



UNIVERSIDAD FIDELITAS

Escuela de Ingeniería Eléctrica

Control automático

Tarea#2

Sistemas de segundo orden

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II cuatrimestre 2018

Fecha: 23 de mayo del 2018

Parte realizada en matlab:

```
>> num=[3]
```

```
num = 3
```

```
>> den=[1 2 1]
```

```
den = 1    2    1
```

```
>> tf(num,den)
```

```
ans =
```

```
    3
```

```
-----
```

```
s^2 + 2 s + 1
```

Continuous-time transfer function.

```
>> G=tf(num,den)
```

```
G =
```

```
    3
```

```
-----
```

```
s^2 + 2 s + 1
```

Continuous-time transfer function.

```
>> H=[1]
```

```
H = 1
```

```
>> feedback(G,H)
```

```
ans =
```

```
    3
```

```
-----
```

```
s^2 + 2 s + 4
```

Continuous-time transfer function.

```
>> [Z,P,K]=tf2zp(num,den)
```

Z =

Empty matrix: 0-by-1

P =

-1

-1

K =

3

```
>> z=[0.5]
```

z =

0.5000

```
>> wn=[2]
```

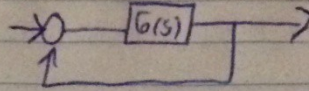
wn =

2

```
>> zgrid(z,wn)
```

Parte realizada a mano:

$$G = \frac{3}{s^2 + 2s + 1}$$



Feedback

$$\frac{\frac{3}{s^2 + 2s + 1}}{\frac{s^2 + 2s + 4}{s^2 + 2s + 1}} \Rightarrow \frac{3}{s^2 + 2s + 4}$$

$$\frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} = \frac{3}{s^2 + 2s + 4}$$

$$\frac{3 \times \frac{4}{4}}{s^2 + 2s + 4} \Rightarrow \frac{\frac{3}{4} \times 4}{s^2 + 2s + 4}$$

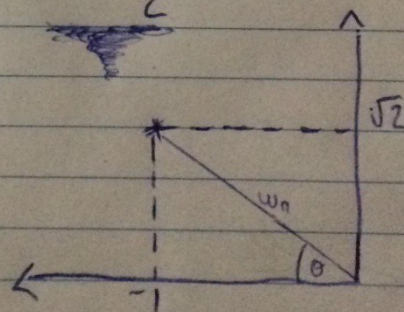
Donde : $\sqrt{\omega_n^2} = \sqrt{4} \quad \omega_n = 2$

$$\zeta \omega_n = \frac{2}{2} \Rightarrow \zeta \cdot 2 = 1 \Rightarrow \zeta = \frac{1}{2}$$

Donde

$$\alpha = -\zeta \omega_n$$

$$\alpha = -1$$



$$\omega = j\sqrt{1 - \zeta^2} \Rightarrow \omega = 2(\sqrt{1 - \frac{1}{4}})$$

$$\omega = \sqrt{2} \approx 1,41$$