MHT Simulation

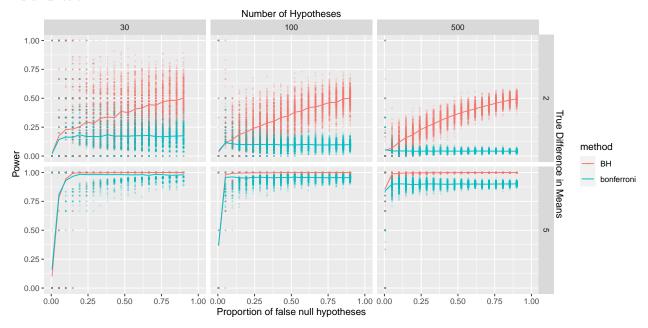
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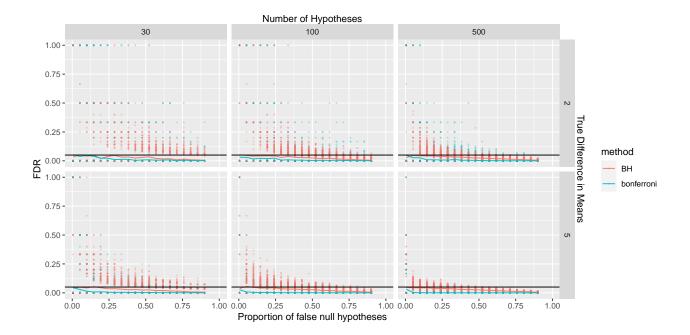
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Simulation study:

- 1) Take 100 samples from N(0,1) and N(5,1) mixed with proportion p in (0,1). Take $\alpha=0.05$. $X_i=(1-p)*N(0,1)+p*N(3,1)$
- 2) Find p values of X
- 3) Use BH, etc
- 4) Get FDP and Power
- 5) Repeat many times to find FDR and avg power across values of p

As a function:





Code:

```
knitr::opts_chunk$set(echo = F, fig.width = 10, fig.height = 5,
                      cache = TRUE, warning = F)
library(tidyverse)
p = 0.4
a = 0.05
num_samples = 100
# True if true mean =/= 0
A = rbernoulli(num_samples, p)
t_nulls = rnorm(num_samples, 0, 1)
f_nulls = rnorm(num_samples, 2, 1)
samples = ifelse(A, f_nulls, t_nulls)
p_vals = pnorm(samples, lower.tail = F)
# Test discoveries
B = (p_vals \le a)
# FP = A' & B
## False_positive = (A & B)
# FDP = P(A' \& B)/P(B)
FDP = ifelse(is.na(sum(!A & B)/sum(B)), 0, sum(!A & B)/sum(B))
# Power = P(reject Null | Null false) = P(reject & Null false)/P(Null false)
Power = ifelse(is.na(sum(A & B)/sum(A)), 0, sum(A & B)/sum(A))
\# FNR = ?????? :)
# m === number of total hypotheses
func = function(p = 0.4, a = 0.05, m = 1000, alt_hyp = 3, method = "none") {
  # A === True discoveries
  A = rbernoulli(m, p)
  t_nulls = rnorm(m, 0, 1)
  f_nulls = rnorm(m, alt_hyp, 1)
```

```
samples = ifelse(A, f_nulls, t_nulls)
  p_vals = pnorm(samples, lower.tail = F)
  adj_p_vals = p.adjust(p = p_vals, method = method)
  # Test discoveries
  B = (adj_p_vals \le a)
  \# FP = A' \& B
 False positive = ifelse(!A & B, 1, 0)
  \# FDP = P(A' \& B)/P(B)
 FDP = ifelse(is.na(sum(!A & B)/sum(B)), 0, sum(!A & B)/sum(B))
  # Power = P(reject Null | Null false) = P(reject & Null false)/P(Null false)
 Power = ifelse(is.na(sum(A & B)/sum(A)), 0, sum(A & B)/sum(A))
 return(c(FDP, Power))
# New function: do.many, where it just does 'many' and returns averages?
# Calculate FDR and Avg Power
# many = replicate(1000, func(method = "none")) %>% apply(., 1, FUN = mean) %>% print
df = expand_grid(p = rep(seq(0.005, 0.9, length.out = 20), each = 300),
                 method = c("bonferroni", "BH"),
                 alt_hyp = c(2,5),
                 m = c(30, 100, 500))
many = t(mapply(func, p = df$p, method = df$method, alt_hyp = df$alt_hyp, m = df$m)) %>%
  as tibble %>%
 rename(FDR = V1, Power = V2) %>%
 mutate(df)
# do_many = function(num_reps = 1000, p = 0.4, a = 0.05, num_samples = 1000, method = "none") {
  many = replicate(num_reps, func(p = p, a = a, num_samples = num_samples, method = method)) %>%
      apply(., 1, FUN = mean)
#
#
  return(many)
# }
\# df = expand_qrid(p = seq(0.1, 0.9, by = 0.01), method = c("none", "BH"))
# df2 = t(mapply(do_many, p = df$p, method = df$method, num_reps = 100)) %>%
  as tibble %>%
  rename(FDR = V1, Power = V2) %>%
  mutate(df)
# Increased p gives more true discoveries
ggplot(data = many, aes(x = p, y = Power, color = method)) +
  geom_point(size = 0.3, alpha = 0.2) +
  stat_summary(fun = "mean", geom = "line") +
  #ylim(0, 1) +
  facet_grid(alt_hyp ~ m) +
  labs(x = "Proportion of false null hypotheses") +
  scale_y_continuous(sec.axis = sec_axis(~ . , name = "True Difference in Means",
                                         breaks = NULL, labels = NULL), limits = c(0,1)) +
  scale_x_continuous(sec.axis = sec_axis(~ . , name = "Number of Hypotheses",
                                         breaks = NULL, labels = NULL), limits = c(0,1))
```