

Predictions

Jeff Walker

Jeff Walker

1/30/2015

- 1 Get Data
- 2 Run Predictions
- 3 Prediction Function
 - 3.1 Conditional Coefficients
 - 3.2 Prepare Input Values
 - 3.3 Compute Predicted Temperature
 - 3.4 prepConditionalCoef() Function
- 4 Model Details
 - 4.1 Model Theory
 - 4.2 Sets of Coefficients
 - * 4.2.1 Fixed Effects
 - * 4.2.2 HUC Effects
 - * 4.2.3 Site Effects
 - * 4.2.4 Year Effects
 - 4.3 Sum All Effects
- 5 Example Predictions for 2006

1 Get Data

```
## Source: local data frame [6 x 7]
##
##   location_id      location_name featureid latitude longitude
## 1      1473             S-1019         NA 46.74704 -67.97143
## 2      1474             S-1016         NA 46.67041 -68.01328
## 3      1428           Finney Brook    833458 42.45973 -72.69103
## 4      1427           99999999    805717 43.18900 -71.47800
## 5      1454      Avery Brook, upper    833141 42.46538 -72.71110
## 6      1452 Obear Brook, below Webber Rd    834183 42.43242 -72.67777
## Variables not shown: agency_name (chr), site (chr)
```

Select a location for making predictions.

```
## [1] 830189
```

Retrieve daymet data for select catchment.

```
##      featureid      date      tmax      tmin
## Min. :830189 Min. :1980-01-01 Min. : -19.25 Min. : -32.000
## 1st Qu.:830189 1st Qu.:1988-07-01 1st Qu.:  5.00 1st Qu.: -4.750
## Median :830189 Median :1996-12-31 Median : 14.50 Median :  2.000
## Mean :830189 Mean :1996-12-31 Mean : 13.82 Mean :  1.978
## 3rd Qu.:830189 3rd Qu.:2005-07-01 3rd Qu.: 23.25 3rd Qu.: 10.250
## Max. :830189 Max. :2013-12-31 Max. : 35.25 Max. : 21.750
##      prcp      dayl      srad      vp
## Min. : 0.000 Min. :32141 Min. : 35.2 Min. : 40.0
## 1st Qu.: 0.000 1st Qu.:35597 1st Qu.:216.0 1st Qu.: 440.0
## Median : 0.000 Median :43200 Median :315.2 Median : 720.0
## Mean : 3.472 Mean :43200 Mean :321.0 Mean : 857.5
## 3rd Qu.: 3.000 3rd Qu.:50803 3rd Qu.:427.2 3rd Qu.:1260.0
## Max. :132.500 Max. :54259 Max. :697.6 Max. :2600.0
##      swe      site      airTemp
## Min. : 0.00 Length:12410 Min. : -23.250
## 1st Qu.: 0.00 Class :character 1st Qu.:  0.125
## Median : 0.00 Mode :character Median :  8.250
## Mean : 26.96 Mean :  7.900
## 3rd Qu.: 40.00 3rd Qu.: 16.625
## Max. :248.00 Max. : 27.875
```

Get the covariates for the selected catchment

```
## Observations: 1
## Variables:
## $ featureid (int) 830189
## $ zone (chr) "upstream"
## $ AreaSqKM (dbl) 2.979
## $ agriculture (dbl) 12.6284
## $ alloffnet (dbl) 2.99094
## $ allonnet (dbl) 3.89728
## $ devel_hi (dbl) 0
## $ devel_low (dbl) 0.543807
## $ devel_med (dbl) 0
## $ devel_opn (dbl) 6.19335
## $ developed (dbl) 6.73716
## $ elev_nalcc (dbl) 282.097
## $ forest (dbl) 79.1238
## $ forest_decid (dbl) 16.5559
## $ forest_evgrn (dbl) 25.8912
## $ forest_mixed (dbl) 37.9758
## $ fwswetlands (dbl) 6.67674
## $ herbaceous (dbl) 0.21148
## $ surfcoarse (dbl) 0
## $ water (dbl) 0
## $ wetland (dbl) 11.2689
```

Get spring/fall breakpoints

```
##      Spring      Fall
## 89.78214 311.69958
```

Join climate data, covariates, observed stream temperature, huc8, lat/lon, spring/fall breakpoints and add dOY. Then filter dataset to be within spring/fall breakpoints.

```
##      featureid      date      tmax      tmin
## Min.      :830189  Min.      :1980-03-30  Min.      :-6.75  Min.      :-12.000
## 1st Qu.:830189  1st Qu.:1988-07-09  1st Qu.:16.00  1st Qu.: 3.000
## Median :830189  Median :1996-10-19  Median :21.50  Median : 8.500
## Mean   :830189  Mean   :1996-12-31  Mean   :20.61  Mean   : 8.079
## 3rd Qu.:830189  3rd Qu.:2005-06-25  3rd Qu.:26.00  3rd Qu.:13.000
## Max.   :830189  Max.   :2013-11-07  Max.   :35.25  Max.   :21.750
##
##      prcp      dayl      srad      vp
## Min.      : 0.000  Min.      :35251  Min.      : 48.0  Min.      : 240
## 1st Qu.: 0.000  1st Qu.:44582  1st Qu.:278.4  1st Qu.: 760
## Median : 0.000  Median :49421  Median :377.6  Median :1120
## Mean   : 3.637  Mean   :48015  Mean   :366.1  Mean   :1163
## 3rd Qu.: 3.500  3rd Qu.:52877  3rd Qu.:456.0  3rd Qu.:1480
## Max.   :132.500  Max.   :54259  Max.   :697.6  Max.   :2600
##
##      swe      site      airTemp      zone
## Min.      : 0.00  Length:7511  Min.      :-9.375  Length:7511
## 1st Qu.: 0.00  Class :character  1st Qu.: 9.625  Class :character
## Median : 0.00  Mode  :character  Median :15.000  Mode  :character
## Mean   :10.17  Mean   :14.342
## 3rd Qu.: 0.00  3rd Qu.:19.312
## Max.   :224.00  Max.   :27.875
##
##      AreaSqKM      agriculture      alloffnet      allonnet
## Min.      :2.979  Min.      :12.63  Min.      :2.991  Min.      :3.897
## 1st Qu.:2.979  1st Qu.:12.63  1st Qu.:2.991  1st Qu.:3.897
## Median :2.979  Median :12.63  Median :2.991  Median :3.897
## Mean   :2.979  Mean   :12.63  Mean   :2.991  Mean   :3.897
## 3rd Qu.:2.979  3rd Qu.:12.63  3rd Qu.:2.991  3rd Qu.:3.897
## Max.   :2.979  Max.   :12.63  Max.   :2.991  Max.   :3.897
##
##      devel_hi  devel_low      devel_med  devel_opn      developed
## Min.      :0  Min.      :0.5438  Min.      :0  Min.      :6.193  Min.      :6.737
## 1st Qu.:0  1st Qu.:0.5438  1st Qu.:0  1st Qu.:6.193  1st Qu.:6.737
## Median :0  Median :0.5438  Median :0  Median :6.193  Median :6.737
## Mean   :0  Mean   :0.5438  Mean   :0  Mean   :6.193  Mean   :6.737
## 3rd Qu.:0  3rd Qu.:0.5438  3rd Qu.:0  3rd Qu.:6.193  3rd Qu.:6.737
## Max.   :0  Max.   :0.5438  Max.   :0  Max.   :6.193  Max.   :6.737
##
##      elev_nalcc      forest      forest_decid      forest_evgrn
## Min.      :282.1  Min.      :79.12  Min.      :16.56  Min.      :25.89
## 1st Qu.:282.1  1st Qu.:79.12  1st Qu.:16.56  1st Qu.:25.89
## Median :282.1  Median :79.12  Median :16.56  Median :25.89
## Mean   :282.1  Mean   :79.12  Mean   :16.56  Mean   :25.89
## 3rd Qu.:282.1  3rd Qu.:79.12  3rd Qu.:16.56  3rd Qu.:25.89
## Max.   :282.1  Max.   :79.12  Max.   :16.56  Max.   :25.89
##
##      forest_mixed  fwswetlands      herbaceous      surfcoarse      water
## Min.      :37.98  Min.      :6.677  Min.      :0.2115  Min.      :0  Min.      :0
## 1st Qu.:37.98  1st Qu.:6.677  1st Qu.:0.2115  1st Qu.:0  1st Qu.:0
```

```

## Median :37.98 Median :6.677 Median :0.2115 Median :0 Median :0
## Mean :37.98 Mean :6.677 Mean :0.2115 Mean :0 Mean :0
## 3rd Qu.:37.98 3rd Qu.:6.677 3rd Qu.:0.2115 3rd Qu.:0 3rd Qu.:0
## Max. :37.98 Max. :6.677 Max. :0.2115 Max. :0 Max. :0
##
## wetland temp huc latitude
## Min. :11.27 Min. : 2.357 Length:7511 Min. :42.44
## 1st Qu.:11.27 1st Qu.:12.079 Class :character 1st Qu.:42.44
## Median :11.27 Median :16.430 Mode :character Median :42.44
## Mean :11.27 Mean :15.423 Mean :42.44
## 3rd Qu.:11.27 3rd Qu.:18.915 3rd Qu.:42.44
## Max. :11.27 Max. :23.514 Max. :42.44
## NA's :7045
## longitude year finalSpringBP sourceSpringBP
## Min. : -72.08 Min. :1980 Min. : 85.0 Length:7511
## 1st Qu.: -72.08 1st Qu.:1988 1st Qu.: 85.0 Class :character
## Median : -72.08 Median :1996 Median : 93.5 Mode :character
## Mean : -72.08 Mean :1996 Mean : 93.3
## 3rd Qu.: -72.08 3rd Qu.:2005 3rd Qu.:102.0
## Max. : -72.08 Max. :2013 Max. :102.0
## NA's :6882
## finalFallBP sourceFallBP dOY
## Min. :293.0 Length:7511 Min. : 90.0
## 1st Qu.:293.0 Class :character 1st Qu.:145.0
## Median :308.0 Mode :character Median :200.0
## Mean :308.5 Mean :200.4
## 3rd Qu.:323.0 3rd Qu.:256.0
## Max. :323.0 Max. :311.0
## NA's :6882

```

Rename some columns to match old variable names

Sort fullDataSync by site, year and dOY. Then compute lagged airTemp and prcp.

```

## featureid date tmax tmin
## Min. :830189 Min. :1980-03-30 Min. : -6.75 Min. : -12.000
## 1st Qu.:830189 1st Qu.:1988-07-09 1st Qu.:16.00 1st Qu.: 3.000
## Median :830189 Median :1996-10-19 Median :21.50 Median : 8.500
## Mean :830189 Mean :1996-12-31 Mean :20.61 Mean : 8.079
## 3rd Qu.:830189 3rd Qu.:2005-06-25 3rd Qu.:26.00 3rd Qu.:13.000
## Max. :830189 Max. :2013-11-07 Max. :35.25 Max. :21.750
##
## prcp dayl srad vp
## Min. : 0.000 Min. :35251 Min. : 48.0 Min. : 240
## 1st Qu.: 0.000 1st Qu.:44582 1st Qu.:278.4 1st Qu.: 760
## Median : 0.000 Median :49421 Median :377.6 Median :1120
## Mean : 3.637 Mean :48015 Mean :366.1 Mean :1163
## 3rd Qu.: 3.500 3rd Qu.:52877 3rd Qu.:456.0 3rd Qu.:1480
## Max. :132.500 Max. :54259 Max. :697.6 Max. :2600
##
## swe site airTemp zone
## Min. : 0.00 Length:7511 Min. : -9.375 Length:7511
## 1st Qu.: 0.00 Class :character 1st Qu.: 9.625 Class :character
## Median : 0.00 Mode :character Median :15.000 Mode :character

```

```

## Mean      : 10.17                      Mean      :14.342
## 3rd Qu.:  0.00                      3rd Qu.:19.312
## Max.      :224.00                    Max.      :27.875
##
## TotDASqKM      agriculture      alloffnet      allonnet
## Min.      :2.979  Min.      :12.63  Min.      :2.991  Min.      :3.897
## 1st Qu.:2.979  1st Qu.:12.63  1st Qu.:2.991  1st Qu.:3.897
## Median :2.979  Median :12.63  Median :2.991  Median :3.897
## Mean      :2.979  Mean      :12.63  Mean      :2.991  Mean      :3.897
## 3rd Qu.:2.979  3rd Qu.:12.63  3rd Qu.:2.991  3rd Qu.:3.897
## Max.      :2.979  Max.      :12.63  Max.      :2.991  Max.      :3.897
##
## devel_hi      devel_low      devel_med      devel_opn      developed
## Min.      :0  Min.      :0.5438  Min.      :0  Min.      :6.193  Min.      :6.737
## 1st Qu.:0  1st Qu.:0.5438  1st Qu.:0  1st Qu.:6.193  1st Qu.:6.737
## Median :0  Median :0.5438  Median :0  Median :6.193  Median :6.737
## Mean      :0  Mean      :0.5438  Mean      :0  Mean      :6.193  Mean      :6.737
## 3rd Qu.:0  3rd Qu.:0.5438  3rd Qu.:0  3rd Qu.:6.193  3rd Qu.:6.737
## Max.      :0  Max.      :0.5438  Max.      :0  Max.      :6.193  Max.      :6.737
##
## ReachElevationM      Forest      forest_decid      forest_evgrn
## Min.      :282.1  Min.      :79.12  Min.      :16.56  Min.      :25.89
## 1st Qu.:282.1  1st Qu.:79.12  1st Qu.:16.56  1st Qu.:25.89
## Median :282.1  Median :79.12  Median :16.56  Median :25.89
## Mean      :282.1  Mean      :79.12  Mean      :16.56  Mean      :25.89
## 3rd Qu.:282.1  3rd Qu.:79.12  3rd Qu.:16.56  3rd Qu.:25.89
## Max.      :282.1  Max.      :79.12  Max.      :16.56  Max.      :25.89
##
## forest_mixed      CONUSWetland      herbaceous      SurficialCoarseC
## Min.      :37.98  Min.      :6.677  Min.      :0.2115  Min.      :0
## 1st Qu.:37.98  1st Qu.:6.677  1st Qu.:0.2115  1st Qu.:0
## Median :37.98  Median :6.677  Median :0.2115  Median :0
## Mean      :37.98  Mean      :6.677  Mean      :0.2115  Mean      :0
## 3rd Qu.:37.98  3rd Qu.:6.677  3rd Qu.:0.2115  3rd Qu.:0
## Max.      :37.98  Max.      :6.677  Max.      :0.2115  Max.      :0
##
## water      wetland      temp      huc
## Min.      :0  Min.      :11.27  Min.      : 2.357  Length:7511
## 1st Qu.:0  1st Qu.:11.27  1st Qu.:12.079  Class :character
## Median :0  Median :11.27  Median :16.430  Mode  :character
## Mean      :0  Mean      :11.27  Mean      :15.423
## 3rd Qu.:0  3rd Qu.:11.27  3rd Qu.:18.915
## Max.      :0  Max.      :11.27  Max.      :23.514
##
## NA's      :7045
## Latitude      Longitude      year      finalSpringBP
## Min.      :42.44  Min.      :-72.08  Min.      :1980  Min.      : 85.0
## 1st Qu.:42.44  1st Qu.: -72.08  1st Qu.:1988  1st Qu.: 85.0
## Median :42.44  Median : -72.08  Median :1996  Median : 93.5
## Mean      :42.44  Mean      :-72.08  Mean      :1996  Mean      : 93.3
## 3rd Qu.:42.44  3rd Qu.: -72.08  3rd Qu.:2005  3rd Qu.:102.0
## Max.      :42.44  Max.      :-72.08  Max.      :2013  Max.      :102.0
##
## NA's      :6882
## sourceSpringBP      finalFallBP      sourceFallBP      d0Y
## Length:7511      Min.      :293.0  Length:7511      Min.      : 90.0

```

```

## Class :character 1st Qu.:293.0 Class :character 1st Qu.:145.0
## Mode :character Median :308.0 Mode :character Median :200.0
## Mean :308.5 Mean :200.4
## 3rd Qu.:323.0 3rd Qu.:256.0
## Max. :323.0 Max. :311.0
## NA's :6882
## ImpoundmentsAllSqKM count airTempLagged1 airTempLagged2
## Min. :11.61 Min. : 1 Min. : -9.375 Min. : -9.375
## 1st Qu.:11.61 1st Qu.:1878 1st Qu.: 9.625 1st Qu.: 9.625
## Median :11.61 Median :3756 Median :15.000 Median :15.000
## Mean :11.61 Mean :3756 Mean :14.343 Mean :14.344
## 3rd Qu.:11.61 3rd Qu.:5634 3rd Qu.:19.344 3rd Qu.:19.375
## Max. :11.61 Max. :7511 Max. :27.875 Max. :27.875
## NA's :1 NA's :2
## prcpLagged1 prcpLagged2 prcpLagged3
## Min. : 0.000 Min. : 0.000 Min. : 0.000
## 1st Qu.: 0.000 1st Qu.: 0.000 1st Qu.: 0.000
## Median : 0.000 Median : 0.000 Median : 0.000
## Mean : 3.637 Mean : 3.638 Mean : 3.638
## 3rd Qu.: 3.500 3rd Qu.: 3.500 3rd Qu.: 3.500
## Max. :132.500 Max. :132.500 Max. :132.500
## NA's :1 NA's :2 NA's :3

```

Standardize covariates and climate data. Note that stdCovs computes the mean/stddev of each variable from the original data frame used to fit the model, and not the new prediction data frame. However, the mean/stddev are computed from columns that have duplicated values for each catchment. So it seems like they would be weighted more heavily towards catchments with more data. Not sure if this is intentional.

```

## featureid date tmax tmin
## Min. :830189 Min. :1980-03-30 Min. : -6.75 Min. : -12.000
## 1st Qu.:830189 1st Qu.:1988-07-09 1st Qu.:16.00 1st Qu.: 3.000
## Median :830189 Median :1996-10-19 Median :21.50 Median : 8.500
## Mean :830189 Mean :1996-12-31 Mean :20.61 Mean : 8.079
## 3rd Qu.:830189 3rd Qu.:2005-06-25 3rd Qu.:26.00 3rd Qu.: 13.000
## Max. :830189 Max. :2013-11-07 Max. :35.25 Max. : 21.750
##
## prcp day1 srad vp
## Min. : -0.45947 Min. : -2.43569 Min. : -2.8043 Min. : 240
## 1st Qu.: -0.45947 1st Qu.: -0.72586 1st Qu.: -0.6588 1st Qu.: 760
## Median : -0.45947 Median : 0.16071 Median : 0.2650 Median :1120
## Mean : -0.07472 Mean : -0.09689 Mean : 0.1575 Mean :1163
## 3rd Qu.: -0.08917 3rd Qu.: 0.79398 3rd Qu.: 0.9950 3rd Qu.:1480
## Max. :13.55918 Max. : 1.04729 Max. : 3.2449 Max. :2600
##
## swe site airTemp zone
## Min. : -0.1633 Length:7511 Min. : -4.6792 Length:7511
## 1st Qu.: -0.1633 Class :character 1st Qu.: -1.3164 Class :character
## Median : -0.1633 Mode :character Median : -0.3651 Mode :character
## Mean : 0.4189 Mean : -0.4815
## 3rd Qu.: -0.1633 3rd Qu.: 0.3982
## Max. :12.6605 Max. : 1.9137
##
## TotDASqKM agriculture alloffnet allonnet
## Min. : -0.1598 Min. :12.63 Min. :2.991 Min. :3.897

```

```

## 1st Qu.: -0.1598 1st Qu.: 12.63 1st Qu.: 2.991 1st Qu.: 3.897
## Median : -0.1598 Median : 12.63 Median : 2.991 Median : 3.897
## Mean : -0.1598 Mean : 12.63 Mean : 2.991 Mean : 3.897
## 3rd Qu.: -0.1598 3rd Qu.: 12.63 3rd Qu.: 2.991 3rd Qu.: 3.897
## Max. : -0.1598 Max. : 12.63 Max. : 2.991 Max. : 3.897
##
## devel_hi devel_low devel_med devel_opn developed
## Min. : 0 Min. : 0.5438 Min. : 0 Min. : 6.193 Min. : 6.737
## 1st Qu.: 0 1st Qu.: 0.5438 1st Qu.: 0 1st Qu.: 6.193 1st Qu.: 6.737
## Median : 0 Median : 0.5438 Median : 0 Median : 6.193 Median : 6.737
## Mean : 0 Mean : 0.5438 Mean : 0 Mean : 6.193 Mean : 6.737
## 3rd Qu.: 0 3rd Qu.: 0.5438 3rd Qu.: 0 3rd Qu.: 6.193 3rd Qu.: 6.737
## Max. : 0 Max. : 0.5438 Max. : 0 Max. : 6.193 Max. : 6.737
##
## ReachElevationM Forest forest_decid forest_evgrn
## Min. : 0.6519 Min. : 0.1746 Min. : 16.56 Min. : 25.89
## 1st Qu.: 0.6519 1st Qu.: 0.1746 1st Qu.: 16.56 1st Qu.: 25.89
## Median : 0.6519 Median : 0.1746 Median : 16.56 Median : 25.89
## Mean : 0.6519 Mean : 0.1746 Mean : 16.56 Mean : 25.89
## 3rd Qu.: 0.6519 3rd Qu.: 0.1746 3rd Qu.: 16.56 3rd Qu.: 25.89
## Max. : 0.6519 Max. : 0.1746 Max. : 16.56 Max. : 25.89
##
## forest_mixed CONUSWetland herbaceous SurficialCoarseC
## Min. : 37.98 Min. : 0.2174 Min. : 0.2115 Min. : -0.923
## 1st Qu.: 37.98 1st Qu.: 0.2174 1st Qu.: 0.2115 1st Qu.: -0.923
## Median : 37.98 Median : 0.2174 Median : 0.2115 Median : -0.923
## Mean : 37.98 Mean : 0.2174 Mean : 0.2115 Mean : -0.923
## 3rd Qu.: 37.98 3rd Qu.: 0.2174 3rd Qu.: 0.2115 3rd Qu.: -0.923
## Max. : 37.98 Max. : 0.2174 Max. : 0.2115 Max. : -0.923
##
## water wetland temp huc
## Min. : 0 Min. : 11.27 Min. : 2.357 Length: 7511
## 1st Qu.: 0 1st Qu.: 11.27 1st Qu.: 12.079 Class : character
## Median : 0 Median : 11.27 Median : 16.430 Mode : character
## Mean : 0 Mean : 11.27 Mean : 15.423
## 3rd Qu.: 0 3rd Qu.: 11.27 3rd Qu.: 18.915
## Max. : 0 Max. : 11.27 Max. : 23.514
## NA's : 7045
##
## Latitude Longitude year finalSpringBP
## Min. : -0.03513 Min. : -0.08475 Min. : 1980 Min. : 85.0
## 1st Qu.: -0.03513 1st Qu.: -0.08475 1st Qu.: 1988 1st Qu.: 85.0
## Median : -0.03513 Median : -0.08475 Median : 1996 Median : 93.5
## Mean : -0.03513 Mean : -0.08475 Mean : 1996 Mean : 93.3
## 3rd Qu.: -0.03513 3rd Qu.: -0.08475 3rd Qu.: 2005 3rd Qu.: 102.0
## Max. : -0.03513 Max. : -0.08475 Max. : 2013 Max. : 102.0
## NA's : 6882
##
## sourceSpringBP finalFallBP sourceFallBP dOY
## Length: 7511 Min. : 293.0 Length: 7511 Min. : -2.1684
## Class : character 1st Qu.: 293.0 Class : character 1st Qu.: -1.1723
## Mode : character Median : 308.0 Mode : character Median : -0.1762
## Mean : 308.5 Mean : -0.1683
## 3rd Qu.: 323.0 3rd Qu.: 0.8380
## Max. : 323.0 Max. : 1.8341
## NA's : 6882

```

```

## ImpoundmentsAllSqKM      count      airTempLagged1      airTempLagged2
## Min.      :-0.1182      Min.      : 1      Min.      :-4.6885      Min.      :-4.6977
## 1st Qu.   :-0.1182      1st Qu.:1878      1st Qu.   :-1.3210      1st Qu.   :-1.3255
## Median    :-0.1182      Median :3756      Median    :-0.3684      Median    :-0.3715
## Mean      :-0.1182      Mean   :3756      Mean      :-0.4849      Mean      :-0.4879
## 3rd Qu.   :-0.1182      3rd Qu.:5634      3rd Qu.   : 0.4015      3rd Qu.   : 0.4050
## Max.      :-0.1182      Max.    :7511      Max.      : 1.9135      Max.      : 1.9136
##                                     NA's      :1      NA's      :2
## prcpLagged1      prcpLagged2      prcpLagged3      Developed
## Min.      :-0.45983      Min.      :-0.45997      Min.      :-0.46006      Min.      : NA
## 1st Qu.   :-0.45983      1st Qu.   :-0.45997      1st Qu.   :-0.46006      1st Qu.   : NA
## Median    :-0.45983      Median    :-0.45997      Median    :-0.46006      Median    : NA
## Mean      :-0.07514      Mean      :-0.07520      Mean      :-0.07516      Mean      :NaN
## 3rd Qu.   :-0.08963      3rd Qu.   :-0.08975      3rd Qu.   :-0.08976      3rd Qu.   : NA
## Max.      :13.55489      Max.      :13.55568      Max.      :13.55823      Max.      : NA
## NA's      :1      NA's      :2      NA's      :3      NA's      :7511
## Herbacious      Agriculture      HydrologicGroupAB      ReachSlopePCNT
## Min.      : NA      Min.      : NA      Min.      : NA      Min.      : NA
## 1st Qu.   : NA      1st Qu.   : NA      1st Qu.   : NA      1st Qu.   : NA
## Median    : NA      Median    : NA      Median    : NA      Median    : NA
## Mean      :NaN      Mean      :NaN      Mean      :NaN      Mean      :NaN
## 3rd Qu.   : NA      3rd Qu.   : NA      3rd Qu.   : NA      3rd Qu.   : NA
## Max.      : NA      Max.      : NA      Max.      : NA      Max.      : NA
## NA's      :7511      NA's      :7511      NA's      :7511      NA's      :7511
## HUC8
## Length:7511
## Class :character
## Mode :character
##
##
##
##

```

Add interaction terms

```

## intercept airTemp.TotDASqKM intercept.site airTemp.prcp
## Min.      :1      Min.      :-0.30582      Min.      :1      Min.      :-15.67231
## 1st Qu.   :1      1st Qu.   :-0.06364      1st Qu.   :1      1st Qu.   :-0.21875
## Median    :1      Median    : 0.05834      Median    :1      Median    : 0.05592
## Mean      :1      Mean      : 0.07696      Mean      :1      Mean      : 0.02908
## 3rd Qu.   :1      3rd Qu.   : 0.21037      3rd Qu.   :1      3rd Qu.   : 0.47270
## Max.      :1      Max.      : 0.74778      Max.      :1      Max.      : 7.39075
##
## intercept.year      dOY2      dOY3
## Min.      :1      Min.      :0.000024      Min.      :-10.195415
## 1st Qu.   :1      1st Qu.   :0.252210      1st Qu.   :-1.611061
## Median    :1      Median    :1.001947      Median    : -0.005472
## Mean      :1      Mean      :1.364366      Mean      : -0.677983
## 3rd Qu.   :1      3rd Qu.   :2.244863      3rd Qu.   : 0.588434
## Max.      :1      Max.      :4.701863      Max.      : 6.169361
##
## airTempLagged1.TotDASqKM airTempLagged2.TotDASqKM prcp.Forest
## Min.      :-0.30580      Min.      :-0.30581      Min.      :-0.08024
## 1st Qu.   :-0.06416      1st Qu.   :-0.06472      1st Qu.   :-0.08024

```



```

## Median : 0.05887      Median : 0.05937      Median : -0.08024
## Mean   : 0.07749      Mean   : 0.07797      Mean   : -0.01305
## 3rd Qu.: 0.21111      3rd Qu.: 0.21183      3rd Qu.: -0.01557
## Max.   : 0.74926      Max.   : 0.75074      Max.   : 2.36796
## NA's   :1             NA's   :2
## airTemp.prcpLagged1 airTemp.prcpLagged2 airTempLagged1.prcpLagged1
## Min.   : -16.34406    Min.   : -15.30292    Min.   : -15.69674
## 1st Qu.: -0.24986    1st Qu.: -0.24931    1st Qu.: -0.21957
## Median : 0.03292     Median : 0.03674     Median : 0.05566
## Mean   : -0.02982     Mean   : -0.02174     Mean   : 0.02947
## 3rd Qu.: 0.42220     3rd Qu.: 0.43251     3rd Qu.: 0.47501
## Max.   : 7.41564     Max.   : 5.38569     Max.   : 7.36981
## NA's   :1             NA's   :2             NA's   :1
## airTempLagged1.prcpLagged2 airTempLagged2.prcpLagged2 airTemp.swe
## Min.   : -16.40563    Min.   : -15.72827    Min.   : -42.63214
## 1st Qu.: -0.25245     1st Qu.: -0.22161     1st Qu.: -0.13187
## Median : 0.03281     Median : 0.05543     Median : -0.01264
## Mean   : -0.02970     Mean   : 0.02962     Mean   : -0.97105
## 3rd Qu.: 0.42420     3rd Qu.: 0.47703     3rd Qu.: 0.13910
## Max.   : 7.40613     Max.   : 7.35371     Max.   : 1.82848
## NA's   :2             NA's   :2
## airTempLagged1.swe airTempLagged2.swe
## Min.   : -42.7168     Min.   : -42.80118
## 1st Qu.: -0.1316     1st Qu.: -0.13226
## Median : -0.0122     Median : -0.01179
## Mean   : -0.9941     Mean   : -1.01145
## 3rd Qu.: 0.1361     3rd Qu.: 0.13675
## Max.   : 1.6991     Max.   : 1.61093
## NA's   :1             NA's   :2

```

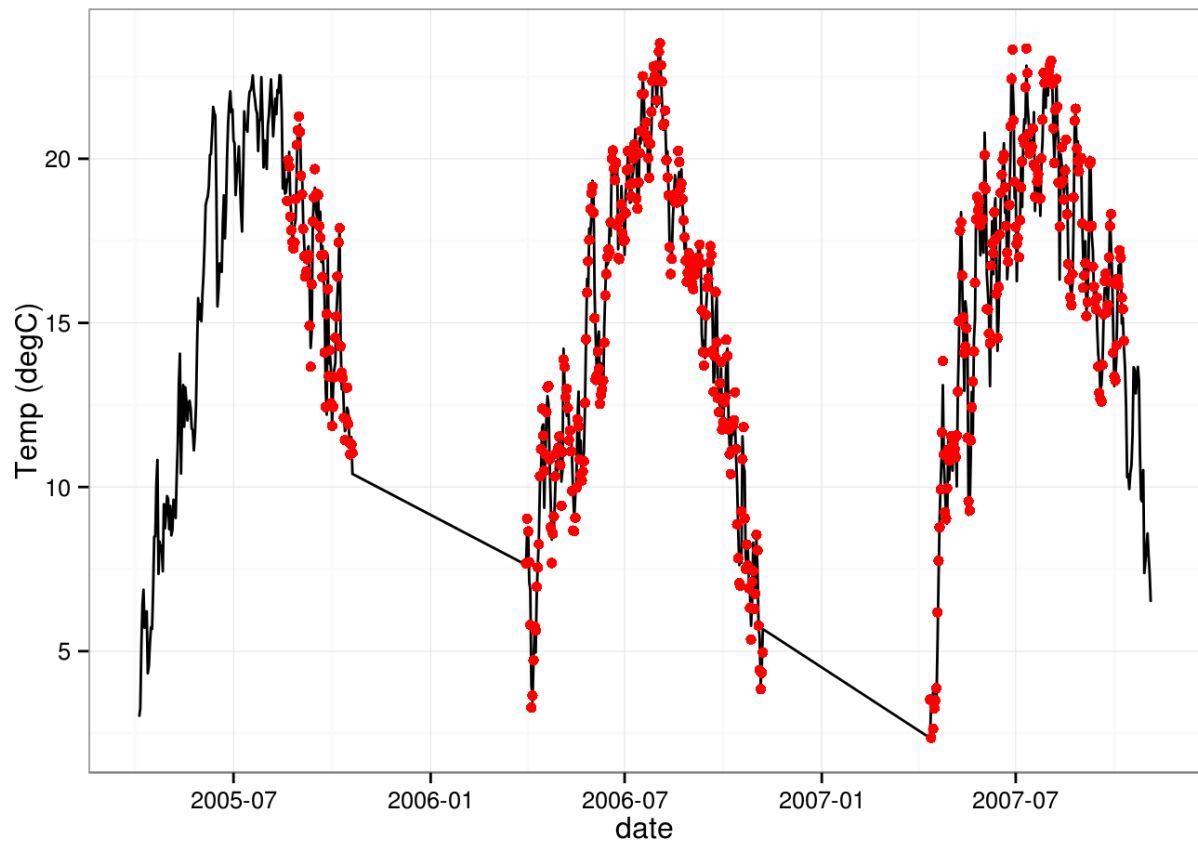
Add deployment index

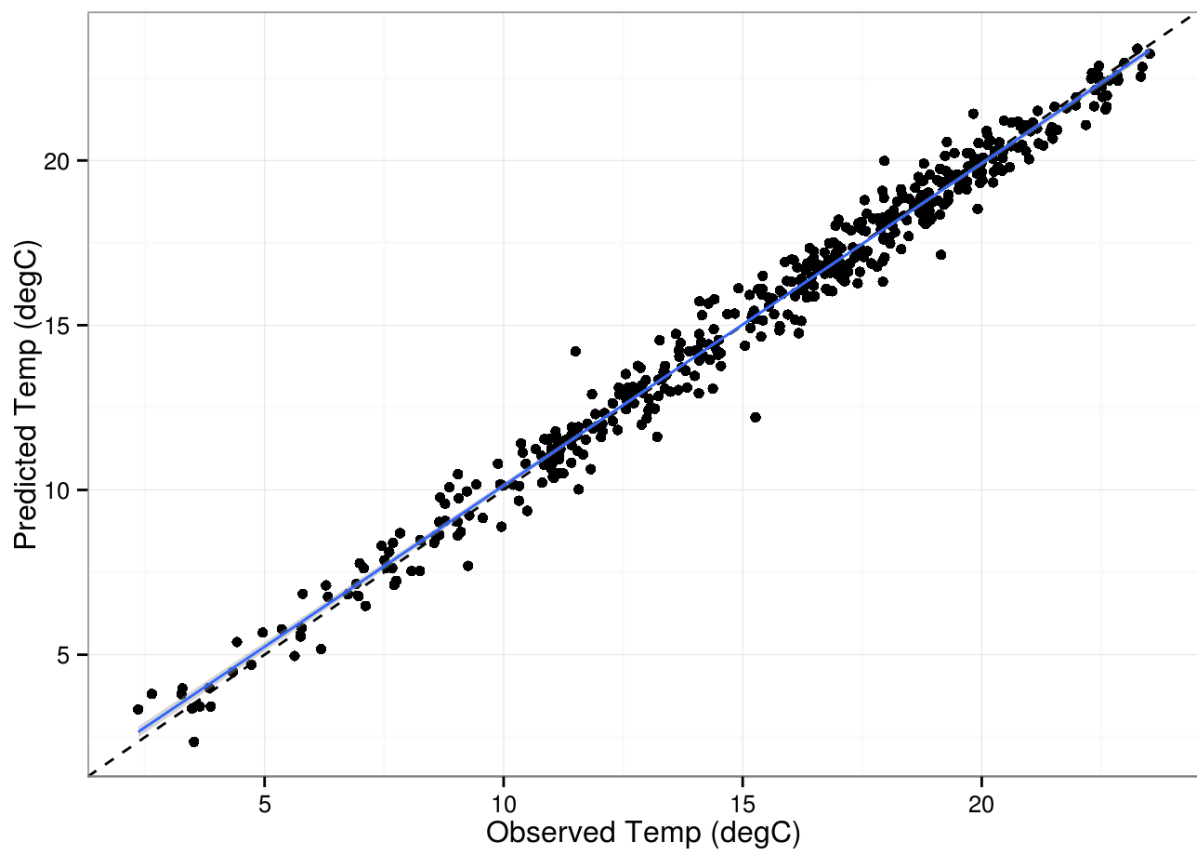
```

##      sitef      rowNum      siteShift      dateShift      newSite
## Min.   :1      Min.   : 1      Min.   :1      Min.   : 1      Mode :logical
## 1st Qu.:1      1st Qu.:1878      1st Qu.:1      1st Qu.: 6764      FALSE:7511
## Median :1      Median :3756      Median :1      Median : 9787      NA's :0
## Mean   :1      Mean   :3756      Mean   :1      Mean   : 9860
## 3rd Qu.:1      3rd Qu.:5634      3rd Qu.:1      3rd Qu.:12958
## Max.   :1      Max.   :7511      Max.   :1      Max.   :16015
##      newDate      isNA      isNAShift      newDeploy
## Mode :logical      Mode :logical      Mode :logical      Min.   :0.0000
## FALSE:7477      FALSE:466      FALSE:467      1st Qu.:1.0000
## TRUE :34         TRUE :7045      TRUE :7044      Median :1.0000
## NA's :0          NA's :0         NA's :0         Mean   :0.9382
##                                     3rd Qu.:1.0000
##                                     Max.   :1.0000
##      deployID
## Min.   : 1
## 1st Qu.:1878
## Median :3756
## Mean   :3658
## 3rd Qu.:5634
## Max.   :7047

```

2 Run Predictions





Join the predicted temperature back with un-standardized input data and compute mean predicted temperature.

```
## [1] 14.1403
```

Compute derived metrics.

```
## Observations: 1
## Variables:
## $ featureid      (int) 830189
## $ totalObs       (lgl) TRUE
## $ meanMaxTemp    (dbl) 22.26713
## $ maxMaxTemp     (dbl) 23.77446
## $ meanDays.18    (dbl) 70
## $ meanDays.20    (dbl) 29
## $ meanDays.22    (dbl) 6
## $ yearsMaxTemp.18 (dbl) 34
## $ yearsMaxTemp.20 (dbl) 34
## $ yearsMaxTemp.22 (dbl) 20
## $ meanResist     (dbl) 135.5553
## $ meanRMSE       (dbl) 0.6443841
```

3 Prediction Function

The prediction function `predictTemp` takes three arguments:

- `data`: dataframe of the prediction input data (standardized climate and covariate variables)
- `coef.list`: list of fitted coefficients for each covariate
- `cov.list`: list of variables used for each nested model 'level'

```
## List of 16
## $ fix.ef      :Classes 'tbl_df', 'tbl' and 'data.frame':  21 obs. of  6 variables:
##   ..$ Parameter: Factor w/ 6979 levels "B.0[1]","B.0[2]",...: 1 2 3 4 5 6 7 8 9 10 ...
##   ..$ mean      : num [1:21] 18.472 -0.366 0.312 -1.099 -0.442 ...
##   ..$ sd        : num [1:21] 0.2071 0.3058 0.355 0.3644 0.0789 ...
##   ..$ qLo       : num [1:21] 18.054 -0.934 -0.417 -1.804 -0.602 ...
##   ..$ qHi       : num [1:21] 18.878 0.269 1.005 -0.404 -0.287 ...
##   ..$ coef      : chr [1:21] "intercept" "Latitude" "Longitude" "TotDASqKM" ...
## $ rand.ef     :Classes 'tbl_df', 'tbl' and 'data.frame':  17 obs. of  6 variables:
##   ..$ Parameter: Factor w/ 6979 levels "B.0[1]","B.0[2]",...: 6970 6971 6972 6973 6974 6975 6964 6965
##   ..$ mean      : num [1:17] 1.8431 0.4566 0.1775 0.1006 0.0583 ...
##   ..$ sd        : num [1:17] 0.04795 0.01215 0.00629 0.00333 0.00229 ...
##   ..$ qLo       : num [1:17] 1.7512 0.4326 0.1653 0.0945 0.054 ...
##   ..$ qHi       : num [1:17] 1.9423 0.4806 0.1902 0.1075 0.0628 ...
##   ..$ coef      : Factor w/ 6989 levels "airTemp","airTemp.prcp",...: 4 1 3 5 6 2 4 1 3 5 ...
## $ B.fixed     :Classes 'tbl_df', 'tbl' and 'data.frame':  10 obs. of  6 variables:
##   ..$ Parameter: Factor w/ 6979 levels "B.0[1]","B.0[2]",...: 1 2 3 4 5 6 7 8 9 10
##   ..$ mean      : num [1:10] 18.472 -0.366 0.312 -1.099 -0.442 ...
##   ..$ sd        : num [1:10] 0.2071 0.3058 0.355 0.3644 0.0789 ...
##   ..$ qLo       : num [1:10] 18.054 -0.934 -0.417 -1.804 -0.602 ...
##   ..$ qHi       : num [1:10] 18.878 0.269 1.005 -0.404 -0.287 ...
##   ..$ coef      : chr [1:10] "intercept" "Latitude" "Longitude" "TotDASqKM" ...
## $ mu.huc      :Classes 'tbl_df', 'tbl' and 'data.frame':   6 obs. of  7 variables:
##   ..$ index      : num [1:6] 1 2 3 4 5 6
##   ..$ Parameter: Factor w/ 6979 levels "B.0[1]","B.0[2]",...: 6900 6901 6902 6903 6904 6905
##   ..$ mean      : num [1:6] 0 2.03077 0.34459 0.00722 0.01432 ...
##   ..$ sd        : num [1:6] 0 0.063 0.0467 0.0362 0.0347 ...
##   ..$ qLo       : num [1:6] 0 1.907 0.2484 -0.0619 -0.0568 ...
##   ..$ qHi       : num [1:6] 0 2.1499 0.438 0.0787 0.0816 ...
##   ..$ coef      : Factor w/ 6 levels "airTemp","airTemp.prcp",...: 4 1 3 5 6 2
## $ mu.year     :Classes 'tbl_df', 'tbl' and 'data.frame':   4 obs. of  7 variables:
##   ..$ index      : num [1:4] 1 2 3 4
##   ..$ Parameter: Factor w/ 6979 levels "B.0[1]","B.0[2]",...: 6906 6907 6908 6909
##   ..$ mean      : num [1:4] 0 -0.421 -2.137 0.133
##   ..$ sd        : num [1:4] 0 0.1124 0.1288 0.0787
##   ..$ qLo       : num [1:4] 0 -0.6525 -2.3961 -0.0152
##   ..$ qHi       : num [1:4] 0 -0.208 -1.882 0.294
##   ..$ coef      : Factor w/ 4 levels "d0Y","d0Y2","d0Y3",...: 4 1 2 3
## $ mu.ar1      :Classes 'tbl_df', 'tbl' and 'data.frame':   1 obs. of  6 variables:
##   ..$ Parameter: Factor w/ 6979 levels "B.0[1]","B.0[2]",...: 6899
##   ..$ mean      : num 0.958
##   ..$ sd        : num 0.0228
##   ..$ qLo       : num 0.913
##   ..$ qHi       : num 0.997
##   ..$ coef      : Factor w/ 6979 levels "B.0[1]","B.0[2]",...: 6899
```

```

## $ sigma.site:Classes 'tbl_df', 'tbl' and 'data.frame': 6 obs. of 7 variables:
## ..$ index : num [1:6] 1 2 3 4 5 6
## ..$ Parameter: Factor w/ 6979 levels "B.0[1]","B.0[2]",...: 6970 6971 6972 6973 6974 6975
## ..$ mean : num [1:6] 1.8431 0.4566 0.1775 0.1006 0.0583 ...
## ..$ sd : num [1:6] 0.04795 0.01215 0.00629 0.00333 0.00229 ...
## ..$ qLo : num [1:6] 1.7512 0.4326 0.1653 0.0945 0.054 ...
## ..$ qHi : num [1:6] 1.9423 0.4806 0.1902 0.1075 0.0628 ...
## ..$ coef : Factor w/ 6 levels "airTemp","airTemp.prcp",...: 4 1 3 5 6 2
## $ sigma.huc :Classes 'tbl_df', 'tbl' and 'data.frame': 6 obs. of 7 variables:
## ..$ index : num [1:6] 1 2 3 4 5 6
## ..$ Parameter: Factor w/ 6979 levels "B.0[1]","B.0[2]",...: 6964 6965 6966 6967 6968 6969
## ..$ mean : num [1:6] 0.683 0.311 0.243 0.201 0.189 ...
## ..$ sd : num [1:6] 0.1585 0.0454 0.0327 0.026 0.0241 ...
## ..$ qLo : num [1:6] 0.414 0.234 0.188 0.157 0.151 ...
## ..$ qHi : num [1:6] 1.04 0.414 0.317 0.258 0.243 ...
## ..$ coef : Factor w/ 6 levels "airTemp","airTemp.prcp",...: 4 1 3 5 6 2
## $ sigma.year:Classes 'tbl_df', 'tbl' and 'data.frame': 4 obs. of 7 variables:
## ..$ index : num [1:4] 1 2 3 4
## ..$ Parameter: Factor w/ 6979 levels "B.0[1]","B.0[2]",...: 6976 6977 6978 6979
## ..$ mean : num [1:4] 0.558 0.479 0.586 0.344
## ..$ sd : num [1:4] 0.0954 0.0914 0.0993 0.0625
## ..$ qLo : num [1:4] 0.403 0.333 0.428 0.247
## ..$ qHi : num [1:4] 0.77 0.688 0.819 0.493
## ..$ coef : Factor w/ 4 levels "d0Y","d0Y2","d0Y3",...: 4 1 2 3
## $ sigma.ar1 :Classes 'tbl_df', 'tbl' and 'data.frame': 1 obs. of 5 variables:
## ..$ Parameter: Factor w/ 6979 levels "B.0[1]","B.0[2]",...: 6963
## ..$ mean : num 0.188
## ..$ sd : num 0.0121
## ..$ qLo : num 0.163
## ..$ qHi : num 0.21
## $ cor.huc : 'data.frame': 6 obs. of 6 variables:
## ..$ intercept.site: chr [1:6] "" "0.367" "0.274" "-0.038" ...
## ..$ airTemp : chr [1:6] "" "" "0.166" "-0.072" ...
## ..$ airTempLagged2: chr [1:6] "" "" "" "-0.075" ...
## ..$ prcp : chr [1:6] "" "" "" "" ...
## ..$ prcpLagged1 : chr [1:6] "" "" "" "" ...
## ..$ airTemp.prcp : chr [1:6] "" "" "" "" ...
## $ cor.year : 'data.frame': 4 obs. of 4 variables:
## ..$ intercept.year: chr [1:4] "" "-0.474" "-0.634" "0.391"
## ..$ d0Y : chr [1:4] "" "" "0.464" "-0.53"
## ..$ d0Y2 : chr [1:4] "" "" "" "-0.464"
## ..$ d0Y3 : chr [1:4] "" "" "" ""
## $ B.site :Classes 'tbl_df', 'tbl' and 'data.frame': 5664 obs. of 9 variables:
## ..$ index2 : num [1:5664] 1 1 1 1 1 1 1 1 1 1 ...
## ..$ index : num [1:5664] 1 2 3 4 5 6 7 8 9 10 ...
## ..$ Parameter: Factor w/ 6979 levels "B.0[1]","B.0[2]",...: 1147 1148 1149 1150 1151 1152 1153 1154
## ..$ mean : num [1:5664] 1.258 -0.908 -0.475 3.893 -1.782 ...
## ..$ sd : num [1:5664] 0.38 0.528 0.516 0.717 0.476 ...
## ..$ qLo : num [1:5664] 0.538 -2.061 -1.435 2.418 -2.718 ...
## ..$ qHi : num [1:5664] 2.007 0.027 0.626 5.264 -0.789 ...
## ..$ site : Factor w/ 944 levels "CTDEP_1","CTDEP_1008",...: 1 2 3 4 5 6 7 8 9 10 ...
## ..$ coef : Factor w/ 6 levels "airTemp","airTemp.prcp",...: 4 4 4 4 4 4 4 4 4 4 ...
## $ B.huc :Classes 'tbl_df', 'tbl' and 'data.frame': 192 obs. of 9 variables:
## ..$ index2 : num [1:192] 1 1 1 1 1 1 1 1 1 1 ...

```

```
## ..$ index      : num [1:192] 1 2 3 4 5 6 7 8 9 10 ...
## ..$ Parameter: Factor w/ 6979 levels "B.0[1]","B.0[2]",...: 955 956 957 958 959 960 961 962 963 964
## ..$ mean       : num [1:192] 0.2116 -0.0128 0.885 -0.0878 0.8979 ...
## ..$ sd         : num [1:192] 0.591 0.413 0.502 0.468 0.564 ...
## ..$ qLo        : num [1:192] -0.9314 -0.8294 -0.0314 -1.0161 -0.1407 ...
## ..$ qHi        : num [1:192] 1.403 0.829 1.93 0.798 2.077 ...
## ..$ huc        : Factor w/ 32 levels "01050001","01050002",...: 1 2 3 4 5 6 7 8 9 10 ...
## ..$ coef       : Factor w/ 6 levels "airTemp","airTemp.prcp",...: 4 4 4 4 4 4 4 4 4 4 ...
## $ B.year       :Classes 'tbl_df', 'tbl' and 'data.frame': 88 obs. of 9 variables:
## ..$ index2      : num [1:88] 1 1 1 1 1 1 1 1 1 1 ...
## ..$ index       : num [1:88] 1 2 3 4 5 6 7 8 9 10 ...
## ..$ Parameter: Factor w/ 6979 levels "B.0[1]","B.0[2]",...: 6811 6812 6813 6814 6815 6816 6817 6818
## ..$ mean       : num [1:88] 0.251 0.125 0.374 0.532 0.741 ...
## ..$ sd         : num [1:88] 0.271 0.276 0.438 0.264 0.177 ...
## ..$ qLo        : num [1:88] -0.276 -0.4141 -0.4801 0.0187 0.3976 ...
## ..$ qHi        : num [1:88] 0.799 0.645 1.243 1.051 1.09 ...
## ..$ year       : Factor w/ 22 levels "1991","1992",...: 1 2 3 4 5 6 7 8 9 10 ...
## ..$ coef       : Factor w/ 4 levels "d0Y","d0Y2","d0Y3",...: 4 4 4 4 4 4 4 4 4 4 ...
## $ B.ar1        :Classes 'tbl_df', 'tbl' and 'data.frame': 944 obs. of 7 variables:
## ..$ index       : num [1:944] 1 2 3 4 5 6 7 8 9 10 ...
## ..$ Parameter: Factor w/ 6979 levels "B.0[1]","B.0[2]",...: 11 12 13 14 15 16 17 18 19 20 ...
## ..$ mean       : num [1:944] 0.872 0.886 0.85 0.977 0.781 ...
## ..$ sd         : num [1:944] 0.0241 0.063 0.066 0.0154 0.1241 ...
## ..$ qLo        : num [1:944] 0.827 0.749 0.724 0.941 0.504 ...
## ..$ qHi        : num [1:944] 0.921 0.987 0.974 0.998 0.98 ...
## ..$ site       : Factor w/ 944 levels "CTDEP_1","CTDEP_1008",...: 1 2 3 4 5 6 7 8 9 10 ...

## List of 5
## $ fixed.ef: chr [1:10] "intercept" "Latitude" "Longitude" "TotDASqKM" ...
## $ site.ef : chr [1:6] "intercept.site" "airTemp" "airTempLagged2" "prcp" ...
## $ year.ef : chr [1:4] "intercept.year" "d0Y" "d0Y2" "d0Y3"
## $ huc.ef : chr [1:6] "intercept.site" "airTemp" "airTempLagged2" "prcp" ...
## $ ar1.ef : chr [1:6] "intercept.site" "airTemp" "airTempLagged2" "prcp" ...
```

The `coef.list` object contains multiple data frames with the mean, sd, low/high values of each coefficient. For example, the fixed effects parameters are:

```
## Source: local data frame [10 x 6]
##
##   Parameter    mean      sd      qLo      qHi
## 1   B.0[1] 18.4720231 0.20711765 18.0538047 18.87760438
## 2   B.0[2] -0.3655001 0.30575498 -0.9339998 0.26915798
## 3   B.0[3] 0.3116465 0.35502875 -0.4168086 1.00544633
## 4   B.0[4] -1.0988664 0.36440642 -1.8041232 -0.40444187
## 5   B.0[5] -0.4424734 0.07889847 -0.6018484 -0.28738823
## 6   B.0[6] 0.1212420 0.14877681 -0.1744810 0.40473439
## 7   B.0[7] -0.2334957 0.06283271 -0.3558321 -0.11107207
## 8   B.0[8] 0.4721499 0.08591556 0.2986466 0.63677912
## 9   B.0[9] 1.3261676 0.37490526 0.6074139 2.06048554
## 10  B.0[10] -0.1183657 0.01772925 -0.1531617 -0.08348063
## Variables not shown: coef (chr)
```

Here is the source of the `predictTemp` function, I'll walk through this step-by-step.

3.1 Conditional Coefficients

First prepare the conditional coefficients.

The site coefficients are unique to each site with observed data.

```
##      site intercept.site.B.site airTemp.B.site airTempLagged2.B.site
## 1 CTDEP_1      1.2578088      -0.1263020      0.08484531
## 2 CTDEP_1008    -0.9084381      0.1529970      0.05039532
## 3 CTDEP_101     -0.4746102      0.2543164     -0.15941858
## 4 CTDEP_1030     3.8932751      0.1256987     -0.14887135
## 5 CTDEP_1038    -1.7819292      0.4934692     -0.03867491
## 6 CTDEP_1068    -0.8706286      0.3800239      0.04002566
## prcp.B.site prcpLagged1.B.site airTemp.prcp.B.site
## 1 -0.03188245    -0.108648733    -0.01731219
## 2  0.03525321     0.070521624     0.04286377
## 3  0.01619213     0.010680232     -0.03284584
## 4 -0.11967470    -0.056528450     -0.03787414
## 5  0.06643119    -0.003515002     0.02056535
## 6 -0.05740766    -0.011369791     -0.02212242
```

The huc coefficients are unique to each huc.

```
##      huc intercept.site.B.huc airTemp.B.huc airTempLagged2.B.huc
## 1 01050001      0.21158768      2.092222      0.3332813
## 2 01050002     -0.01284352      2.151131      0.5113379
## 3 01050004      0.88495896      2.362157      0.6099687
## 4 01070001     -0.08777879      2.052302      0.2688639
## 5 01070003      0.89789031      1.949856      0.2812626
## 6 01070004     -0.04145645      1.989773      0.2675478
## prcp.B.huc prcpLagged1.B.huc airTemp.prcp.B.huc
## 1 -0.19788329    -0.12627457    -0.02869864
## 2 -0.05692102    -0.01896205    -0.02761145
## 3 -0.15396541    -0.09055544    -0.01155171
## 4  0.13898328     0.04421415    -0.17412735
## 5  0.04254797     0.01746611    -0.14322564
## 6  0.05820669     0.08519798    -0.01110612
```

The year coefficients are unique to each year.

```
##   year intercept.year.B.year d0Y.B.year d0Y2.B.year d0Y3.B.year
## 1 1991      0.2507031 -0.5705137   -2.333859   0.11411258
## 2 1992      0.1246343 -0.6890643   -2.518361   0.57819012
## 3 1993      0.3738921 -0.6395225   -2.826071   0.27454656
## 4 1994      0.5322970 -1.0960559   -3.070439   0.51926832
## 5 1995      0.7412415 -1.3646546   -2.776573   0.58597807
## 6 1996     -0.3906299 -0.1215034   -2.404118   0.06153273
```

The ar1 coefficients are unique to each site with data.

```
## Source: local data frame [6 x 7]
##
##   index Parameter      mean      sd      qLo      qHi      site
```

```
## 1      1 B.ar1[1] 0.8722118 0.02411020 0.8269491 0.9210643      CTDEP_1
## 2      2 B.ar1[2] 0.8862273 0.06304729 0.7494881 0.9871344 CTDEP_1008
## 3      3 B.ar1[3] 0.8497359 0.06602661 0.7243748 0.9736101 CTDEP_101
## 4      4 B.ar1[4] 0.9766260 0.01535073 0.9410493 0.9983677 CTDEP_1030
## 5      5 B.ar1[5] 0.7807974 0.12414357 0.5036907 0.9801836 CTDEP_1038
## 6      6 B.ar1[6] 0.6845157 0.06934852 0.5465087 0.8180291 CTDEP_1068
```

3.2 Prepare Input Values

We then add the input values for each set of coefficients (site, huc, year, ar1) to the dataframe.

```
##      intercept.site.B.site airTemp.B.site airTempLagged2.B.site prcp.B.site
## 1      -0.5871427      0.06820972      0.01741933 -0.04672892
## 2      -0.5871427      0.06820972      0.01741933 -0.04672892
## 3      -0.5871427      0.06820972      0.01741933 -0.04672892
## 4      -0.5871427      0.06820972      0.01741933 -0.04672892
## 5      -0.5871427      0.06820972      0.01741933 -0.04672892
## 6      -0.5871427      0.06820972      0.01741933 -0.04672892
```

```
##      prcpLagged1.B.site airTemp.prcp.B.site
## 1      -0.05062016      0.0246564
## 2      -0.05062016      0.0246564
## 3      -0.05062016      0.0246564
## 4      -0.05062016      0.0246564
## 5      -0.05062016      0.0246564
## 6      -0.05062016      0.0246564
```

```
##      intercept.site.B.huc airTemp.B.huc airTempLagged2.B.huc prcp.B.huc
## 1      0.1734929      2.17277      0.4267125 0.02741676
## 2      0.1734929      2.17277      0.4267125 0.02741676
## 3      0.1734929      2.17277      0.4267125 0.02741676
## 4      0.1734929      2.17277      0.4267125 0.02741676
## 5      0.1734929      2.17277      0.4267125 0.02741676
## 6      0.1734929      2.17277      0.4267125 0.02741676
```

```
##      prcpLagged1.B.huc airTemp.prcp.B.huc
## 1      0.03232941      -0.02919445
## 2      0.03232941      -0.02919445
## 3      0.03232941      -0.02919445
## 4      0.03232941      -0.02919445
## 5      0.03232941      -0.02919445
## 6      0.03232941      -0.02919445
```

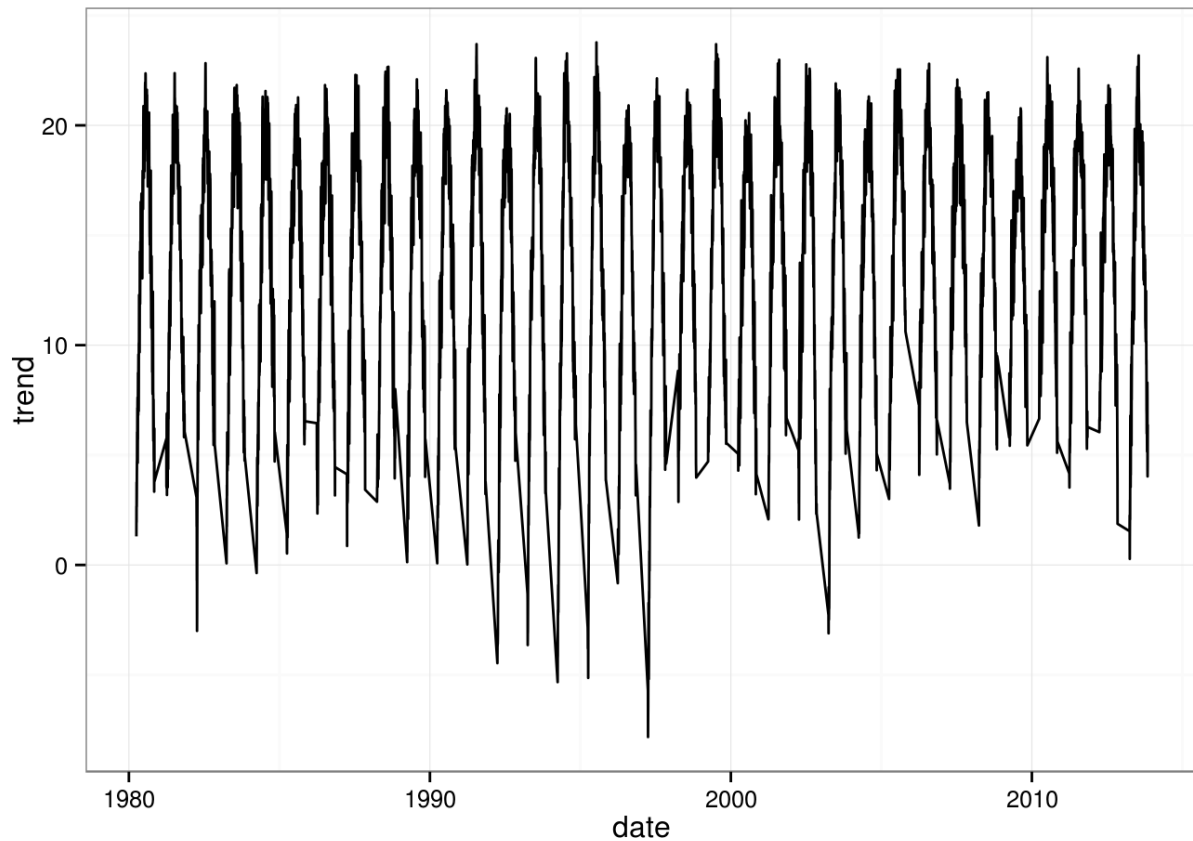
```
##      intercept.year.B.year d0Y.B.year d0Y2.B.year d0Y3.B.year
## 1      -0.002493817 -0.4230527      -2.136294 0.1334195
## 2      -0.002493817 -0.4230527      -2.136294 0.1334195
## 3      -0.002493817 -0.4230527      -2.136294 0.1334195
## 4      -0.002493817 -0.4230527      -2.136294 0.1334195
## 5      -0.002493817 -0.4230527      -2.136294 0.1334195
## 6      -0.002493817 -0.4230527      -2.136294 0.1334195
```

```
## [1] "B.ar1"
```

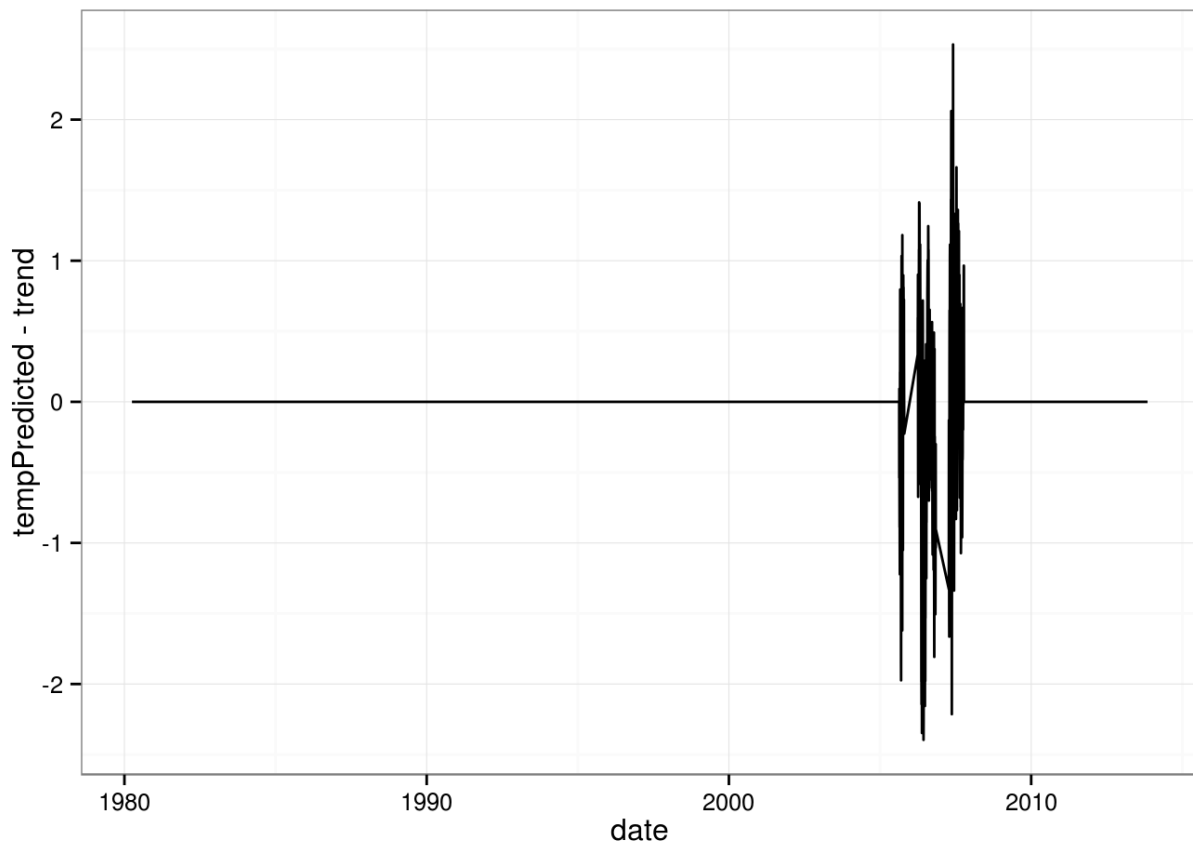
```
## [1] 0.8188234 0.8188234 0.8188234 0.8188234 0.8188234 0.8188234
```


3.3 Compute Predicted Temperature

To compute the predicted temperatures, we take the linear sum of each set of factors using matrix multiplication. The plot below shows the predicted temperature time series over all years.



The final predicted temperature is adjusted using the autoregressive residual term (`B.ar1`). The plot below shows the change in predicted temperature due to the autoregressive residuals which ranges from -2 to +2 degC.



3.4 prepConditionalCoef() Function

```
##      site intercept.site.B.site airTemp.B.site airTempLagged2.B.site
## 1   CTDEP_1      1.2578088      -0.1263020      0.08484531
## 2 CTDEP_1008     -0.9084381      0.1529970      0.05039532
## 3   CTDEP_101     -0.4746102      0.2543164     -0.15941858
## 4 CTDEP_1030      3.8932751      0.1256987     -0.14887135
## 5 CTDEP_1038     -1.7819292      0.4934692     -0.03867491
## 6 CTDEP_1068     -0.8706286      0.3800239      0.04002566
##  prcp.B.site prcpLagged1.B.site airTemp.prcp.B.site
## 1 -0.03188245    -0.108648733    -0.01731219
## 2  0.03525321     0.070521624     0.04286377
## 3  0.01619213     0.010680232     -0.03284584
## 4 -0.11967470    -0.056528450     -0.03787414
## 5  0.06643119    -0.003515002     0.02056535
## 6 -0.05740766    -0.011369791    -0.02212242

## Source: local data frame [6 x 9]
##
##   index2 index  Parameter      mean      sd      qLo      qHi
## 1      1      1 B.site[1,1]  1.2578088 0.3801636 0.5378338 2.00670015
## 2      1      2 B.site[2,1] -0.9084381 0.5284053 -2.0607052 0.02701856
## 3      1      3 B.site[3,1] -0.4746102 0.5164547 -1.4351361 0.62642156
## 4      1      4 B.site[4,1]  3.8932751 0.7172009  2.4181247 5.26401947
```

```
## 5      1      5 B.site[5,1] -1.7819292 0.4758603 -2.7184497 -0.78930650
## 6      1      6 B.site[6,1] -0.8706286 0.2469199 -1.3521983 -0.37851881
## Variables not shown: site (fctr), coef (fctr)
```

```
##      site      airTemp airTemp.prcp airTempLagged2 intercept.site
## 1 CTDEP_1 -0.1263020 -0.01731219 0.08484531 1.2578088
## 2 CTDEP_1008 0.1529970 0.04286377 0.05039532 -0.9084381
## 3 CTDEP_101 0.2543164 -0.03284584 -0.15941858 -0.4746102
## 4 CTDEP_1030 0.1256987 -0.03787414 -0.14887135 3.8932751
## 5 CTDEP_1038 0.4934692 0.02056535 -0.03867491 -1.7819292
## 6 CTDEP_1068 0.3800239 -0.02212242 0.04002566 -0.8706286
##      prcp prcpLagged1
## 1 -0.03188245 -0.108648733
## 2 0.03525321 0.070521624
## 3 0.01619213 0.010680232
## 4 -0.11967470 -0.056528450
## 5 0.06643119 -0.003515002
## 6 -0.05740766 -0.011369791
```

```
## [1] "site" "intercept.site.B.site" "airTemp.B.site"
## [4] "airTempLagged2.B.site" "prcp.B.site" "prcpLagged1.B.site"
## [7] "airTemp.prcp.B.site"
```

Add the site covariates to the data frame

```
##      intercept.site.B.site airTemp.B.site airTempLagged2.B.site prcp.B.site
## 1 -0.5871427 0.06820972 0.01741933 -0.04672892
## 2 -0.5871427 0.06820972 0.01741933 -0.04672892
## 3 -0.5871427 0.06820972 0.01741933 -0.04672892
## 4 -0.5871427 0.06820972 0.01741933 -0.04672892
## 5 -0.5871427 0.06820972 0.01741933 -0.04672892
## 6 -0.5871427 0.06820972 0.01741933 -0.04672892
##      prcpLagged1.B.site airTemp.prcp.B.site
## 1 -0.05062016 0.0246564
## 2 -0.05062016 0.0246564
## 3 -0.05062016 0.0246564
## 4 -0.05062016 0.0246564
## 5 -0.05062016 0.0246564
## 6 -0.05062016 0.0246564
```

Create two matrices with columns for covariates and coefficients

```
## [1] "intercept.site" "airTemp" "airTempLagged2" "prcp"
## [5] "prcpLagged1" "airTemp.prcp"

## [1] "intercept.site.B.site" "airTemp.B.site" "airTempLagged2.B.site"
## [4] "prcp.B.site" "prcpLagged1.B.site" "airTemp.prcp.B.site"

##      intercept.site      airTemp airTempLagged2      prcp prcpLagged1
## [1,]      1 -2.157086      NA 0.5985377      NA
## [2,]      1 -2.665931      NA -0.4594738 0.5978843
## [3,]      1 -2.665931 -2.168564 -0.4594738 -0.4598302
```

```
## [4,]          1 -2.046468      -2.678835 -0.4594738 -0.4598302
## [5,]          1 -2.444694      -2.678835 -0.1420704 -0.4598302
## [6,]          1 -1.847355      -2.057635 -0.4594738 -0.1425159
##      airTemp.prcp
## [1,]    -1.2910975
## [2,]     1.2249253
## [3,]     1.2249253
## [4,]     0.9402984
## [5,]     0.3473186
## [6,]     0.8488112
```

```
## [1] 7511      6
```

```
##      intercept.site.B.site airTemp.B.site airTempLagged2.B.site
## [1,]    -0.5871427      0.06820972      0.01741933
## [2,]    -0.5871427      0.06820972      0.01741933
## [3,]    -0.5871427      0.06820972      0.01741933
## [4,]    -0.5871427      0.06820972      0.01741933
## [5,]    -0.5871427      0.06820972      0.01741933
## [6,]    -0.5871427      0.06820972      0.01741933
##      prcp.B.site prcpLagged1.B.site airTemp.prcp.B.site
## [1,] -0.04672892      -0.05062016      0.0246564
## [2,] -0.04672892      -0.05062016      0.0246564
## [3,] -0.04672892      -0.05062016      0.0246564
## [4,] -0.04672892      -0.05062016      0.0246564
## [5,] -0.04672892      -0.05062016      0.0246564
## [6,] -0.04672892      -0.05062016      0.0246564
```

```
## [1] 7511      6
```

Multiple two matrices and sum the rows

```
## [1] 7511
```

```
## [1]          NA          NA -0.7318103 -0.7054634 -0.7620790 -0.6993793
```

4 Model Details

4.1 Model Theory

This equation defines the predicted temperature without the autoregressive residual term.

$$\omega_{s,h,d,y} = X^0 B^0 + X_h^{huc} B_h^{huc} + X_{s,h}^{site} B_{s,h}^{site} + X_y^{year} B_y^{year}$$

where $\omega_{s,h,d,y}$ is the expected temperature without residual error terms of site (s) , within HUC (h) , on julian day (d) within year (y) . This value is a linear combination of four terms:

- $(X^0 B^0)$: fixed effects including the intercept
- $(X_h^{huc} B_h^{huc})$: effects for HUC (h)
- $(X_{s,h}^{site} B_{s,h}^{site})$: effects for site (s)
- $(X_y^{year} B_y^{year})$: effects for year (y)

Each of these terms produces a vector of length (n_d) .

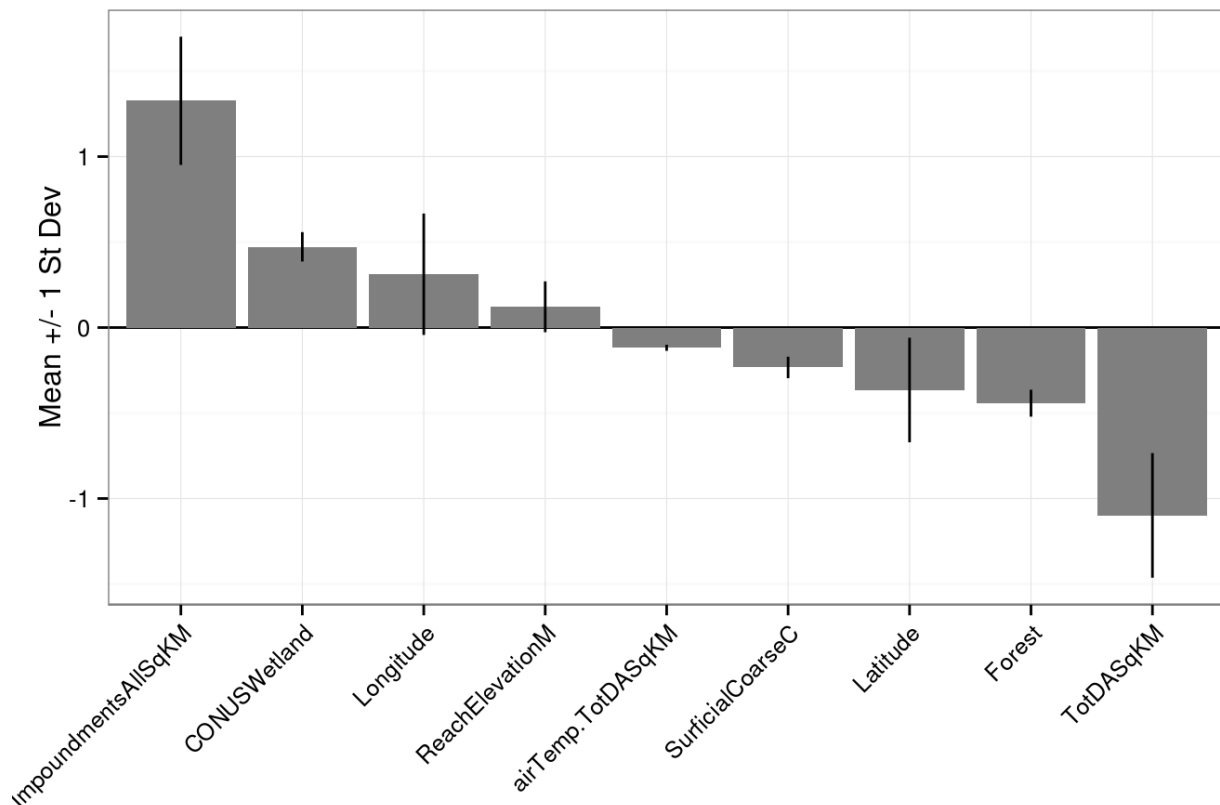
4.2 Sets of Coefficients

4.2.1 Fixed Effects

The fixed effect variables include:

```
## Source: local data frame [10 x 3]
##
##           coef      mean      sd
## 1      intercept 18.4720231 0.20711765
## 2         Latitude -0.3655001 0.30575498
## 3         Longitude  0.3116465 0.35502875
## 4      TotDASqKM -1.0988664 0.36440642
## 5         Forest -0.4424734 0.07889847
## 6 ReachElevationM  0.1212420 0.14877681
## 7 SurificialCoarseC -0.2334957 0.06283271
## 8      CONUSWetland  0.4721499 0.08591556
## 9 ImpoundmentsAllSqKM 1.3261676 0.37490526
## 10 airTemp.TotDASqKM -0.1183657 0.01772925
```

This plot shows the mean \pm 1 stdev for each effect excluding the intercept.

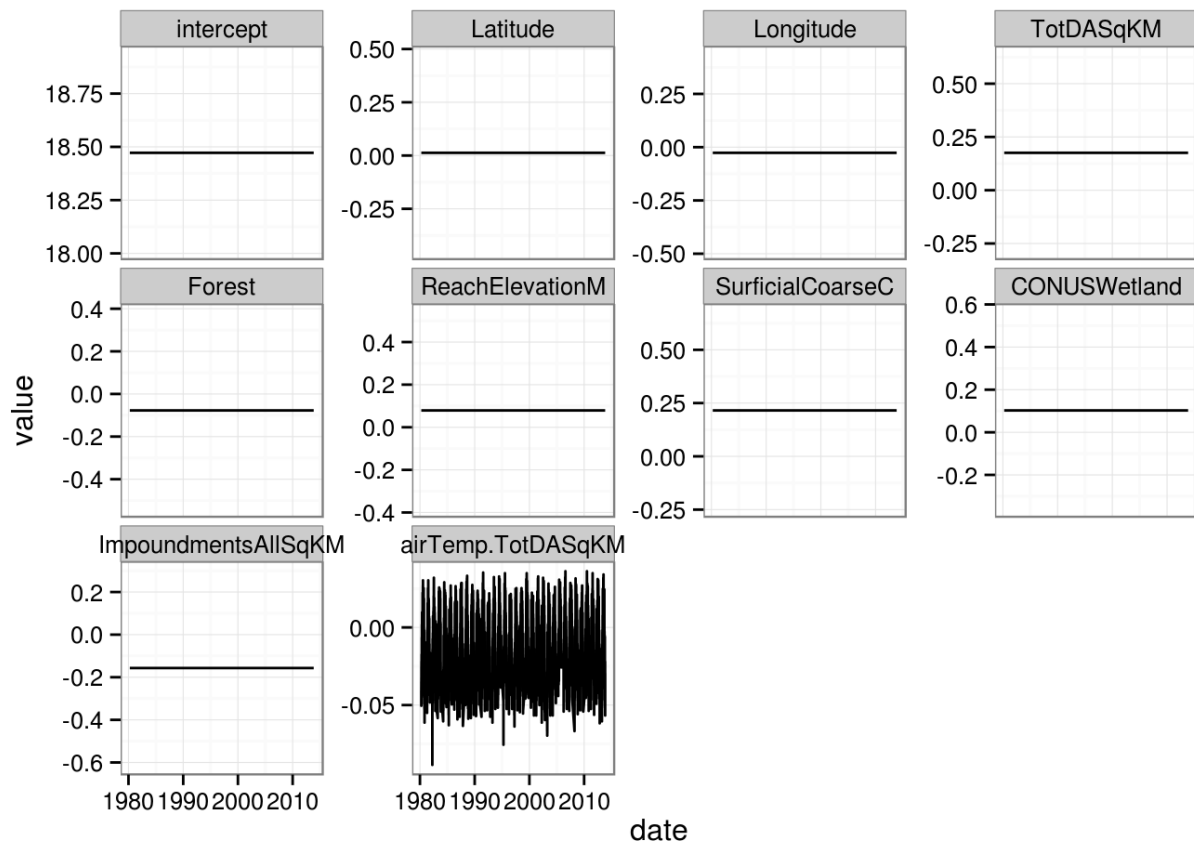


Only one of these variables (`airTemp.TotDASqKM`) varies by day, the rest are constant for each site/catchment.

```
##  intercept  Latitude  Longitude  TotDASqKM  Forest  ReachElevationM
```

```
## 1      1 -0.03513392 -0.08475244 -0.1598095 0.1746388      0.6518523
## 2      1 -0.03513392 -0.08475244 -0.1598095 0.1746388      0.6518523
## 3      1 -0.03513392 -0.08475244 -0.1598095 0.1746388      0.6518523
## 4      1 -0.03513392 -0.08475244 -0.1598095 0.1746388      0.6518523
## 5      1 -0.03513392 -0.08475244 -0.1598095 0.1746388      0.6518523
## 6      1 -0.03513392 -0.08475244 -0.1598095 0.1746388      0.6518523
##      SurficialCoarseC CONUSWetland ImpoundmentsAllSqKM airTemp.TotDASqKM
## 1      -0.9230302      0.2173934      -0.1182131      0.3447229
## 2      -0.9230302      0.2173934      -0.1182131      0.4260411
## 3      -0.9230302      0.2173934      -0.1182131      0.4260411
## 4      -0.9230302      0.2173934      -0.1182131      0.3270451
## 5      -0.9230302      0.2173934      -0.1182131      0.3906854
## 6      -0.9230302      0.2173934      -0.1182131      0.2952249
```

Using matrix multiplication to compute the row-wise sum of the fixed effects.



4.2.2 HUC Effects

The huc effects include:

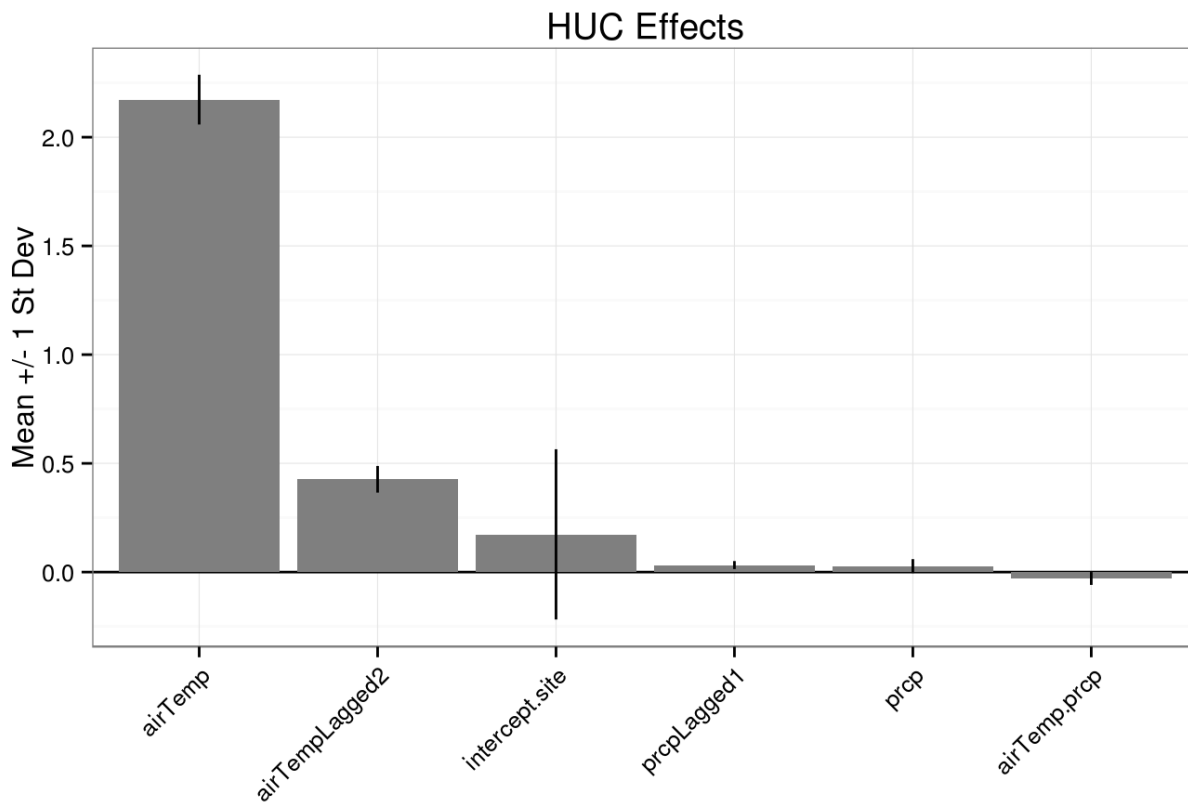
```
## Source: local data frame [32 x 7]
##
##      huc  airTemp airTemp.prcp airTempLagged2 intercept.site
## 1  01050001 2.092222 -0.02869864      0.3332813      0.21158768
```

```
## 2 01050002 2.151131 -0.02761145 0.5113379 -0.01284352
## 3 01050004 2.362157 -0.01155171 0.6099687 0.88495896
## 4 01070001 2.052302 -0.17412735 0.2688639 -0.08777879
## 5 01070003 1.949856 -0.14322564 0.2812626 0.89789031
## 6 01070004 1.989773 -0.01110612 0.2675478 -0.04145645
## 7 01070005 2.511778 0.17565874 0.2483573 0.27816628
## 8 01070006 2.445114 -0.13298623 0.3975328 0.37746070
## 9 01080101 1.817906 -0.19321300 0.2161348 -1.23386557
## 10 01080102 1.792537 -0.21922670 0.2784511 -0.17613027
## .. ... .. ... ..
## Variables not shown: prcp (dbl), prcpLagged1 (dbl)
```

For the selected catchment, which is in HUC 01080204, the parameters are:

```
## Source: local data frame [6 x 4]
##
##      huc      coef      mean      sd
## 1 01080204 intercept.site 0.17349293 0.39150153
## 2 01080204 airTemp 2.17276986 0.11441445
## 3 01080204 airTempLagged2 0.42671247 0.06129833
## 4 01080204 prcp 0.02741676 0.03203091
## 5 01080204 prcpLagged1 0.03232941 0.01830023
## 6 01080204 airTemp.prcp -0.02919445 0.02962109
```

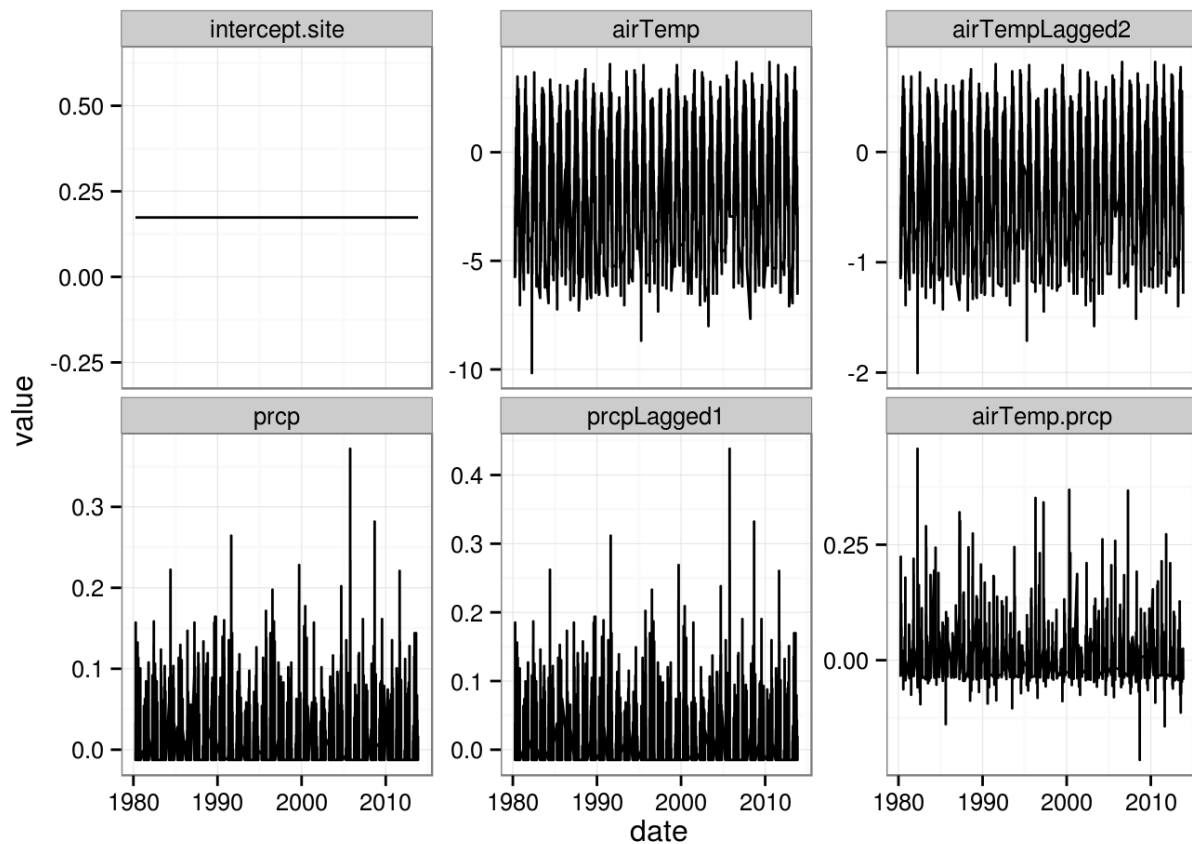
This plot shows the mean \pm 1 stdev for each effect within HUC 01080204.



All of these variables varies by day, except for the site intercept, which is always 1.

```
##      intercept.site  airTemp airTempLagged2      prcp prcpLagged1
## 1          1 -2.157086             NA  0.5985377      NA
## 2          1 -2.665931             NA -0.4594738  0.5978843
## 3          1 -2.665931      -2.168564 -0.4594738 -0.4598302
## 4          1 -2.046468      -2.678835 -0.4594738 -0.4598302
## 5          1 -2.444694      -2.678835 -0.1420704 -0.4598302
## 6          1 -1.847355      -2.057635 -0.4594738 -0.1425159
##      airTemp.prcp
## 1      -1.2910975
## 2       1.2249253
## 3       1.2249253
## 4       0.9402984
## 5       0.3473186
## 6       0.8488112
```

Using matrix multiplication to compute the row-wise sum of the fixed effects.



4.2.3 Site Effects

The site effects include:

```
## Source: local data frame [944 x 7]
```

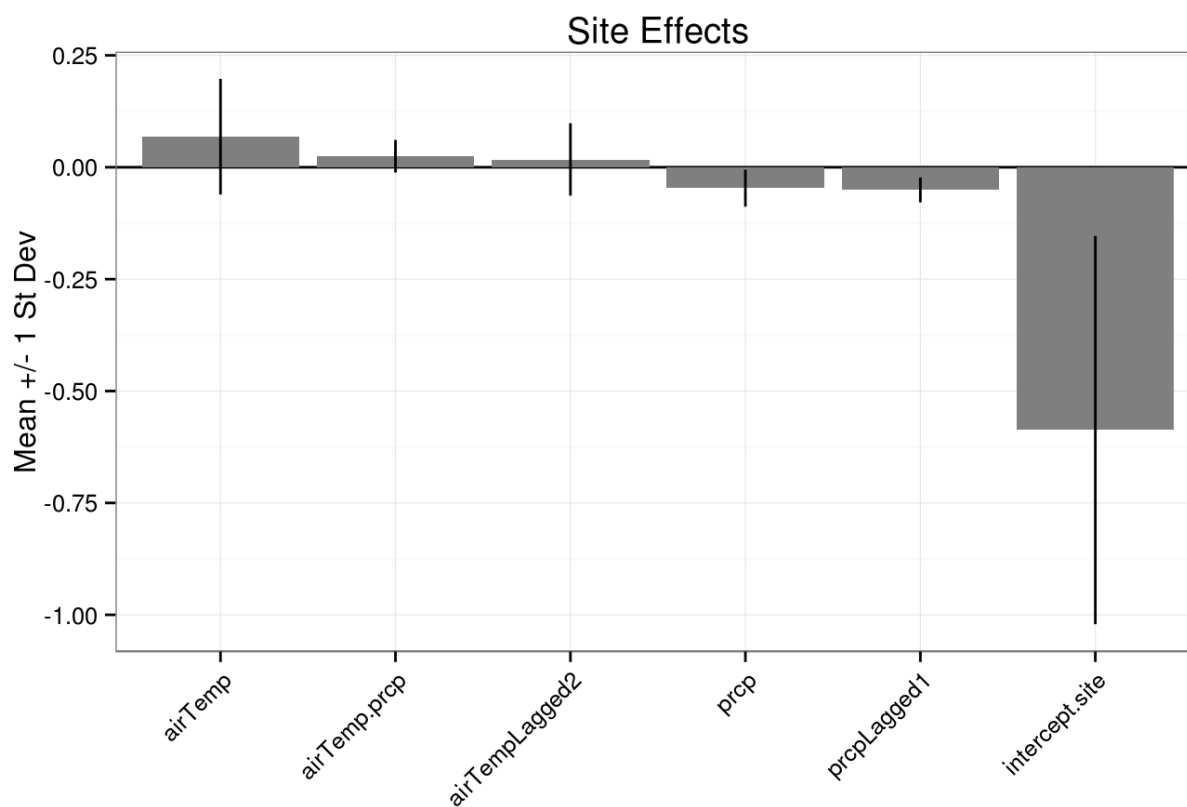


```
##
##      site      airTemp airTemp.prcp airTempLagged2 intercept.site
## 1 CTDEP_1 -0.12630205 -0.017312187 0.08484531 1.2578088
## 2 CTDEP_1008 0.15299703 0.042863774 0.05039532 -0.9084381
## 3 CTDEP_101 0.25431639 -0.032845844 -0.15941858 -0.4746102
## 4 CTDEP_1030 0.12569869 -0.037874140 -0.14887135 3.8932751
## 5 CTDEP_1038 0.49346919 0.020565352 -0.03867491 -1.7819292
## 6 CTDEP_1068 0.38002386 -0.022122422 0.04002566 -0.8706286
## 7 CTDEP_1081 0.14522074 -0.001672359 0.13879345 1.2955307
## 8 CTDEP_1083 0.03244799 0.027782866 0.04201264 0.1108283
## 9 CTDEP_1084 0.13868452 0.004551128 0.02550003 -3.2756975
## 10 CTDEP_1088 0.20342990 0.002046396 0.11325701 -0.7732254
## .. ...
## Variables not shown: prcp (dbl), prcpLagged1 (dbl)
```

For the selected site, which is MAFW_MAPleas55, the parameters are:

```
## Source: local data frame [6 x 4]
##
##      site      coef      mean      sd
## 1 MAFW_MAPleas55 intercept.site -0.58714267 0.43383025
## 2 MAFW_MAPleas55      airTemp 0.06820972 0.12927053
## 3 MAFW_MAPleas55 airTempLagged2 0.01741933 0.08083308
## 4 MAFW_MAPleas55      prcp -0.04672892 0.04125514
## 5 MAFW_MAPleas55 prcpLagged1 -0.05062016 0.02782671
## 6 MAFW_MAPleas55      airTemp.prcp 0.02465640 0.03642801
```

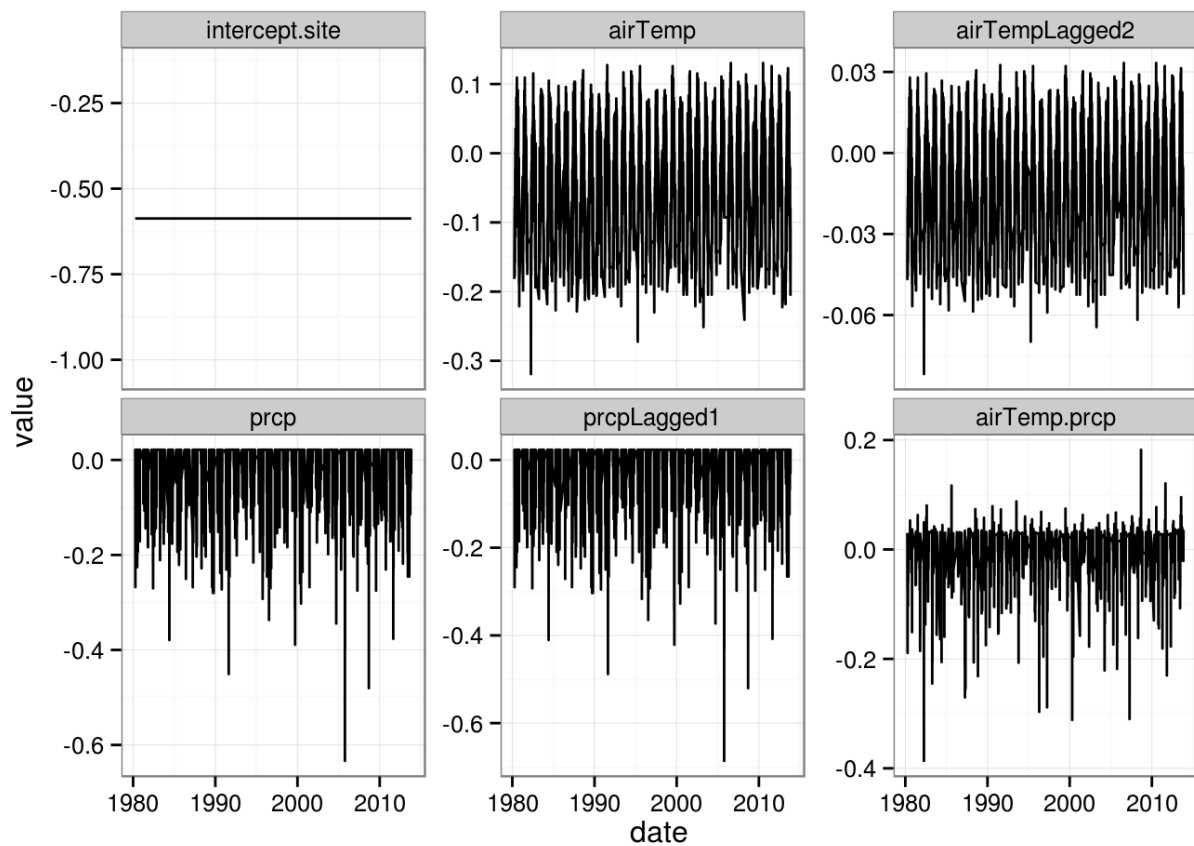
This plot shows the mean \pm 1 stdev for each effect for site MAFW_MAPleas55.



All of these variables varies by day, except for the site intercept, which is always 1.

```
##   intercept.site   airTemp airTempLagged2      prcp prcpLagged1
## 1             1 -2.157086             NA  0.5985377          NA
## 2             1 -2.665931             NA -0.4594738  0.5978843
## 3             1 -2.665931      -2.168564 -0.4594738 -0.4598302
## 4             1 -2.046468      -2.678835 -0.4594738 -0.4598302
## 5             1 -2.444694      -2.678835 -0.1420704 -0.4598302
## 6             1 -1.847355      -2.057635 -0.4594738 -0.1425159
##   airTemp.prcp
## 1   -1.2910975
## 2    1.2249253
## 3    1.2249253
## 4    0.9402984
## 5    0.3473186
## 6    0.8488112
```

Using matrix multiplication to compute the row-wise sum of the fixed effects.

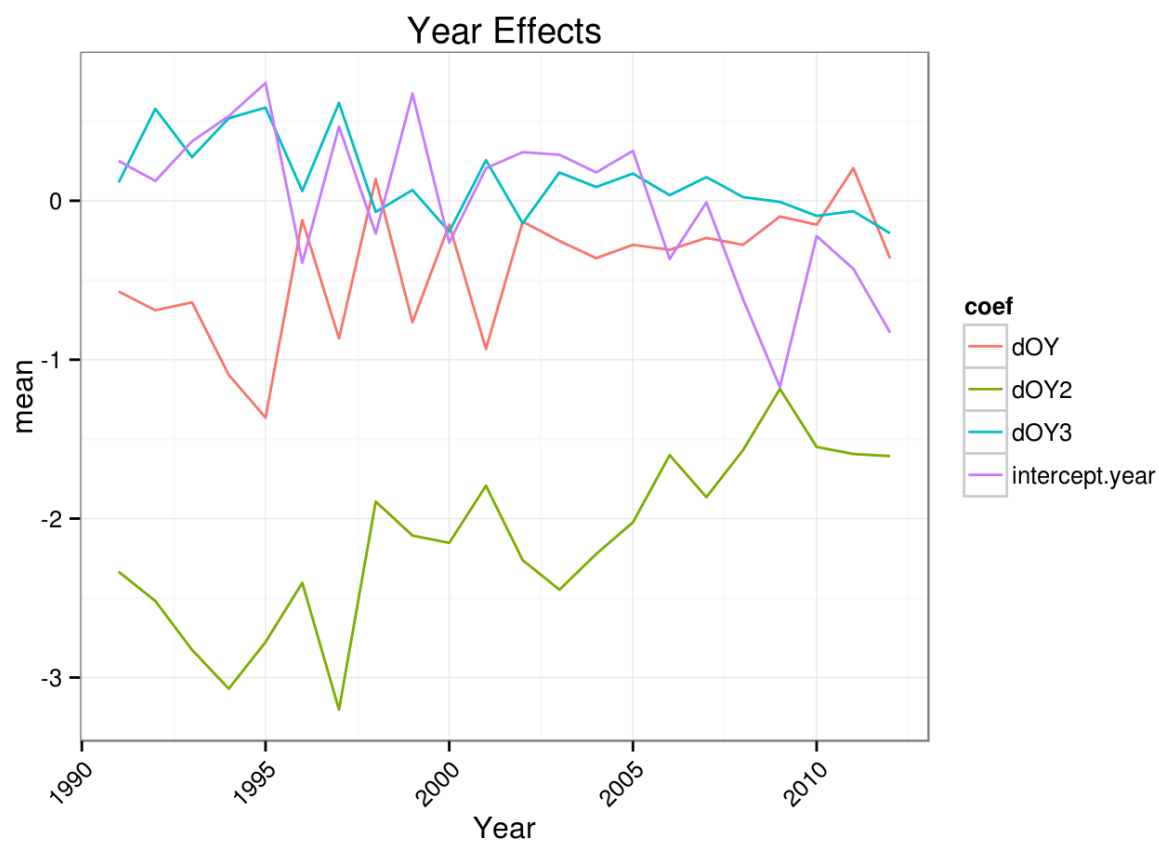


4.2.4 Year Effects

The year effects include:

```
## Source: local data frame [22 x 5]
##
##   year      d0Y      d0Y2      d0Y3 intercept.year
## 1  1991 -0.5705137 -2.333859  0.11411258  0.2507031
## 2  1992 -0.6890643 -2.518361  0.57819012  0.1246343
## 3  1993 -0.6395225 -2.826071  0.27454656  0.3738921
## 4  1994 -1.0960559 -3.070439  0.51926832  0.5322970
## 5  1995 -1.3646546 -2.776573  0.58597807  0.7412415
## 6  1996 -0.1215034 -2.404118  0.06153273 -0.3906299
## 7  1997 -0.8659866 -3.201794  0.61576778  0.4666966
## 8  1998  0.1369618 -1.893005 -0.07001396 -0.2070093
## 9  1999 -0.7643593 -2.106699  0.06774042  0.6747621
## 10 2000 -0.1498699 -2.152647 -0.19433576 -0.2641565
## .. ...
```

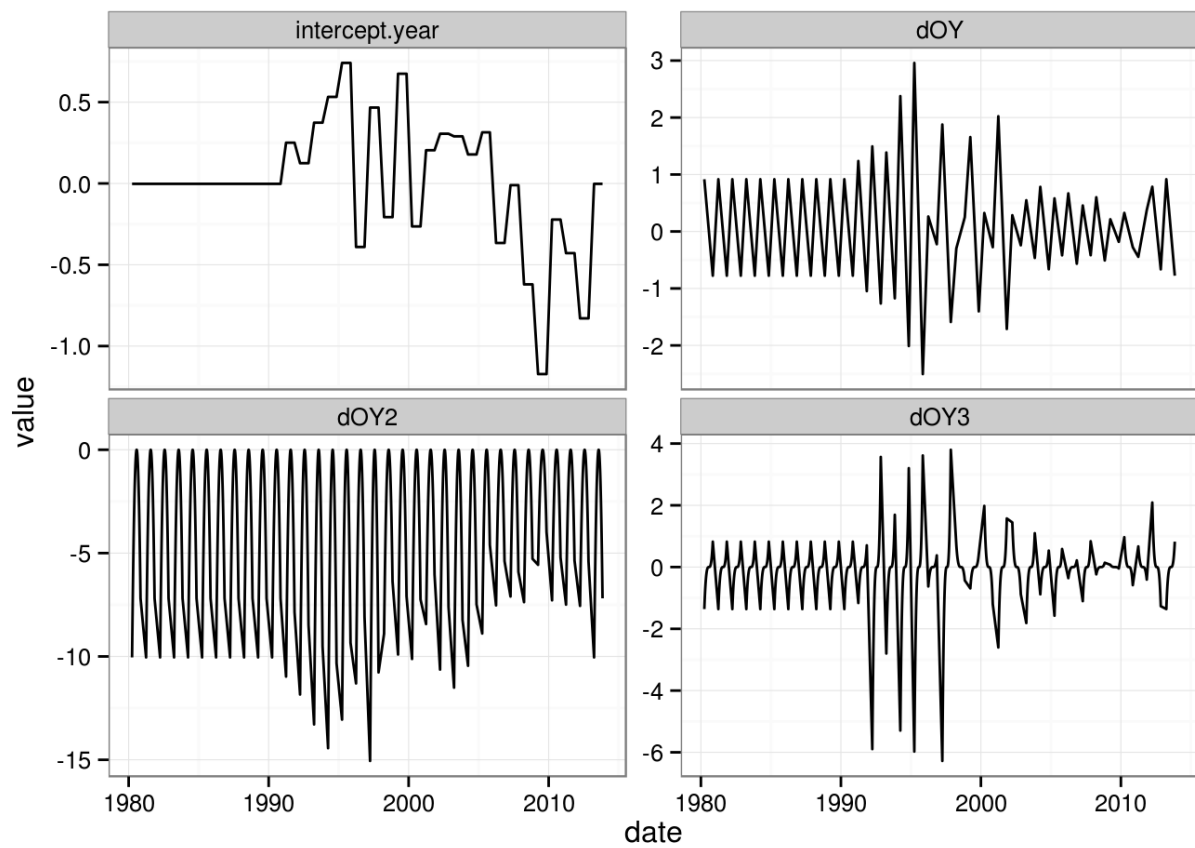
This plot shows the mean \pm 1 stdev for each year.



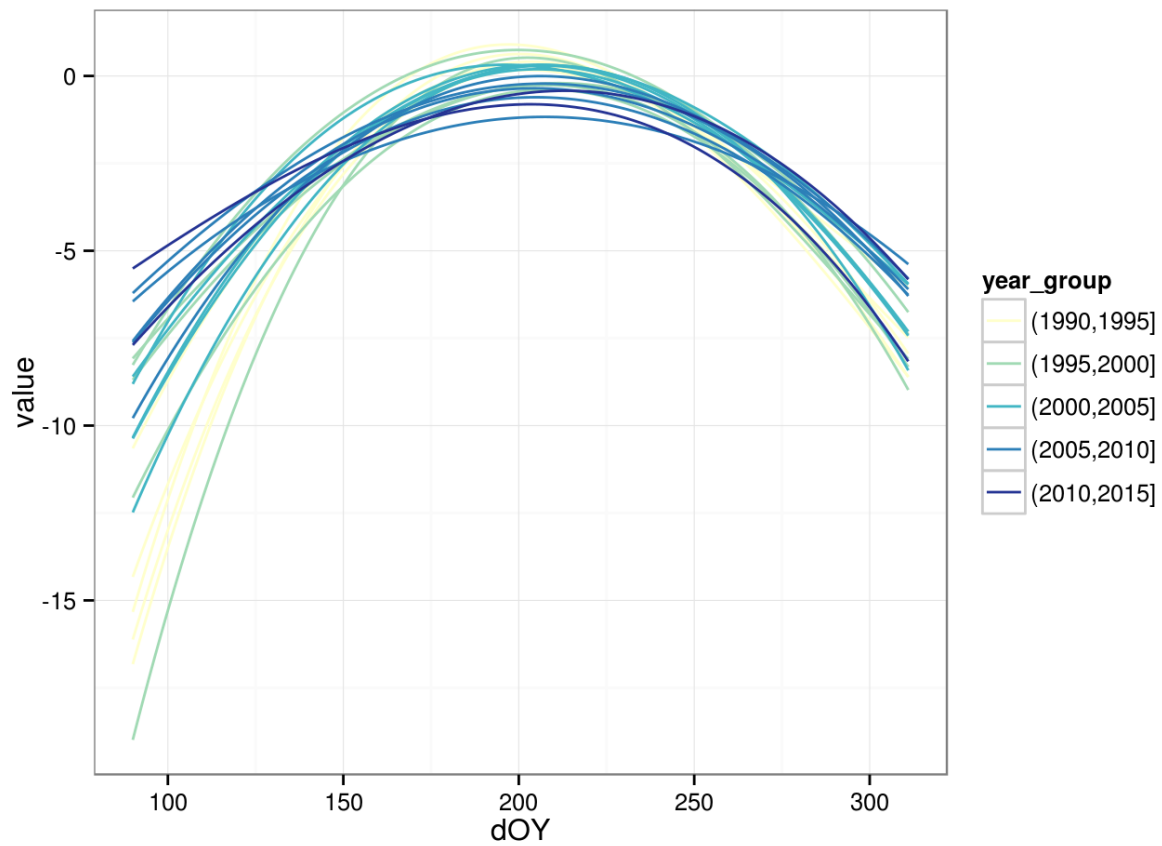
All of these variables varies by day, except for the intercept, which is always 1.

##	intercept.year	dOY	dOY2	dOY3
## 1	1	-2.168378	4.701863	-10.195415
## 2	1	-2.150267	4.623650	-9.942082
## 3	1	-2.132157	4.546092	-9.692981
## 4	1	-2.114046	4.469191	-9.448076
## 5	1	-2.095936	4.392946	-9.207332
## 6	1	-2.077825	4.317357	-8.970712

Using matrix multiplication to compute the row-wise sum of the fixed effects.

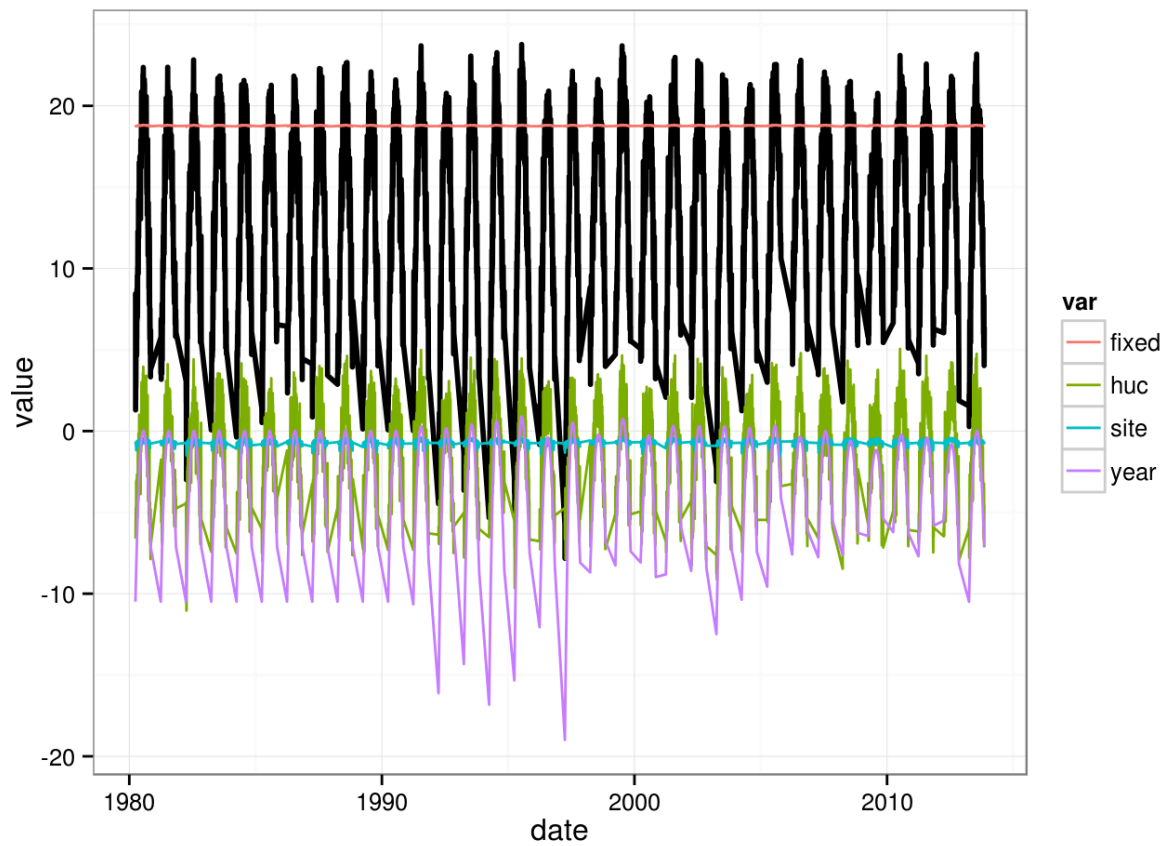


Curious to see how variable the cubic spline is for each year.



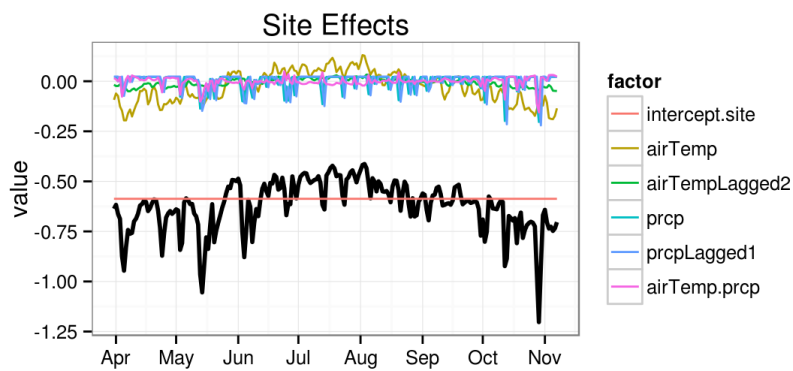
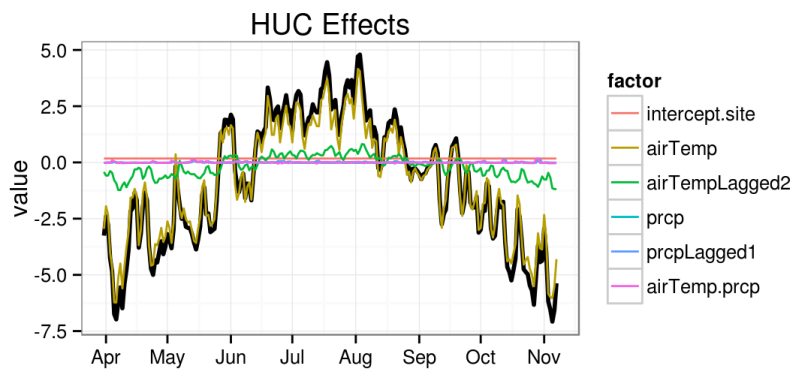
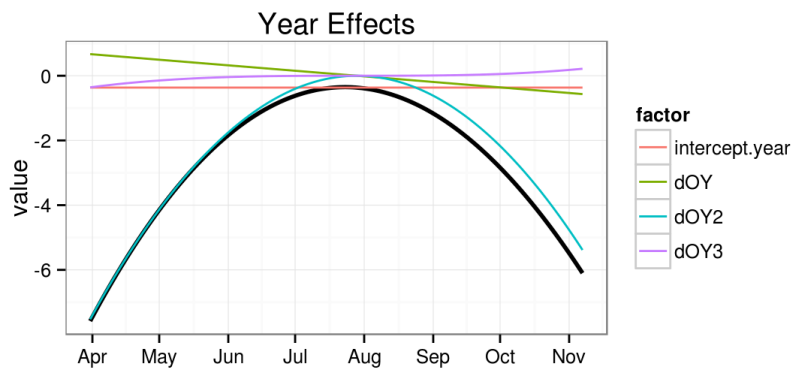
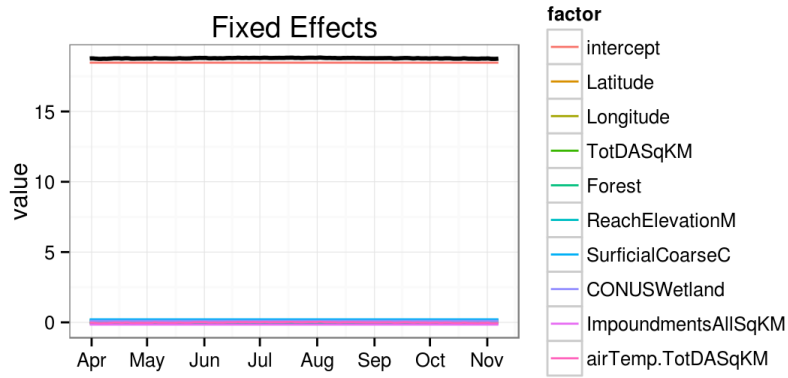
4.3 Sum All Effects

This figure shows the contributions from each set of factors. The black line is the overall sum representing the predicted temperature for this site (excluding the autoregressive error term).



5 Example Predictions for 2006

This section focuses on the predictions for one site (MAFW_MAPleas55), which is in catchment (830189) and HUC8 (01080204), and one year (2006). This figure shows the contributions from each set of factors. The black lines are the sum of all lines within each panel.



This figure takes the sum of each set of factors (black line in each panel above) and computes the overall predicted temperature (shown in this figure as the black line). This does not include the autoregressive residual term.

