

geostan: An R package for Bayesian spatial analysis

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Summary

Analyses of data collected across areal units, such as census tracts and states, are now ubiquitous in the social and health sciences. Data sources include surveys (especially large government-backed surveys like the US Census Bureau’s American Community Survey (ACS)), vital statistics systems, and disease registries (particularly cancer registries). These data sources can provide crucial information about population health and socio-economic outcomes, but many standard (non-spatial) statistical methods and workflows are either not applicable to spatial data or they require adjustment (Cressie 2015; Haining and Li 2020).

This paper introduces **geostan**, an R (R Core Team 2021) package for analyzing spatial data using Bayesian inference. **geostan**’s spatial models were built using Stan, a platform for Markov chain Monte Carlo (MCMC) sampling (Gabry, Goodrich, and Lysy 2020; Stan Development Team 2022a, 2022b). The primary focus of the package is areal data for socio-economic and health research. The package provides tools for a complete workflow for spatial regression and disease mapping, and has unique spatial measurement error (ME) models suitable for researchers using ACS estimates as covariates (Donegan, Chun, and Griffith 2021).

Statement of need

The distinguishing characteristic of spatial data is that maps of the data typically contain moderate to strong spatial patterns, or spatial autocorrelation, which typically reduces effective sample size (ESS) and renders many standard statistical methods inappropriate (“Student” [W.S. Gausset] 1914; Clifford, Richardson, and Hémon 1989). In addition, spatial patterns are often of direct interest—for example, disease mapping studies are concerned primarily with understanding how disease or mortality risk vary over space.

A major challenge for spatial analysis is data quality, particularly for researchers using survey-based covariates. A single spatial analysis may use dozens, or even thousands, of error-laden survey estimates. Sampling error in ACS estimates is often substantial in magnitude and socially patterned (Folch et al. 2016; Donegan, Chun, and Griffith 2021), which can have real consequences on communities and service providers (Bazuin and Fraser 2013). Spatial ME models are required to avoid ME biases and unwarranted levels of confidence in results.

Existing R packages with spatial modeling functions include **spatialreg** (R. Bivand and Piras 2015), **INLA** (Rue, Martino, and Chopin 2009), **ngspatial** (Hughes and Cui 2020), **BayesX** (Belitz et al. 2022; Umlauf et al. 2015), **CARBayes** (Lee 2013), and **nimble** (de Valpine et al. 2017). Custom spatial models can be built using **rstan** (Stan Development Team 2022a), **INLA**, and **nimble**, including spatial ME models, but this requires specialized programming and statistical skills.

geostan fills two gaps in this software landscape. First, **geostan** offers spatial ME models that are appropriate for survey-based covariates. Second, **geostan** provides spatial model diagnostic functions that make it easy for users to evaluate model results even if they are unfamiliar with MCMC analysis.

Functionality

geostan provides tools for spatial data visualization, construction of spatial weights matrices, spatial ME models, models for censored count data, and multiple types of spatial statistical models for continuous and

discrete data types. The `shape2mat` function creates spatial weights matrices by first calling the `spdep` package (R. S. Bivand, Pebesma, and Gomez-Rubio 2013) to identify the adjacency structure of the spatial data, and results are returned to the user in sparse matrix format using the `Matrix` package (Bates, Maechler, and Jagan 2022).

`geostan` uses MCMC for inference, which allows users to conduct formal inference on generated quantities of interest. The models are built using the Stan modeling language, a state-of-the-art platform for MCMC sampling (Gabry, Goodrich, and Lysy 2020; Stan Development Team 2022a, 2022b), but users only need to be familiar with the standard R formula interface. Because `geostan` returns `stanfit` objects from `rstan`, it is compatible with the `rstan` ecosystem of packages including `shinystan` for visual summaries of model parameters and MCMC diagnostics (Gabry 2018), `tidybayes` for working with MCMC samples (Kay 2022), and `bridgesampling` for model comparison using Bayes factors (Gronau, Singmann, and Wagenmakers 2020).

Exploratory spatial data analysis (ESDA)

The package provides convenience functions for visualizing spatial patterns and conducting ESDA, including

- Moran scatter plot for visualizing spatial autocorrelation (Chun and Griffith 2013)
- Moran coefficient and Geary Ratio for measuring global spatial autocorrelation (Chun and Griffith 2013)
- Local Moran’s I and local Geary’s C for measuring and visualizing local spatial autocorrelation (Anselin 1995)
- The Approximate Profile Likelihood (APLE) estimator for measuring spatial autocorrelation (Li, Calder, and Cressie 2007)
- Effective sample size (ESS) calculation (D. A. Griffith 2005)

These tools are provided for exploratory analysis, but not for detection of clusters. For this and other reasons, p-values are not provided. Graphics are created with `ggplot2` (Wickham 2016).

`geostan` also provides a convenience function for obtaining a quick visual summary of a variable (see Figure 1). When a fitted model is provided, the `sp_diag` function returns graphical diagnostics for model residuals.

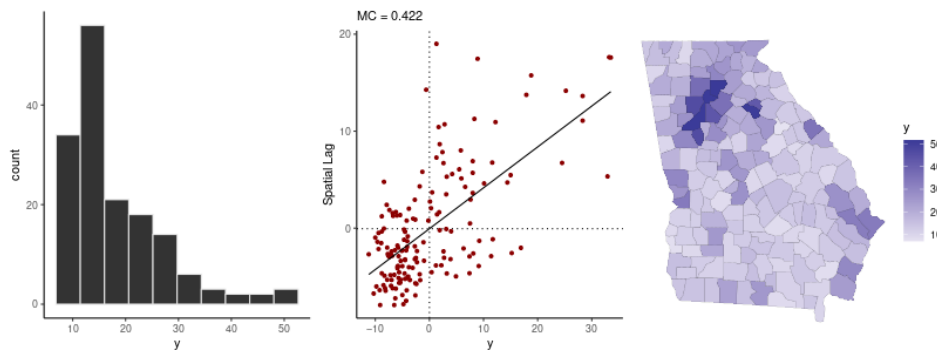


Figure 1: Spatial diagnostic summary for percent college educated, Georgia counties.

Spatial models

Table 1 lists the types of spatial models that are implemented in `geostan`. In addition to (non-spatial) generalized linear models (GLMs), options include spatial conditional autoregressive (CAR) models (Donegan 2021), intrinsic conditional autoregressive (ICAR) models including the BYM (Besag, York, and Mollié 1991) and BYM2 specifications (Riebler et al. 2016; Morris et al. 2019; Donegan and Morris 2021), simultaneously-specified spatial autoregressive (SAR) models (Cliff and Ord 1981) (which are referred to as the spatial error model (SEM) in the econometrics literature (LeSage 2014)), and eigenvector spatial filtering (ESF) (D. Griffith, Chun, and Li 2019; Donegan, Chun, and Hughes 2020).

Table 1: Spatial models currently implemented in **geostan**.

	Gaussian	Student's t	Poisson	Binomial
CAR	x		x	x
ESF	x	x	x	x
GLM	x	x	x	x
ICAR			x	x
SAR	x		x	x

All of the models allow for a set of exchangeable ‘random effects’ to be added, and spatially lagged covariates (SLX) can also be added to any of the models. While proper CAR models have been avoided in the past due to their computational burden, the CAR model is the most efficient spatial model in **geostan**. It is fast enough to work interactively on a laptop with more than 3000 observations, such as U.S. county data (Donegan 2021).

A set of functions for working with model results conveniently extracts fitted values, marginal effects, residuals, spatial trends, and posterior (or prior) predictive distributions. Users are encouraged to always undertake a thoughtful spatial analysis of model residuals and other quantities to critique and improve their models through successive rounds of ESDA (cf. Gabry et al. 2019).

Spatial ME models

ME models can be added to any **geostan** model. These are models for covariates measured with error, particularly small-area survey estimates with standard errors. The ME models treat the true covariate values as unknown parameters or latent variables, which are assigned a spatial CAR prior model. Users provide the scale of observational uncertainty or ME (e.g., survey standard errors) as data (Donegan, Chun, and Griffith 2021; cf. Bernardinelli et al. 1997; Xia and Carlin 1998; Kang, Liu, and Cressie 2009; Logan et al. 2019). All uncertain inferences from the ME models are automatically propagated throughout the regression or a disease mapping model, and graphical diagnostics are provided for evaluating results of spatial ME models.

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