# ALICE: Towards Understanding Adversarial Learning for Joint Distribution Matching

### Authored by:

Lawrence Carin Ricardo Henao Changyou Chen Chunyuan Li Yuchen Pu Liqun Chen Hao Liu

#### Abstract

We investigate the non-identifiability issues associated with bidirectional adversarial training for joint distribution matching. Within a framework of conditional entropy, we propose both adversarial and non-adversarial approaches to learn desirable matched joint distributions for unsupervised and supervised tasks. We unify a broad family of adversarial models as joint distribution matching problems. Our approach stabilizes learning of unsupervised bidirectional adversarial learning methods. Further, we introduce an extension for semi-supervised learning tasks. Theoretical results are validated in synthetic data and real-world applications.

## 1 Paper Body

Deep directed generative models are a powerful framework for modeling complex data distributions. Generative Adversarial Networks (GANs) [1] can implicitly learn the data generating distribution; more specifically, GAN can learn to sample from it. In order to do this, GAN trains a generator to mimic real samples, by learning a mapping from a latent space (where the samples are easily drawn) to the data space. Concurrently, a discriminator is trained to distinguish between generated and real samples. The key idea behind GAN is that if the discriminator finds it difficult to distinguish real from artificial samples, then the generator is likely to be a good approximation to the true data distribution. In its standard form, GAN only yields a one-way mapping, i.e., it lacks an inverse mapping mechanism (from data to latent space), preventing GAN from being able to do inference. The ability to compute a posterior distribution

of the latent variable conditioned on a given observation may be important for data interpretation and for downstream applications (e.g., classification from the latent variable) [2, 3, 4, 5, 6, 7]. Efforts have been made to simultaneously learn an efficient bidirectional model that can produce high-quality samples for both the latent and data spaces [3, 4, 8, 9, 10, 11]. Among them, the recently proposed Adversarially Learned Inference (ALI) [4, 10] casts the learning of such a bidirectional model in a GAN-like adversarial framework. Specifically, a discriminator is trained to distinguish between two joint distributions: that of the real data sample and its inferred latent code, and that of the real latent code and its generated data sample. While ALI is an inspiring and elegant approach, it tends to produce reconstructions that are not necessarily faithful reproductions of the inputs [4]. This is because ALI only seeks to match two joint distributions, but the dependency structure (correlation) between the two random variables (conditionals) within each joint is not specified or constrained. In practice, this results in solutions that satisfy ALI?s objective and that are able to produce real-looking samples, but have difficulties reconstructing observed data [4]. ALI also has difficulty discovering the correct pairing relationship in domain transformation tasks [12, 13, 14]. In this paper, (i) we first describe the non-identifiability issue of ALI. To solve this problem, we propose to regularize ALI using the framework of Conditional Entropy (CE), hence we call the proposed approach ALICE. (ii) Adversarial learning schemes are proposed to estimate the conditional 31st Conference on Neural Information Processing Systems (NIPS 2017), Long Beach, CA, USA.

entropy, for both unsupervised and supervised learning paradigms. (iii) We provide a unified view for a family of recently proposed GAN models from the perspective of joint distribution matching, including ALI [4, 10], CycleGAN [12, 13, 14] and Conditional GAN [15]. (iv) Extensive experiments on synthetic and real data demonstrate that ALICE is significantly more stable to train than ALI, in that it consistently yields more viable solutions (good generation and good reconstruction), without being too sensitive to perturbations of the model architecture, i.e., hyperparameters. We also show that ALICE results in more faithful image reconstructions. (v) Further, our framework can leverage paired data (when available) for semi-supervised tasks. This is empirically demonstrated on the discovery of relationships for cross domain tasks based on image data.

2

### Background

Consider two general marginal distributions q(x) and p(z) over x? X and z? Z. One domain can be inferred based on the other using conditional distributions, q(z-x) and p(x-z). Further, the combined structure of both domains is characterized by joint distributions q(x, z) = q(x)q(z-x) and p(x, z) = p(z)p(x-z). To generate samples from these random variables, adversarial methods [1] provide a sampling mechanism that only requires gradient backpropagation, without the need to specify the conditional densities. Specifically, instead of sampling directly from the desired conditional distribution, the random variable is generated as a deterministic transformation of two inputs,

the variable in the source domain, and an independent noise, e.g., a Gaussian distribution. Without loss of generality, we use an universal distribution approximator specification [9], i.e., the sampling procedure for conditionals?? p? (x—z) and z?? q? (z—x) is carried out through the following two generating processes: x ? = g? (z, ), z ? p(z), ? N (0, I), and z ? = g? (x, ?), x ? q(x),? ? N (0, I), x (1) where g? (?) and g? (?) are two generators, specified as neural networks with parameters? and?, respectively. In practice, the inputs of g? (?) and g? (?) are simple concatenations, [z] and [x?], respectively. Note that (1) implies that p? (x—z) and q? (z—x) are parameterized by ? and ? respectively, hence the subscripts. R The goal of GAN [1] is to match the marginal p? (x) = p? (x-z)p(z)dz to q(x). Note that q(x) denotes the true distribution of the data (from which we have samples) and p(z) is specified as a simple parametric distribution, e.g., isotropic Gaussian. In order to do the matching, GAN trains a ?-parameterized adversarial discriminator network, f? (x), to distinguish between samples from p? (x) and q(x). Formally, the minimax objective of GAN is given by the following expression: min max LGAN (?, ?) = Ex?q(x) [log ?(f? (x))] + Ex? ?p? (x-z),z?p(z) [log(1 ? ?(f? (? x)))],(2) ?

where ?(?) is the sigmoid function. The following lemma characterizes the solutions of (2) in terms of marginals p? (x) and q(x). Lemma 1 ([1]) The optimal decoder and discriminator, parameterized by {??,??}, correspond to a saddle point of the objective in (2), if and only if p?? (x) = q(x). Alternatively, ALI [4] matches the joint distributions p? (x, z) = p? (x-z)p(z) and q? (x, z)= q(x)q? (z—x), using an adversarial discriminator network similar to (2), f? (x, z), parameterized by ?. The minimax objective of ALI can be then written as ? ))] min max LALI (?, ?, ?) = Ex?q(x),?z?q? (z-x) [log ?(f? (x, z ?,?))]? (3) + Ex? ?p? (x-z),z?p(z)  $[\log(1??(f? (? x, z)))]$ . Lemma 2 ([4]) The optimum of the two generators and the discriminator with parameters {?? ?? , ? ? } form a saddle point of the objective in (3), if and only if p?? (x, z) = q?? (x, z). From Lemma 2, if a solution of (3) is achieved, it is guaranteed that all marginals and conditional distributions of the pair  $\{x, z\}$  match. Note that this implies that q? (z—x) and p? (z—x) match; however, (3) imposes no restrictions on these two conditionals. This is key for the identifiability issues of ALI described below.

3

Adversarial Learning with Information Measures

The relationship (mapping) between random variables x and z is not specified or constrained by ALI. As a result, it is possible that the matched distribution ?(x, z), p??(x, z) = q??(x, z) is undesirable for a given application. 2

 x1 1/2 0 1/2 x2 1/2 0 x2 0 sented as a 2? 2 contingency table. Figure 1(a) repre-  $x^2(1)/2$  sents all possible solutions of the ALI objective in (3), (c) (b) (a) for any ? ? [0, 1]. Figures 1(b) and 1(c) represent opposite extreme solutions when ? = 1 and ? = 0, respec- Figure 1: Illustration of possible solutions to tively. Note that although we can generate ?realistic? the ALI objective. The first row shows the map values of x from any sample of p(z), for 0;?; 1, we pings between two domains, The second row will have poor reconstruction ability since the sequence shows matched joint distribution, ?(x, z), as?? q? (z—x), x?? p? (x—? x? q(x), zz), can easily contingency tables parameterized by ? = [0, 1]. ? 6 = x. The two (trivial) exceptions where the model can achieve perfect reconstruction result in x correspond to  $? = \{1,$ 0, and are illustrated in Figures 1(b) and 1(c), respectively. From this simple example, we see that due to the flexibility of the joint distribution, ?(x, z), it is quite likely to obtain an undesirable solution to the ALI objective. For instance, i) one with poor reconstruction ability or ii) one where a single instance of z can potentially map to any possible value in X, e.g., in Figure 1(a) with ? = 0.5, z1 can generate either x1 or x2 with equal probability. Many applications require meaningful mappings. Consider two scenarios: ? A1: In unsupervised learning, one desirable property is cycle-consistency [12], meaning that the inferred z of a corresponding x, can reconstruct x itself with high probability. In Figure 1 this corresponds to either? ? 1 or? ? 0, as in Figures 1(b) and 1(c). A2: In supervised learning, the pre-specified correspondence between samples imposes restrictions on the mapping between x and z, e.g., in image tagging, x are images and z are tags. In this case, paired samples from the desired joint distribution are usually available, thus we can leverage this supervised information to resolve the ambiguity between Figure 1(b) and (c). From our simple example in Figure 1, we see that in order to alleviate the identifiability issues associated with the solutions to the ALI objective, we have to impose constraints on the conditionals q? (z—x) and p? (z—x). Furthermore, to fully mitigate the identifiability issues we require supervision, i.e., paired samples from domains X and Z. To deal with the problem of undesirable but matched joint distributions, below we propose to use an information-theoretic measure to regularize ALI. This is done by controlling the ?uncertainty? between pairs of random variables, i.e., x and z, using conditional entropies. 3.1 Conditional Entropy Conditional Entropy (CE) is an information-theoretic measure that quantifies the uncertainty of random variable x when conditioned on z (or the other way around), under joint distribution ?(x, z): H ? (x—z) , ?E?(x,z) [log ?(x—z)], and H ? (z—x) , ?E?(x,z) [log ?(z—x)].

```
(4)
min max LALICE (?, ?, ?) = LALI (?, ?, ?) + L?CE (?, ?).
(5)
?
```

The uncertainty of x given z is linked with H (x—z); in fact, H (x—z) = 0 if only if x is a deterministic mapping of z. Intuitively, by controlling the uncertainty of q? (z—x) and p? (z—x), we can restrict the solutions of the ALI

objective to joint distributions whose mappings result in better reconstruction ability. Therefore, we propose to use the CE in (4), denoted as L?CE (?, ?) = H? (x—z) or H? (z—x) (depending on the task; see below), as a regularization term in our framework, termed ALI with Conditional Entropy (ALICE), and defined as the following minimax objective: ?,?

L?CE (?, ?) is dependent on the underlying distributions for the random variables, parametrized by (?, ?), as made clearer below. Ideally, we could select the desirable solutions of (5) by evaluating their CE, once all the saddle points of the ALI objective have been identified. However, in practice, L?CE (?, ?) is intractable because we do not have access to the saddle points beforehand. Below, we propose to approximate the CE in (5) during training for both unsupervised and supervised tasks. Since x and z are symmetric in terms of CE according to (4), we use x to derive our theoretical results. Similar arguments hold for z, as discussed in the Supplementary Material (SM). 3

3.2 Unsupervised Learning In the absence of explicit probability distributions needed for computing the CE, we can bound?, via the CE using the criterion of cycle-consistency [12]. We denote the reconstruction of x as x?? p? (? generating procedure (cycle) x x—z) have x—z), z? q? (z—x), x? q(x). We desire that p? (??=x, for the x? q(x) that begins the cycle x? z? x?, and hence that x? high likelihood for x be similar to the original x. Lemma 3 below shows that cycle-consistency is an upper bound of the conditional entropy in (4). Lemma 3 For joint distributions p? (x, z) or q? (x, z), we have H q? (x—z), ?Eq? (x,z) [log q? (x—z)] = ?Eq? (x,z) [log p? (x—z)]? Eq? (z) [KL(q? (x—z)kp? (x—z))]? ?Eq? (x,z) [log p? (x—z)], LCycle (?,?).

where q? (z) = dxq? (x, z). The proof is in the SM. Note that latent z is implicitly involved in LCycle (?, ?) via Eq? (x,z) [?]. For the unsupervised case we want to leverage (6) to optimize the following upper bound of (5): min max LALI (?, ?, ?) + LCycle (?, ?) . ?,?

? (7)

Note that as ALI reaches its optimum, p? (x, z) and q? (x, z) reach saddle point ?(x, z), then LCycle (?, ?)? H q? (x-z)? H ? (x-z) in (4) accordingly, thus (7) effectively approaches (5) (ALICE). Unlike L?CE (?, ?) in (4), its upper bound, LCycle (?, ?), can be easily approximated via Monte Carlo simulation. Importantly, (7) can be readily added to ALI?s objective without additional changes to the original training procedure. The cycle-consistency property has been previously leveraged in CycleGAN [12], DiscoGAN [13] and DualGAN [14]. However, in [12, 13, 14], cycle-consistency, LCycle (?, ?), is implemented via 'k losses, for k = 1, 2, and real-valued data such as images. As a consequence of an '2-based pixel-wise loss, the generated samples tend to be blurry [8]. Recognizing this limitation, we further suggest to enforce cycle-consistency (for better reconstruction) using fully adversarial training (for better generation), as an alternative to LCycle (?, ?) in (7). Specifically, to reconstruct x, we specify

an ? ) to distinguish between x and its reconstruction x ?: ?-parameterized discriminator f? (x, x A min max LCycle (?, ?, ?) = Ex?q(x) [log ?(f? (x, x))] ?.?

Finally, the fully adversarial training algorithm for unsupervised learning using the ALICE framework is the result of replacing LCycle (?, ?) with LA Cycle (?, ?, ?) in (7); thus, for fixed (?, ?), we maximize wrt {?, ?}.

? } in (8) is critical. It encourages the generators to mimic the The use of paired samples  $\{x, x \text{ reconstruction relationship implied in the first joint; on the contrary, the model may reduce to the basic GAN discussed in Section 3, and generate any realistic sample in X . The objective in (8) enjoys many theoretical properties of GAN. Particularly, Proposition 1 guarantees the existence of the optimal generator and discriminator. Proposition 1 The optimal generators and discriminator <math>\{?\ ?\ ,??\ ,?\ ?\ \}$  of the objective in (8) is ? ). achieved, if and only if Eq?? (z-x) p??  $(?\ x-z)=?(x\ ?\ x$  The proof is provided in the SM. Together with Lemma 2 and 3, we can also show that: Corollary 1 When cycleconsistency is satisfied (the optimum in (8) is achieved), (i) a deterministic mapping enforces Eq? (z)  $[KL(q?\ (x-z)kp?\ (x-z))]=0$ , which indicates the conditionals are matched. (ii) On the contrary, the matched conditionals enforce H q? (x-z)=0, which indicates the corresponding mapping becomes deterministic.

3.3 Semi-supervised Learning When the objective in (7) is optimized in an unsupervised way, the identifiability issues associated with ALI are largely reduced due to the cycle-consistency-enforcing bound in Lemma 3. This means that samples in the training data have been probabilistically ?paired? with high certainty, by conditionals p? (x—z) and p? (z—x), though perhaps not in the desired configuration. In realworld applications, obtaining correctly paired data samples for the entire dataset is expensive or 4

even impossible. However, in some situations obtaining paired data for a very small subset of the observations may be feasible. In such a case, we can leverage the small set of empirically paired samples, to further provide guidance on selecting the correct configuration. This suggests that ALICE is suitable for semi-supervised classification. For a paired sample drawn from empirical distribution ? ? (x, z), its desirable joint distribution is well specified. Thus, one can directly approximate the CE as H ?? (x—z) ? E?? (x,z) [log p? (x—z)] , LMap (?) ,

(9) where the approximation (?) arises from the fact that p? (x—z) is an approximation to ? ? (x—z). For the supervised case we leverage (9) to approximate (5) using the following minimax objective: min max LALI (?, ?, ?) + LMap (?). ?,?

(10)

Note that as ALI reaches its optimum, p? (x, z) and q? (x, z) reach saddle point ?(x, z), then LMap (?)? H?? (x—z)? H? (x—z) in (4) accordingly, thus (10) approaches (5) (ALICE).

We can employ standard losses for supervised learning objectives to approximate LMap (?) in (10), such as cross-entropy or 'k loss in (9). Alternatively, to also improve generation ability, we propose an adversarial learning scheme to directly match p? (x-z) to the paired empirical conditional ? ? (x-z), using conditional GAN [15] as an alternative to LMap (?) in (10). The ?-parameterized discriminator f? is used to distinguish the true pair  $\{x, z\}$  from the artificially generated one  $\{? x, z\}$  (conditioned on z), using min max LA x, z)))]. (11) ? ?p? (? ? (x,z) [log ?(f? (x,z)) + Ex x—z) log(1 ? ?(f? (? Map (x,z)) = Ex,z?? ?

The fully adversarial training algorithm for supervised learning using the ALICE in (11) is the result of replacing LMap (?) with LA Map (?, ?) in (10), thus for fixed (?, ?) we maximize wrt {?, ?}. Proposition 2 The optimum of generators and discriminator {? ? , ?? } form saddle points of objective in (11), if and only if ? ? (x-z) = p?? (x-z) and ? ? (x, z) = p?? (x, z)z). The proof is provided in the SM. Proposition 2 enforces that the generator will map to the correctly paired sample in the other space. Together with the theoretical result for ALI in Lemma 2, we have Corollary 2 When the optimum in (10) is achieved, ? ? (x, z) = p?? (x, z) = q?? (x, z). Corollary 2 indicates that ALI?s drawbacks associated with identifiability issues can be alleviated for the fully supervised learning scenario. Two conditional GANs can be used to boost the perforance, each for one direction mapping. When tying the weights of discriminators of two conditional GANs, ALICE recovers Triangle GAN [16]. In practice, samples from the paired set?? (x, z) often contain enough information to readily approximate the sufficient statistics of the entire dataset. In such case, we may use the following objective for semi-supervised learning: min max LALI (?, ?, ?) + LCycle (?, ?) + LMap (?) . ?,?

? (12)

The first two terms operate on the entire set, while the last term only applies to the paired subset. Note that we can train (12) fully adversarially by replacing LCycle (?, ?) and LMap (?) with LA Cycle (?, ?, ?) A and LMap (?, ?) in (8) and (11), respectively. In (12) each of the three terms are treated with equal weighting in the experiments if not specifically mentioned, but of course one may introduce additional hyperparameters to adjust the relative emphasis of each term.

4

Related Work: A Unified Perspective for Joint Distribution Matching

Connecting ALI and CycleGAN. We provide an information theoretical interpretation for cycleconsistency, and show that it is equivalent to controlling conditional entropies and matching conditional distributions. When cycleconsistency is satisfied, Corollary 1 shows that the conditionals are matched in CycleGAN. They also train additional discriminators to guarantee the matching

of marginals for x and z using the original GAN objective in (2). This reveals the equivalence between ALI and CycleGAN, as the latter can also guarantee the matching of joint distributions p? (x, z) and q? (x, z). In practice, CycleGAN is easier to train, as it decomposes the joint distribution matching objective (as in ALI) into four subproblems. Our approach leverages a similar idea, and further improves it with adversarially learned cycle-consistency, when high quality samples are of interest. 5

- (a) True x
- (b) True z
- (c) Inception Score
- (d) MSE

Figure 2: Quantitative evaluation of generation (c) and reconstruction (d) results on toy data (a,b). Stochastic Mapping vs. Deterministic Mapping. We propose to enforce the cycle-consistency in ALI for the case when two stochastic mappings are specified as in (1). When cycle-consistency is achieved, Corollary 1 shows that the bounded conditional entropy vanishes, and thus the corresponding mapping reduces to be deterministic. In the literture, one deterministic mapping has been empirically tested in ALI?s framework [4], without explicitly specifying cycle-consistency. BiGAN [10] uses two deterministic mappings. In theory, deterministic mappings guarantee cycle-consistency in ALI?s framework. However, to achieve this, the model has to fit a delta distribution (deterministic mapping) to another distribution in the sense of KL divergence (see Lemma 3). Due to the asymmetry of KL, the cost function will pay extremely low cost for generating fake-looking samples [17]. This explains the underfitting reasoning in [4] behind the subpar reconstruction ability of ALI. Therefore, in ALICE, we explicitly add a cycle-consistency regularization to accelerate and stabilize training. Conditional GANs as Joint Distribution Matching. Conditional GAN and its variants [15, 18, 19, 20] have been widely used in supervised tasks. Our scheme to learn conditional entropy borrows the formulation of conditional GAN [15]. To the authors? knowledge, this is the first attempt to study the conditional GAN formulation as joint distribution matching problem. Moreover, we add the potential to leverage the well-defined distribution implied by paired data, to resolve the ambiguity issues of unsupervised ALI variants [4, 10, 12, 13, 14].

5

### Experimental Results

The code to reproduce these experiments is at https://github.com/ChunyuanLI/ALICE 5.1 Effectiveness and Stability of Cycle-Consistency To highlight the role of the CE regularization for unsupervised learning, we perform an experiment on a toy dataset. q(x) is a 2D Gaussian Mixture Model (GMM) with 5 mixture components, and p(z) is chosen as a standard Gaussian, N (0, I). Following [4], the covariance matrices and centroids are chosen such that the distribution exhibits severely separated modes, which makes it a relatively hard task despite its 2D nature. Following [21], to study stability, we run an exhaustive grid search over a set of architectural choices and hyper-parameters, 576 experiments for each method. We report Mean Squared Error (MSE) and inception score (denoted

as ICP) [22] to quantitatively evaluate the performance of generative models. MSE is a proxy for reconstruction quality, while ICP reflects the plausibility and variety of sample generation. Lower MSE and higher ICP indicate better results. See SM for the details of the grid search and the calculation of ICP. We train on 2048 samples, and test on 1024 samples. The ground-truth test samples for x and z are shown in Figure 2(a) and (b), respectively. We compare ALICE, ALI and Denoising Auto-Encoders (DAEs) [23], and report the distribution of ICP and MSE values, for all (576) experiments in Figure 2 (c) and (d), respectively. For reference, samples drawn from the ?oracle? (groundtruth) GMM yield ICP=4.977?0.016. ALICE yields an ICP larger than 4.5 in 77% of experiments, while ALI?s ICP wildly varies across different runs. These results demonstrate that ALICE is more consistent and quantitatively reliable than ALI. The DAE yields the lowest MSE, as expected, but it also results in the weakest generation ability. The comparatively low MSE of ALICE demonstrates its acceptable reconstruction ability compared to DAE, though a very significantly improvement over ALI. Figure 3 shows the qualitative results on the test set. Since ALI?s results vary largely from trial to trial, we present the one with highest ICP. In the figure, we color samples from different mixture components to highlight their correspondance between the ground truth, in Figure 2(a), and their reconstructions, in Figure 3 (first row, columns 2, 4 and 6, for ALICE, ALI and DAE, respectively). Importantly, though the reconstruction of ALI can recover the shape of manifold in x (Gaussian mixture), each individual reconstructed sample can be substantially far away from its ?original? mixture component (note the highly mixed coloring), hence the poor MSE. This occurs because the adversarial training in ALI only requires that the generated samples look realistic, i.e., to be located 6

- (a) ALICE
- (b) ALI
- (c) DAEs

Figure 3: Qualitative results on toy data. Two-column blocks represent the results of each method, with left for z and right for x. For the first row, left is sampling of z, and right is reconstruction of x. Colors indicate mixture component membership. The second row shows reconstructions, x, from linearly interpolated samples in z.

near true samples in X, but the mapping between observed and latent spaces (x? z and z? x) is not specified. In the SM we also consider ALI with various combinations of stochastic/deterministic mappings, and conclude that models with deterministic mappings tend to have lower reconstruction ability but higher generation ability. In terms of the estimated latent space, z, in Figure 3 (first row, columns 1, 3 and 5, for ALICE, ALI and DAE, respectively), we see that ALICE results in a better latent representation, in the sense of mapping consistency (samples from different mixture components remain clustered) and distribution consistency (samples approximate a Gaussian distribution). The results for reconstruction of z and sampling of x are shown in the SM. In Figure 3 (second row), we also investigate latent space interpolation between a pair of test set examples. We use x1 = [?2.2, ?2.2] and x9 = [2.2, 2.2], map them

into z 1 and z 9, linearly interpolate between z 1 and z 9 to get intermediate points z 2, . . . , z 8, and then map them back to the original space as x2 , . . . , x8 . We only show the index of the samples for better visualization. Figure 3 shows that ALICE?s interpolation is smooth and consistent with the ground-truth distributions. Interpolation using ALI results in realistic samples (within mixture components), but the transition is not order-wise consistent. DAEs provides smooth transitions, but the samples in the original space look unrealistic as some of them are located in low probability density regions of the true model. We investigate the impact of different amount of regularization on three datasets, including the toy dataset, MNIST and CIFAR-10 in SM Section D. The results show that our regularizer can improve image generation and reconstruction of ALI for a large range of weighting hyperparameter values. 5.2 Reconstruction and Cross-Domain Transformation on Real Datasets Two image-to-image translation tasks are considered. (i) Car-to-Car [24]: each domain (x and z) includes car images in 11 different angles, on which we seek to demonstrate the power of adversarially learned reconstruction and weak supervision. (ii) Edge-to-Shoe [25]: x domain consists of shoe photos and z domain consists of edge images, on which we report extensive quantitative comparisons. Cycle-consistency is applied on both domains. The goal is to discover the cross-domain relationship (i.e., cross-domain prediction), while maintaining reconstruction ability on each domain.

Classification Accuracy (%)

Adversarially learned reconstruction To demonstrate the effectiveness of our fully adversarial scheme in (8) (Joint A.) on real datasets, we use it in place of the '2 losses in DiscoGAN [13]. In practice, feature matching [22] is used to help the adversarial objective in (8) to reach its optimum. We also compared with a baseline scheme (Marginal A.) in [12], which adversarially discriminates? between x and its reconstruction x 80 The results are shown in Figure 4 (a). From Inputs 60 top to bottom, each row shows ground-truth Joint A. ALICE (10% sup.) ALICE (1% sup.) images, DiscoGAN (with Joint A., '2 loss Disco-GAN 40 BiGAN 'loss and Marginal A. schemes, respectively) and 2 20 BiGAN [10]. Note that BiGAN is the best Marginal A. ALI variant in our grid search compasion. BiGAN 2 4 6 8 10 The proposed Joint A. scheme can retain the Number of Paired Angles same crispness characteristic to adversarially(a) Reconstruction (b) Prediction trained models, while '2 tends to be blurry. Figure 4: Results on Car-to-Car task. Marginal A. provides realistic car images, but not faithful reproductions of the inputs. This explains 7

Lcycle+'A Lcycle+'2 BiGAN BiGAN

(a) Cross-domain transformation (b) Reconstruction (c) Generated edges Figure 5: SSIM and generated images on Edge-to-Shoe dataset.

the observations in [12] in terms of no performance gain. The BiGAN learns the shapes of cars, but misses the textures. This is a sign of underfitting, thus indicating BiGAN is not easy to train. Weak supervision The DiscoGAN and Bi-GAN are unsupervised methods, and exhibit very different cross-domain pairing

configurations during different training epochs, which is indicative of nonidentifiability issues. We leverage very weak supervision to help with convergence and guide the pairing. The results on shown in Figure 4 (b). We run each methods 5 times, the width of the colored lines reflect the standard deviation. We start with 1% true pairs for supervision, which yields significantly higher accuracy than DiscoGAN/BiGAN. We then provided 10% supervison in only 2 or 6 angles (of 11 total angles), which yields comparable angle prediction accuracy with full angle supervison in testing. This shows ALICE?s ability in terms of zero-shot learning, i.e., predicting unseen pairs. In the SM, we show that enforcing different weak supervision strategies affects the final pairing configurations, i.e., we can leverage supervision to obtain the desirable joint distribution. Quantitative comparison To quantitatively assess the generated images, we use structural similarity (SSIM) [26], which is an established image quality metric that correlates well with human visual perception. SSIM values are between [0, 1]; higher is better. The SSIM of ALICE on prediction and reconstruction is shown in Figure 5 (a)(b) for the edge-to-shoe task. As a baseline, we set DiscoGAN with '2 -based supervision ('2 -sup). BiGAN/ALI, highlighted with a circle is outperformed by ALICE in two aspects: (i) In the unpaired setting (0% supervision), cycle-consistency regularization (LCycle) shows significant performance gains, particularly on reconstruction. (ii) When supervision is leveraged (10%), SSIM is significantly increased on prediction. The adversarial-based supervision ('A -sup) shows higher prediction than '2 -sup. ALICE achieves very similar performance with the 50% and full supervision setup, indicating its advantage of in semi-supervised learning. Several generated edge images (with 50% supervision) are shown in Figure 5(c), 'A -sup tends to provide more details than '2 -sup. Both methods generate correct paired edges, and quality is higher than BiGAN and DiscoGAN. In the SM, we also report MSE metrics, and results on edge domain only, which are consistent with the results presented here. Oneside cycle-consistency When uncertainty in one domain is desirable, we consider one-side cycle-consistency. This is demonstrated on the CelebA face dataset [27]. Each face is associated with a 40-dimensional attribute vector. The results are in the Figure 8 of SM. In the first task, we consider the images x are generated from a 128-dimensional Gaussian latent space z, and apply LCycle on x. We compare ALICE and ALI on reconstruction in Figure 8 (a)(b). ALICE shows more faithful reproduction of the input subjects. In the second task, we consider z as the attribute space, from which the images x are generated. The mapping from x to z is then attribute classification. We only apply LCycle on the attribute domain, and LA Map on both domains. When 10% paired samples are considered, the predicted attributes still reach 86% accuracy, which is comparable with the fully supervised case. To test the diversity on x, we first predict the attributes of a true face image, and then generated multiple images conditioned on the predicted attributes. Four examples are shown in Figure 8 (c).

6

Conclusion

We have studied the problem of non-identifiability in bidirectional adversar-

ial networks. A unified perspective of understanding various GAN models as joint matching is provided to tackle this problem. This insight enables us to propose ALICE (with both adversarial and non-adversarial solutions) to reduce the ambiguity and control the conditionals in unsupervised and semi-supervised learning. For future work, the proposed view can provide opportunities to leverage the advantages of each model, to advance joint-distribution modeling. 8

Acknowledgements We acknowledge Shuyang Dai, Chenyang Tao and Zihang Dai for helpful feedback/editing. This research was supported in part by ARO, DARPA, DOE, NGA, ONR and NSF.

### 2 References

[1] I. Goodfellow, J. Pouget-Abadie, M. Mirza, B. Xu, D. Warde-Farley, S. Ozair, A. Courville, and Y. Bengio. Generative adversarial nets. In NIPS, 2014. [2] D. P. Kingma and M. Welling. Auto-encoding variational Bayes. In ICLR, 2014. [3] X. Chen, Y. Duan, R. Houthooft, J. Schulman, I. Sutskever, and P. Abbeel. InfoGAN: Interpretable representation learning by information maximizing generative adversarial nets. In NIPS, 2016. [4] V. Dumoulin, I. Belghazi, B. Poole, A. Lamb, M. A., O. Mastropietro, and A. Courville. Adversarially learned inference. ICLR, 2017. [5] L. Mescheder, S. Nowozin, and A. Geiger. Adversarial variational bayes: Unifying variational autoencoders and generative adversarial networks. ICML, 2017. [6] Y. Pu, Z. Gan, R. Henao, X. Yuan, C. Li, A. Stevens. and L. Carin. Variational autoencoder for deep learning of images, labels and captions. In NIPS, 2016. [7] Y. Pu, Z. Gan, R. Henao, C. Li, S. Han, and L. Carin. Vae learning via Stein variational gradient descent. NIPS, 2017. [8] A. B. L. Larsen, S. K. S?nderby, H. Larochelle, and O. Winther. Autoencoding beyond pixels using a learned similarity metric. ICML, 2016. [9] A. Makhzani, J. Shlens, N. Jaitly, I. Goodfellow, and B. Frey. Adversarial autoencoders. arXiv preprint arXiv:1511.05644, 2015. [10] J. Donahue, K. Philipp, and T. Darrell. Adversarial feature learning. ICLR, 2017. [11] Y. Pu, W. Wang, R. Henao, L. Chen, Z. Gan, C. Li, and L. Carin. Adversarial symmetric variational autoencoder. NIPS, 2017. [12] J. Zhu, T. Park, P. Isola, and A. Efros. Unpaired image-to-image translation using cycle-consistent adversarial networks. ICCV, 2017. [13] T. Kim, M. Cha, H. Kim, J. Lee, and J. Kim. Learning to discover cross-domain relations with generative adversarial networks. ICML, 2017. [14] Z. Yi, H. Zhang, and P. Tan. DualGAN: Unsupervised dual learning for imageto-image translation. ICCV, 2017. [15] M. Mirza and S. Osindero. Conditional generative adversarial nets. arXiv preprint arXiv:1411.1784, 2014. [16] Z. Gan, L. Chen, W. Wang, Y. Pu, Y. Zhang, H. Liu, C. Li, and L. Carin. Triangle generative adversarial networks. NIPS, 2017. [17] M. Arjovsky and L. Bottou. Towards principled methods for training generative adversarial networks. In ICLR, 2017. [18] S. Reed, Z. Akata, X. Yan, L. Logeswaran, B. Schiele, and H. Lee. Generative adversarial text to image synthesis. In ICML, 2016. [19] P. Isola, J. Zhu, T. Zhou, and A. Efros. Image-to-image translation with conditional adversarial networks. CVPR, 2017. [20] C. Li, K. Xu, J. Zhu, and B. Zhang. Triple generative adversarial nets. NIPS, 2017. [21] J. Zhao, M. Mathieu, and Y. LeCun. Energy-based generative adversarial network. ICLR, 2017. [22] T. Salimans, I. Goodfellow, W. Zaremba, V. Cheung, A. Radford, and X. Chen. Improved techniques for training GANs. In NIPS, 2016. [23] P. Vincent, H. Larochelle, Y. Bengio, and P. Manzagol. Extracting and composing robust features with denoising autoencoders. In ICML, 2008. [24] S. Fidler, S. Dickinson, and R. Urtasun. 3D object detection and viewpoint estimation with a deformable 3D cuboid model. In NIPS, 2012. [25] A. Yu and K. Grauman. Fine-grained visual comparisons with local learning. In CVPR, 2014. [26] Z. Wang, A. C Bovik, H. R Sheikh, and E. P Simoncelli. Image quality assessment: from error visibility to structural similarity. IEEE trans. on Image Processing, 2004. [27] Z. Liu, P. Luo, X. Wang, and X. Tang. Deep learning face attributes in the wild. In ICCV, 2015.