

## 1.1 Introduction

### Introduction to Natural Numbers

Non-negative counting numbers excluding zero are called **Natural Numbers**.

$N = 1, 2, 3, 4, 5, \dots$

### Whole Numbers

All-natural numbers including zero are called **Whole Numbers**.

$W = 0, 1, 2, 3, 4, 5, \dots$

### Integers

All-natural numbers, negative numbers and 0, together are called **Integers**.

$Z = -3, -2, -1, 0, 1, 2, 3, 4, \dots$

### Rational Numbers

The number 'a' is called **Rational** if it can be written in the form of  $r/s$  where 'r' and 's' are integers and  $s \neq 0$ ,

$Q = 2/3, 3/5$ , etc. all are rational numbers.

### How to find a rational number between two given numbers?

To find the rational number between two given numbers 'a' and 'b'.

$$\frac{a + b}{2}$$

#### Example:

Find 2 rational numbers between 4 and 5.

#### Solution:

To find the rational number between 4 and 5

$$\frac{a + b}{2} = \frac{4 + 5}{2} = \frac{9}{2}$$

To find another number we will follow the same process again.

$$\frac{1}{2} \left( 4 + \frac{9}{2} \right) = \left( \frac{1}{2} \right) \frac{17}{2} = \frac{17}{4}$$

Hence the two rational numbers between 4 and 5 are  $9/2$  and  $17/4$ .

**Remark:** There could be unlimited rational numbers between any two rational numbers.