

## Question 1 Loading Packages and Data

```
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v dplyr      1.1.3      v readr      2.1.4
## v forcats    1.0.0      v stringr   1.5.0
## v ggplot2    3.4.3      v tibble    3.2.1
## v lubridate  1.9.2      v tidyr     1.3.0
## v purrr      1.0.2
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()     masks stats::lag()
## i Use the conflicted package (<http://conflicted.r-lib.org/>) to force all conflicts to become errors
##
## Attaching package: 'gridExtra'
##
##
## The following object is masked from 'package:dplyr':
##
##      combine
```

## Question 2 Frequency Table

```
freq_table_oecd <- table(world.data$oecd)
ft.oecd <- data.frame(freq_table_oecd)
# renames variable
ft.oecd <- ft.oecd %>% rename("OECD Member?" = "Var1")
# adds percentage to the table
ft.oecd $ Percentage <- round(prop.table(ft.oecd $ Freq) * 100, digits = 2)
ft.oecd
```

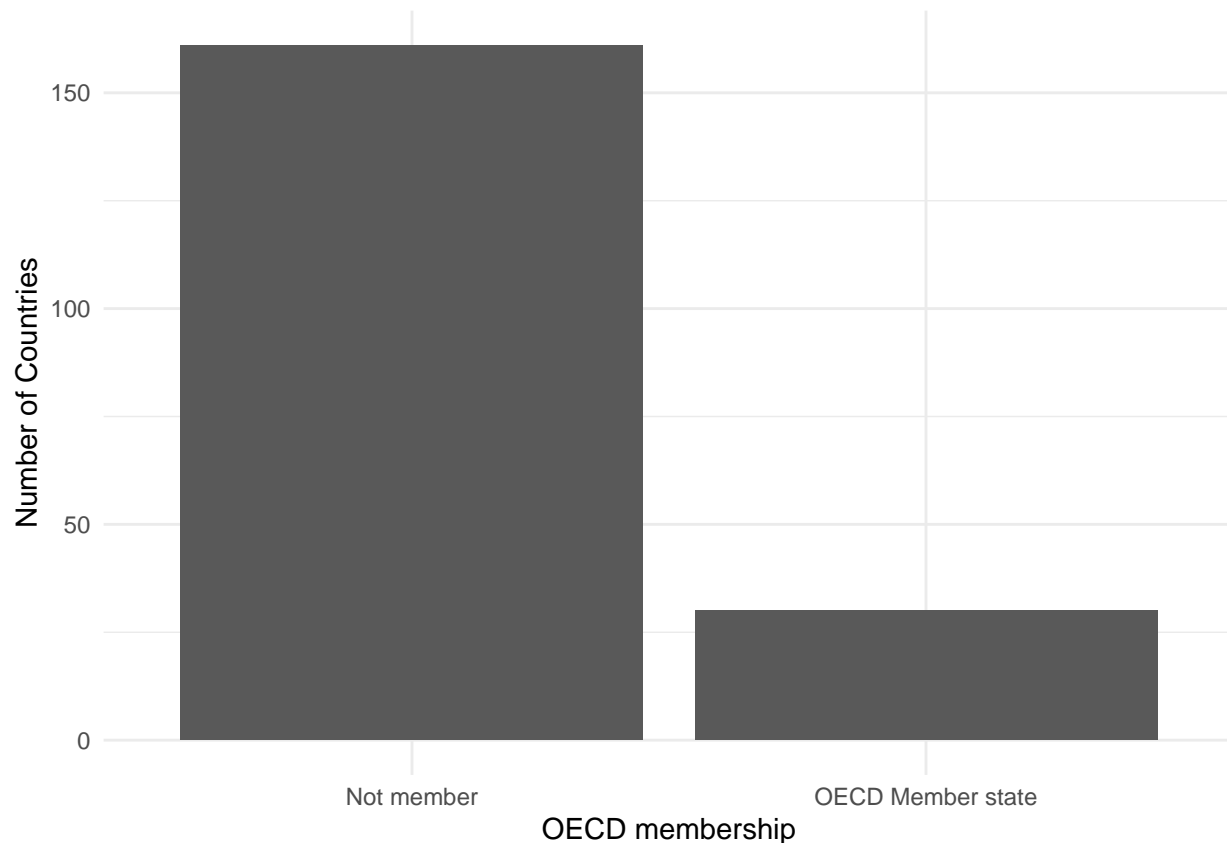
```
##      OECD Member? Freq Percentage
## 1      Not member  161      84.29
## 2 OECD Member state   30      15.71
```

## Question 3

3A. 30 countries within the data set are OECD members 3B. 161 countries within the data set are not OECD members 3C. 15.71% of countries within the data set are OECD members, and 3D. 84.29% of countries within the data set are not OECD members.

## Question 4 Creating a bar chart of OECD country membership

```
ggplot(world.data, aes (x = oecd)) + geom_bar() +
  labs (x = "OECD membership", y = "Number of Countries") +
  theme_minimal()
```



Question 5 three countries that are OECD members, and three countries that aren't democracies

```
# filters out for OECD members and puts them in a vector
oecd_members <- world.data %>% filter (oecd == "OECD Member state")
# shows the top 3 OECD members
head(oecd_members, 3)
```

```
##      country      colony confidence decentralization dem_other dem_other5
## 1 Australia      UK    46.83889                1.74      58.3 Approx 60%
## 2  Austria      Other  49.68019                1.81     100.0      100%
## 3  Belgium Netherlands 43.31516                1.38     100.0      100%
##      democ_regime      district_size3 durable effectiveness      enpp_3
## 1      Yes      single member      99      90.07092 1-3 parties
## 2      Yes 6 or more members      54      88.88889 4-5 parties
## 3      Yes 6 or more members      55      90.30733 6-11 parties
##      eu fhrate04_rev fhrate08_rev frac_eth frac_eth3 free_business
## 1      Not member      Most free      12  0.0929      Low      90.3
## 2 EU Member state      Most free      12  0.1068      Low      73.6
## 3 EU Member state      Most free      12  0.5554      Medium     92.9
##      free_corrupt free_finance free_fiscal free_govspend free_invest free_labor
## 1      87      90      61.4      64.9      80      94.9
## 2      81      70      51.2      28.8      75      79.1
## 3      73      70      42.2      30.0      80      67.1
##      free_monetary free_overall free_property free_trade gdp08 gdp_10_thou
## 1      82.7      82.6      90      85.1 762.6      2.0822
## 2      79.3      71.6      90      87.5 318.4      2.5356
```

```
## 3      77.9      70.1      80      87.5 369.2      2.3749
##      gdp_cap2 gdp_cap3 gdppcap08 gender_equal3 gini04 gini08      hi_gdp indy
## 1      High      High      35677      High      35.2      35.2 High GDP 1901
## 2      High      High      38152      High      30.0      29.1 High GDP 1156
## 3      High      High      34493      High      25.0      33.0 High GDP 1830
##      oecd old2006 old2003      pmat12_3      pop03 pop08      pop08_3
## 1 OECD Member state 12.84444 12.49083 High post-mat 19881000 21.0      >=16.8 mil
## 2 OECD Member state 17.03215 16.02893 High post-mat 8090000 8.3 4.4-16.4 mil
## 3 OECD Member state 17.61054 16.74956 High post-mat 10376000 10.7 4.4-16.4 mil
##      popcat3 pr_sys protact3      regime_type3      region sources
## 1 Moderate (1-29m)      No      High Parliamentary democ Asia-Pacific      NA
## 2 Moderate (1-29m)      Yes Moderate Parliamentary democ      W. Europe      NA
## 3 Moderate (1-29m)      Yes      High Parliamentary democ      W. Europe      NA
##      typerel unions urban03 urban06 vi_rel3 votevap00s women05 women09
## 1      Protestant 28.6 91.8942 88.38 20-50%      82.74 24.7 26.7
## 2 Roman Catholic 36.6 67.7750 66.12 20-50%      75.61 33.9 27.9
## 3 Roman Catholic 38.1 97.5114 97.22 20-50%      86.00 34.7 35.3
##      womyear      womyear2 yng2003 young06
## 1      1902 1944 or before 19.97719 19.31490
## 2      1918 1944 or before 16.16753 15.21968
## 3      1919 1944 or before 16.96234 16.64644
```

```
# filters out the non-democracies
non_democracies <- world.data %>% filter (democ_regime == "No")
# shows the top 3 non-democracies
head(non_democracies, 3)
```

```
##      country      colony confidence decentralization dem_other dem_other5
## 1 Afghanistan      UK      NA      NA      10.5      10%
## 2      Algeria      France 52.05573      NA      40.8 Approx 40%
## 3      Angola Portugal      NA      NA      40.8 Approx 40%
##      democ_regime      district_size3 durable effectiveness enpp_3      eu
## 1      No      single member      4      13.71158      Not member
## 2      No 6 or more members      5      32.62411      Not member
## 3      No      3      19.14894      Not member
##      fhrate04_rev fhrate08_rev frac_eth frac_eth3 free_business free_corrupt
## 1      2.5      3      0.7693      High      NA      NA
## 2      2.5      3      0.3394      Medium      71.2      32
## 3      2.5      3      0.7867      High      43.4      19
##      free_finance free_fiscal free_govspend free_invest free_labor free_monetary
## 1      NA      NA      NA      NA      NA      NA
## 2      30      83.5      73.4      45      56.4      77.2
## 3      40      85.1      62.8      35      45.2      62.6
##      free_overall free_property free_trade gdp08 gdp_10_thou gdp_cap2 gdp_cap3
## 1      NA      NA      NA      30.6      NA
## 2      56.9      30      70.7 276.0      0.1785      Low Middle
## 3      48.4      20      70.4 106.3      0.0857      Low Middle
##      gdppcap08 gender_equal3 gini04 gini08 hi_gdp indy      oecd old2006
## 1      NA      NA      NA      NA      1919 Not member      NA
## 2      8033      35.3      35.3 Low GDP 1962 Not member 4.578136
## 3      5899      NA      NA Low GDP 1975 Not member 2.450295
##      old2003 pmat12_3      pop03 pop08      pop08_3      popcat3 pr_sys protact3
## 1      NA      NA      27.4 >=16.8 mil Moderate (1-29m)      No
## 2 4.045199      31832610 34.4 >=16.8 mil Moderate (1-29m)      Yes
```

```
## 3 2.930542      13522110  18.0 >=16.8 mil Moderate (1-29m)    Yes
##   regime_type3      region sources      typerel unions urban03 urban06
## 1 Dictatorship Middle East      NA      Muslim      NA      NA      23.28
## 2 Dictatorship      Africa      NA      Muslim      NA 58.8302      63.94
## 3 Dictatorship      Africa      NA Roman Catholic      NA 36.1806      53.96
##   vi_rel3 votevap00s women05 women09 womyear   womyear2 yng2003   young06
## 1      NA      NA      27.7      NA      NA      NA      NA
## 2   >50%      NA      NA      7.7   1962 After 1944 33.91887 28.94154
## 3      NA      NA      37.3   1975 After 1944 47.62524 46.32196
```

Question 6 statistics on GDP

```
# summary provides the range, median, mean, and 1st and 3rd quartile
summary(world.data$gdp_10_thou)
```

```
##      Min. 1st Qu.  Median      Mean 3rd Qu.      Max.      NA's
## 0.0090  0.0503  0.1897  0.6018  0.6320  4.7354      14
```

```
# creating a vector of gdp with no NAs to determine the standard deviation
gdp_no_na <- na.omit(world.data$gdp_10_thou)
sd(gdp_no_na)
```

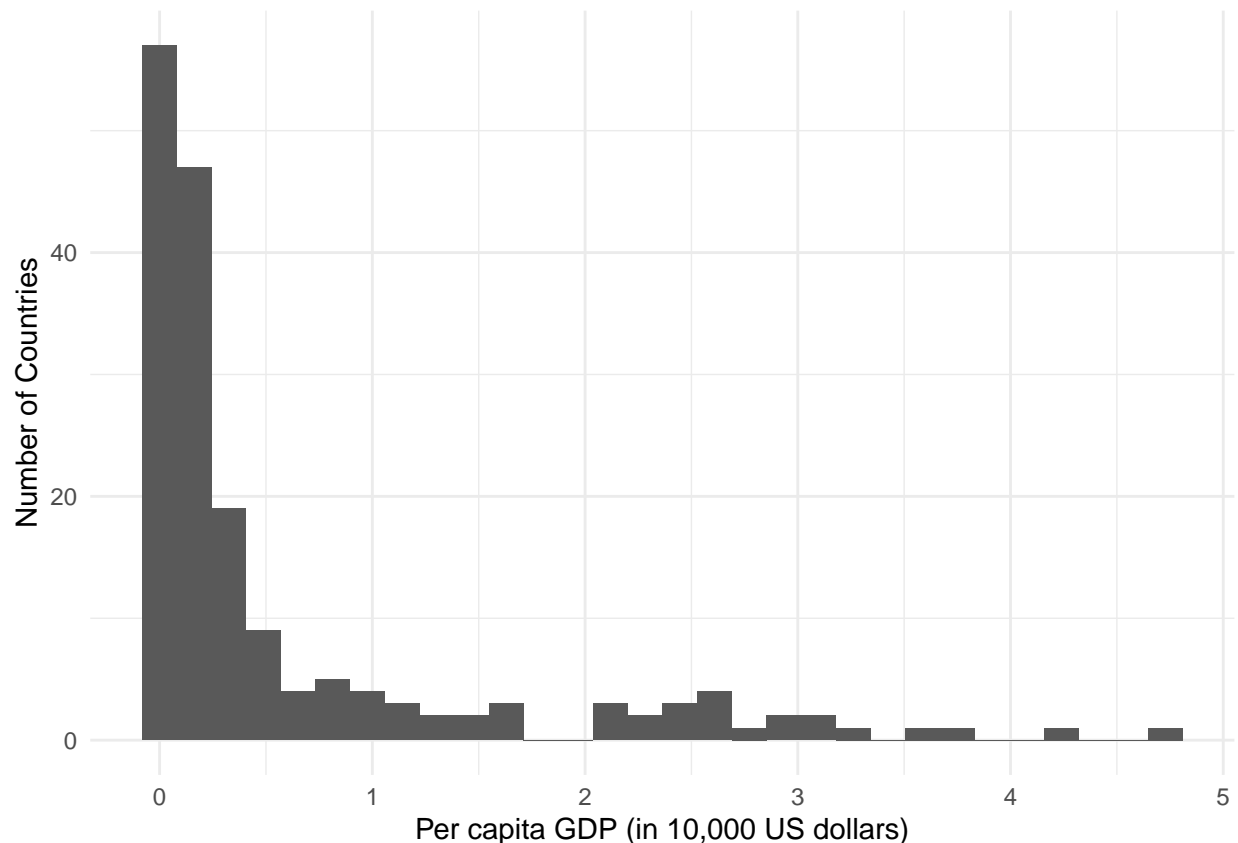
```
## [1] 0.9433982
```

Question 7 Since the median is lower than the mean, the distribution will have a positive skew. That is, the majority of case will occur on the left side of the graph, but there will be a longer tail on the right side of the graph that pulls the mean up.

Question 8 Graphing GDP

```
gdp_data_frame <- data.frame (gdp_no_na)
ggplot (gdp_data_frame, aes (x = gdp_no_na)) + geom_histogram() +
  labs (x = "Per capita GDP (in 10,000 US dollars)", y = "Number of Countries") +
  theme_minimal()
```

```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```



Question 9 Listing 2 countries with gdp per capita over 40k

```
# filter out countries to just have the countries that are at 40k or higher
gdp_40k <- world.data %>% filter (gdp_10_thou >= 4)
head(gdp_40k)
```

```
##      country      colony confidence decentralization dem_other dem_other5
## 1 Luxembourg Netherlands      NA          1.16         100         100%
## 2 Norway      none    66.45381          1.79         100         100%
##   democ_regime    district_size3 durable effectiveness      enpp_3
## 1      Yes 6 or more members      NA    96.92672 4-5 parties
## 2      Yes 6 or more members    54    90.07092 6-11 parties
##           eu fhrate04_rev fhrate08_rev frac_eth frac_eth3 free_business
## 1 EU Member state    Most free          12  0.5302    Medium          75.1
## 2    Not member    Most free          12  0.0586     Low          88.8
##   free_corrupt free_finance free_fiscal free_govspend free_invest free_labor
## 1           83           80        65.9         58.5           95         40.4
## 2           79           60        50.5         49.8           65         47.1
##   free_monetary free_overall free_property free_trade gdp08 gdp_10_thou
## 1          78.9          75.4           90        87.5  38.3      4.7354
## 2          74.2          69.4           90        89.2 277.3      4.1974
##   gdp_cap2 gdp_cap3 gdppcap08 gender_equal3 gini04 gini08   hi_gdp indy
## 1    High    High    78599           High    30.8   31.0 High GDP 1839
## 2    High    High    58138           High    25.8   25.8 High GDP 1905
##           oecd old2006 old2003          pmat12_3   pop03 pop08
## 1 OECD Member state 13.79791 14.92056          448000    0.5
```

```
## 2 OECD Member state 15.03641 14.87521 Moderate post-mat 4562000 4.8
##      pop08_3      popcat3 pr_sys protact3      regime_type3      region
## 1   <=4.3 mil Small (under 1m)   Yes      Parliamentary democ   W. Europe
## 2  4.4-16.4 mil Moderate (1-29m)   Yes      High Parliamentary democ Scandinavia
##      sources      typerel unions urban03 urban06 vi_rel3 votevap00s women05
## 1      NA Roman Catholic   39.5 92.4990  82.68   <20%      56.50   23.3
## 2      NA   Protestant    51.7 75.5492  77.50   <20%      76.54   38.2
##      women09 womyear      womyear2 yng2003  young06
## 1      20.0      1919 1944 or before 18.94910 18.81388
## 2      38.2      1907 1944 or before 19.73542 19.38013
```

Question 10 Calculating Standard Error Standard Error = standard deviation / sqrt of n

```
n <- length(gdp_no_na)
s <- sd(gdp_no_na)
s/sqrt(n)
```

```
## [1] 0.07091015
```

The standard error is 0.0709

Question 11 Calculating the 95% confidence interval for GDP capita

```
# placing the mean in a variable for easy use
mean_gdp_capita <- mean(gdp_no_na)
mean_gdp_capita
```

```
## [1] 0.6018186
```

```
# placing the standard error in a variable for easy use
standard_error <- s/sqrt(n)
standard_error *2
```

```
## [1] 0.1418203
```

```
# Upper bound of the confidence interval
mean_gdp_capita + (standard_error *2)
```

```
## [1] 0.7436389
```

```
# Lower bound of the confidence interval
mean_gdp_capita - (standard_error *2)
```

```
## [1] 0.4599983
```

the confidence interval is 0.6 plus or minus 0.14 yielding a range from 0.46 to 0.74. It should be remembered that this variable is in units of 10,000, meaning that the confidence interval is \$4,600 - \$7,400

Question 12 Graphing Gdp per capita by whether democracy or not

```

# separating democracies and non-democracies
gdp_cap_demo <- world.data %>% filter (democ_regime == "Yes") %>% select (gdp_10_thou)
dp_cap_no_demo <- world.data %>% filter (democ_regime == "No") %>% select (gdp_10_thou)

# putting these into a data frame to use ggplot
demo_gdp_frame <- data.frame (gdp_cap_demo)
no_demo_gdp_frame <- data.frame (dp_cap_no_demo)

# creating ggplots of each
demo_plot <- ggplot(demo_gdp_frame, aes(x = gdp_10_thou)) + geom_histogram() +
  labs (x = "Per capita GDP (in 10,000 US dollars)", y = "Number of Democratic Countries") +
  theme_minimal()

non_demo_plot <- ggplot(no_demo_gdp_frame, aes(x = gdp_10_thou)) + geom_histogram() +
  labs (x = "Per capita GDP (in 10,000 US dollars)", y = "Number of Non-Democratic Countries") + theme_m

# putting the plots side by side
grid.arrange(demo_plot, non_demo_plot, ncol=2)

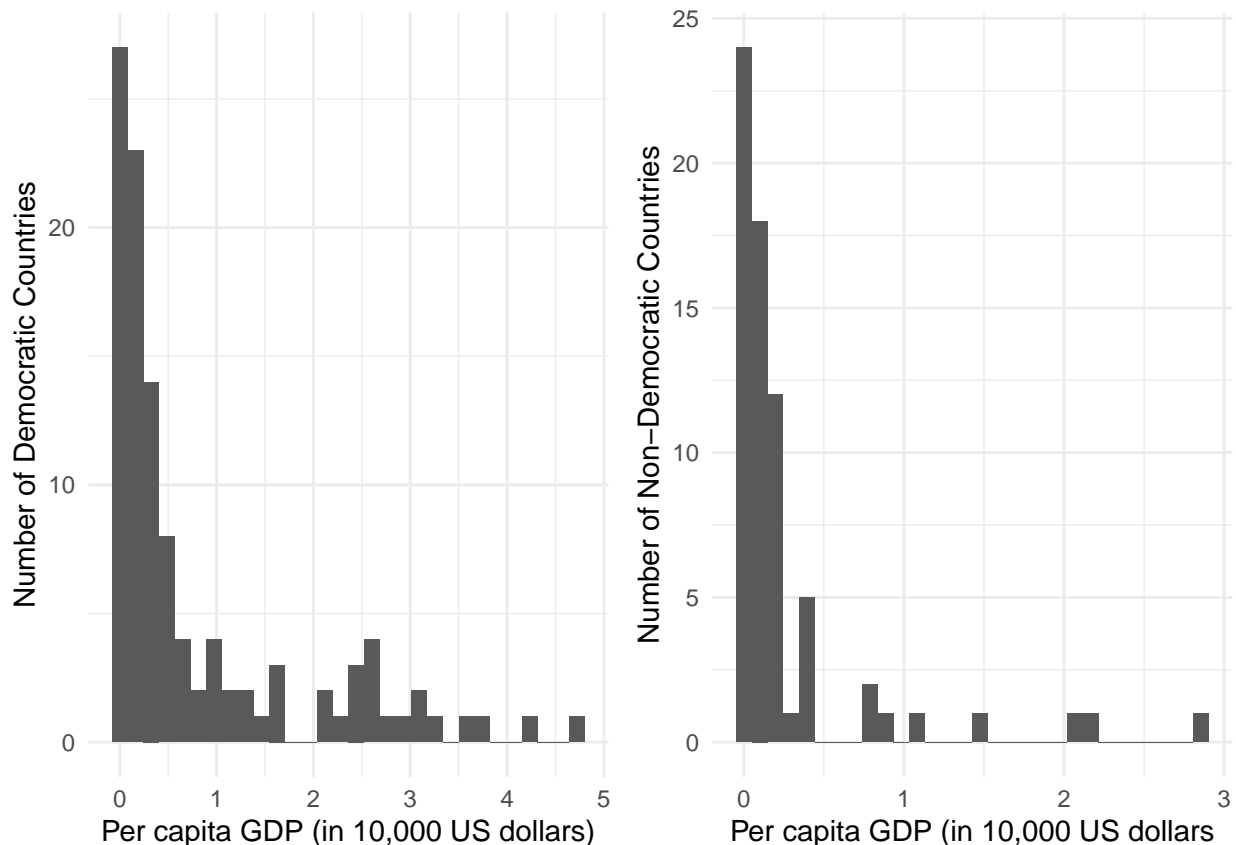
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.

## Warning: Removed 5 rows containing non-finite values ('stat_bin()').

## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.

## Warning: Removed 7 rows containing non-finite values ('stat_bin()').

```



Question 13 Regraphing the graphs above

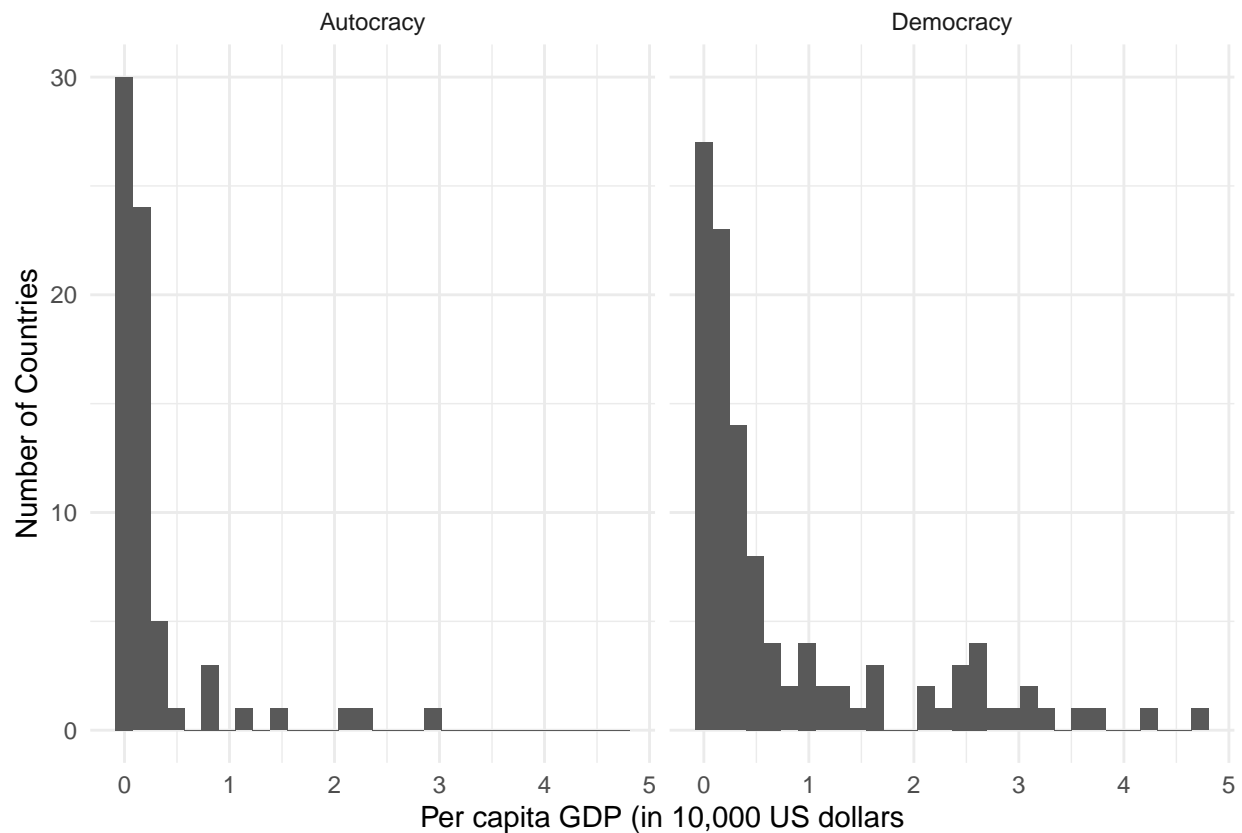
```
# creating new isolate data frame
dem_data <- world.data[c("democ_regime", "gdp_10_thou")]

# removing NAs from democratic data
dem.gdp <- na.omit(dem_data)
data_frame_dem_gdp <- data.frame(dem.gdp)

# Changing yes and no to be democracy and autocracy
dem.gdp$democ_regime <- ifelse (dem.gdp$democ_regime == "Yes", "Democracy", "Autocracy")

# Creating the dual plots
g <- ggplot (dem.gdp, aes (x = gdp_10_thou))
g <- g + geom_histogram()
g <- g + xlab("Per capita GDP (in 10,000 US dollars)")
g <- g + ylab ("Number of Countries")
g <- g + theme_minimal()
g <- g + facet_wrap (~ democ_regime)
g
```

## 'stat\_bin()' using 'bins = 30'. Pick better value with 'binwidth'.



Question 14 Calculating the confidence interval for democracies



```

# Calculating the mean and standard deviation
mean_gdp_capita_demo <- mean(subset(dem.gdp, democ_regime == "Democracy")$gdp_10_thou)
sd_gdp_capita_demo <- sd(subset(dem.gdp, democ_regime == "Democracy")$gdp_10_thou)

# Finding the n to determine the standard error
n_demo <- length(subset(dem.gdp, democ_regime == "Democracy")$gdp_10_thou)

# Calculating the standard error
standard_error_demo <- sd_gdp_capita_demo / sqrt(n_demo)

# 95% confidence interval
#Upper Bound
mean_gdp_capita_demo + (standard_error_demo *2)

```

```
## [1] 1.008499
```

```

# Lower Bound
mean_gdp_capita_demo - (standard_error_demo *2)

```

```
## [1] 0.5942867
```

Democracies have a mean per capita GDP of 8,014 plus or minus \$2,071, leaving a 95% confidence interval of \$5,943 to \$10,084 (numbers are rounded)

Question 15 Calculating the confidence interval for autocracies

```

# Calculating the mean and standard deviation
mean_gdp_capita_auto <- mean(subset(dem.gdp, democ_regime == "Autocracy")$gdp_10_thou)
sd_gdp_capita_auto <- sd(subset(dem.gdp, democ_regime == "Autocracy")$gdp_10_thou)

# Finding the n to determine the standard error
n_auto <- length(subset(dem.gdp, democ_regime == "Autocracy")$gdp_10_thou)

# Calculating the standard error
standard_error_auto <- sd_gdp_capita_auto / sqrt(n_auto)
standard_error_auto *2

```

```
## [1] 0.129515
```

```

# 95% confidence interval
#Upper Bound
mean_gdp_capita_auto + (standard_error_auto *2)

```

```
## [1] 0.4114282
```

```

# Lower Bound
mean_gdp_capita_auto - (standard_error_auto *2)

```

```
## [1] 0.1523983
```

Autocracies have a mean gdp/capita of \$2,819, plus or minus \$1,295 to construct a 95% confidence interval. This leaves a range of \$4,114 to \$1,523

Since there is no cross over between the two confidence intervals, we can be very confident that democracies do have higher GDPs/capita on average than autocracies.

Question 16 Determining the probability of rain after clouds.

```
# first determine the probability of just clouds.
# c = clouds
# r = rain
# Using the law of total probability to find the probability of clouds are any
# day
#  $p(c) = p(c/r) * p(r) + p(c/\sim r) * p(\sim r)$ 
#  $p(c/r) = 95\%$ 
#  $p(r) = 30\%$ 
#  $p(c/\sim r) = 25\%$ 
#  $p(r) = 100 - 30 = 70\%$ 

prob_clouds <- (.95*.3) + (.25*.7)
prob_clouds
```

```
## [1] 0.46
```

```
# prob cloud = 46%

# Using Bayes' rule to determine  $p(r/c)$ 
#  $p(r/c) = (p(c/r)*p(r)) / p(c)$ 

prob_rain_given_clouds <- (.95*.3)/.46
prob_rain_given_clouds
```

```
## [1] 0.6195652
```

The probability of seeing rain after seeing clouds is fairly high at 61.96%

Question 17 Multiple Bayesian Questions

17a.

```
# using the formulas given within the question, the mean is determined by
#  $a/(a+b)$  and the standard deviation by  $ab/(a+b+1)(a+b)^2$ 
# a and b are both equal to 1.5

prior_mean <- 1.5/(1.5+1.5)
prior_standard_d <- (1.5*1.5)/(((1.5+1.5+1)*(1.5+1.5))^2)
prior_mean
```

```
## [1] 0.5
```

```
prior_standard_d
```

```
## [1] 0.015625
```

The prior mean is 0.5 and the prior standard deviation is 0.0156

17b.

```
# Again, using the formula given:  
pbeta(.6, 1.5, 1.5)
```

```
## [1] 0.62647
```

The probability of the prior theta being greater than 60% is 62.6%

17c.

```
# Using the idea that theta is equal to 60%, we use the formula given.  
likelihood <- (.6^37)*((1-.6)^13)  
likelihood
```

```
## [1] 4.153136e-14
```

The likelihood of the data given the prior appears to be very small (though I'm not sure what is a typical range for likelihoods) at 4.15e-14

17d.

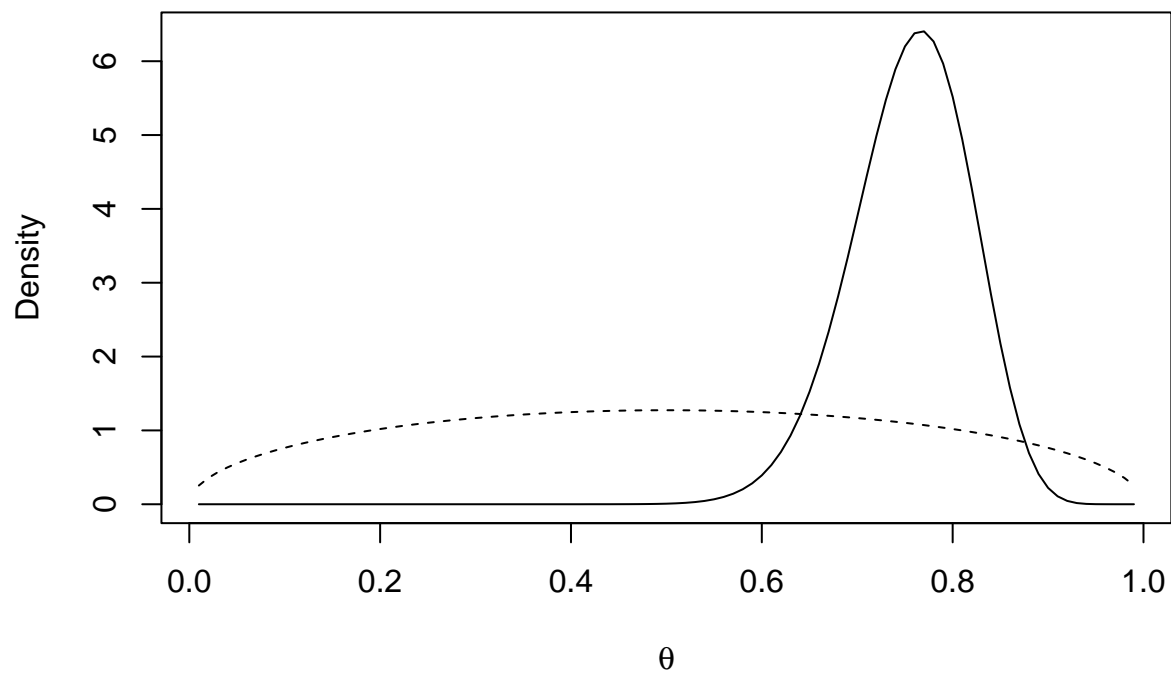
```
# the prior distribution  
prior_dist <- (.6^.5)*(.4^.5)  
posterior_dist <- likelihood * prior_dist  
posterior_dist
```

```
## [1] 2.034613e-14
```

Again, without knowing a typical value to judge by, the posterior distribution is 2.034613e-14

17e.

```
theta<-seq(0.01,0.99,0.01)  
a <- 1.5  
b <- 1.5  
c <- 37 - 1.5  
d <- 13 - 1.5  
prior<-dbeta(theta,a,b)  
posterior<-dbeta(theta,c,d)  
plot(theta,posterior,xlab=expression(theta),ylab="Density",type="l")+  
lines(theta, prior,lty=2)
```



```
## integer(0)
```

17f.

The graph above is showing both the prior and posterior distributions. The prior is the dotted line, the posterior is the solid line. The posterior shows that the distribution we have thus far has more approval of the professor than initially anticipated