that determine  
81 the optimization directions.

82 The package is registered in Julia package repository and it is available  
83 for downloading and installing using Julia's package manager.

```
84 julia> using Pkg  
85 julia> Pkg.add("JMcDM")
```

86 and

```
87 julia> ]  
88 (@v1.5) pkg> add JMcDM
```

89 present two distinct ways of install the package.

## 90 *2.2. Software Functionalities*

91 **Present the major functionalities of the software.**

92 The package implements methods for TOPSIS (Technique for Order Pref-  
93 erence by Similarity to Ideal Solutions)(10), ELECTRE (Elimination and

94 Choice Translating Reality)(11), PROMETHEE (Preference Ranking Or-  
 95 ganization METHod for Enrichment of Evaluations)(12), DEMATEL (The  
 96 Decision Making Trial and Evaluation Laboratory)(13), MOORA (Multi-  
 97 Objective Optimization By Ratio Analysis)(14), VIKOR (Vlsekriterijumska  
 98 Optimizacija I Kompromisno Resenje in Serbian)(15; 16), AHP (Analytic  
 99 Hierarchy Process)(17), GRA (Grey Relational Analysis)(18), NDS (Non-  
 100 dominated Sorting)(1), SAW (Simple Additive Weighting)(19; 20), ARAS  
 101 (Additive Ratio Assessment)(21), WPM (Weighted Product Model)(20), WAS-  
 102 PAS (Weighted Aggregated Sum Product ASsessment)(22), EDAS (Evalua-  
 103 tion based on Distance from Average Solution)(23), MARCOS (Measurement  
 104 Alternatives and Ranking according to COMpromise Solution)(24), MABAC  
 105 (Multi-Attributive Border Approximation area Comparison)(25), MAIRCA  
 106 (Multi Attributive Ideal-Real Comparative Analysis)(26), COPRAS (COM-  
 107 plex PROportional ASsessment)(27), COCOSO (Combined Compromise Solution)(28),  
 108 and CRITIC (CRiteria Importance Through Intercriteria Correlation)(29)  
 109 for multiple-criteria tools. The package also performs DEA for Data Envel-  
 110 opment Analysis(30) and includes a method for zero-sum game solver.

### 111 2.3. Sample code snippets analysis

112 Suppose a decision problem is given in Table 3.

Criteria	Age	Size	Price	Distance	Population
Weights	0.35	0.15	0.25	0.20	0.05
Functions	min	max	min	min	max
$A_1$	6	140	150000	950	1500
$A_2$	4	90	100000	1500	2000
$A_3$	12	140	75000	550	1100

Table 3: Decision matrix

113 In this sample problem, a decision maker is subject to select an apartment  
114 by considering age of the building, size (in  $m^2$ s), price (in \$), distance to city  
115 centre, and nearby population. The data can be entered as a two-dimensional  
116 array (matrix) or as a DataFrame object:

```

117 julia> using JMCDM, DataFrames
118 julia> df = DataFrame(
119 :age      => [6.0, 4, 12],
120 :size     => [140.0, 90, 140],
121 :price    => [150000.0, 100000, 75000],
122 :distance => [950.0, 1500, 550],
123 :population => [1500.0, 2000, 1100]);
124
125 julia> w = [0.35, 0.15, 0.25, 0.20, 0.05];
126 julia> fns = [minimum, maximum, minimum, minimum, maximum];
127 julia> result = topsis(df, w, fns);
128 julia> result.scores
129 3-element Array{Float64,1}:

```



```
130 0.5854753145549456
131 0.6517997936899308
132 0.41850223305822903
133
134 julia> result.bestIndex
135 2
```

136 In the output above it is shown that the alternative  $A_2$  has a score of  
137 0.65179 and it is selected as the best. The same analysis can be performed  
138 using `saw()` for the method of Simple Additive Weighting

```
139 julia> result = saw(df, w, fns);
140 julia> result.bestIndex
141 2
```

142 as well as using `wpm` for the method of Weighted Product Method

```
143 julia> result = wpm(df, w, fns);
144 julia> result.bestIndex
145 2
```

146 For any method, `?methodname` shows the documentation as in the same  
147 way in other Julia packages.

### 148 3. Illustrative Examples

149 Provide at least one illustrative example to demonstrate the major func-  
150 tions.

```
julia> result1
```

3x7 DataFrame

Row	topsis	electre	cocoso	moora	vikor	wpm	waspas
	String	String	String	String	String	String	String
1			✓	✓	✓		
2	✓	✓				✓	✓
3		✓					

Figure 1: Results of TOPSIS, ELECTRE, VIKOR, MOORA, COCOSO, WPM, and WASPAS

151 Since *JMcDM* is designed as a software library and for REPL use, it does  
 152 not implement a significant user interface. However, the `summary()` function  
 153 provides a useful way to perform a list of methods and returns a text based  
 154 result to compare results.

```
155 julia> methods1 = [:topsis, :electre, :vikor,  
156 :moora, :cocoso, :wpm, :waspas]  
157 julia> result1 = summary(df, w, fns, methods1);
```

158 Figure 1 represents the output of the `summary()` call for methods TOP-  
 159 SIS, ELECTRE, VIKOR, MOORA, COCOSO, WPM, and WASPAS, re-  
 160 spectively.

```
161 julia> methods2 = [:aras, :saw, :edas, :marcos,  
162 :mabac, :mairca, :grey];  
163 julia> result2 = summary(df, w, fns, methods2);
```

164 Figure 2 represents the output of the `summary()` call for methods ARAS,  
 165 SAW, EDAS, MARCOS, MABAC, MAIRCA, and GREY, respectively.

```
[julia> result2
```

3x7 DataFrame

Row	grey	aras	saw	edas	marcos	mabac	mairca
	String	String	String	String	String	String	String
1							
2		✓	✓	✓	✓		
3	✓					✓	✓

Figure 2: Results of ARAS, SAW, EDAS, MARCOS, MABAC, MAIRCA, and GREY

#### 166 4. Impact

167 **This is the main section of the article and the reviewers weight**  
 168 **the description here appropriately** Indicate in what way new research  
 169 questions can be pursued as a result of the software (if any). Indicate in  
 170 what way, and to what extent, the pursuit of existing research questions is  
 171 improved (if so). Indicate in what way the software has changed the daily  
 172 practice of its users (if so). Indicate how widespread the use of the software  
 173 is within and outside the intended user group. Indicate in what way the  
 174 software is used in commercial settings and/or how it led to the creation of  
 175 spin-off companies (if so).

176 *JMcDM* provides a moderate number of MCDA tools and utility func-  
 177 tions for developing new methods as well as performing decision analysis  
 178 using a single function call for each method. A researcher can easily perform  
 179 sequential analysis by changing the problem parameters and can compare  
 180 results of many tools. Existing software packages are mainly focused on pro-  
 181 viding a small subset of methods. *JMcDM* is an all-in-one solution and has  
 182 potential for increasing user productivity. Seeing the different results pro-

183 duced by the methods together also helps to discover which parameters the  
184 research is more sensitive to and the reasons for them.

## 185 5. Conclusions

186 Set out the conclusion of this original software publication.

## 187 6. Conflict of Interest

188 We wish to confirm that there are no known conflicts of interest associated  
189 with this publication and there has been no significant financial support for  
190 this work that could have influenced its outcome.

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194 Journal.

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### 310 **Current executable software version**

311 Ancillary data table required for sub version of the executable software:  
 312 (x.1, x.2 etc.) kindly replace examples in right column with the correct  
 313 information about your executables, and leave the left column as it is.

Nr.	(Executable) software meta-data description	Please fill in this column
S1	Current software version	For example 1.1, 2.4 etc.
S2	Permanent link to executables of this version	For example: <i>https</i> : <i>//github.com/combogenomics/DuctApe/releases/tag/DuctApe-0.16.4</i>
S3	Legal Software License	List one of the approved licenses
S4	Computing platforms/Operating Systems	For example Android, BSD, iOS, Linux, OS X, Microsoft Windows, Unix-like , IBM z/OS, distributed/web based etc.
S5	Installation requirements & dependencies	
S6	If available, link to user manual - if formally published include a reference to the publication in the reference list	For example: <i>http</i> : <i>//mozart.github.io/documentation/</i>
S7	Support email for questions	

Table 4: Software metadata (optional)