MECH 570C Code Project 1

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1 InO

2 N-S

Function Definition

 $\rho u_t + \rho u.divu - div(mu * gradu) + gradp = fin\Omega$, divu = 0 in Ω , Dirichlet boundary condition $u = g_D on\Gamma_D$, Neumann boundary condition $du/dn - np = g_N on\Gamma_N$.

• Function Name: navierStokes

• Inputs:

- solver, fluid, pmc: Structures containing various solver settings, fluid properties, and numerical method parameters.
- Sol: Structure holding the solution vectors.
- cnn, crd: Connectivity and coordinate matrices for the mesh.
- elemType, ndof, nen, nElem, BCCyl: Parameters defining the type of elements used, degrees of freedom, number of nodes per element, total number of elements, and boundary condition information.

Quadrature Rules

- Sets up quadrature points (gP) and weights (gW) based on the element type (triangular or quadrilateral). These are used for numerical integration.
- Defines shape functions (N) and their derivatives (Nx, Ny) for the finite elements.

Boundary Conditions

• Applies Dirichlet and Neumann boundary conditions to the solution vector Sol.u.

Interpolation for Alpha Values

• Interpolates values for the generalized-alpha method, a numerical technique for time integration in transient problems.

Navier-Stokes Equations

• Prepares variables (xxf, yyf, ux, uy, etc.) for assembling the finite element matrices. These include coordinates, velocities, pressure, and additional variables.

Assembly of Galerkin and Petrov-Galerkin Terms

- Calls functions to form the left-hand side (LHS) and right-hand side (RHS) of the Navier-Stokes equations. This involves complex operations based on the finite element method.
- The Galerkin method is used for discretizing the problem, while Petrov-Galerkin is an enhanced approach for stability and accuracy.

Solving the Linear System

- Determines the free nodes not constrained by boundary conditions.
- Solves the linear system for the unknowns (Increment) using the assembled LHS and RHS.

Update and Output

- Updates the solution vectors (Sol.u, Sol.uDot, Sol.p) with the new increments.
- Calculates a norm (NSnormIndicator) to indicate the convergence or error of the current iteration.
- Outputs the updated solution structure Sol and the convergence/error indicator.

Summary of Data Flow

- 1. **Input Processing:** Takes in initial conditions, mesh information, and solver parameters.
- 2. **Setup:** Establishes quadrature rules and boundary conditions.
- 3. **Equation Assembly:** Forms the Navier-Stokes equations using finite element discretization.
- 4. **Solution Update:** Solves for increments and updates the solution.
- 5. Output: Returns the updated solution and a convergence/error metric.

3 Integraded Output

Function Definition

- Function Name: IntegratedOutput
- Inputs:
 - Sol: A structure containing the solution vectors (velocity, pressure, etc.).
 - crd: The coordinates of the mesh nodes.
 - BCCyl: Boundary condition data.
 - fluid: A structure containing fluid properties.
 - cnn: Connectivity matrix for the mesh elements.

Initialization

- Sets the number of element nodes (nen) for a 2D element (4 for a quadrilateral element).
- Swaps the columns of BCCyl for further processing.
- Determines the number of elements (nElem) and degrees of freedom (ndof) involved in the boundary condition.

Boundary Layer Elements

- Identifies elements corresponding to the first layer of the boundary using cnn and BCCyl.
- Reorders the element points for reduced integration.

Quadrature Integration Setup

- Defines Gauss points (gP) and weights (gW) for numerical integration.
- Sets up shape functions (N) and their derivatives (Nx, Ny).

Localizing Data

• Extracts local coordinates (xxf, yyf), velocities (ux, uy), and pressure (pres) for each element.

Integration Process

- Loops over quadrature points to:
 - Calculate the Jacobian matrix J for coordinate transformation.
 - Compute the volume and normal vectors for each element.
 - Evaluate pressure and velocity gradients (locgradUx, locgradUy, locgradVx, locgradVy).
 - Compute the length/area (A0) of the line/surface integral.

Calculation of Forces

- The loop sums up the contributions from all quadrature points to calculate the integrated force over the element surface.
- The force components (X and Y directions) are to be computed within the loop (currently not implemented in the provided code).

Output

• Returns the total length of the integrated area (Length) and the force components (Force).