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1. Para cada punto obtener  $\zeta$  y  $W_n$ .

Se utiliza la fórmula  $\zeta = \cos(\theta)$

$$\zeta = \cos(30^\circ) \quad \zeta = \frac{\sqrt{3}}{2}$$

$$\zeta = \cos(60^\circ) \quad \zeta = \frac{1}{2}$$

y luego utilizamos  $W_n = \frac{\alpha}{\zeta}$

$$\begin{array}{ll} W_n = \frac{3}{\frac{\sqrt{3}}{2}} & W_n = 2\sqrt{3} \\ W_n = \frac{3}{\frac{1}{2}} & W_n = 6 \end{array}$$

$$\begin{array}{ll} W_n = \frac{6}{\frac{\sqrt{3}}{2}} & W_n = 4\sqrt{3} \\ W_n = \frac{6}{\frac{1}{2}} & W_n = 12 \end{array}$$

2. Para cada punto obtener  $M_p$  y  $T_{s2\%}$ .

Para el sobre-impulso se utiliza la fórmula  $M_p = e^{-\left(\frac{\zeta\pi}{\sqrt{1-\zeta^2}}\right)}$ .

$$\begin{array}{l} M_p = e^{-\left(\frac{\frac{\sqrt{3}}{2}\pi}{\sqrt{1-\frac{\sqrt{3}^2}{2}^2}}\right)} \\ M_p = 4.33 \times 10^{-3} \end{array}$$

$$\begin{array}{l} M_p = e^{-\left(\frac{\frac{1}{2}\pi}{\sqrt{1-\frac{1}{2}^2}}\right)} \\ M_p = 0.163 \end{array}$$

Luego se aplica la fórmula  $T_{s2\%} = \frac{4}{\zeta W_n}$

$$\begin{array}{l} T_{s2\%} = \frac{4}{\frac{\sqrt{3}}{2} \cdot 2\sqrt{3}} \\ T_{s2\%} = \frac{4}{3} \end{array}$$

$$\begin{array}{l} T_{s2\%} = \frac{4}{\frac{\sqrt{3}}{2} \cdot 4\sqrt{3}} \\ T_{s2\%} = \frac{2}{3} \end{array}$$

$$T_{s2\%} = \frac{4}{\frac{1}{2} \cdot 6}$$

$$T_{s2\%} = \frac{4}{3}$$

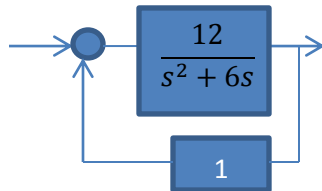
$$T_{s2\%} = \frac{4}{\frac{1}{2} \cdot 12}$$

$$T_{s2\%} = \frac{2}{3}$$

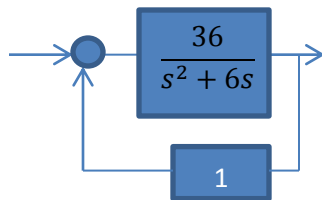
3. Para cada punto sugiera un sistema.

Para las funciones usamos la siguiente fórmula  $G = \frac{Wn^2}{s^2 + 2\zeta Wns + Wn^2}$

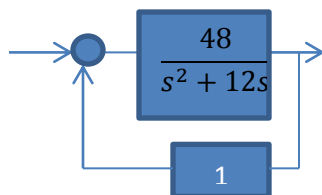
$$\text{➤ } G1 = \frac{2\sqrt{3}^2}{s^2 + 2 \cdot \frac{\sqrt{3}}{2} \cdot 2\sqrt{3}s + 2\sqrt{3}^2} \quad G1 = \frac{12}{s^2 + 6s + 12}$$



$$\text{➤ } G2 = \frac{6^2}{s^2 + 2 \cdot \frac{1}{2} \cdot 6s + 6^2} \quad G2 = \frac{36}{s^2 + 6s + 36}$$



$$\text{➤ } G3 = \frac{4\sqrt{3}^2}{s^2 + 2 \cdot \frac{\sqrt{3}}{2} \cdot 4\sqrt{3}s + 4\sqrt{3}^2} \quad G3 = \frac{48}{s^2 + 12s + 48}$$



$$\Rightarrow G4 = \frac{12^2}{s^2 + 2\frac{1}{2}12s + 12^2}$$

$$G4 = \frac{144}{s^2 + 12s + 144}$$

