

# MECH 570C-FSI: Coding Project 1

## Fluid-structure interaction of a rigid circular cylinder

Winter Term 2, Year 2021-2022

The assignment will help build fundamentals for the fluid-structure interaction problem for a canonical problem of vortex-induced vibration by flow across a smooth circular cylinder. The fluid is modeled by the incompressible two-dimensional Navier-Stokes equations written in the arbitrary Lagrangian-Eulerian (ALE) framework. The rigid body structure with two degrees-of-freedom translation is solved in the Lagrangian description. The velocity continuity and the traction equilibrium is satisfied at the fluid-structure interface. The given code in MATLAB consists of the following functions:

1. `navierStokes.m`: Solves the Navier-Stokes equations in the ALE framework with generalized- $\alpha$  time integration written in predictor-corrector format. The different terms in the variational form of the Navier-Stokes equations are in turn specified in the following functions:
  - `GalerkinTerms.m`
  - `PetrovGalerkinTerms1.m`
  - `PetrovGalerkinTerms2.m`
  - `PetrovGalerkinTerms3.m`
2. `rigidBody.m`: Solves the rigid body equation by the generalized-  $\alpha$  time integration.
3. `IntegratedOutput.m`: Calculate the integrated traction values at the fluid-structure interface which is then transferred to the structural equation.
4. `aleMesh.m`: Solves the ALE mesh Laplace equation to move the fluid mesh nodes.

The problem definition and the sequence of solution is written in `main.m`. The assignment consists of the following parts:

1. Read through the implementation and understand the data structures and the sequence of data transfer.
2. The function `IntegratedOutput.m` is incomplete with respect to the evaluation of the traction forces along the fluid-structure interface. Complete the function and validate the solver (without any ALE mesh movement) for flow over stationary cylinder at Reynolds number of  $Re = (\rho^f U_\infty D / \mu^f) = 100$ , where  $\rho^f$  and  $\mu^f$  are the density and dynamic viscosity of the fluid,  $U_\infty$  is the freestream velocity and  $D$  is the diameter of the cylinder. Plot the temporal variation of the lift and drag coefficients for the time steps of around 2000 with  $\Delta t = 0.1$  and find out the mean drag and root mean square and maximum lift coefficients. The validation values are the following:  $\bar{C}_D = 1.375$ ,  $C_l^{\max} = 0.3352$  and  $\bar{C}_l^{\text{rms}} = 0.2368$  (about mean).
3. After validating the stationary circular cylinder problem, write the function `aleMesh.m` which will solve the ALE mesh Laplace equation to compute the ALE displacements and velocity for the fluid nodes. The variable for ALE displacement and velocity are `Sol.aleDisp` and `Sol.aleVel` respectively. Note that `Sol.aleVel = (Sol.aleDisp - Sol.aleDispPrev)/solver.dt`. You can get some help in writing the function by the HINT file provided for solving a 2D Poisson equation for a scalar (`Poisson2D.m`).
4. Once the ALE mesh equation is implemented correctly, run a case of two degrees-of-freedom VIV of the cylinder with no damping coefficient at  $Re = 200$  with mass ratio,  $m^* = 4m / (\rho^f \pi D^2) = 10$ , reduced velocity  $U_r = U_\infty / (f_n D) = 5$ , where  $m$  is the mass of the cylinder and  $f_n = (1/2\pi)\sqrt{k/m}$  is the natural frequency of the elastically mounted cylinder with  $k = k_x = k_y$  being the stiffness of the spring. The results can be

compared to the computations carried out in Table 1 of the following paper:

”On the vortex-induced oscillations of a freely vibrating cylinder in the vicinity of a stationary plane wall,” L. Zhong, W. Yao, K. Yag, R. Jaiman, B. C. Khoo, Journal of Fluids and Structures, 65, Pg. 495-526 (2016).

Grading breakdown of this coding Project 1:

- Coding and debugging (60%): As described earlier, you need to program and debug your new codes systematically.
- Verification and validation (20%): You need to perform a systematic mesh convergence and comparison of your numerical solutions with the reference data.
- Project report (20%): In the report, you need to provide the description of FSI methodology, numerical implementation details, FSI coupling strategy. You need to critically summarize what has been done and what you learned.