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 * HW2 Programming Q2
 */
```

Runtime Analysis of TwoStackQueue

1. Enqueue: $O(1)$

```
public void enqueue(AnyType x){
    S1.push(x);
}
```

The enqueue method consists of one call to `S1.push`. Thus the runtime is the same as runtime for `push()` method in `MyStack` class. `MyStack` class pushes an element on the stack by adding it to the beginning of its `LinkedList` (instance variable of `MyStack` class). Since the cost of adding an element at index 0 of a `LinkedList` is $O(1)$ operation the runtime of `push()` is also $O(1)$. Thus runtime of enqueue is also $O(1)$

2. Dequeue: Worst Case: $O(n)$, Best Case: $O(1)$

```
public AnyType dequeue() {
    if (!S2.isEmpty()) {
        return S2.pop();
    } else if (!S1.isEmpty()) {
        transfer();
        return S2.pop();
    } else {
        System.out.println("Queue Empty");
    }
    return null;
}
```

If `S2` is non-empty then dequeue is a single call to the `push` method of `MyStack`. For `MyStack` this is a $O(1)$ operation because removing an element from index 0 of `LinkedList` is $O(1)$ operation. However in the worst case all the n elements in the queue are on `Stack 1` and `Stack2` is empty. In such a scenario the `transfer()` method is called which loops through `S1` and one-by-one pushes an element off it and puts it on `S2`. This takes linear time in size of `Stack1` (and thus the size of the queue) since there is one push and put operation per element in the queue.