

# The Constellation Token Model

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## Abstract

We propose the Constellation Token Model, a distributed consensus protocol governed by model that achieves equilibria irrespective of speculative market fluctuations.

## Introduction

A Generative Economy is a living economy that is designed to generate the conditions for life to thrive, an economy with a built-in tendency to be socially fair and ecologically sustainable <sup>1</sup>. This definition could be paraphrased as essentially a game where the rules of play enforce certain invariants, the result of which is emergent stabilization. Essentially, the act of playing the game itself is what enforces the invariant. Distributed consensus protocols, and the currencies they support, can be modeled as generative economies. Network stability is governed by eventually consistent equilibrium and equilibrium is defined in terms of invariant measures (we want to enforce that something doesn't change, or can be relied upon) that are maintained. Why do we need this? It allows for the the enforcement of real world performance specifics that are decoupled from external market dynamics (gas/exchange prices) which allows for technology focused adoption while also providing an external speculation market similar to traditional commodities markets.

## Constellation Economics

Consensus protocols exist to provide a utility and that utility is the basis of a generative economic game. In Constellation, that utility is throughput. Like all

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<sup>1</sup>Kelly, Marjorie, "Toward A Generative Economy"  
<https://www.opendemocracy.net/ourkingdom/marjorie-kelly/toward-generative-economy>

consensus protocols, access to rewards is governed by delegate selection. In turn delegate selection is governed by a seeder/leacher ratio of transactions validated vs transactions submitted. We will use the term 'utility ratio' to describe the throughput a potential delegate has provided vs the throughput used. As nodes play they get ranked based on their utility ratio. Based on ranks they get access to rewards. Fees are charged relative to the scarcity of the utility that the protocol provides and are only charged if an account breaches its allotted utility ratio. The \$DAG token acts as an inflation mechanism like cash, which can be used to pay transaction fees when an account has not or can not maintain their required utility ratio. \$DAG is injected into the pool of validator rewards, and there is incentive to validate transactions that have an accompanying fee attached. Holders of the token assume the role of central bank, deploying \$DAG capital with the understanding that the free market dynamics of the protocol will ensure their account gets access to the network utility when capital is deployed.

Reputation is a unit that represents a 'stake' of total network utility (throughput). It is a perishable good in the constellation economy as accounts that leave the network will watch their reputation recede until 0 and they are replaced by a new player. Accounts' reputation is varying and falls according to various tiers which follow our definition of rank along with a branching factor.

## Equilibrium and Market Dynamics

Constellation's value can be thought of as stake within a total computational space. Constellation's data model was designed to follow combinatorial models in distributed computing, where network state can be described in terms of simplicial geometry and transitions are defined in terms of a discrete gradient. The value of our network derives from the total computational space available for verifying transactions i.e. its maximum throughput. We can loosely model the total computational space as the volume of 'space' across nodes with respect to rank  $r$

$$\int_M \epsilon_1 \wedge \dots \wedge \epsilon_r$$

where  $M$  is a manifold,  $\epsilon$  is the sheaf of the vector space of rank  $r$ . Within our model this would be explicitly defined as the numerical integration over the outer product of our cohomological definition<sup>2</sup> which is a vector space given by the tensor product of each space across ranks

$$\sum_{1 \dots r} \Gamma^{\epsilon_1} \otimes \dots \otimes \Gamma^{\epsilon_r}$$

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<sup>2</sup><https://arxiv.org/abs/1805.07047>

Figure 1: We need two figures, One of the tiered cluster hierarchy and another top down look at the graph showing 'constellations' notes separated by tiers of rep score. Looks like gravity

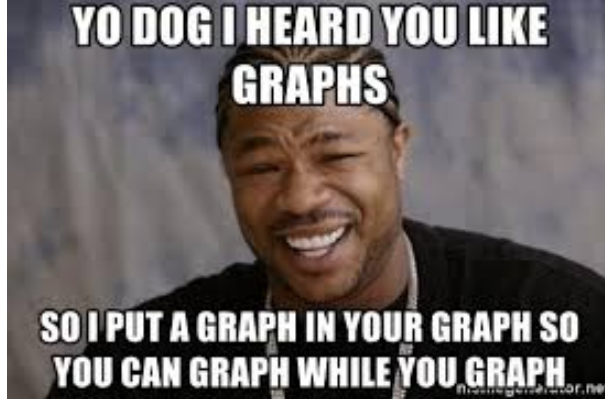
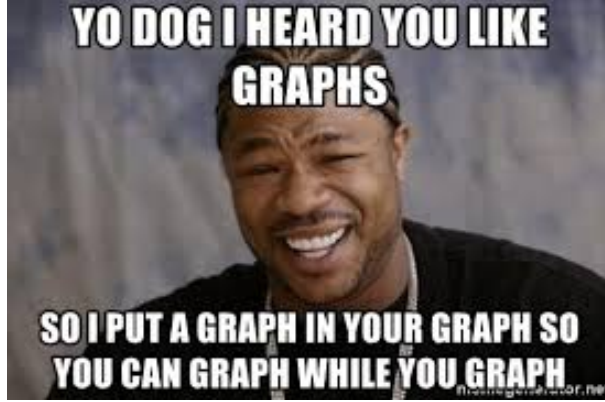


Figure 2: Formulate a ringed space as a hashmap and how each key is like a basis. If there are collisions there is like a singularity that appears. Sheaves are like subsets of the hashmap and represents the newest state of the partition of unity (sheaves are charts)



where each  $\Gamma^\epsilon$  is a manifold corresponding to a rank in the differential form above, subordinate to the rank before it. If we define bandwidth (fiber/sec) as the total space<sup>3</sup> of the resources given by each node

$$B_{(fiber/sec)} = \sum_r \int \rho_i \theta_i \omega$$

where  $\rho_i$  is a partition of unity and  $\theta_i$  is a discrete diffeomorphism (protocol)

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<sup>3</sup>sec 9.2 [ftp.cis.upenn.edu/pub/cis610/public\\_html/diffgeom4.pdf](http://ftp.cis.upenn.edu/pub/cis610/public_html/diffgeom4.pdf)

on our r-form  $\omega$  and fibers are Signed Observation Edges<sup>4</sup> of our data model. (make sure to elaborate that the total space is made up of all actions and the diffeomorphism itself is what determines the solution plane once we solidify into a snapshot. It is essentially a cut on the graph where we keep a subset of bundles not cut as tips new bundles are latched on. The diffeomorphism

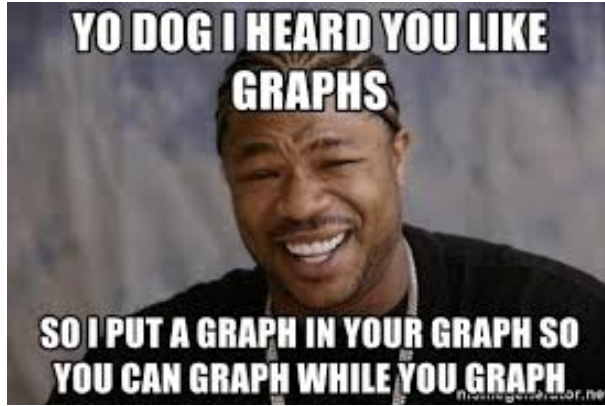
The actual value of our network can be described as the cost to host the resources each node provides.

$$R_{(\frac{s}{sec})} = \sum_r \int \rho_i T_i \omega$$

This is a slight modification to our definition of bandwidth above by replacing  $\theta$  with  $T$  a mapping to instance types and cost. The total space of all value per node is given by the product of  $R$  and  $B$ , however in order to give a some measure of performance, we can do this by mapping each entry in the bandwidth space to it's normalized Shannon entropy (bits), giving us a measure of relative information gain to cost.

$$S_{(\frac{bits * s}{sec})} = B_{entropy} \oplus R = (\sum_r \int \rho_i H_i \omega) \oplus R$$

Figure 3: Show how the dag gets quilted an how agreed data adds negentropy while disagreed data causes entropy. Use this to quantify a node's shannon entropy (coloring subgraph of each node within the total space of all observations? highlight paths)



where  $H$  is our normalized Shannon entropy

$$H_n(p) = - \sum_i \frac{p_i \log_b p_i}{\log_b n}$$

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<sup>4</sup>link to arch blog post

and  $p$  is a probability measure of how the result of a node's actions deviate from the acceptable state of the protocol and  $b$  is our base, bits in the case of Shannon entropy. Deficiency in entropy can be seen as a measure of efficiency. We want to use normalized entropy as using normal Shannon entropy scales with sample size.