Chain Rule Practice Problems

Connor Lincycomb

Chain Rule Practice Problems

Differentiate each of the following functions with respect to x using the chain rule:

1.
$$f(x) = (2x+1)^2$$

2.
$$f(x) = \sqrt{9x^4 + 3}$$

3.
$$f(x) = (5x^2 + x - 6)^3$$

4.
$$f(x) = \sin(5x^3)$$

5.
$$f(x) = \tan(3x - 2)$$

6.
$$f(x) = 2\csc(\sqrt{x})$$

$$7. \ f(x) = e^{3x}$$

8.
$$f(x) = 2e^{7x-5}$$

9.
$$f(x) = -5e^{\sin(x)}$$

10.
$$f(x) = e^{-\cot(5x^2+4)}$$

11.
$$f(x) = \ln(3x^2)$$

$$12. \ f(x) = \ln(\cos(2x))$$

13.
$$f(x) = -\ln(7x^6 - 3x + 2)$$

14.
$$f(x) = \sin^2(e^{3x} + 2)$$

15.
$$f(x) = e^{\frac{3x(1-x^2)}{2}}$$

Solutions

1.
$$f'(x) = 8x + 4$$

2.
$$f'(x) = \frac{18x^3}{\sqrt{9x^4 + 3}}$$

3.
$$f'(x) = (30x + 3)(5x^2 + x - 6)^2$$

4.
$$f'(x) = 15x^2 \cos(5x^3)$$

5.
$$f'(x) = 3\sec^2(3x - 2)$$

6.
$$f'(x) = -\frac{\csc(\sqrt{x})\cot(\sqrt{x})}{\sqrt{x}}$$

7.
$$f'(x) = 3e^{3x}$$

8.
$$f'(x) = 14e^{7x-5}$$

9.
$$f'(x) = -5e^{\sin(x)}\cos(x)$$

10.
$$f'(x) = e^{-\cot(5x^2+4)} \cdot 10x \csc^2(5x^2+4)$$

11.
$$f'(x) = \frac{2}{x}$$

12.
$$f'(x) = -2\tan(2x)$$

13.
$$f'(x) = \frac{-42x^5 + 3}{7x^6 - 3x + 2}$$

14.
$$f'(x) = 6e^{3x}\sin(e^{3x} + 2)\cos(e^{3x} + 2)$$

15.
$$f'(x) = \frac{3 - 9x^2}{2} \cdot e^{\frac{3x(1 - x^2)}{2}}$$