

Fast and robust learning by reinforcement signals: explorations in the insect brain

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Abstract

We propose a model for pattern recognition in the insect brain. Departing from a well-known body of knowledge about the insect brain we investigate which of the potentially present features may be useful to learn input patterns rapidly and in a stable manner. The plasticity underlying pattern recognition is situated in the insect mushroom bodies and requires an error signal to associate the stimulus with a proper response. As a proof of concept we used our model insect brain to classify the well-known MNIST database of handwritten digits which is a popular benchmark for classifiers. We show that the structural organization of the insect brain appears to be suitable for both fast learning of new stimuli and reasonable performance in stationary conditions. It, furthermore, is extremely robust to damage to the brain structures involved in sensory processing. Finally, we

also suggest that spatio-temporal dynamics can improve the level of confidence in a classification decision. The proposed approach allows testing the effect of hypothesized mechanisms rather than speculating on their benefit for system performance or confidence in its responses.

Keywords: MNIST database, Rosenblatt perceptron, insect mushroom bodies, classification

1 Introduction

A foraging moth or bee can visit on the order of 100 flowers in a day. During these trips the colors, shapes, textures and odors of the flowers are associated with nectar rewards. The association process is dynamical in nature and the stored information is perpetually updated to the varying conditions [Smith et al., 2005; Mackintosh, 1974; Rescorla, 1988]. The machinery involved in this process is designed to learn fast and reliably. Honeybees, in particular, can associate a stimulus with a reward within just 2 or 3 paired presentations in control conditions [Wright and Smith, 2004; Menzel and Bittermann, 1983; Bitterman et al., 1983; Smith et al., 1991]. This observation led us to investigate what aspects of the structural organization of the insect brain are most suitable for fast, robust and efficient formation of associative memories while not jeopardizing reasonable performance after long training time.

The mushroom bodies (MB) are areas of the insect brain that have been shown to be involved in memory formation [Heisenberg, 2003; Dubnau et al., 2003; Menzel, 2001; McGuire et al., 2001; Dubnau et al., 2001; Zars et al., 2000; Mizunami et al., 1998]. The MBs are organized in two modules: The calyx/Kenyon cells (KCs) and the mushroom body lobes [Strausfeld et al., 1998]. The calyx receives and integrates multimodal sensory information [Strausfeld et al., 1998; Heisenberg, 2003], and the mushroom body lobes are involved in memory formation and storage [McGuire et al., 2001; Dubnau et al., 2001; Zars et al., 2000]. There is a large number of KCs in the MB: 200000 in cockroach, 170000 in the honeybee, 50000 in locust, and 2500 in the fruit fly *Drosophila*. This large group of neurons sends afferents to the MB lobes which contain on the order of a few hundred output neurons.

Corresponding to the difference in cell numbers the connectivity from the antennal lobe (AL) to the KCs of the MB is highly divergent and the connectivity from KCs to output neurons is highly convergent. In [Huerta et al., 2004; Nowotny et al., 2005] we analyzed the effects of this structural organization on classification of structured sets of generic stimuli. We showed that random divergence and convergence of connectivity, sparse activity of the neurons in the middle layer, the KCs, and standard Hebbian learning

can account for efficient, potentially self-organized, classification of the input space. Here, we propose to include reinforcement learning to accomplish fast and efficient classification of predefined pattern classes. In order to prove the efficiency of the structural organization of the insect brain for general pattern recognition, we use the well-known MNIST database of handwritten digits [LeCun and Cortes, 1998]. This database contains 60000 training samples and 10000 test samples of handwritten digits. Many pattern recognition schemes have been tested on this database to benchmark their abilities in different situations. In [Garcia-Sanchez and Huerta, 2003; Huerta et al., 2004] the connectivity to the calyx of the MB was chosen randomly arguing that it is not specifically tuned to a given input space. We argued that such non-specific connectivity should accommodate the large variety of information types in the multimodal input to the MB (visual, olfactory, tactile and motor activity) with each modality’s own very different statistics. Here, we aim to substantiate this claim by testing our artificial MB, which was developed with olfaction in mind, on the unrelated task of classifying the MNIST database.

To evaluate the performance of the artificial MB as an universal classifier rather than the quality of preprocessing, we present each of the digits of the MNIST database to our insect brain “as is” (see Figure 1) even though smart feature extraction in the images is known to improve classification considerably. We, furthermore, threshold the grayscales into binary representations to take into account that KC processing of PN activity is likely in form of coincidence detection of single spikes [Perez-Orive et al., 2002; Assisi et al., 2007], which are all-or-none events.

The fundamental learning rule is characterized by two parameters, p_+ and p_- . We analyze a succession of several increasingly more sophisticated learning mechanisms. In the most basic one, plasticity is triggered only if an input triggers a correct response. In this case, connections from active KCs to the correctly firing output neuron are enhanced with probability p_+ corresponding to the imperative for this correct output neuron to respond to the features present in the input in question. Synapses from inactive KCs are decreased with probability p_- corresponding to the requirement to disregard features that are not present. This learning rule needs a selective reward signal, which gates plasticity whenever a digit is classified correctly. Only when this signal arrives, connections involved in the response will change. The biological basis for the reward signal is found in a class of giant neurons that receive input from the gustatory system (see Fig 1c in [Hammer and Menzel, 1998]). These neurons release neuromodulators at various locations throughout the insect brain including the MB when the honeybee tastes food. Release of octopamine onto the MB replicated the expected behav-

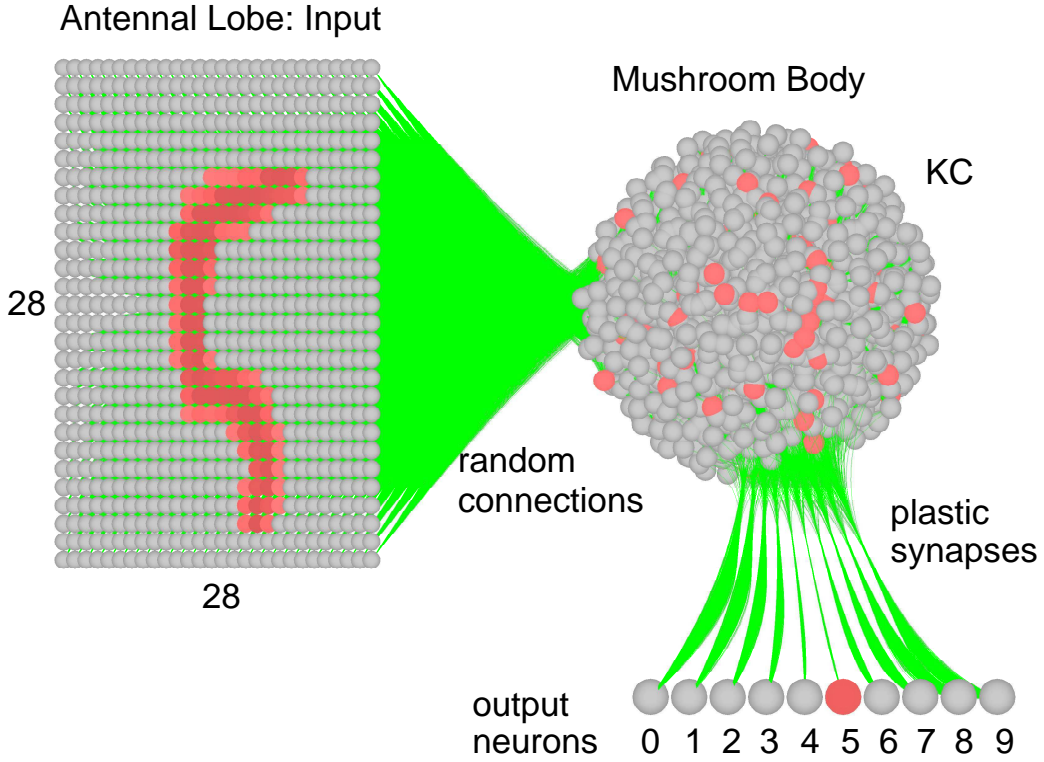


Figure 1: Diagram of the basic system: 28×28 input neurons are randomly connected to $N_{\text{KC}} = 50000$ Kenyon cells. These are read out by 10 output neurons in the MB lobes. The output neurons are connected to all KCs with fairly homogeneous initial weights. Subsequently these connections are modified by the learning rule described in section 4.4.

ior observed during odor conditioning [Hammer and Menzel, 1998; Menzel, 2001].

It may be relevant at this point to note that the proposed learning rule is consistent with the recently found STDP type plasticity of the synapses in question [Cassenaer and Laurent, 2007]. Synapses are potentiated if a presynaptic KC spike is followed by a postsynaptic output spike. The depression part can be interpreted as a general decay of inactive synapses or a depression for unpaired postsynaptic spikes (both conditions for which the STDP rule does not make direct predictions). The learning implemented here, however, differs from a simple STDP rule insofar as it is gated by a reward signal.

In an incremental series of refinements we added a mechanism for adjusting the KC response profiles, a modification of the input layer through populations of “on” and “off” cells, an additional negative error signal for

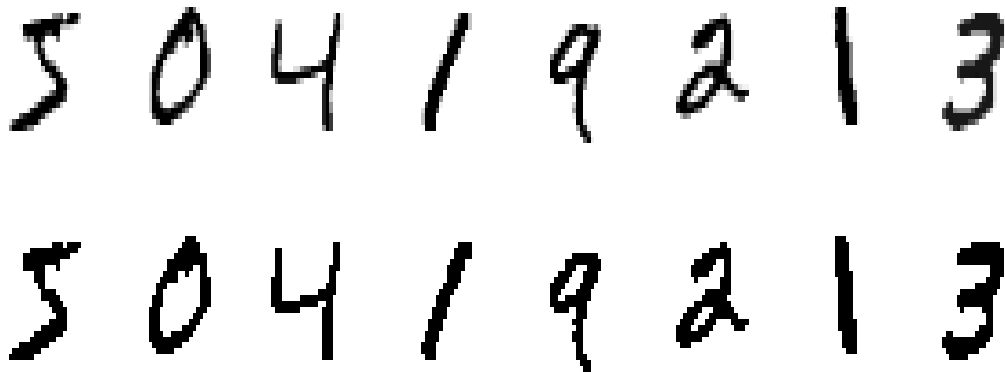


Figure 2: Illustrative example of the MNIST handwritten digits. The upper row are the original gray-scale digits and the lower row the thresholded digits in a $\{0, 1\}$ representation.

incorrectly recognized inputs and a correlate of the dynamics of the AL. To gain an understanding of the role of each of the ingredients in the process of learning, we introduced them one at a time and compared the advantages in terms of fast and robust performance. As a benchmark and general reference we also compared to support vector machines [Cortes and Vapnik, 1995], one of the most successful learning machines. SVMs are known to perform outstandingly well in the MNIST database[Burges and Schoelkopf, 1997]. This comparison is meant to be a guide to judge which of the characteristics of the insect brain model affect which aspect of the performance (speed, final recognition, etc.) in comparison to a standard method.

The paper is organized as follows: First we describe the structural organization of the system, then we show the effect of different types of learning, we investigate the problem of robustness and, finally, we provide the SVM performance as a reference.

2 State of the art

Probably the most representative biomimetic approach to solving pattern recognition problems is the Rosenblatt perceptron [Rosenblatt, 1962], which is a three layered neural network resembling the MBs of insects. A follow-up work on Rosenblatt’s perceptron by Kussul and coworkers [Kussul et al., 2001] forty years later has shown how the Rosenblatt network can achieve competitive performance on the MNIST database. Rosenblatt himself was critical of the abilities of his 3-layered perceptron because of the required

excessive size of the system. With today’s powerful computers, and the potential offered by massively parallel electronic implementations [Arthur and Boahen, 2007; Indiveri et al., 2006; Vogelstein et al., 2007] this is not a barrier any longer. The size of the system and the number of neurons may still be important but it is not a critical issue any more. For example, Kussul and colleagues [Kussul et al., 2001] emphasize the importance of the size of the middle layer of the Rosenblatt perceptron but the numbers they propose are easily handled in current PCs at a competitive computational speed.

More recently, approaches trying to replicate the structure of the cortex have proved to be useful for solving complex pattern recognition problems [Johansson and Lansner, 2006; Peper and Shirazi, 1996; Bartlett and Sejnowski, 1998; Amit and Mascaró, 2001]. In these approaches, feature extractors are used, in analogy to the visual cortex, that are associated by means of attractor networks [Hopfield, 1982]. To place an attractor network in the cortex might be optimistic, but the common language to all these approaches is the use of Hebbian learning, and of inhibition as a way to enhance competitive learning.

It is interesting to note, that, although all approaches mentioned emphasize the need of local learning rules and smart local feature extraction algorithms in order to be able to parallelize the schemes, the speed of learning is not discussed much. Insects and mammals can learn very quickly compared to the prevalent biomimetic technical systems. One of the aspects we would like to explore here is, how a structure similar to the MB of insects allows such quick and stable learning concurrently.

3 Biological basis of the model

While making certain simplifications, our model is firmly based on biological observations, in particular:

1. Structurally, the organization of information processing in the brain is in layered, feed-forward networks [Abeles, 1991; Diesmann et al., 1999; Hertz and Prügel-Bennett, 1996; Câteau and Fukai, 2001; Nowotny and Huerta, 2003]. In, particular, early sensory processing is typically organized in a layered fan-out, fan-in structure. In the olfactory system of insects, the ratio of the number of neurons in the Antennal Lobe to the number of KCs in the MB is on the order of 1:10. The KCs send projections to output neurons in the MB lobes, which are a lot less numerous [Strausfeld et al., 1998; Heisenberg, 2003]. The original model of Rosenblatt [Rosenblatt, 1962] already had this structure without a direct motivation from neurobiology.

2. KCs in the MB Calyces rarely fire [Perez-Orive et al., 2002; Szyszka et al., 2005] and do so reliably whenever there is sufficient coincident input [Wüstenberg et al., 2004]. The combination of sparse activity and the apparent absence of intrinsic dynamics in KCs make McCullough-Pitts neurons a valid approximation for their behavior.
3. The sparse activity in the Calyx [Perez-Orive et al., 2002; Szyszka et al., 2005] matches the observation that sparse activity is very effective in artificial associative models [Willshaw et al., 1969; Marr, 1969; Palm, 1980; Tsodyks and Feigel'man, 1988; Amari, 1989; Buhman, 1989; Vicente and Amit, 1989; Curti et al., 2004; Itskov and Abbott, 2008; Ranzato and LeCun, 2007; Lee et al., 2007], which in our mind strengthens the hypothesis that the MB are associative learning machines.
4. The connectivity between the AL and the MB is probably unspecific. While the connections from the AL to the protocerebrum appear to have a good amount of similarity across individuals, the investigation of connectivity patterns from the AL to the MB have not revealed any clear structure [Masuda-Nakagawa et al., 2005; Wong et al., 2002].
5. Behavioral studies have localized the plasticity underlying learning ("the memory trace") predominantly in the MB [Heisenberg, 2003; Dubnau et al., 2003; Menzel, 2001; McGuire et al., 2001; Dubnau et al., 2001; Zars et al., 2000; Mizunami et al., 1998].
6. In support of the behavioral evidence, direct electrophysiological evidence for synaptic plasticity (in the form of spike timing dependent plasticity [Gerstner et al., 1996; Markram et al., 1997; q. Bi and m. Poo, 2001]) has recently been discovered in the synapses from the Kenyon cells to the output neurons of the MB [Cassenaer and Laurent, 2007].
7. This type of local synaptic plasticity differs from common global learning methods as, for example, gradient descent and quadratic programming.
8. Local inhibition, e.g., the local GABAergic neurons recently identified in the MB lobes of bees [Schürmann et al., 2008], may underly competition among output neurons. Mutual inhibition is the most likely mechanism by which the nervous system can select the proper classifier in a multiclass problem [O'Reilly, 2001].
9. Synaptic changes do not occur in a deterministic manner [Harvey and Svoboda, 2007]. i Changes in the maximal conductance of individual

synapses may best be described by a stochastic process of transitions between discrete states [Abarbanel et al., 2005]. (ii) Axons make additional connections to dendrites of other neurons with some probability. Thus, if new synapses are formed to strengthen a connection between two neurons, the more realistic model is a stochastic process as well. Stochastic learning in neural systems has already been proposed, e.g., in [Seung, 2003] and an interesting application can be found in birdsong learning [Fiete et al., 2007].

10. There are giant neurons which receive gustatory input that release octopamine in the MBs when a stimulus is presented [Hammer and Menzel, 1998; Menzel, 2001]. This is the basis of the reinforcement signals in our model.

Our model, as detailed below, is based on these key observations. Departing from this basis we investigate how refining the information representations and the learning rules in particular, improve the performance of the system in the MNIST problem. These additions are hypotheses for mechanisms we expect to be found in future experimental studies of insect brains.

4 System organization

Following [Garcia-Sanchez and Huerta, 2003; Huerta et al., 2004; Nowotny et al., 2005] and as shown in Fig. 1 there are four essential elements in our model: i) a nonlinear expansion from the input digits, \mathbf{x} , that resembles the connectivity from the Antennal Lobe to the MBs, ii) a gain control mechanism in the MB to achieve a uniform level of sparse activity of the KCs, \mathbf{y} , (but also see the discussion in 5.1), iii) a classification phase where the connections from the KCs to the output neurons, \mathbf{z} are modified according to a Hebbian learning rule and mutual inhibition in the output neurons, and iv) an error signal that determines when and which output neuron’s synapses are potentiated or depressed.

4.1 Mushroom Body projection

It has been shown in locusts that the activity patterns in the AL are practically time-discretized by a periodic feedforward inhibition onto the MB calyces and it is well-known that the activity levels in KCs are very low [Perez-Orive et al., 2002]. Accordingly, the information is represented by time-discrete, sparse activity patterns in the MB in which each KC fires at most once in each 50 ms LFP oscillation cycle. This time-discretization is further

enhanced by general properties of random feedforward networks [Nowotny and Huerta, 2003] and, potentially, synaptic plasticity [Nowotny et al., 2003; Cassenaer and Laurent, 2007]. Given the representation in discrete activity “snapshots”, we chose simple McCulloch-Pitts ‘neurons’ [McCulloch and Pitts, 1943] to represent all neurons in our system. The neural activity values taken by this neural model are binary (0 = no spike and 1 = spike). More explicitly, the McCulloch-Pitts KCs are described by

$$y_j = \Theta\left(\sum_{i=1}^{N_{\text{input}}} c_{ji}x_i - \theta_{\text{KC}}\right) \quad j = 1, \dots, N_{\text{KC}}. \quad (1)$$

where the firing threshold θ_{KC} is an integer number and the Heaviside function $\Theta(\cdot)$ is unity when its argument is positive and zero when its argument is negative. The vector \mathbf{x} is the representation of the MNIST digits, consisting of 28×28 pixels. It has dimension $N_{\text{AL}} = 28 \times 28 = 784$. The components of the vector $\mathbf{x} = (x_1, x_2, \dots, x_{N_{\text{AL}}})$ are gray tones in the range from 0 to 255 in the original MNIST database. Considering the transmission of these patterns by coincidence detection on individual spikes [Perez-Orive et al., 2002], we thresholded these values to $x'_i = 0$ for $x_i < 50$ and $x'_i = 1$ for $x_i \geq 50$ (see the images in figure 2). The binary representation \mathbf{x}' will be used in the following sections. The state vector \mathbf{y} of the KC layer is N_{KC} dimensional and $c_{ij} \in \{0, 1\}$ are the components of the connectivity matrix which is $N_{\text{AL}} \times N_{\text{KC}}$ in size.

It is known that the use of features in the input patterns, e.g., based on the topology of digits or on chemical features of odorants, can improve classification performance [Hinton et al., 1997; Belongie et al., 2000; Schmuken and Schneider, 2007]. We will not exploit this observation here and will stick to the idea of having a naive and unspecific system that is capable of learning in many different sensory spaces. Our system does not preserve the topology of the digits in the projection from the AL onto the KC neurons. Instead, the connectivity matrix c_{ji} is determined randomly by independent Bernoulli processes with probability $p_{\text{PN} \rightarrow \text{KC}}$ for each c_{ji} to be one and $1 - p_{\text{PN} \rightarrow \text{KC}}$ to be zero, following the same approach as in [Garcia-Sanchez and Huerta, 2003; Huerta et al., 2004]. The existence of non-specific connectivity is substantiated in [Wong et al., 2002; Masuda-Nakagawa et al., 2005] where PN neurons appear to connect to different locations in the MBs in different individuals. The choice for the degree of connectivity from the input neurons to the KC neurons was guided by the imperative to avoid information loss from the input to the output [Garcia-Sanchez and Huerta, 2003]. In the following we always worked with a connection probability $p_{\text{PN} \rightarrow \text{KC}} = 0.1$.

4.2 Gain control in the Mushroom Body

It has been shown experimentally that the activity levels in the MBs are very sparse [Perez-Orive et al., 2002; Szyszka et al., 2005]. Our theoretical work has also demonstrated that sparse coding is advantageous in an unsupervised learning system [Huerta et al., 2004; Nowotny et al., 2005]. Sparse activity in the basic system described above is, however, very unstable against fluctuations in the total number of active input neurons (pixels) due to the strong divergence of the connectivity. This almost precludes a sparse activity that is constant across inputs. A potential mechanism to remove this instability is gain control by feedforward inhibition [Nowotny et al., 2005; Assisi et al., 2007]. For our purposes, we pre-determined a number n_{KC} of simultaneously active KCs, and allowed spikes only in the n_{KC} neurons that receive the most excitation according to equation (1). As we will see below, this gain control mechanism becomes unnecessary with the introduction of “on” and “off” cells because the number of active inputs (pixels) then becomes exactly the same for all inputs. We removed the gain control at this point in our investigation.

4.3 Mushroom Body Fan-in

It is known that the MBs are involved in memory formation and storage [McGuire et al., 2001; Dubnau et al., 2001; Zars et al., 2000]. In addition it was recently discovered that the synapses from the KC neurons to the output neurons exhibit spike timing dependent plasticity [Cassenaer and Laurent, 2007]. Based on this biological evidence one can extend the model into the MB lobes as

$$z_l = \Theta\left(\sum_{j=1}^{N_{KC}} w_{lj} \cdot y_j - \theta_{LB}\right), \quad l = 1, \dots, N_{LB}. \quad (2)$$

Here, the index LB denotes the MB *Lobes*. The output vector \mathbf{z} of the MB lobes has dimension N_{LB} and θ_{LB} is the threshold for the decision neurons in the MB lobes. The $N_{KC} \times N_{LB}$ connectivity matrix has values $\tilde{w}_{lj} \in [0, 1]$ that are governed by

$$\tilde{w}_{lj} = \tanh(w_{lj}/10000) \quad (3)$$

with underlying integer entries $w_{lj} \in \mathbb{N}_0$. These underlying synaptic strengths w_{lj} are subject to changes during learning according to a Hebbian type plasticity rule described in the following section. The sigmoid filter (3) ensures

that the strength of synapses does not grow unbounded and reflects that biological synapses have limited resources that limits their maximal strength.

Every column vector $\tilde{\mathbf{w}}_l$ (\tilde{w}_{lj} for fixed j) of a connectivity matrix defines a hyperplane in the intrinsic KC layer coordinates \mathbf{y} . This is the plane normal to $\tilde{\mathbf{w}}_l$. There is a different hyperplane for each MB lobe neuron and the combinatorial placement of hyperplanes determines the classification space.

We hypothesize that mutual inhibition exists in the MB lobes and, in joint action with ‘Hebbian’ learning is able to organize a non-overlapping response of the decision neurons. This is often considered a neural mechanism for self-organization in the brain. The combination of ‘Hebbian’ learning and mutual inhibition has already been proposed as a biologically feasible mechanism to account for learning in neural networks [O’Reilly, 2001; Nowotny et al., 2005].

In connectionist models with McCulloch-Pitts neurons mutual inhibition is implemented in an abstract way. Similar to the above-mentioned gain control, we only allow the decision neuron that receives the highest synaptic input to fire. One could also allow for a population code with groups n_W simultaneously responsive neurons, a classical n_W -winner-take-all configuration.

4.4 Hebbian and Type-I learning

The hypothesis of locating Hebbian learning in the mushroom bodies goes back to Montague and collaborators [Montague et al., 1995]. They proposed a predictive form of Hebbian learning that succeeded in explaining the foraging behavior of bees. The problem we are addressing here is related but also different because we are focusing on classification. Nonetheless, the learning mechanism in our model is certainly departing from the existence of giant reward neurons that send massive inputs to many parts of the the insect brain including the MBs [Hammer and Menzel, 1995].

Every digit prototype is associated to an output neuron of the MB that represents this digit. During training, a digit is presented to the AL which elicits an output response. If the response matches the correct digit then a reinforcement signal will be sent back to apply Hebbian learning. If the output does not match then no learning will be applied.

The plasticity rule is applied to a naive connectivity matrix in which all entries are randomly and independently chosen as $w_{ij} \in \{7500, \dots, 7502\}$. The small variation is to ensure that initially not all neurons have the same inputs and fire together. We tried other random initial distributions and observed differences in learning speed but not in final performance. For example, the standard deviation of the performance in 10 independent trials reached a maximum of 0.041 after about 12000 inputs, while it was only

$6 \cdot 10^{-4}$ for the final performance after $7 \cdot 10^5$ inputs for initial connections $w_{lj} \in \{6500, \dots, 8500\}$.

The inputs are presented to the system in an arbitrary order. The (un-filtered) entries of the connectivity matrix at the time of the n th input are denoted by $w_{lj}(n)$. If the next input leads to a correct output, the updated values $w_{lj}(n+1)$, are given by the rule

$$w_{lj}(n+1) = H(z_l, y_j, w_{lj}(n)), \quad (4)$$

where

$$H(z, y, w) = \begin{cases} w + 1 & z = 1, y = 1, \xi < p_+, \\ [w - 1]_+ & z = 1, y = 0, \xi < p_-, \\ w & \text{otherwise.} \end{cases} \quad (5)$$

where ξ is a uniformly distributed random variable with values in $[0, 1]$ and $[x]_+$ denotes the positive part in x , i.e.

$$[x]_+ = \begin{cases} x & x \geq 0, \\ 0 & \text{otherwise.} \end{cases} \quad (6)$$

A synaptic connection is strengthened with probability p_+ if presynaptic activity is accompanied by postsynaptic activity. The connection is weakened with probability p_- if postsynaptic activity occurs in absence of presynaptic excitation. In the remaining cases the synapse remains unaltered. This learning rule is inspired by the original ideas of Hebb [Hebb, 1949] and the observation that postsynaptic activity, and in particular the ensuing changes in intra-cellular Ca levels, seem to be mandatory for synaptic plasticity to occur [Yang et al., 1999; Abarbanel et al., 2003]. The stochastic nature of the learning rule reflects the non-deterministic manner in which synapses are formed [Harvey and Svoboda, 2007].

The protocol of learning is as follows: i) the input is presented in the AL; ii) one output neuron representing a given class or digit win the response; iii) if the response is correct a positive reinforcement signal is sent back and the learning rule is applied; iv) if the response is not correct the system does not receive a reinforcement signal and no plasticity takes place. We name this learning mechanism type-I learning.

5 Results

The system is trained with type-I learning on the training set and then the performance levels shown on figure 3 are obtained directly on the test set.

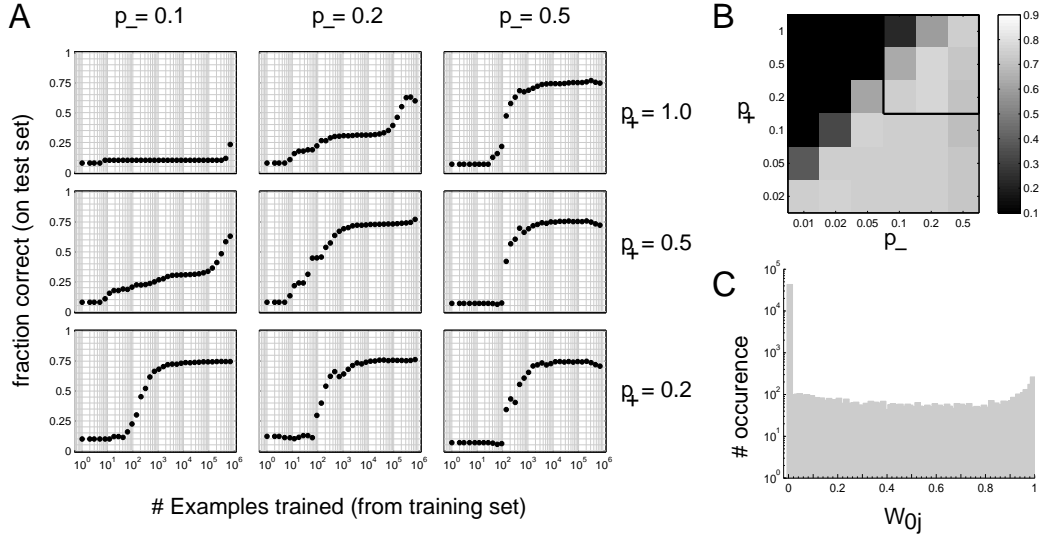


Figure 3: Classification performance after different training stages using type-I learning in a system with $N_{KC} = 50000$. The performance shown is calculated directly on the 10000 digit MNIST test set (A) With increasing number of inputs seen of the training set, the performance increases for most (p_+, p_-) pairs. However, if p_- is too large the performance decreases again after more learned examples. B) The final performance depends on p_+ and p_- and shows a clear division between successful pairings obeying roughly $p_- \geq 0.2p_+$ and unsuccessful ones for smaller p_- . One reason for the premature flattening or even decrease of the recognition performance after about 1000 seen digits is that some synapses are over-trained. C) distribution of synaptic strengths to the neuron representing digit 0 (as an example). There are two peaks around 0 and the maximal synaptic strength (note the log scale on the y axis).

This is the best way to determine the progression of system performance during training. The most influential and experimentally least constrained parameters in this basic type-I learning system are the speed of potentiation, p_+ , and depression, p_- , at the synapses from the KCs to the MB outputs. They can be interpreted as the speed of learning to pay attention to some feature (encoded by the activity of a given KC) or to disregard it. We measured the performance of the system on the 10000 digit MNIST test set at logarithmically increasing intervals with respect to the number of presented training examples. Figure 3A shows examples of performance with respect to training time for 9 (p_+, p_-) parameter pairs. The performance is acceptable when $p_- \geq 0.2p_+$. Within this constraint the exact values do not seem to matter too much for the final performance (figure 3B). It is very clear in

the figures, and maybe obvious, that the speed of learning is improved by using a deterministic learning rule $p_+ = 1$ for potentiation of connections. The prediction at the experimental level is that positive synaptic changes from the KCs to the MB lobes have to be very effective when concurrent depolarization of intrinsic KCs and output neurons occurs.

One detrimental factor for the performance became apparent from the response profile of KCs. Some KCs respond to almost any input (Figure 4). This obviously cannot be helpful for discrimination. Similarly, KCs that never fire, a large proportion of the population, cannot contribute. Thus, we introduce a new ingredient to the system such that KC responses are sparse but non-silent *over time*. This requirement is consistent with experimental observations in many neural systems, where neurons are seen to adjust their firing threshold or the efficacy of the incoming synaptic input [Desai et al., 1999; Him and Dutia, 2001] to achieve some average target activity level. In practice, we form the AL \rightarrow MB connectivity in three stages. We first use independent Bernoulli processes to determine an initial connectivity as before. Then we present inputs to the system (without calculating a final output), average the responses of KCs over time and rescale the synaptic input to KCs that fire to more than $f_{\max} = 10\%$ of the inputs or that fail to fire. Inputs of too active KCs are scaled down by a factor $k_{\text{down}} = 0.9$ and synapses of silent KCs are scaled up with $k_{\text{up}} = 1.1$. This process is repeated 25 times followed by another 25 iterations in which only neurons that fire too often are considered.

The effect of this 'pre-training' adjustment of AL-MB connectivity on the response profile of the MB is illustrated in Fig. 4. The long tail towards very active KC is removed, and the sharp peak at 0 response is strongly attenuated. In the typical example shown in the figure, the number of KCs that are active more than 30% of the time is 1579 before and 0 after pre-training. On the other hand, the number of KCs that are active less than 2% of the time is 29081 before and 1533 after pre-training.

The effect of this tuning of KC responses on the performance can be seen in figure 6 for the dark circles (type I learning without pre-training) and grey circles (type I learning with pre-training). The other curves reflect type-II learning, explained below, where the dark triangles are without pre-training and the grey ones use pre-training. Overall, the pre-training process substantially helps the performance of the system.

5.1 On and off cells

Encoding the MNIST digits digitally as 0 and 1 and analyzing them using equally digital 0 and 1-valued connections may not extract the most infor-

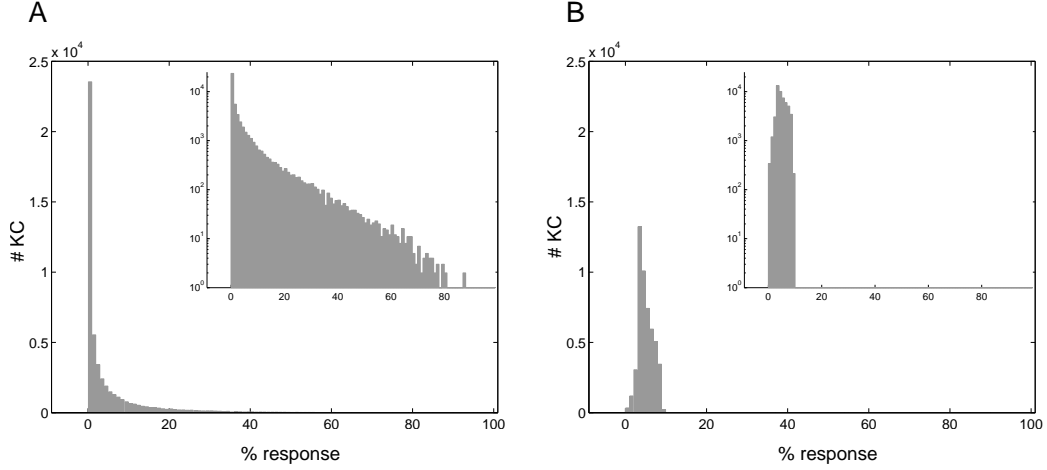


Figure 4: Change of the response characteristic of KCs due to 'pre-training'. (A) Distribution of the number of active KCs without pre-training. (B) Distribution of the number of active KCs with pre-training. Both distributions were calculated on the training set and are shown on a linear scale (main panels) and a logarithmic scale (insets). Note the reduction of the peak at 0 (cells active < 2%, 29081 before and 1533 after pre-training) and the removed fat tail of very responsive cells (cells with more than 30% response, 1579 before and 0 after pre-training).

Learning type	Description
Type-I	The input is processed. The output is checked. If it is correct a reinforcement signal is received and Hebbian learning is applied to the synapses leading to the active neuron (section 4.4)
Type-II	Type-I + selective elimination of corrupted synapses by negative reinforcement (section 5.2)

Table 1: Summary of the different types of learning signals included in the model of the mushroom bodies

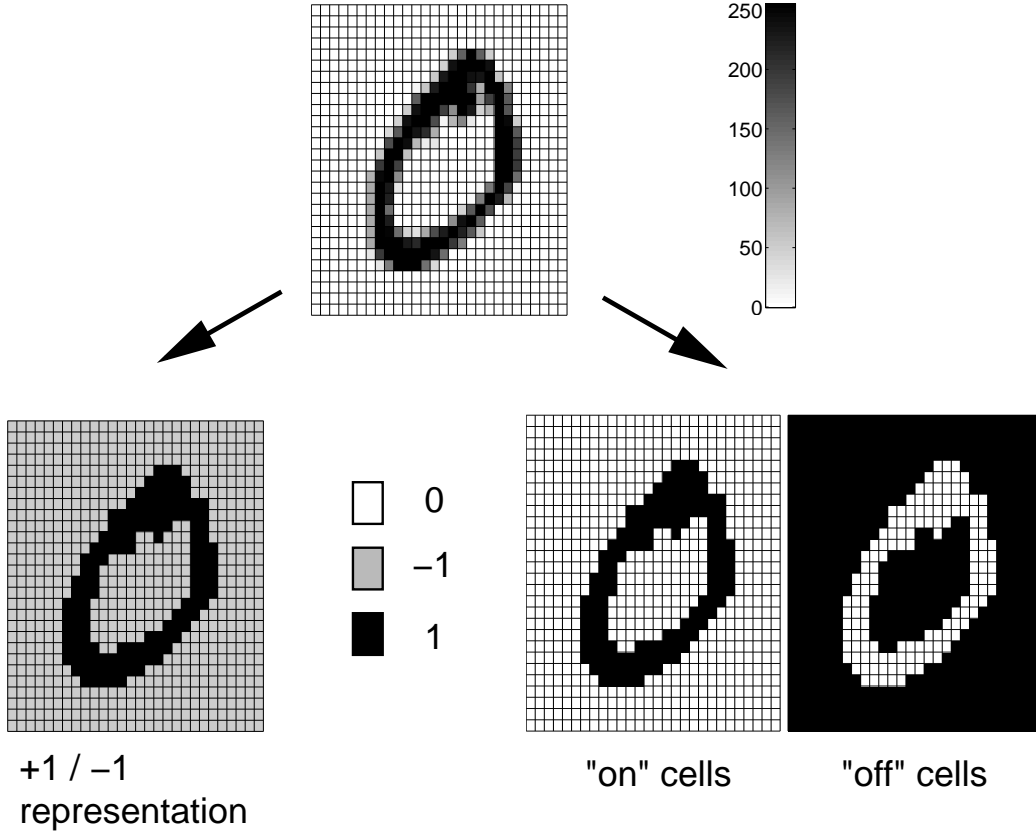


Figure 5: Different strategies to conserve or extract more information from the original digit. The grayscale image can be thresholded to give a representation with values $+1$ and -1 ([Kussul et al., 2001], left), or one can use two populations of neurons that respond inversely to each other loosely equivalent to “on” and “off” cells in the visual system (used here, right).

mation from the input patterns. As an example, there cannot be a KC that specifically fires if certain pixels are *not* activated. In a sense, we are only extracting the ‘light’ information, not the ‘dark’ parts. Kussul and collaborators [Kussul et al., 2001] suggested to use representations of $+1, -1$ and synapses of $+1, -1$ to overcome this deficit. Nature has actually found its own solution to the problem. It is well known that in the visual system so-called “on” cells, i.e., cells that respond to light in their receptive field, coexist with “off” cells that are particularly active when their receptive field does *not* contain light [Jones and Palmer, 1987; DeAngelis et al., 1993]. We are adopting this view here and introduce a second population of input neurons that responds in the opposite way to the original cells (see figure 5). Con-

nections are then formed to neurons of both populations in the unspecific manner as before.

As a free benefit of this on/off cell representation the number of active cells is constant removing the need for gain control. We can (and will), therefore, use the more primitive system with a fixed firing threshold θ_{KC} which is chosen as $\theta_{KC} = 92$ for $p_{PN \rightarrow KC} = 0.1$ and $N_{KC} = 50000$. In general we adjust θ_{KC} such that typically about 2 – 5 % of the KC population is active at any given time, consistent with experimental observations [Perez-Orive et al., 2002; Szyszka et al., 2005].

In Fig. 6 the circles represent the previous result with the 0 and 1 representation and type-I reinforcement learning. The diamonds show the performance with on/off cell input. We observe a slight improvement reaching now about 81% of correct recognition. However, learning takes a slightly higher number of digit presentations to reach significant levels of performance.

5.2 Type-II reinforcement: Negative reinforcement

Rather than only re-enforcing synapses that fire the correct output neuron and thus making it more likely to fire, one can in addition decrease the efficacy of synapses that caused a wrong output neuron to fire. This form of additional “negative” reinforcement can be added to our learning rule (5) as follows:

$$w_{kj}(n+1) = K(z_k, y_j, w_{kj}(n)). \quad (7)$$

where K is given by

$$K(z, y, w) = [w - 1]_+ \quad \text{if } z = 1, y = 1, \xi < p_+. \quad (8)$$

and the rule is applied whenever output neuron k fires and is not the correct output. The protocol, therefore, is the following: i) the input is presented in the AL; ii) an output neuron representing a given class or digit wins the response; iii) if the response is correct a positive reinforcement signal is sent back and the learning rule H in (4.4) is applied; iv) if the response is not correct, a negative signal is sent back and the rule K above is applied to the active output neuron. We name this learning mechanism type-II learning.

We expect the additional mechanism of negative reinforcement to help disambiguate confusing inputs. The simulations show that this expectation is correct. The additional negative reinforcement improves the final performance (figure 6; triangles). Furthermore, it becomes only important in late stages of the training. At the beginning the performance is almost unchanged but continues to improve respect to the previous evolutions.

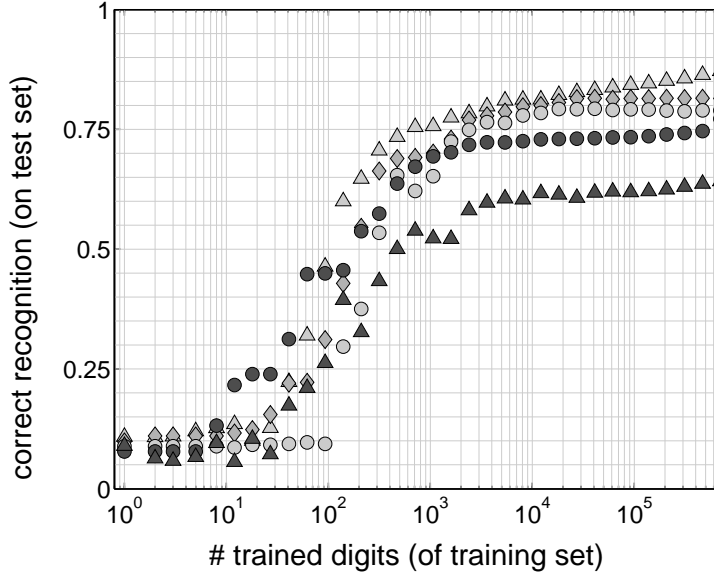


Figure 6: Performance of the system with the previous set of features ($p_+ = 0.5$, $p_- = 0.2$; black circles), pre-trained $AL - KC$ connectivity (grey circles), on and off cells ($p_+ = 0.2$, $p_- = 0.05$; diamonds) compared to further modified systems. The introduction of “punishment” in form of depression of synapses connecting active KC and a wrong active output neuron (type II learning) improves performance for pre-trained MBs ($p_+ = 1$, $p_- = 0.05$; grey triangles) but not for the fully random connections (black triangles). Results are shown for $p_{PN \rightarrow KC} = 0.1$, $N_{KC} = 50000$, and $\theta_{KC} = 92$, which leads to an average activity level of $\approx 2-5\%$ in the MB. Note that the displayed performance is calculated directly on the 10000 digit MNIST test set.

5.3 MB size

We also re-examined the well known important role of MB size in system performance. From our earlier work [Garcia-Sanchez and Huerta, 2003; Huerta et al., 2004; Nowotny et al., 2005] we expected it to play an essential role for successful classification. This prediction was confirmed (Figure 7). The performance of the system depends strongly on the MB size.

Biologically the question of MB size is interesting because it is known that insects have quite different cell numbers in their MBs. Notably honeybees have much larger MBs than *Drosophila* and not surprisingly in the light of this investigation show much more complex behaviors and a larger ability to learn different classes of odors.

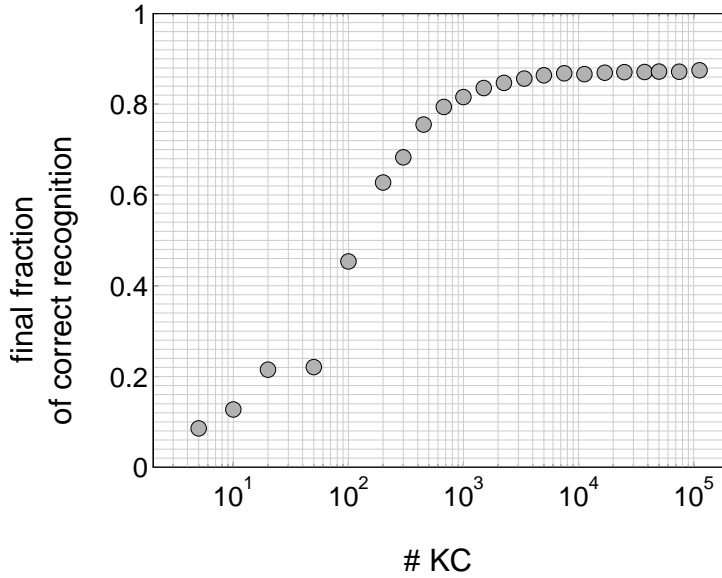


Figure 7: Recognition performance in dependence on the size of the MB. Note that the performance is calculated directly on the 10000 digit MNIST test set. It depends strictly monotonically on the size and the most prominent improvements can be seen up to $N_{KC} = 10000$, even though the performance is never fully saturated. This graph reflects that larger MB sizes in insects may correlate with more complex behaviors.

5.4 Robustness

An important characteristic in biological systems is robustness. The brain can be damaged but still find ways to recover from a malfunction. An inherent property of the structural organization of the insect brain is resilience. The system as described does not depend on specific feature detectors or identified neurons. It is highly parallel, distributed and redundant. We, therefore, expect that it is very stable against perturbations, e.g., in form of failing elements (neurons). We tested this hypothesis by randomly removing KCs (Figure 8; triangles) and input neurons (Figure 8; diamonds). The system is highly stable against failures of the KCs. A measurable decrease in performance only appears when more than 90 % of the KCs are removed. One part of this resilience is certainly that not all KCs are used such that removal does not affect performance. If this was the only effect one would, however, expect that there are cases where by chance the important cell(s) are removed leading to a much worse performance. We do not observe such an effect. The worst and best performance in 10 independent trials of cell removal (shown as error bars in figure 8) do not vary from the average. We

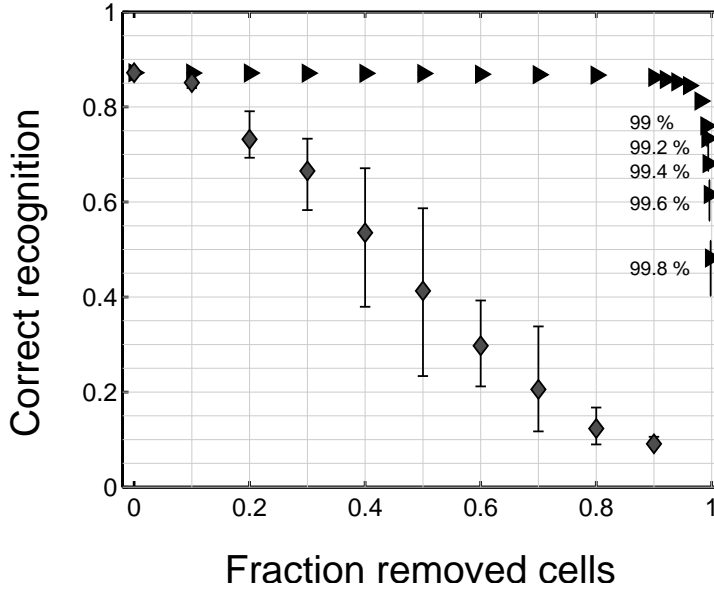


Figure 8: Robustness of the system against removal of cells. The system remains at peak performance beyond 90 % of KC removal (triangles), while it is more sensitive to damaging the input space (diamonds). The performance with KC removal is very similar to the performance of systems which have from the a smaller MB size from the outset (compare to Figure 7, e.g. 99.8 % KC removal corresponds to a MB size of 100 KCs). The error bars mark the worst and best performance seen in 10 independent instances of removed cells. This test was run with $p_{\text{PN} \rightarrow \text{KC}} = 0.1$, on and off cells, no gain control in the MB and temporally sparse KCs with a target activity of 10 % responses to inputs. The learning rule was (8) with $p_+ = 1$ and $p_- = 0.05$. Note that the displayed performance is calculated directly on the 10000 digit MNIST test set after the system was learning from the training set.

conclude that it is not just luck of only removing unimportant cells that makes the system so robust.

The impact of removing input cells is more dramatic. The KC firing thresholds have to be adjusted such that the active KCs remain roughly the same for different number of input neurons. In Fig. 8 (diamonds) we can see that the system shows less resilience to the input space compared to KC removal. This result suggests that we should be able to observe in experiments that the performance of insects degrades faster for AL damage than for Calyx removal.

5.5 Dynamics in the input space: investigating the role of the Antennal Lobe spatio-temporal activity

It is known that early olfactory processing generates spatio-temporal dynamics [Stopfer et al., 1997; Friedrich and Laurent, 2001; Rabinovich et al., 2001; Wehr and Laurent, 1996; Gelperin, 1999; Christensen et al., 1998; Christensen et al., 2003; Abel et al., 2001; Meredith, 1986; Wellis et al., 1989; Lam et al., 2000]. There is still an open debate on whether the dynamics of the odor input is really needed for pattern recognition purposes. To shed some light on this question within our framework we introduced a correlate of AL dynamics and investigated its additional value for classification. To generate a metaphor for the nonlinear AL dynamics we transformed the digits with a non-linear transformation that mapped pixels from the center to the sides. In particular the gray-level $\rho(x, y)$ is added to $\rho'(x', y')$ where

$$\begin{aligned}x' &= \bar{x} + \sqrt{1/d} (x - \bar{x}) \\y' &= \bar{y} + \sqrt{1/d} (y - \bar{y})\end{aligned}\tag{9}$$

and $d = \max\{2(x - \bar{x})/w, 2(y - \bar{y})/h\}$ is the maximum of the normed distances from the center ($\bar{x}, \bar{y} = 13.5, 13.5$) in x or y direction (width $w = 28$, $h = 28$, $x = 0 \dots w - 1$, $y = 0 \dots h - 1$). Pixels closest to the center are moved most while those on the outer boundary stay where they are. The resulting new gray-scales ρ' are cut off at a maximum of 255 to obtain the same representation as before.

This process was applied once to give the equivalent of a second snapshot of AL activity and again for a third (figure 9). Then, during training, these three input patterns were presented in sequence for each input digit and the learning rule was applied for each of them. During testing, the three patterns were again presented in sequence and a recognition decision was made based on a voting rule similar to [Freund and Schapire, 1999].

We compared how unanimous the recognition for the three snapshots was and how often the resulting classification was correct (figure 10). When all three snapshots led to the same recognition decision, the decision was true in 91.5 % of the cases. If the three snapshots all gave different results the success rate was by construction about 1/3 (31.1 % in this case). But if the decision was a 2:1 vote, the rate of correct recognition was 71.6 %. In other words, if there was an unanimous result we could be to 91.5 % sure that we have recognized the digit correctly, if the decision is 2 : 1 we know that our chance to be right is about 71.6 % and if we are thoroughly undecided we know that we will be right for about 1/3 of the time. Depending on the

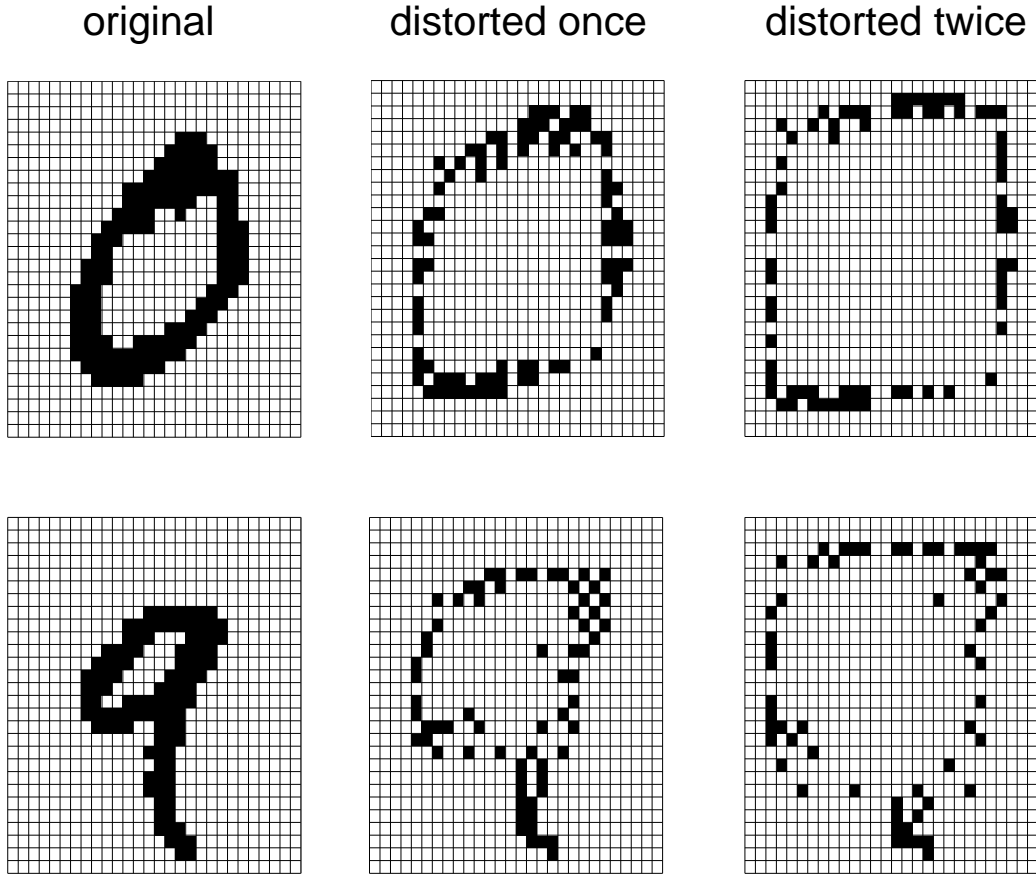


Figure 9: Primitive analogue of a dynamical transformation in the AL. Digits are stretched towards the edge of the 28×28 cell according to (9). All three representations are learned within the same system unlike in boosting techniques.

importance of the correct recognition we can, therefore, adjust our behavior based on this additional “confidence measure”. We hypothesize based on these results that the temporal dynamics in the AL may be a mechanism to convey a measure of confidence in a decision in addition to other hypothesized functions of decorrelation of very similar inputs [Galán et al., 2004; Bazhenov et al., 2001b; Bazhenov et al., 2001a] or added robustness against uncorrelated noise in the input signal. The existence and importance of neural correlates of confidence has recently been shown in orbitofrontal cortex [Kepecs et al., 2008] where neuronal activity in addition to carrying the outcome of a decision also appears to provide a measure of the confidence (risk) in the decision.

A similar idea of voting on the output of several perceptrons to achieve

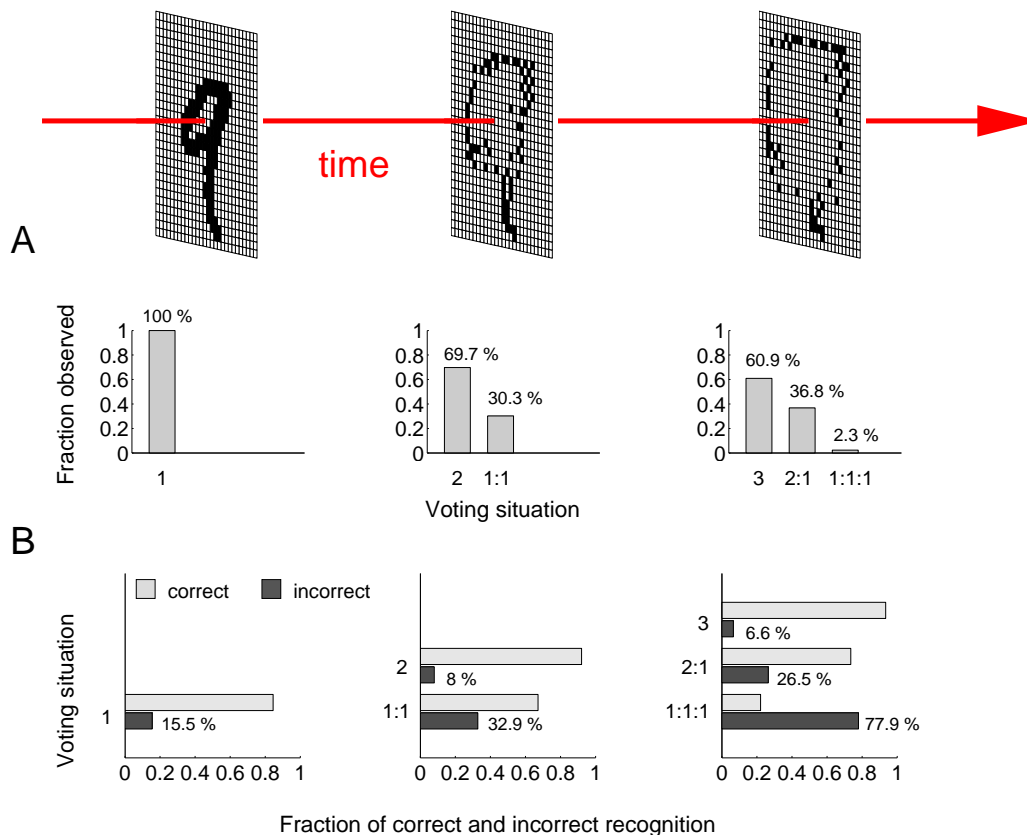


Figure 10: Integration over several temporal 'snapshots' provides additional information on the 'level of confidence' for a classification decision. If only one snapshot is used the overall success rate is almost the same as when 3 are used. However, if 2 or 3 snapshots are used and the vote on what digit is recognized is split (1:1 for two snapshots or 1:2 and 1:1:1 for three) we have the additional information that the resulting recognition may be less successful than with an unanimous vote. Panels A and B show how often the voting situations appear and how successful recognition is in each of the situations.

better performance was already proposed by [Freund and Schapire, 1999] (named the voted-perceptron algorithm). The combination of this idea with the fact the AL generates spatio-temporal patterns provides a good rationale for the hypothesis of the need of spatio-temporal dynamics in the AL. However, the overall performance actually does not improve significantly. Rather, one gains additional information for each output on the level of confidence in the outcome based on the split of the vote. Note that this output-by-output confidence measure is somewhat different from the classical notion of a margin that describes the quality of a classifier as a whole.

5.6 Comparison to Support Vector Machines

The performance of artificial systems in the MNIST database is already outstanding [LeCun et al., 1998; Belongie et al., 2000; Burges and Schoelkopf, 1997]. It has been suggested that it already surpasses human abilities. Our goal has not been to create another new system for pattern classification but rather to determine what aspects of the structural organization of the insect brain can accomplish better stable performance. Nevertheless, it is interesting to show what this simplified insect brain that uses reinforcement learning can do in comparison with one of the most successful supervised machine learning devices, the support vector machines (SVMs) [Burges and Schoelkopf, 1997]. We compare both systems in similar conditions by using exactly the same amount of data for both, the artificial MB and the SVM. We also do not pre-process the digits in either and threshold them to binary values in both. We used the standard libsvm [Chang and Lin, 2007] implementation as a well-tested SVM toolbox and classified data of on/off cell patterns as described in section 5.1. Fig. 11 shows the classification results for a polynomial kernel of order 3 that appeared to give the best results for a wide range of parameters of the training algorithm. The best performance obtained was 93 % for the binarized input space analyzed in this paper. Be aware that SVMs can achieve over 98% success with the full digits and different types of kernels. With appropriate preprocessing schemes performances of > 99% have been achieved.

In terms of comparing learning speed, our insect classifier processes each digit only once. Only when more than the 60000 inputs of the database are processed digits will be repeated. To compare to the partial training with n presented digits, we introduced a subset of n training samples in the SVM training. These were then used to minimize a quadratic problem under constraints as usual for SVMs. In this process, the number of evaluations of each digit in the quadratic optimization problem will certainly be the same but probably much higher than the one-shot learning of the insect classifier.

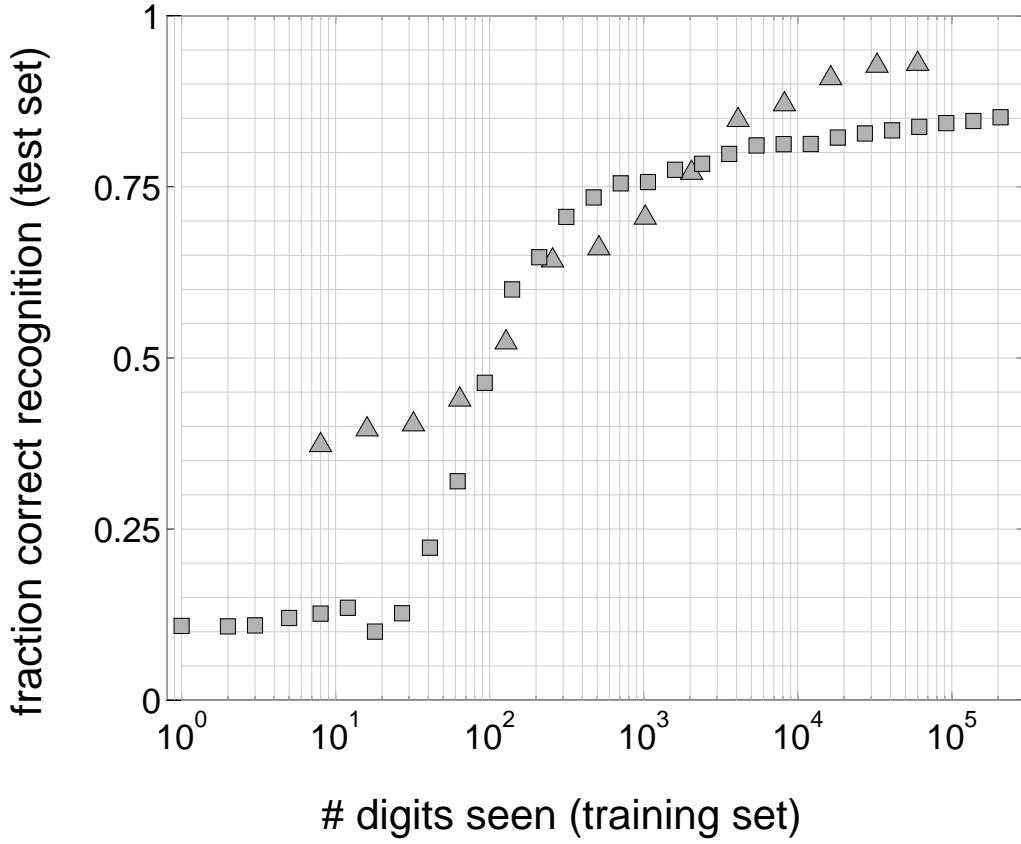


Figure 11: Comparison of an SVM trained on partial data sets (squares) and the insect brain after limited number of seen digits (triangles).

As expected the SVM performs slightly better because it is a supervised learning scheme. It serves us to obtain a hypothetical upper limit to what the artificial insect brain can do. Surprisingly, the SVM does not perform exceptionally well on the binarized on/off cell input.

6 Conclusion

We have shown that the structural organization of the MB can account for successful classification in a very well-known problem of hand-written digit recognition. We see that the most important critical parameters are the learning probability p_+ , and different forms of reinforcement signals as described in table (1). We also propose a new interpretation of the role of temporal coding in introducing the concept of confidence in the individual recognition decisions.

Typically the learning curves have two stages. The first stage is a fast rise of performance up to a saturation value which is typically reached after 1000 input presentations or less. In the following second stage performance continues to improve but very slowly. We have shown that the most simple type of reinforcement signal which we denoted type-I reinforcement leads to sufficiently quick learning but performance saturates early after only 1000 presentations. This is due to an “overload” of information for some of the synapses. Refinements of the MB response profile, on/off cell representation of the inputs and selective removal of wrong synapses help to improve the second phase of learning. These refinements of the basic classification system have not been discovered experimentally. However, they are all analogous to known mechanisms in neural systems. (i) Neurons adjust their excitability analogous to our pre-training, (ii) The notion of a second population of “off” cells was borrowed from the toolbox of the vision community and is an interesting hypothesis for two reasons: a) The MB is a multi-modal integration region and receives visual inputs in a separate population of cells in the bee [Mobbs, 1982; Ehmer and Gronenberg, 2002] but the same population as olfactory input in the ant [Ehmer and Gronenberg, 2004]. b) The identification of an “off” cell in the olfactory system is not as simple as in the visual system because it is hard to identify whether a PN is active in response to activity of a certain ORN type or in response to the quiescence of certain ORNs. The fact that intrinsically active ORNs [de Bruyne et al., 2001] as well as inhibitory responses of PNs [Laurent et al., 1996], figure 1, have been found, illustrate that the information transduction in the AL is not a simple excitatory feedforward pathway. (iii) the existence of giant reward cells in the insect brain suggests that different forms of reinforcement may operate in the system.

The methodology that we followed to increase the level of complexity in the learning procedure was parsimonious. We started from the most plausible or simple to the more complex but still biologically possible. We always remained within the limits of what is consistent with the body of knowledge from biological experimentation. One of the most interesting observations we made is that there is a broad range of parameter values of p_+ , p_- , of connectivities, and of sparseness that lead to satisfactory results, see, e.g., figure 3B. This indicates that the structural organization of the mushroom bodies is generically very well-suited to support classification with Hebbian type learning.

In addition to good classification abilities, the organization of the mushroom bodies also offers a surprising robustness of performance against damage to the system. Parts of this robustness may be attributed to simple

redundancy in large populations of neurons but resilience beyond 90 % damage to the systems seems more than naively expected. We also concluded that the system is more sensitivity to damage in the AL than in the MB.

Finally, we proposed an new computational role for temporal dynamics in the neural code. We observed that presenting different activity snapshots over time can convey information on the confidence in the answer of the classifier for each individual input by a simple voting procedure. In general, such voting procedures can be easily implemented by temporal integration and lateral inhibition using the winner-take-all concept. This certainly is a departure from previous suggestions that focused on decorrelation of similar inputs as the main function of temporal dynamics.

More than a decade ago Montague and collaborators [Montague et al., 1995] proposed the need of reinforcement and Hebbian learning in the mushroom bodies of insects. The body of knowledge has grown since then and now it is possible to acquire multi-unit recordings and genetically manipulate the insect brain by a large variety of techniques. Although most of the work in reinforcement learning has been directed towards the mammalian brain (see, for example, [Schultz et al., 1997]) we see good prospects of finding the neural substrates and mechanisms of reinforcement learning in the insect brain.

Acknowledgments

RH acknowledges partial support by ONR N00014-07-1-0741 and CAM S-SEM-0255-2006. TN was partially supported by a RCUK fellowship of the Research Councils of the UK and by the Biotechnology and Biological Sciences Research Council (grant number BB/F005113/1).

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