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function [t_vals, x_vals, y_vals, X, delta_xy, delta_t] = general_heat_2D(t_iter, x_iter, y_iter, alpha)

    t_0 = 0;
    t_f = 8;
    t_vals = linspace(t_0, t_f, t_iter);

    L = 4;
    H = 4;
    X = zeros(x_iter, y_iter, t_iter);
    x_0 = @(x, y) double(y >= x);
    x_vals = linspace(0, L, x_iter);
    y_vals = linspace(0, H, y_iter);
    for i = 1:length(x_vals)
        for j = 1:length(y_vals)
            X(i, j, 1) = x_0(x_vals(i), y_vals(j));
        end
    end

    X(1, :, 1) = X(2, :, 1);
    X(end, :, :) = 0;
    X(:, 1, 1) = X(:, 2, 1);
    for x_num = 1:x_iter
        X(x_num, end, :) = exp(-t_vals);
    end

    delta_t = t_vals(2) - t_vals(1);
    delta_xy = x_vals(2) - x_vals(1);

    if delta_t > 0.25*delta_xy^2/alpha
        fprintf('Upper Bound: %g\n', 0.25*delta_xy^2/alpha)
        fprintf('Delta t: %g\n', delta_t)
        disp("Unstable, increase t_iter or decrease x_iter")
        return
    end

    for i = 2:t_iter
        X(2:x_iter-1, 2:x_iter-1, i) = alpha*delta_t/delta_xy^2*...
            (X(3:x_iter, 2:x_iter-1, i-1) + X(1:x_iter-2, 2:x_iter-1, i-1) + ...
            X(2:x_iter-1, 3:x_iter, i-1) + X(2:x_iter-1, 1:x_iter-2, i-1) - 4*X(2:
x_iter-1, 2:x_iter-1, i-1)) + ...
            (exp(-t_vals(i))*delta_t + 1)*X(2:x_iter-1, 2:x_iter-1, i-1);
        X(1, :, i) = X(2, :, i);
        X(:, 1, i) = X(:, 2, i);
    end

    str = "";
    if t_iter >= 1000
        str = "Caution: At current number of iterations, animation may take a long

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time. ";
end
decide = input(str + "Press enter to exit. Type 1 for Finite Difference
Animation", "s");
switch decide
    case "1"
        animation_speed = 0.0;

        % Create meshgrid for surface plot
        [X_grid, Y_grid] = meshgrid(x_vals, y_vals); % Assuming x and y are 1D
vectors

        figure;
        hold on
        h = surf(X_grid, Y_grid, X(:,:,1), "FaceAlpha", 0.25, 'FaceColor', 'b');
        xlabel('x');
        ylabel('y');
        zlabel('Temperature');
        title('2D Heat Equation Solution');
        % Fix z-axis limits to avoid recalculating each frame
        zlim([min(X(:)), max(X(:))]);
        view(3);

        % Improve rendering performance by reducing overhead
        set(gcf, 'Renderer', 'painters');

        for timestep = 1:size(X,3)
            set(h, 'ZData', X(:,:,timestep));
            title(sprintf('Temperature Distribution at Time Step: %d',
timestep));
            drawnow limitrate;
            pause(animation_speed);
        end
    case isempty(decide)
        return
end

end
```