

1. Q1

1.1. Brute force

- 1.1.1. **Design:** Approaching this problem logically, and inefficiently, the most simple method of brute forcing is to check for all inversions of each index of our data array. To accomplish this, I will construct a nested for loop. The outer layer will keep track of the element from which I will be comparing others and the inner layer will be the element to compare that to. The inner layer will iterate  $n$  times for each iteration of the outer layer. Thus, my algorithm will have an efficiency class of  $\theta \in n^2$

1.1.2. Pseudocode

```
12 ALGORITHM bruteInversionCount
13 //Computes the number of inversions of an array of integers A[0,n-1]
14 i<-n-1
15 inversions<-0
16 while i>=0
17     j<-i+1
18     while j<n
19         if A[i]>A[j]
20             inversions<-inversions+1
21         j<-j+1
22     i<-i-1
```

1.2. Divide and conquer: My algorithm go brr

1.2.1. This algorithm is  $\theta \in n \log n$

1.2.2. Pseudocode

```
24 ALGORITHM divideInversionCount
25 // Performs mergesort but also counts the amount of inversions
26 // Takes in an array of integers A[0..n-1]
27 // I'm not going to use the floor thing because you know that I didn't need it in C
28
29 if n<=1
30     end
31
32 copy A[0..(n/2)-1] to B[0..(n/2)-1]
33 copy A[(n/2)..n-1] to C[0..(n/2)-1]
34 divideInversionCount(B)
35 divideInversionCount(C)
36 merge(A,B,C)
37
38 ALGORITHM (A[0..An-1],B[0..Bn-1],C[0..Cn-1])
39 a<-0, b<-0, k<-0
40 while b<Bn and c<Cn do
41     if B[b] <= C[c]
42         A[a]<-B[b]
43         i<-i+1
44     else
45         A[a]=C[c]
46         b<-b+1
47         add up inversions here
48     a<-a+1
49
50 if B=Bn
51     copy C[c..Cn-1] to A[a..An-1]
52 else
53     copy B[b..Bn-1] to A[a..An-1]
```

- 2. Q2
  - 2.1. Brute force
    - 2.1.1. Efficiency class of  $\theta \in n^3$
  - 2.2. Divide and conquer
    - 2.2.1. Efficiency  $\theta \in (n \log n)$