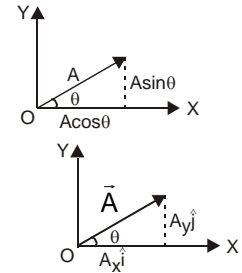


- Resolution of a vector in two dimensions** : If \vec{A} is a vector making an angle θ with x-axis, then X-component = $A \cos \theta$, Y-component = $A \sin \theta$.

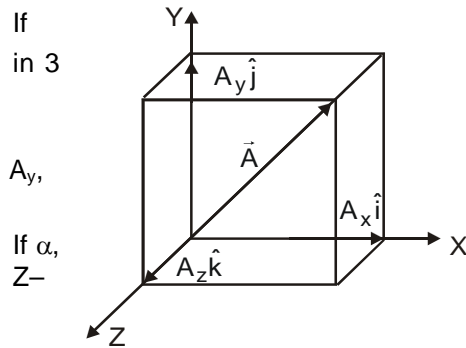


- If \hat{i} and \hat{j} are unit vectors along X and Y axes, any vector lying in XOY plane can be represented as $\vec{A} = A_x \hat{i} + A_y \hat{j}$;

- $|\vec{A}| = A = \sqrt{A_x^2 + A_y^2}$; $\tan \theta = \frac{A_y}{A_x}$

- The component of a vector can have a magnitude greater than that of the vector itself.
- The rectangular component cannot have magnitude greater than that of the vector itself.
- If a number of vectors $\vec{A}, \vec{B}, \vec{C}, \vec{D}, \dots$ acting at a point are resolved along X-direction as $A_x, B_x, C_x, D_x, \dots$ along Y-direction as $A_y, B_y, C_y, D_y, \dots$ and if \vec{R} is the resultant of all the vectors, then the components of \vec{R} along X-direction and Y-direction are given by $R_x = A_x + B_x + C_x + D_x + \dots$ and $R_y = A_y + B_y + C_y + D_y + \dots$ respectively, and $R = \sqrt{R_x^2 + R_y^2}$; $\tan \theta = \frac{R_y}{R_x}$ where θ is the angle made by the resultant with X-direction.

- If in 3



\hat{i}, \hat{j} and \hat{k} are unit vectors along X, Y and Z-axes, any vector dimensional space can be expressed as

$$\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}; |\vec{A}| = A = \sqrt{A_x^2 + A_y^2 + A_z^2} \quad \text{Here } A_x, A_z \text{ are the components of } \vec{A} \text{ and } \vec{B} \text{ are scalars. } \vec{A} \text{ is body diagonal of the cube.}$$

- If α, β, γ are the angles made by \vec{A} with X-axis, Y-axis and Z-axis respectively, then

$$\cos \alpha = \frac{A_x}{A}; \cos \beta = \frac{A_y}{A}; \cos \gamma = \frac{A_z}{A} \quad \text{and}$$

$$\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$$

$$\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma = 2$$

- If $\cos \alpha = l, \cos \beta = m$ and $\cos \gamma = n$, then l, m, n are called direction cosines of the vector. $l^2 + m^2 + n^2 = 1$.

- If vectors $\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$ and $\vec{B} = B_x \hat{i} + B_y \hat{j} + B_z \hat{k}$ are parallel, then $\frac{A_x}{B_x} = \frac{A_y}{B_y} = \frac{A_z}{B_z}$

and $\vec{A} = K\vec{B}$ where K is a scalar.

- The vector $\hat{i} + \hat{j} + \hat{k}$ is equally inclined to the coordinate axes at an angle of 54.74° .

- The position vector of a point $P(x, y, z)$ is given by $\vec{OP} = x\hat{i} + y\hat{j} + z\hat{k}$ and $|\vec{OP}| = \sqrt{x^2 + y^2 + z^2}$

- The vector having initial point $P(x_1, y_1, z_1)$ and final point $Q(x_2, y_2, z_2)$ is given by $\vec{PQ} = (x_2 - x_1)\hat{i} + (y_2 - y_1)\hat{j} + (z_2 - z_1)\hat{k}$.