

Grupo

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In [1]: import matplotlib.pyplot as plt
import matplotlib.image as mpimg
import numpy as np
from IPython.display import display
from matplotlib import rcParams
```

```
In [2]: images = {}

for i in range(10):
    images[i] = mpimg.imread(f'data/{i}.png')

images[0]
```

```
Out[2]: array([[1., 1., 1., 1.],
               [0., 0., 0., 1.],
               [0., 0., 0., 1.],
               [1., 1., 1., 1.]],

               [[0., 0., 0., 1.],
               [1., 1., 1., 1.],
               [1., 1., 1., 1.],
               [0., 0., 0., 1.]],

               [[0., 0., 0., 1.],
               [1., 1., 1., 1.],
               [1., 1., 1., 1.],
               [0., 0., 0., 1.]],

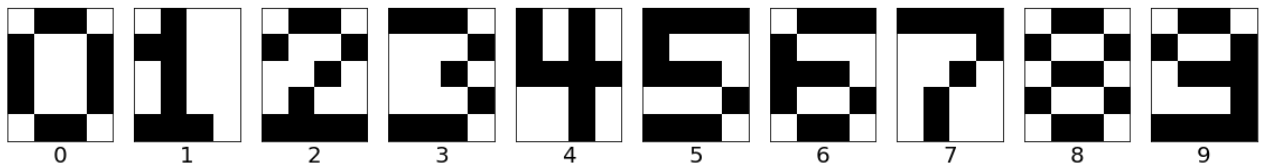
               [[0., 0., 0., 1.],
               [1., 1., 1., 1.],
               [1., 1., 1., 1.],
               [0., 0., 0., 1.]],

               [[1., 1., 1., 1.],
               [0., 0., 0., 1.],
               [0., 0., 0., 1.],
               [1., 1., 1., 1.]], dtype=float32)
```

```
In [3]: rcParams['figure.figsize'] = 20, 15

fig, ax = plt.subplots(1, 10)

for axis, (i, pixels) in zip(ax.reshape(-1), images.items()):
    axis.imshow(pixels)
    axis.set_xticks([])
    axis.set_yticks([])
    axis.set_xlabel(i, fontsize=20)
```



```
In [4]: numbers = {}

for i, pixels in images.items():
    number = []
    for row in pixels:
        for col in row:
            number.append(int(not col[0]))
    numbers[i] = number

numbers
```

```
Out[4]: {0: [0, 1, 1, 0, 1, 0, 0, 1, 1, 0, 0, 1, 1, 0, 0, 1, 0, 1, 1, 0],
1: [0, 1, 0, 0, 1, 1, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 1, 1, 1, 0],
2: [0, 1, 1, 0, 1, 0, 0, 1, 0, 0, 1, 0, 0, 1, 0, 0, 1, 1, 1, 1],
3: [1, 1, 1, 0, 0, 0, 0, 1, 0, 0, 1, 0, 0, 0, 0, 1, 1, 1, 1, 0],
4: [1, 0, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 0, 0, 1, 0, 0, 0, 1, 0],
5: [1, 1, 1, 1, 1, 0, 0, 0, 1, 1, 1, 0, 0, 0, 0, 1, 1, 1, 1, 0],
6: [0, 1, 1, 1, 1, 0, 0, 0, 1, 1, 1, 0, 1, 0, 0, 1, 0, 1, 1, 0],
7: [1, 1, 1, 1, 0, 0, 0, 1, 0, 0, 1, 1, 0, 1, 0, 0, 0, 1, 0, 1],
8: [0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 1, 0],
9: [0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 1, 1, 0, 0, 0, 1, 1, 1, 1, 1]}
```

```
In [5]: def onehot(n_classes, index):
    arr = [0] * n_classes
    arr[index] = 1
    return arr

onehot(10, 0)
```

```
Out[5]: [1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]
```

```
In [6]: def make_xy(_dict):
    x = []
    y = []

    for key, values in _dict.items():
        x.append(values)
        y.append(onehot(10, key))

    x = np.array(x)
    y = np.array(y)

    return x, y

x, y_true = make_xy(numbers)

print(x)
print('\n', y_true)

[[0 1 1 0 1 0 0 1 1 0 0 1 1 0 0 1 0 1 1 0]
 [0 1 0 0 1 1 0 0 0 1 0 0 0 1 0 0 1 1 1 0]
 [0 1 1 0 1 0 0 1 0 0 1 0 0 1 0 0 1 1 1 1]
 [1 1 1 0 0 0 0 1 0 0 1 0 0 0 0 1 1 1 1 0]
 [1 0 1 0 1 0 1 0 1 1 1 1 0 0 1 0 0 0 1 0]
 [1 1 1 1 1 0 0 0 1 1 1 0 0 0 0 1 1 1 1 0]]
```

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[0 1 1 1 1 0 0 0 1 1 1 0 1 0 0 1 0 1 1 0]
[1 1 1 1 0 0 0 1 0 0 1 1 0 1 0 0 0 1 0 1]
[0 1 1 0 1 0 0 1 0 1 1 0 1 0 0 1 0 1 1 0]
[0 1 1 0 1 0 0 1 0 1 1 1 0 0 0 1 1 1 1 1]]

[[1 0 0 0 0 0 0 0 0 0]
[0 1 0 0 0 0 0 0 0 0]
[0 0 1 0 0 0 0 0 0 0]
[0 0 0 1 0 0 0 0 0 0]
[0 0 0 0 1 0 0 0 0 0]
[0 0 0 0 0 1 0 0 0 0]
[0 0 0 0 0 0 1 0 0 0]
[0 0 0 0 0 0 0 1 0 0]
[0 0 0 0 0 0 0 0 1 0]
[0 0 0 0 0 0 0 0 0 1]]

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In [7]: one_wrong_set = {}
        two_wrong_set = {}
        three_wrong_set = {}

        np.random.seed(6)

        for key, value in numbers.items():
            random = np.random.randint(0, 20, size=3)

            # -----
            new_value = value.copy()
            new_value[random[0]] = int(not new_value[random[0]])

            one_wrong_set[key] = new_value

            # -----
            new_value = value.copy()
            new_value[random[0]] = int(not new_value[random[0]])
            new_value[random[1]] = int(not new_value[random[1]])

            two_wrong_set[key] = new_value

            # -----
            new_value = value.copy()
            new_value[random[0]] = int(not new_value[random[0]])
            new_value[random[1]] = int(not new_value[random[1]])
            new_value[random[2]] = int(not new_value[random[2]])

            three_wrong_set[key] = new_value

```

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In [8]: rcParams['figure.figsize'] = 15, 5
        fig, ax = plt.subplots(1, 3)

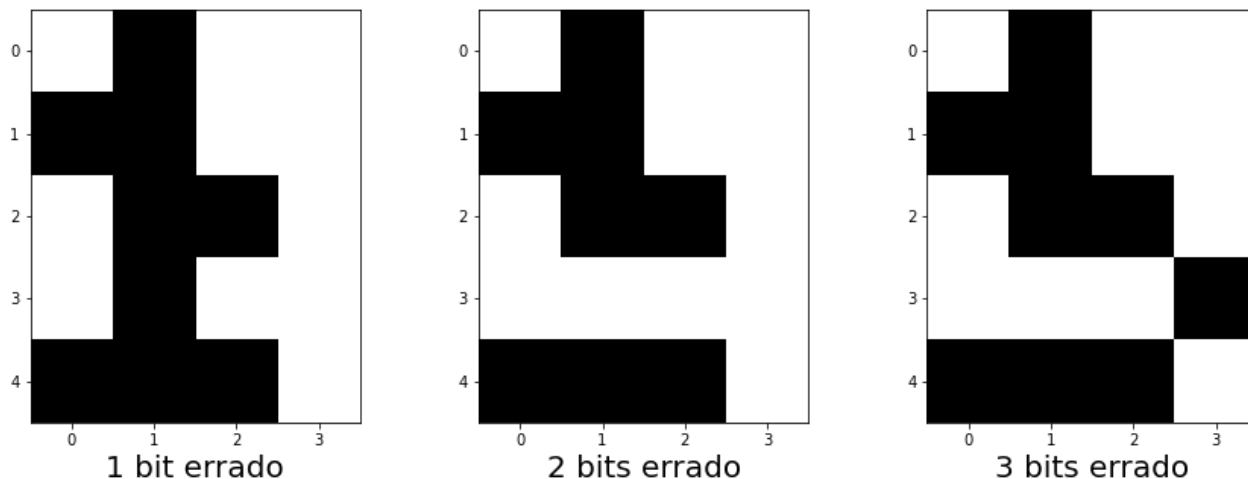
        ax[0].imshow(
            np.array(one_wrong_set[1]).reshape((5,4)),
            cmap='gray_r'
        )
        ax[0].set_xlabel('1 bit errado', fontsize=20)

        ax[1].imshow(
            np.array(two_wrong_set[1]).reshape((5,4)),
            cmap='gray_r'
        )
        ax[1].set_xlabel('2 bits errado', fontsize=20)

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ax[2].imshow(
    np.array(three_wrong_set[1]).reshape((5,4)),
    cmap='gray_r'
)
ax[2].set_xlabel('3 bits errado', fontsize=20)

plt.show()
```



```
In [9]: one_wrong_x, one_wrong_y = make_xy(one_wrong_set)

two_wrong_x, two_wrong_y = make_xy(two_wrong_set)

three_wrong_x, three_wrong_y = make_xy(three_wrong_set)
```

```
In [10]: import tensorflow as tf

def build_and_evaluate_nn(hidden, activation_hidden, output, activation_output, lr, mom):
    np.random.seed(10)
    tf.compat.v1.logging.set_verbosity(tf.compat.v1.logging.ERROR)

    print(f'''
    Parâmetros
    Hidden layer: {hidden}, ({activation_hidden})
    Output layer: {output}, ({activation_output})
    Learning Rate: {lr}
    Momentum: {momentum}
    ''')

    model = tf.keras.models.Sequential([
        tf.keras.layers.InputLayer(input_shape=(20, )),
        tf.keras.layers.Dense(hidden, activation=activation_hidden),
        tf.keras.layers.Dense(output, activation=activation_output)
    ])

    loss_fn = tf.keras.losses.MeanSquaredError()

    sgd = tf.keras.optimizers.SGD(
        learning_rate=lr, momentum=momentum
    )

    model.compile(
        optimizer=sgd,
        loss=loss_fn,
        metrics=["accuracy"]
    )
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)

history = model.fit(x, y_true, epochs=epochs, verbose=0)
history = history.history

rcParams['figure.figsize'] = 15, 5

fig, (ax1, ax2) = plt.subplots(1, 2)

fig.suptitle('Training loss (MSE) and accuracy')

ax1.plot(history['loss'])
ax1.set_xlabel('Epochs')
ax1.set_ylabel('Loss (MSE)')

ax2.plot(history['accuracy'])
ax2.set_xlabel('Epochs')
ax2.set_ylabel('Accuracy')

plt.show()

print(f'''
Final training loss (MSE): {history['loss'][-1]}
Final training accuracy: {history['accuracy'][-1]}
''')

print(f'''
Teste nos números com bits errados
''')

print('\n\t1 bit errado:')
model.evaluate(one_wrong_x, one_wrong_y, verbose=2)

print('\n\t2 bit errado:')
model.evaluate(two_wrong_x, two_wrong_y, verbose=2)

print('\n\t3 bit errado:')
model.evaluate(three_wrong_x, three_wrong_y, verbose=2)

print('''
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''')

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In [11]: parameters = [
        [0.1, 0],
        [0.4, 0],
        [0.9, 0],
        [0.1, 0.4],
        [0.9, 0.4],
        ]

```

```

In [12]: for lr, momentum in parameters:
        build_and_evaluate_nn(15, 'tanh', 10, 'linear', lr=lr, momentum=momentum)

```

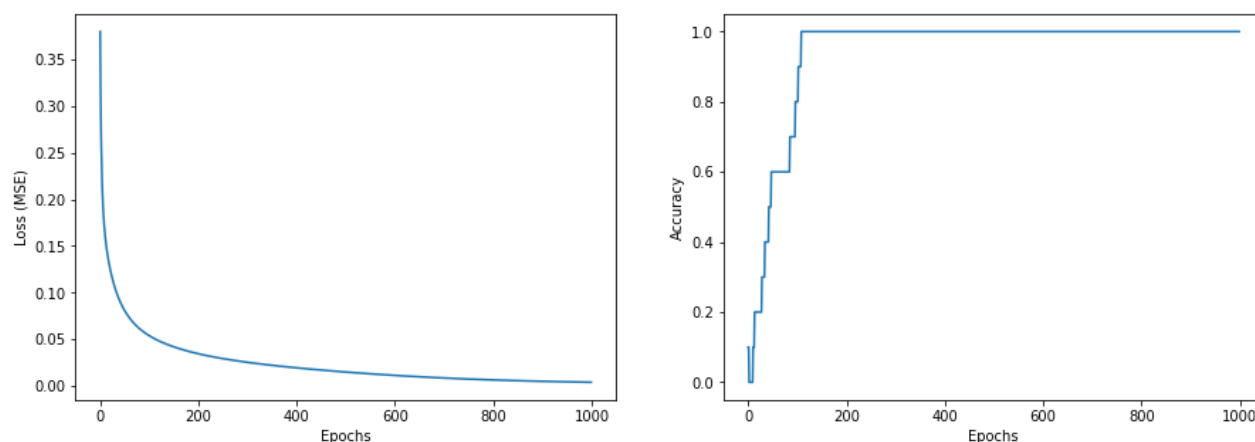
Parâmetros
Hidden layer: 15, (tanh)

Output layer: 10, (linear)

Learning Rate: 0.1

Momentum: 0

Training loss (MSE) and accuracy



Final training loss (MSE): 0.0039929794147610664

Final training accuracy: 1.0

Teste nos números com bits errados

1 bit errado:

1/1 - 0s - loss: 0.0479 - accuracy: 1.0000

2 bit errado:

1/1 - 0s - loss: 0.0760 - accuracy: 0.8000

3 bit errado:

1/1 - 0s - loss: 0.0949 - accuracy: 0.8000

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Parâmetros

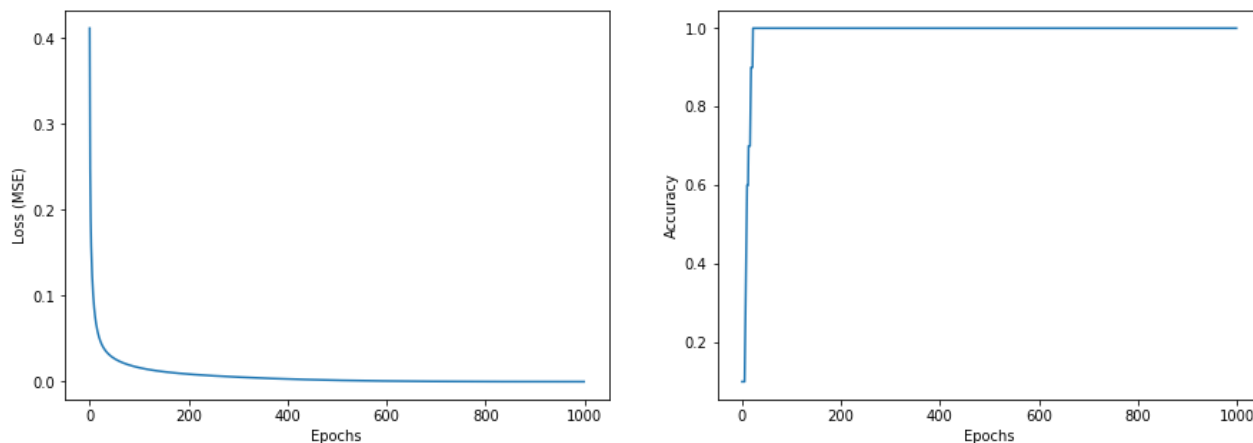
Hidden layer: 15, (tanh)

Output layer: 10, (linear)

Learning Rate: 0.4

Momentum: 0

Training loss (MSE) and accuracy



Final training loss (MSE): 2.227047116321046e-05

Final training accuracy: 1.0

Teste nos números com bits errados

1 bit errado:

1/1 - 0s - loss: 0.0665 - accuracy: 0.9000

2 bit errado:

1/1 - 0s - loss: 0.0953 - accuracy: 0.6000

3 bit errado:

1/1 - 0s - loss: 0.1169 - accuracy: 0.7000

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Parâmetros

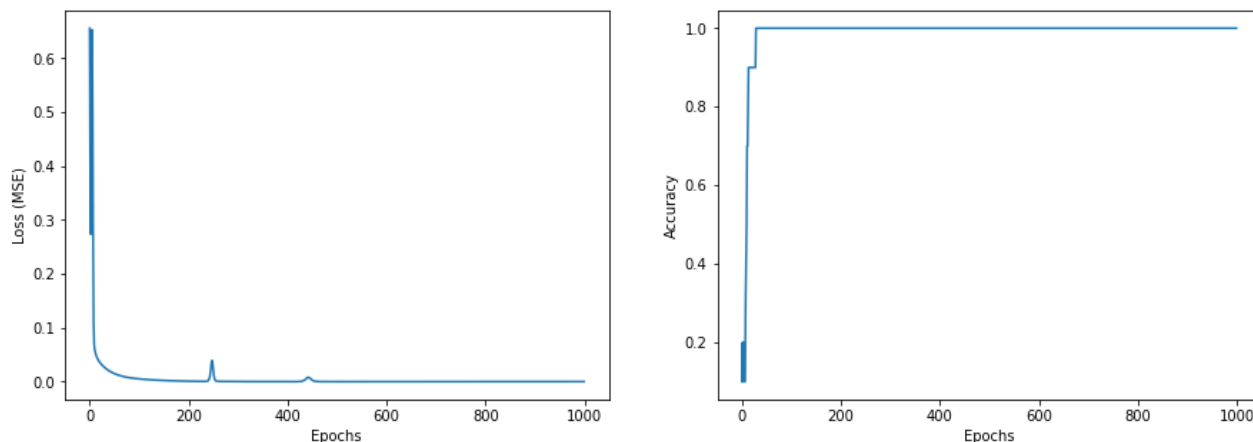
Hidden layer: 15, (tanh)

Output layer: 10, (linear)

Learning Rate: 0.9

Momentum: 0

Training loss (MSE) and accuracy



Final training loss (MSE): 0.00013518193736672401

Final training accuracy: 1.0

Teste nos números com bits errados

1 bit errado:

1/1 - 0s - loss: 0.0404 - accuracy: 0.9000

2 bit errado:

1/1 - 0s - loss: 0.0675 - accuracy: 0.9000

3 bit errado:

1/1 - 0s - loss: 0.0976 - accuracy: 0.7000

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Parâmetros

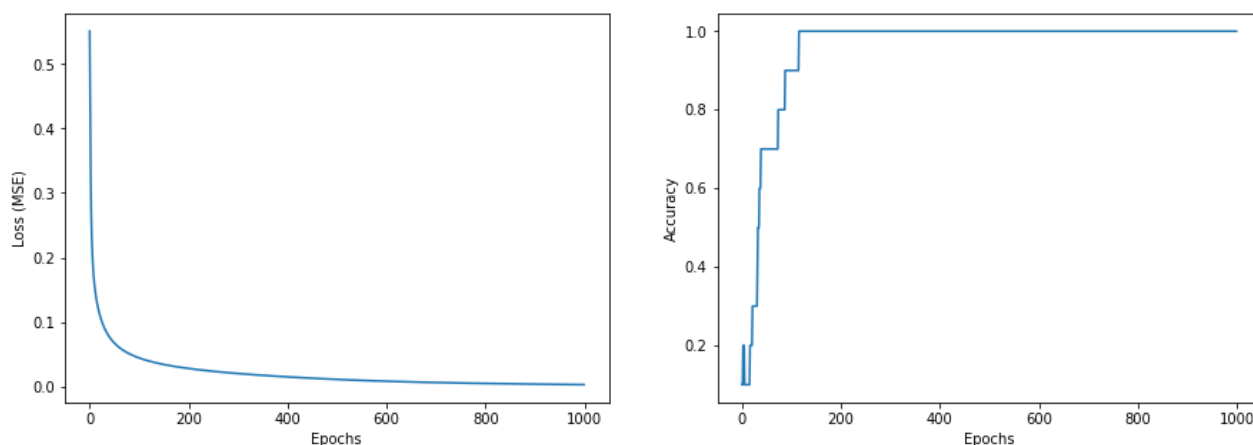
Hidden layer: 15, (tanh)

Output layer: 10, (linear)

Learning Rate: 0.1

Momentum: 0.4

Training loss (MSE) and accuracy



Final training loss (MSE): 0.002740252995863557

Final training accuracy: 1.0

Teste nos números com bits errados

1 bit errado:

1/1 - 0s - loss: 0.0463 - accuracy: 1.0000

2 bit errado:

1/1 - 0s - loss: 0.0722 - accuracy: 0.9000

3 bit errado:

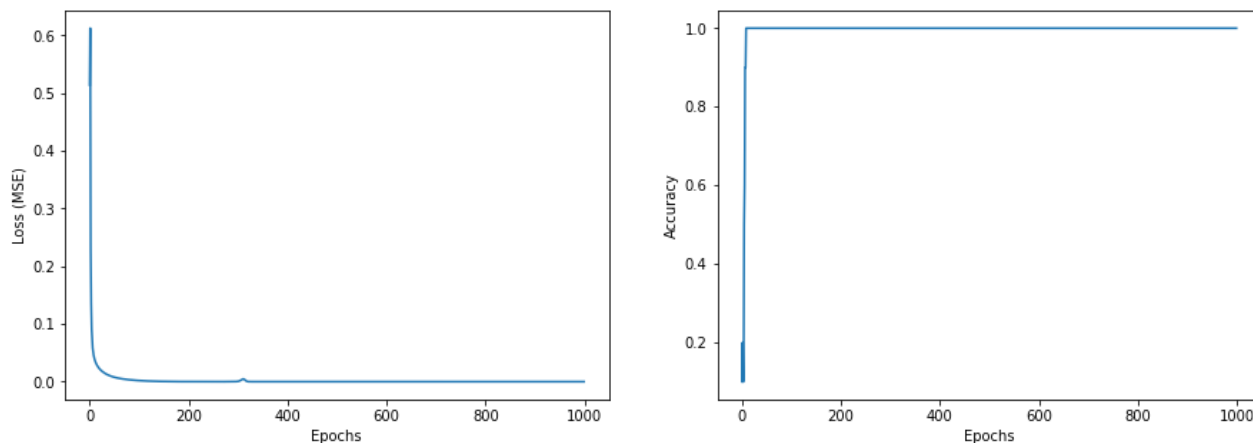
1/1 - 0s - loss: 0.0825 - accuracy: 0.7000

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Parâmetros

Hidden layer: 15, (tanh)
 Output layer: 10, (linear)
 Learning Rate: 0.9
 Momentum: 0.4

Training loss (MSE) and accuracy



Final training loss (MSE): 1.205334795731719e-13
 Final training accuracy: 1.0

Teste nos números com bits errados

1 bit errado:
 1/1 - 0s - loss: 0.0438 - accuracy: 0.9000

2 bit errado:
 1/1 - 0s - loss: 0.1100 - accuracy: 0.7000

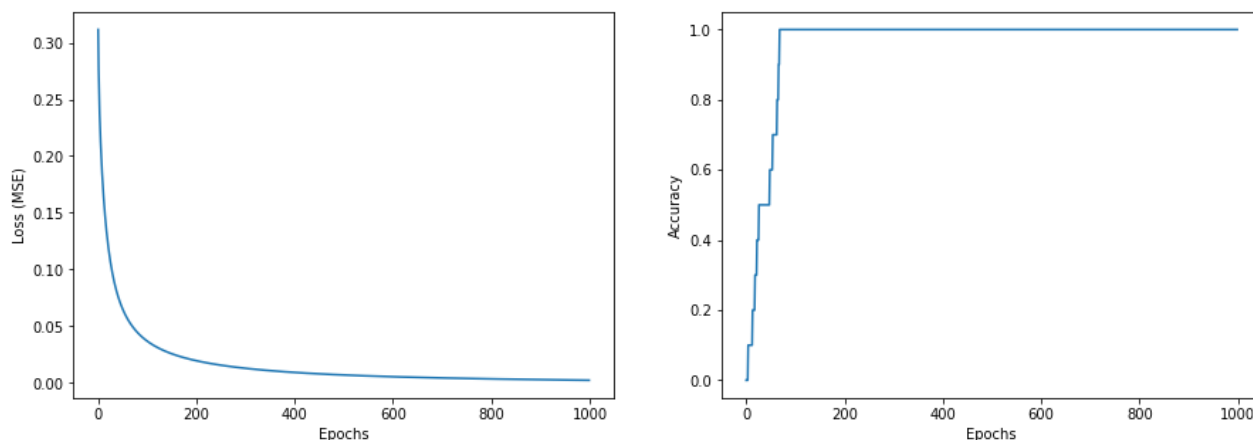
3 bit errado:
 1/1 - 0s - loss: 0.1508 - accuracy: 0.7000

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```
In [13]: for lr, momentum in parameters:
          build_and_evaluate_nn(25, 'tanh', 10, 'linear', lr=lr, momentum=momentum)
```

Parâmetros
 Hidden layer: 25, (tanh)
 Output layer: 10, (linear)
 Learning Rate: 0.1
 Momentum: 0

Training loss (MSE) and accuracy



Final training loss (MSE): 0.0023930338211357594

Final training accuracy: 1.0

Teste nos números com bits errados

1 bit errado:

1/1 - 0s - loss: 0.0430 - accuracy: 1.0000

2 bit errado:

1/1 - 0s - loss: 0.0689 - accuracy: 0.9000

3 bit errado:

1/1 - 0s - loss: 0.0914 - accuracy: 0.8000

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Parâmetros

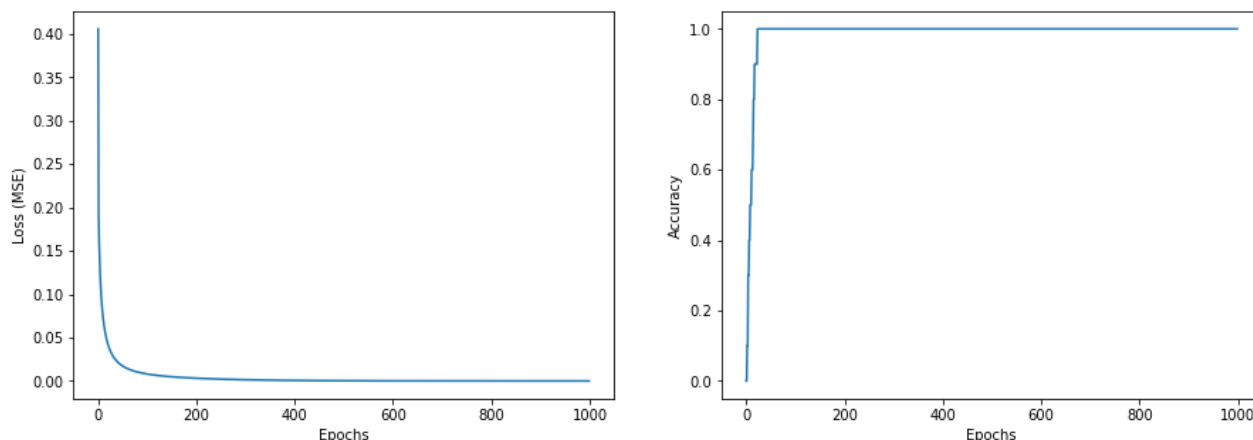
Hidden layer: 25, (tanh)

Output layer: 10, (linear)

Learning Rate: 0.4

Momentum: 0

Training loss (MSE) and accuracy



Final training loss (MSE): 1.476572037972801e-06

Final training accuracy: 1.0

Teste nos números com bits errados

1 bit errado:

1/1 - 0s - loss: 0.0773 - accuracy: 0.8000

2 bit errado:

1/1 - 0s - loss: 0.1270 - accuracy: 0.5000

3 bit errado:

1/1 - 0s - loss: 0.1545 - accuracy: 0.6000

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Parâmetros

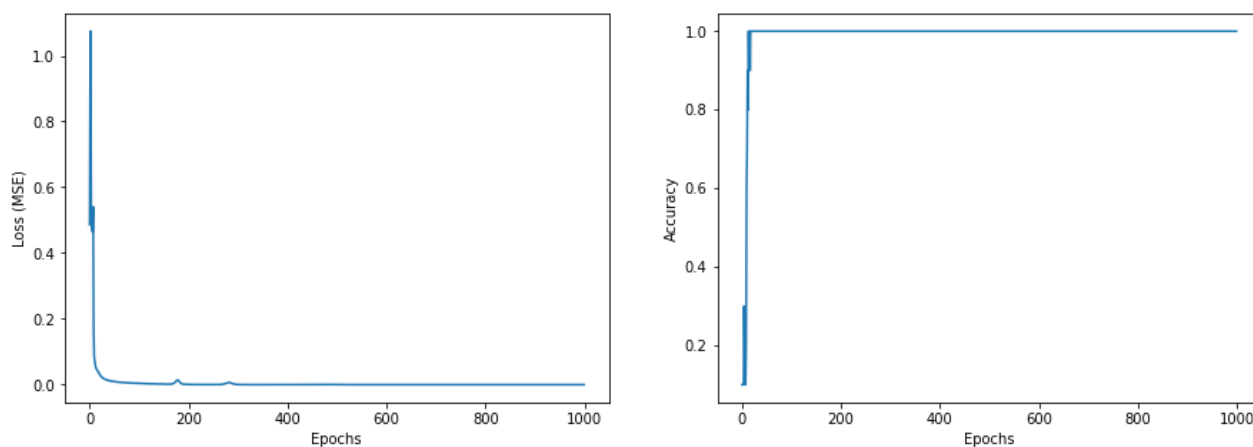
Hidden layer: 25, (tanh)

Output layer: 10, (linear)

Learning Rate: 0.9

Momentum: 0

Training loss (MSE) and accuracy



Final training loss (MSE): 8.184719568760102e-10

Final training accuracy: 1.0

Teste nos números com bits errados

1 bit errado:

1/1 - 0s - loss: 0.0361 - accuracy: 1.0000

2 bit errado:

1/1 - 0s - loss: 0.0702 - accuracy: 0.9000

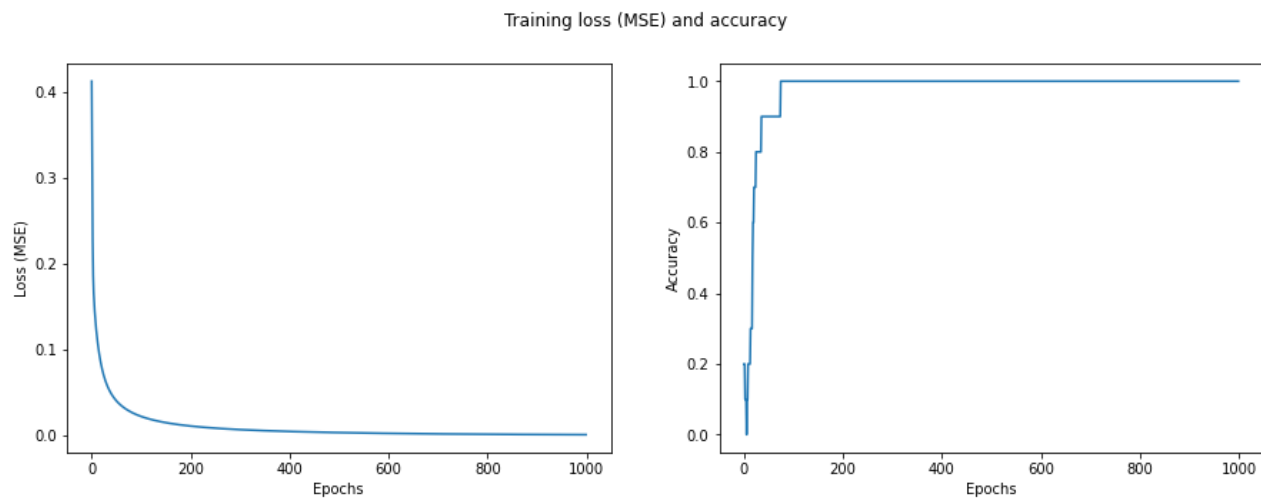
3 bit errado:

1/1 - 0s - loss: 0.0728 - accuracy: 0.8000

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Parâmetros

Hidden layer: 25, (tanh)
Output layer: 10, (linear)
Learning Rate: 0.1
Momentum: 0.4



Final training loss (MSE): 0.00031166954431682825
Final training accuracy: 1.0

Teste nos números com bits errados

1 bit errado:
1/1 - 0s - loss: 0.0374 - accuracy: 1.0000

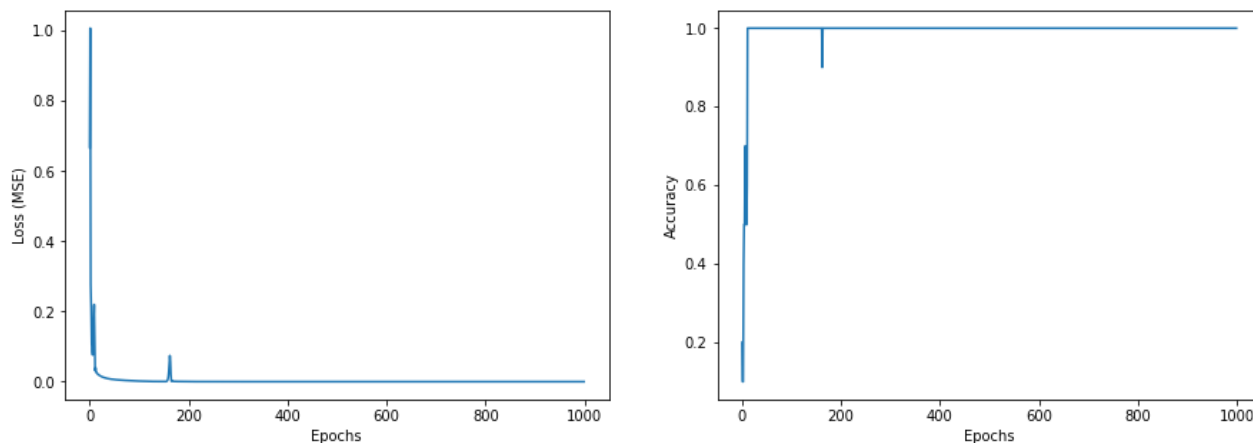
2 bit errado:
1/1 - 0s - loss: 0.0721 - accuracy: 0.8000

3 bit errado:
1/1 - 0s - loss: 0.0723 - accuracy: 0.7000

#####

Parâmetros
Hidden layer: 25, (tanh)
Output layer: 10, (linear)
Learning Rate: 0.9
Momentum: 0.4

Training loss (MSE) and accuracy



Final training loss (MSE): 3.12565897914608e-14

Final training accuracy: 1.0

Teste nos números com bits errados

1 bit errado:

1/1 - 0s - loss: 0.0465 - accuracy: 0.9000

2 bit errado:

1/1 - 0s - loss: 0.0792 - accuracy: 0.8000

3 bit errado:

1/1 - 0s - loss: 0.1103 - accuracy: 0.7000

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In [14]: for lr, momentum in parameters:
          build_and_evaluate_nn(35, 'tanh', 10, 'linear', lr=lr, momentum=momentum)
```

Parâmetros

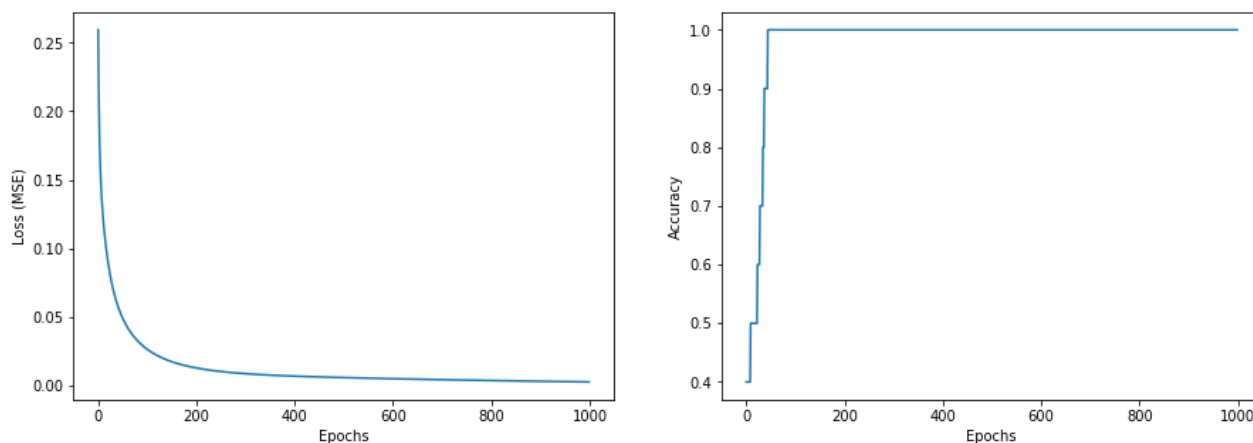
Hidden layer: 35, (tanh)

Output layer: 10, (linear)

Learning Rate: 0.1

Momentum: 0

Training loss (MSE) and accuracy



Final training loss (MSE): 0.0022911611013114452
Final training accuracy: 1.0

Teste nos números com bits errados

1 bit errado:
1/1 - 0s - loss: 0.0377 - accuracy: 0.9000

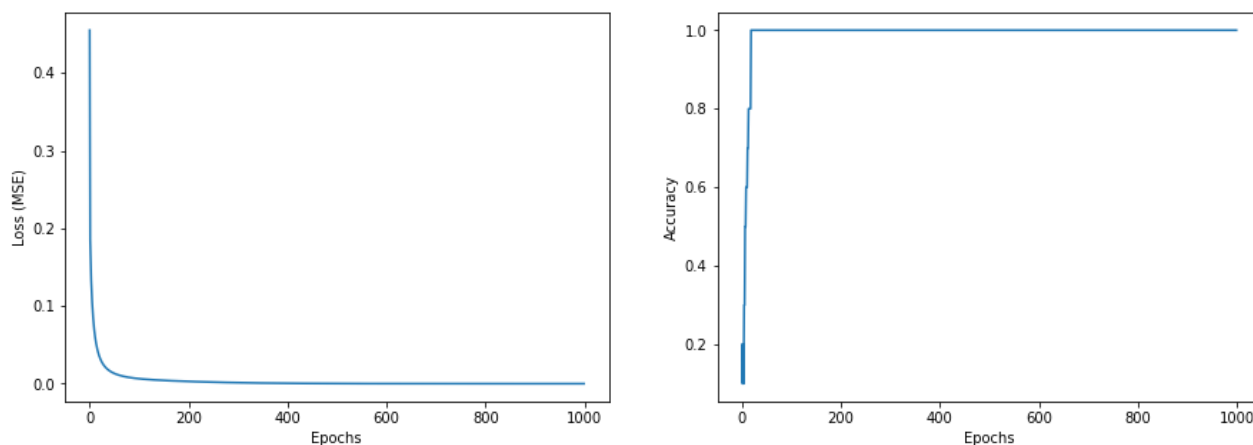
2 bit errado:
1/1 - 0s - loss: 0.0850 - accuracy: 0.8000

3 bit errado:
1/1 - 0s - loss: 0.1116 - accuracy: 0.8000

#####

Parâmetros
Hidden layer: 35, (tanh)
Output layer: 10, (linear)
Learning Rate: 0.4
Momentum: 0

Training loss (MSE) and accuracy



Final training loss (MSE): 9.131940714723896e-07
Final training accuracy: 1.0

Teste nos números com bits errados

1 bit errado:
1/1 - 0s - loss: 0.0622 - accuracy: 0.9000

2 bit errado:
1/1 - 0s - loss: 0.1133 - accuracy: 0.8000

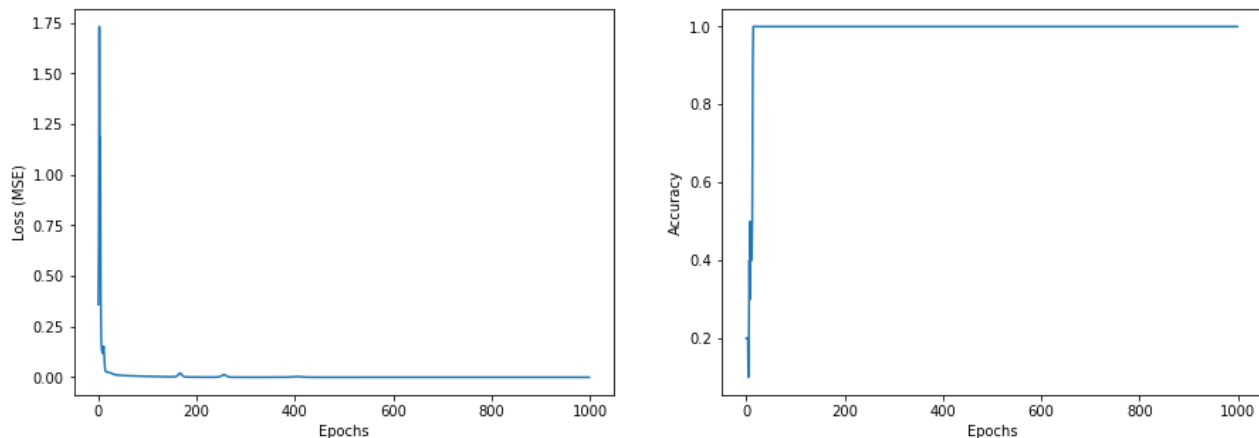
3 bit errado:
1/1 - 0s - loss: 0.1489 - accuracy: 0.6000

#####

Parâmetros

Hidden layer: 35, (tanh)
Output layer: 10, (linear)
Learning Rate: 0.9
Momentum: 0

Training loss (MSE) and accuracy



Final training loss (MSE): 2.693912392714992e-06

Final training accuracy: 1.0

Teste nos números com bits errados

1 bit errado:

1/1 - 0s - loss: 0.0332 - accuracy: 1.0000

2 bit errado:

1/1 - 0s - loss: 0.0537 - accuracy: 1.0000

3 bit errado:

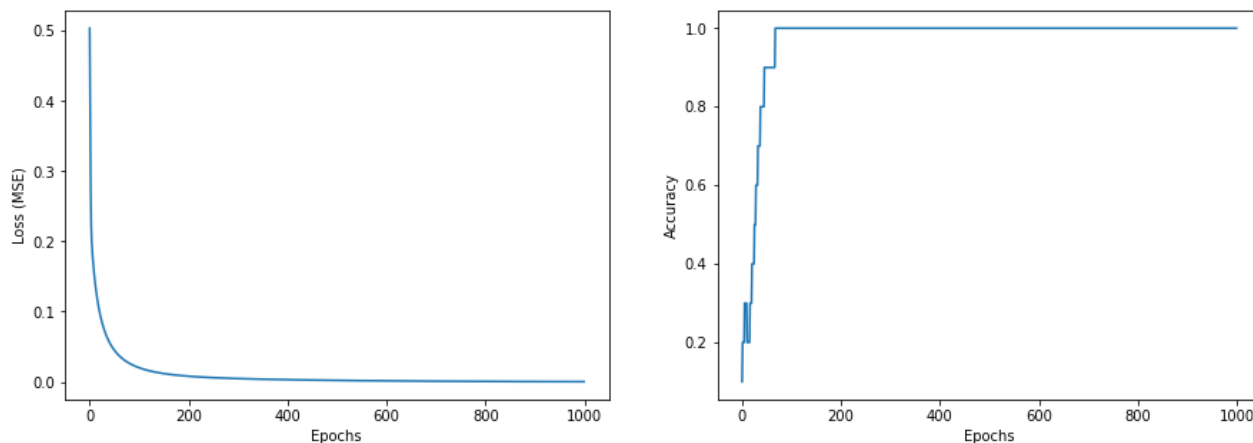
1/1 - 0s - loss: 0.0695 - accuracy: 0.8000

#####

Parâmetros

Hidden layer: 35, (tanh)
Output layer: 10, (linear)
Learning Rate: 0.1
Momentum: 0.4

Training loss (MSE) and accuracy



Final training loss (MSE): 0.00022103285300545394

Final training accuracy: 1.0

Teste nos números com bits errados

1 bit errado:

1/1 - 0s - loss: 0.0418 - accuracy: 0.9000

2 bit errado:

1/1 - 0s - loss: 0.0917 - accuracy: 0.8000

3 bit errado:

1/1 - 0s - loss: 0.1085 - accuracy: 0.8000

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Parâmetros

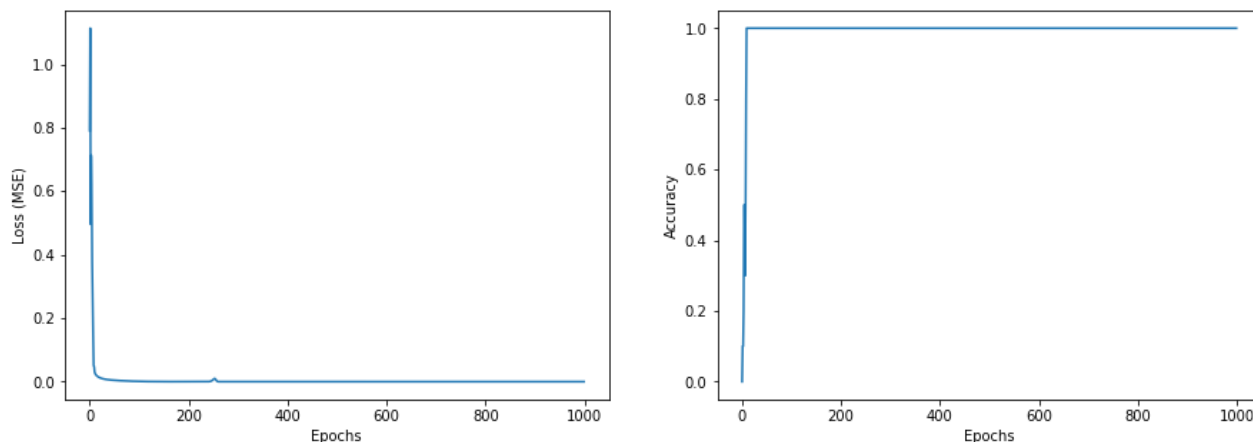
Hidden layer: 35, (tanh)

Output layer: 10, (linear)

Learning Rate: 0.9

Momentum: 0.4

Training loss (MSE) and accuracy



Final training loss (MSE): 1.889589220228742e-14

Final training accuracy: 1.0

Teste nos números com bits errados

1 bit errado:

1/1 - 0s - loss: 0.0451 - accuracy: 0.9000

2 bit errado:

1/1 - 0s - loss: 0.0839 - accuracy: 0.9000

3 bit errado:

1/1 - 0s - loss: 0.1015 - accuracy: 1.0000

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In []: