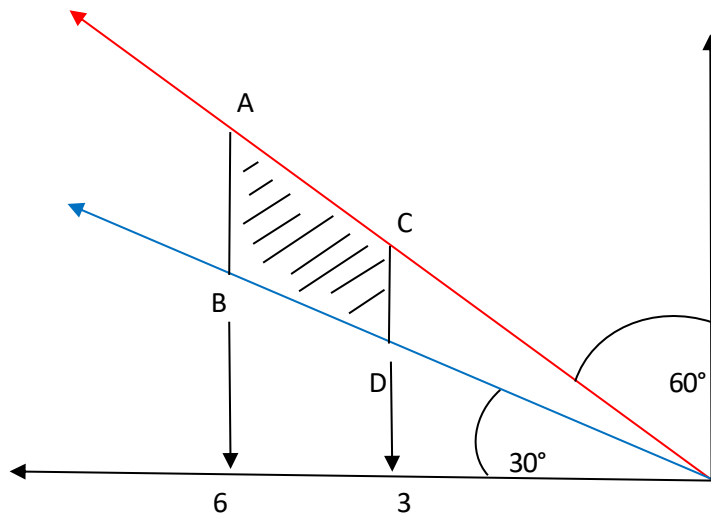


CONTROL AUTOMATICO

Tiempos de Estabilización y Sobre Impulso

Profesor: Erick Salas Chaverri.

Jeffry Calderón Montero



1) ENCONTRAR ω_n y ζ

$$\zeta = \cos(30) = \sqrt{3}/2$$

$$\zeta = \cos(60) = 1/2$$

PUNTO A

$$3 = \omega_n \zeta$$

$$6 = 1/2 \omega_n$$

$$(6 \cdot 2)/1 = \omega_n$$

$$\omega_n = 12$$

PUNTO B

$$6 = \omega_n \zeta$$

$$6 = \sqrt{3}/2 \omega_n$$

$$(6 \cdot 2)/\sqrt{3} = \omega_n$$

$$\omega_n = 4\sqrt{3}$$

PUNTO C

$$3 = \omega_n \zeta$$

$$3 = 1/2 \omega_n$$

$$(3)/(1/2) = \omega_n$$

$$\omega_n = 6$$

PUNTO D

$$3 = \omega_n \zeta$$

$$3 = (\sqrt{3})/2 \omega_n$$

$$(3 \cdot 2)/\sqrt{3} = \omega_n$$

$$\omega_n = 2\sqrt{3}$$

2)

SOBREIMPULSO

$$M=e^{-(\zeta\pi/\sqrt{1-\zeta^2})}$$

$$M_1=e^{-((1/2)\pi/\sqrt{1-(1/2)^2})}$$

$$M_1=0.163$$

$$M_2=e^{-((\sqrt{3}/2)\pi/\sqrt{1-(\sqrt{3}/2)^2})}$$

$$M_2=0.004$$

TIEMPOS DE ESTABILIZACION

$$T_{s2}=4/\omega_n\zeta$$

PUNTO A

$$T_{s2}=4/(1/2)*12$$

$$T_{s2}=0.66 \%$$

PUNTO B

$$T_{s2}=4/(1/2)*12$$

$$T_{s2}=0.66 \%$$

PUNTO C

$$T_{s2}=4/(1/2)*6$$

$$T_{s2}=1.33 \%$$

PUNTO D

$$T_{s2}=4/(\sqrt{3}/2)*2\sqrt{3}$$

$$T_{s2}=1.33 \%$$

3)

FUNCION DE TRANSFERENCIA

$$\frac{\omega n^2}{S^2 + 2\omega n \zeta S + \omega n^2}$$

PUNTO A

$$\frac{(12)^2}{S^2 + 2(1/2)12S + (12)^2}$$

$$\frac{144}{S^2 + 12S + 144}$$

PUNTO C

$$\frac{(6)^2}{S^2 + 2(1/2)6S + (6)^2}$$

$$\frac{36}{S^2 + 6S + 36}$$

PUNTO B

$$\frac{(4\sqrt{3})^2}{S^2 + 2(\sqrt{3}/2)(4\sqrt{3})S + (4\sqrt{3})^2}$$

$$\frac{48}{S^2 + 12S + 48}$$

PUNTO A

$$\frac{(12)^2}{S^2 + 2(1/2)12S + (12)^2}$$

$$\frac{12}{S^2 + 6S + 12}$$

PUNTO A

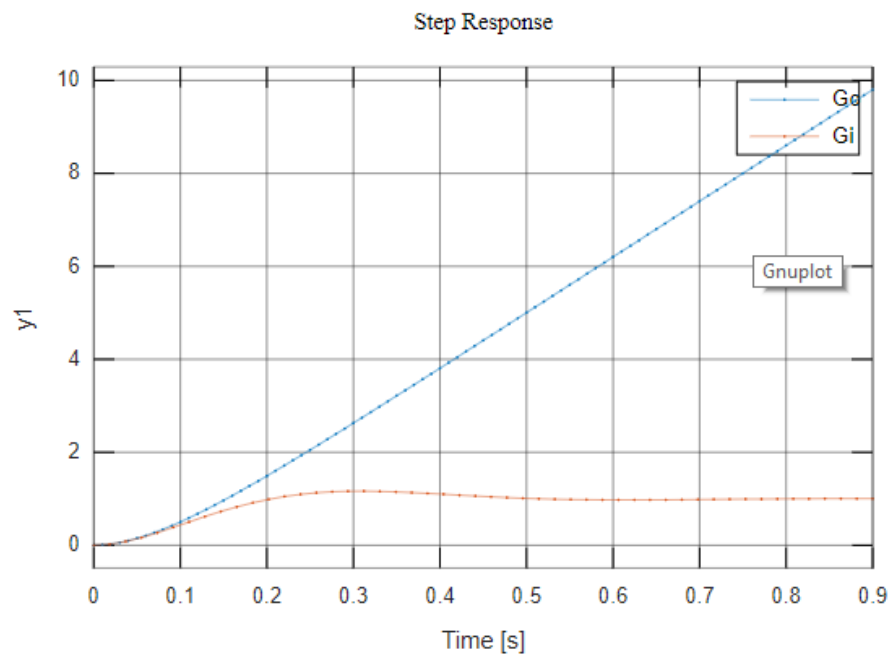
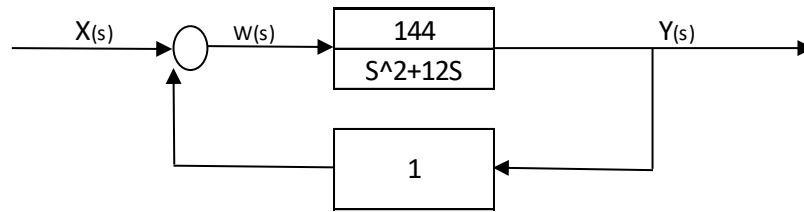
$$\frac{Q_s}{P_s + Q_s} = \frac{144}{S^2 + 12S + 144}$$

$$\frac{144}{P_s} = \frac{144}{S^2 + 12S}$$

$$P_s = \frac{S^2 + 12S}{144} \quad *144$$

$$P_s = S^2 + 12S$$

$$\frac{Q_s}{P_s} = \frac{144}{S^2 + 12S}$$



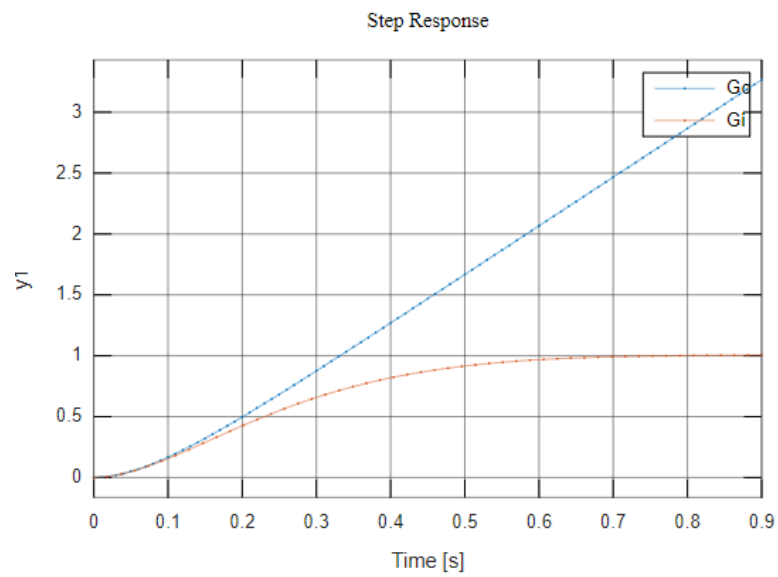
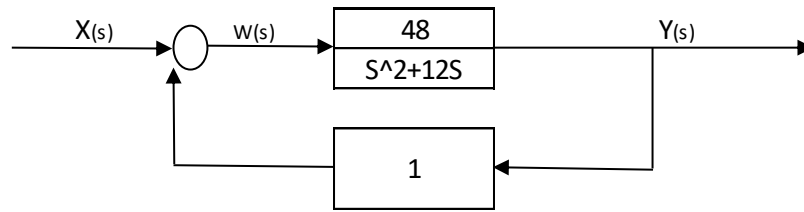
PUNTO B

$$\frac{Q_s}{P_s + Q_s} = \frac{48}{s^2 + 12s + 48}$$

$$\frac{48}{P_s} = \frac{48}{s^2 + 12s}$$

$$P_s = \frac{s^2 + 12s}{48} \quad *48$$

$$P_s = s^2 + 12s \quad \frac{Q_s}{P_s} = \frac{48}{s^2 + 12s}$$



PUNTO C

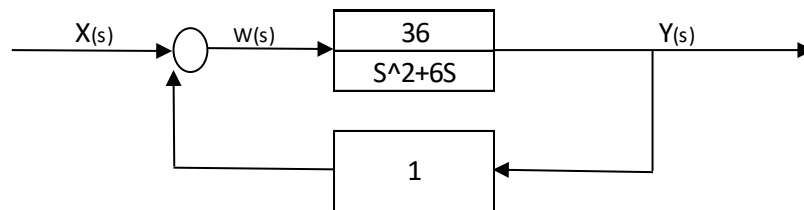
$$\frac{Q_s}{P_s + Q_s} = \frac{36}{S^2 + 6S + 36}$$

$$\frac{36}{P_s} = \frac{36}{S^2 + 6S}$$

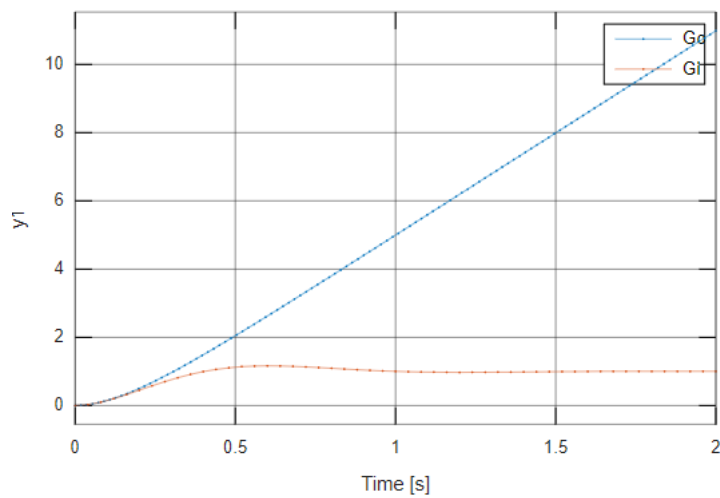
$$P_s = \frac{S^2 + 6S}{*36}$$

$$P_s = \frac{36}{S^2 + 6S}$$

$$\frac{Q_s}{P_s} = \frac{36}{S^2 + 6S}$$



Step Response



PUNTO C

$$\frac{Q_s}{P_s + Q_s} = \frac{12}{s^2 + 6s + 12}$$

$$\frac{12}{P_s} = \frac{12}{s^2 + 6s}$$

$$P_s = \frac{s^2 + 6s}{12} \quad *12$$

$$P_s = s^2 + 6s \quad \frac{Q_s}{P_s} = \frac{12}{s^2 + 6s}$$

