

1998

	Mach			E/M		
	B	BB	BBR	B	BB	BBR
M	30	34	35	31	32	35
MCS	38.6	43.7	45	40.0	41.1	45
FK	42.5	45	45	34	42	44
Tot	78.1	88.7	90	74	83.1	89

1998 Mech MC

1) b ✓ 2) e ✓ 3) d ✓

4) 2F = 0 when $a = 0$

$$\frac{dx}{dt} = 3t^2 - 12t + 9$$

$$\frac{d^2x}{dt^2} = 6t - 12$$

$$\frac{d^2x}{dt^2} \quad t=2 \quad (b) \checkmark$$

5) \leftarrow 2F3R - F3R - F2R - F3R
6FR - 6FR - 2FR (c) ✓

6) $V = RW$ (a) ✓

$$7) (a) \checkmark \quad F = \frac{GMm}{R^2} \quad F_a = \frac{GMm}{UR^2} \quad (d) \checkmark$$

$$8) \frac{dx}{dt} = -\frac{a}{2}x^2 \quad x(1) = -\frac{3}{2}x^3 \quad (c) \checkmark$$

$$9) T = 2\pi\sqrt{\frac{r}{g}} \quad (e) \alpha$$

$$10) e \checkmark \quad 11) F_{\text{tot}} = DP = m v \cos \theta \quad (a) \circ$$

$$12) mv = (3m) v_f$$

$$v_f = \frac{1}{3}v \quad (a) \checkmark$$

$$13) \frac{mv^2}{r} = F_c = \frac{F_g}{k} \quad = F_g = kx = (100N/m)(0.03m) \quad = 3N \quad (b) \checkmark$$

14) (a) ✓

$$15) 3V_0 - V_0 = \frac{1}{2}mv^2$$

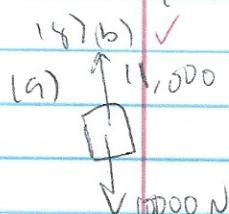
$$4U_0 = mv^2 \quad (c) \checkmark$$

$$v_f = \sqrt{\frac{4U_0}{m}}$$

$$16) V(r) = br^{-\frac{3}{2}} + C$$

$$W = \int F \cdot dr \quad \frac{dW}{dr} = F$$

$$F = -\frac{3}{2}br^{-\frac{5}{2}} \quad (a) \checkmark$$



$$2F = ma$$

$$a = 1m/s^2$$

$$\text{total mech: } 45 \cdot \frac{30}{35} + 42 = \frac{80.6}{80}$$

$$45 \cdot \frac{30}{35} + 42 = \frac{80.6}{80}$$

$$v_f = v_0^2 + 2ax$$

$$v_0^2 = -2ax$$

$$v_0 = \sqrt{2(1)(8)}$$

$$= \sqrt{16} = 4 \text{ (a)}$$

$$17) F = G \frac{Mm}{r^2} = \frac{Mm}{r^2}$$

$$\frac{GM^2}{r^2} = \frac{2Mv^2}{r}$$

$$v = \sqrt{\frac{GM}{r}} \quad (b) \checkmark$$

$$18) F \cos \theta - f = ma \quad (d) \checkmark$$

$$19) F_{\text{sin}} \theta + N - mg = 0$$

$$N = mg - F \sin \theta$$

$$f = \mu N \quad \mu = \frac{f}{N} = \frac{f}{mg - F \sin \theta} \quad (e) \checkmark$$

$$20) X/N/A$$

$$21) (a) \checkmark \quad 22) (b) \checkmark$$

$$23) \bar{x} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$24) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$25) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$26) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$27) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$28) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$29) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$30) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$31) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$32) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$33) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$34) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$35) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$36) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$37) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$38) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$39) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$40) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$41) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$42) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$43) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$44) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$45) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$46) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$47) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$48) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$49) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$50) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$51) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$52) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$53) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$54) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$55) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$56) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$57) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$58) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$59) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$60) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$61) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$62) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$63) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$64) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$65) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$66) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$67) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$68) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$69) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$70) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$71) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$72) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$73) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$74) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$75) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$76) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$77) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$78) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$79) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$80) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$81) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$82) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$83) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$84) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$85) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$86) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$87) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$88) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$89) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$90) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$91) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$92) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$93) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$94) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$95) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$96) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$97) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$98) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$99) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$100) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$101) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$102) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$103) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$104) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$105) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$106) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$107) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$108) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$109) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$110) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$111) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$112) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$113) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$114) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$115) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$116) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$117) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$118) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$119) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$120) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$121) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$122) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$123) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$124) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$125) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$126) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$127) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$128) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$129) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$130) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$131) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$132) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$133) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$134) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$135) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$136) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$137) \bar{v} = \frac{\Delta x}{t} \quad \bar{v} = \frac{\Delta x}{t}$$

$$138) \bar{v} = \frac{\Delta x}{$$

$$\frac{dy}{dt} = -A\omega^2 \cos(\omega t + \phi)$$

$$\frac{d^2y}{dt^2} = -A\omega^2 \sin(\omega t + \phi)$$

Assuming $t=0$?

$$y = -A\omega^2 (\cos(\omega t) + \sin(\omega t))$$

$$= -1.5(u)(1)$$

$$= b \quad (e) \checkmark$$

$$30) \Delta y = 2x = 0$$

$$m_1 g u = m_2 g b \quad (b) \checkmark$$

$$31) (c) \quad 32) \quad \Sigma I = I \omega \quad \omega_f = \omega_i + \alpha t$$

$$\omega = \frac{I \omega_i}{T} \quad (c) \checkmark$$

$$33) W = \int \Sigma da \quad \text{Slight 32}$$

$$K_E = \frac{1}{2} \sum m_i v_i^2$$

$$\frac{W}{t} = \int \Sigma \frac{da}{dt}$$

$$\frac{W}{t} = \frac{I \omega}{T} \quad (b) \checkmark$$

$$34) \frac{dv}{dt} = g - bv$$

$$\frac{dv}{g-bv} = dt$$

$$u = g - bv \quad \frac{du}{dv} = -b$$

$$t = -\frac{1}{b} \ln|g - bv|$$

$$dv = \frac{du}{-b}$$

$$-bt = \ln|g - bv|$$

$$g - bv = e^{-bt}$$

$$bv = g - e^{-bt}$$

$$v = \frac{1}{b}(g - e^{-bt}) \quad (a) \checkmark$$

~ 1998 Mech FR

$$\frac{42.5}{45} \rightarrow \frac{42}{45} (\text{true})$$

1) a) (i) $\bar{v} = \frac{x}{t} = \frac{0.5m}{0.5s} = 1 \text{ m/s}$

(ii) $\bar{v} = \frac{x}{t} = \frac{0.44m}{0.8s} = 0.55 \text{ m/s}$

(iii) $\bar{v} = \frac{x}{t} =$

b) a) $m v_0 = 3m(v_f) + 1$

$$v_f = \frac{v_0}{3} + 1$$

$$KE = \frac{1}{2} (3m) v_f^2$$

$$= \frac{1}{2} (3m) \left(\frac{v_0}{3} + 1\right)^2$$

$$= \frac{1}{6} m v_0^2 + 1$$

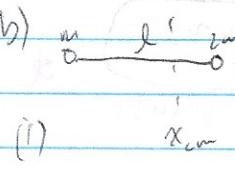
(i) $\bar{v} = \frac{\Delta x}{t} = \frac{0.8m}{0.2s} = 1 \text{ m/s}$ ✓ +1

(ii) $\bar{v} = \frac{\Delta x}{t} = \frac{0.12m}{0.2s} = 0.6 \text{ m/s}$ ✓ +1

(iii) $\bar{v} = \frac{\Delta x}{t} = \frac{0.04m}{0.2s} = 0.2 \text{ m/s}$ ✗

(i) $KE_0 = \frac{1}{2} m v_0^2$

$$\Delta KE = KE_f - KE_0 = -\frac{1}{3} m v_0^2$$

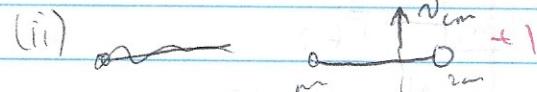


$$x_{cm} = \frac{m x_1 + m_2 x_2}{m_{total}}$$

$$= \frac{(m)(0m) + 2m(l)}{3m}$$

$$= \frac{2}{3} l \text{ from the left end}$$

c) (i) $m_a v_{a0} + m_b v_{b0} = m_a v_{af} + m_b v_{bf}$ ✗



(i) $(0.40 \text{ kg})(1 \text{ m/s}) = 0.40 \text{ kg m/s}$ ✗

(iii) $m v_{a0} + m v_{b0} = 3m(v_f)$

$$0.40 \text{ kg } v_{a0} + 0.60 \text{ kg } v_{b0}$$

$$v_f = \frac{v_0}{3} + 1$$

$$= 0.40 \text{ kg } (0.2 \text{ m/s}) + 0.60 \text{ kg } (v_b)$$

$$= \frac{v_0}{3} + 1$$

$$v_{b0} = \frac{0.40 \text{ kg } (1 \text{ m/s} - 0.2 \text{ m/s})}{0.60 \text{ kg}} = 1.2 \text{ m/s}$$

(iv) $I_0 = I_f$

$$I = m \left(\frac{l}{3}\right)^2 + 2m \left(\frac{l}{3}\right)^2$$

$$= \frac{4}{9} ml^2 + \frac{2}{9} ml^2$$

$$= \frac{2}{3} ml^2 + 1$$

d) (i) Yes; KE is conserved. ✗

$$I_p = I w_f$$

$$\omega_f = \frac{1}{3} k \cdot m v_0 = \sqrt{\frac{v_0}{2l}} + 1$$

(ii) the kinetic energy is stored in spring potential energy.

$$(i) KE_0 = \frac{1}{2} m v_0^2$$

$$KE_f = \frac{1}{6} m v_0^2 + \frac{1}{2} \left(\frac{2}{3} m^2 \right) \left(\frac{v_0}{2} \right)^2$$

kinetic
Potential (part)

rotational
+1

$$\begin{aligned} &= \frac{1}{6} m v_0^2 + \frac{1}{3} m^2 \cdot \frac{v_0^2}{4} \\ &= \frac{3}{12} m v_0^2 - \boxed{\frac{1}{4} m v_0^2} \end{aligned}$$

$$\Delta KE = KE_f - KE_0 = \boxed{-\frac{1}{2} m v_0^2}$$

$$3) a) i) \quad \begin{array}{c} \uparrow N_1 \\ \boxed{m} \end{array} \quad \text{friction}$$

$$N_1 = m_1 g$$

(ii)

$$\boxed{m_1} \rightarrow F_f$$

$$F_f = M_{S1} N = M_{S1} m_1 g$$

(iii)

$$\boxed{m_2} \rightarrow T$$

$$\begin{array}{c} \uparrow T \\ M \end{array} \quad \sum F = 0 \quad T = Mg$$

$$\begin{array}{c} \uparrow N_2 \\ \boxed{m_2} \end{array}$$

$$N_2 = (m_1 + m_2) g$$

(iv)

$$\begin{array}{c} \leftarrow F_f \\ \boxed{m_2} \end{array} \quad F_f = M_{S2} (m_1 + m_2) g$$

-2.5

$$b) \boxed{Mg - M_{S2}(m_1 + m_2)g = 0}$$

$$M = M_{S2}(m_1 + m_2) + 1$$

$$c) \sum F = ma$$

$$Mg - M_{K2}(m_1 + m_2)g = ma (M + m_1 + m_2) a$$

$$\boxed{a = \frac{Mg - M_{K2}(m_1 + m_2)g}{M + m_1 + m_2}} + 1$$

$$d) \sum F = ma$$

$$i) F_f = m_1 a$$

$$M_{K1} m_1 g = m_1 a$$

$$a_1 = M_{K1} g$$

$$ii) \sum F_{sys} = M_{K2} m_2 a_2$$

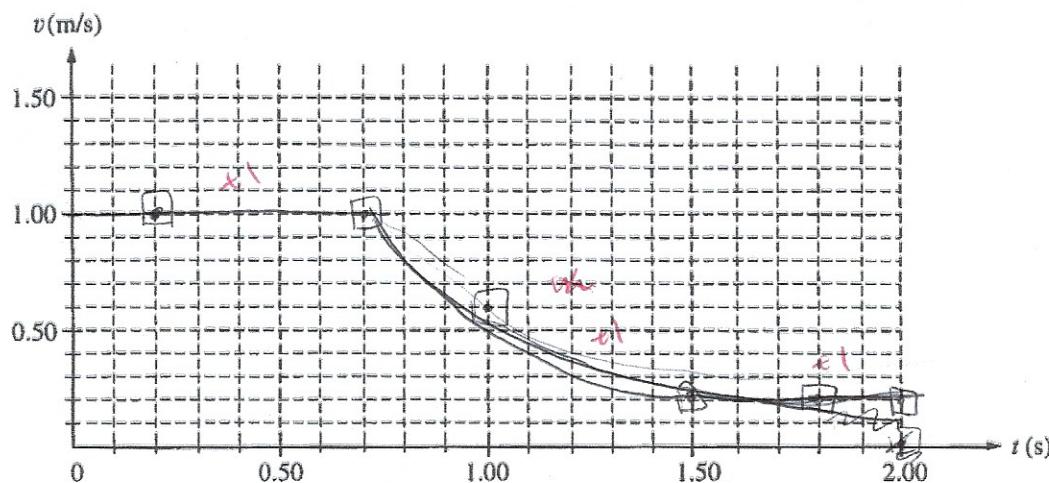
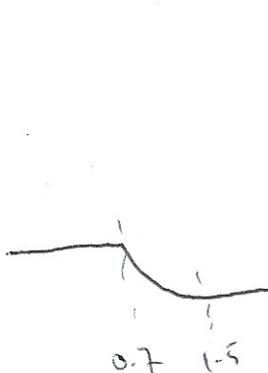
$$Mg - \mu_{K2}(m_1 + m_2)g - \mu_{K1} m_1 g = (M + m_2) a_2$$

$$\boxed{a_2 = \frac{Mg - M_{K2}(m_1 + m_2)g - \mu_{K1} m_1 g}{M + m_2}} + 1$$

1998 PHYSICS C—MECHANICS

(b)

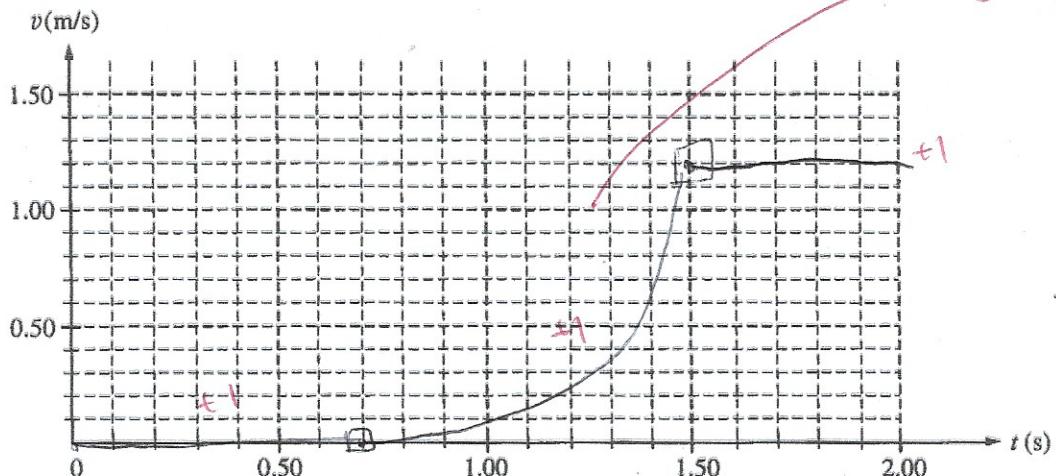
- On the axes below, sketch a graph, consistent with the data above, of the speed of glider A as a function of time t for the 2.00 s interval.



- (c) i. Use the data to calculate the speed of glider B immediately after it separates from the spring.

- ii. On the axes below, sketch a graph of the speed of glider B as a function of time t .

monotonic
& S shape



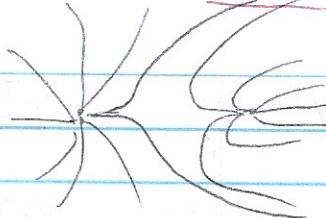
GO ON TO THE NEXT PAGE

~ 1998 EM MC

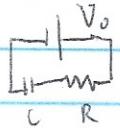
$$\frac{31}{35} \text{ m}$$

Exn total

$$\frac{45}{35} \cdot \frac{31}{35} \cdot \frac{35}{35} + \frac{34}{35} = \boxed{\frac{74}{98}}$$



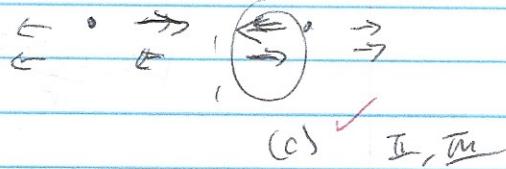
36)



$$I = \frac{dQ}{dt}$$

(P) (a) ✓ (b) ✓

$$P = I^2 R \quad V = \frac{Q}{C} \quad (\text{b}) \checkmark$$



$$37) P = I \Delta V = \frac{V^2}{R}$$

$$R = \frac{V^2}{P} = \frac{100 \times 10^3}{200} = 6 \Omega$$

$$46) V = \frac{Q}{C} \quad (\text{e}) \checkmark$$

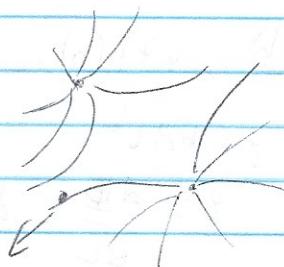
(c) ✓ II, III



$$47) (\text{a}) \quad 48) W = \Delta V = q \Delta V$$

$$\Delta V = \frac{V}{2} = \frac{53}{2 \times 10^3} = 2.65 \times 10^3 \text{ V}$$

~ 38) (c) ✓ 39)



49)

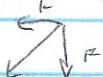


(a) ✓

(c) ✓

~~$$50) (\text{d}) \checkmark \quad 51) \delta F_{\text{ext}} = \frac{1}{2} qV$$~~

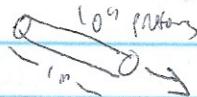
$$40) R = \frac{kQd}{S^2}$$



$E F_2$ (d) ✓

$$41) (\text{a}) \checkmark \quad 42) R = 2^2 R \quad (\text{d}) \checkmark$$

$$43) I = \frac{dQ}{dt}$$



$$= \frac{Q}{t} \cdot \frac{d}{d} \cdot \frac{Q}{d} \cdot d$$

$$= \frac{Q}{d} \cdot \frac{d}{t} = (10^9 \text{ C/m}^2)(1000 \text{ m})(1) \cdot \bar{V}$$

$$= 1.6 \times 10^{-3} \text{ A}$$

$$\bar{V} = 10^7 \text{ V} \quad (\text{d}) \checkmark$$

~~$$E = \frac{Qd}{C_0 A} = \frac{Qd}{\epsilon_0 A}$$~~

$$U = \frac{1}{2} QV = \frac{Q^2 d}{2 \epsilon_0 A} \quad (\text{a}) \checkmark$$

~~$$52) (\text{d}) \checkmark \quad 53) (\text{c}) \checkmark \quad 54) (\text{e}) \checkmark$$~~

$$55) \frac{mv^2}{R} = \frac{qE^2 L}{R^2}$$

$$mv^2 = \frac{1}{4\pi\epsilon_0} \frac{q^2}{R}$$

$$k = \frac{1}{4\pi\epsilon_0} \frac{q^2}{R^2} \quad (\text{b}) \checkmark$$

$$56) \text{Coul's law} \quad \mathbf{F} = \frac{q_1 q_2}{4\pi\epsilon_0 r^2} \hat{r} = -\frac{d\Phi}{dr}$$

$$= -\frac{q^2}{4\pi\epsilon_0} \frac{dB}{dt} = -\frac{q^2}{4\pi\epsilon_0} \frac{B^2}{r^2} \quad (\text{e}) \checkmark$$

$$I = \frac{q}{R} = \frac{V^2}{R}$$

$$57) qv/B = \frac{mv^2}{r}$$

$$\frac{v\pi r}{T} = v$$

$$(a) \left(\left(6\mu F^{-1} \right) + \left(3\mu F^{-1} \right) \right)^{-1}$$

$$= 2\mu F \quad (b) \checkmark$$

$$v = \frac{qBr}{m}$$

answ

$$2\pi r f = v$$

$$f = \frac{v}{2\pi r}$$

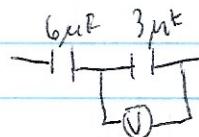
$$f = \frac{qB}{r} \times \frac{1}{2\pi r}$$

$$(a) \checkmark$$

$$(b) V = \frac{Q}{C}$$

$$Q_{\text{form}} = CV = (2\mu F)(12V)$$

$$= 24\mu C$$



Q equal V splits

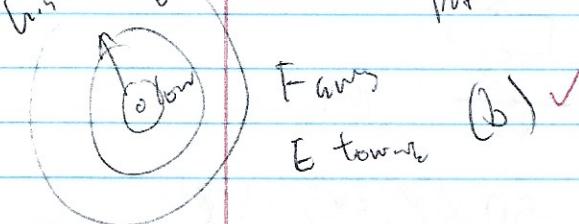
58) constant field \rightarrow constant force \rightarrow constant acceleration

$$(a) \checkmark$$

$$59) E = -\frac{dv}{dr} = -2\pi r, \quad (c) \checkmark$$

$$24\mu C \quad V = \frac{24\mu C}{3\mu F} = 8V \quad (d) \checkmark$$

60) electron goes b/w to high potential



$$E_{\text{towards}} \quad (b) \checkmark$$

$$(b) (b) \checkmark \quad (b) \checkmark$$

$$(c) \checkmark$$

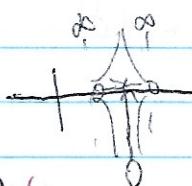
$$E = \frac{d\Phi}{dt} = \frac{dAt^2}{dt}$$

$$\Delta dB = \frac{dAt^2}{dt} dt$$

$$B = \frac{dAt^2}{3} dt$$

$$= \frac{2\pi}{3} t^{3/2} \quad (c) \checkmark$$

(d)



$$(a) \checkmark$$

$$62) (d) \checkmark \quad 63) V = 2V$$

$$(b) \checkmark$$

$$V_{\text{max}} = \frac{kA}{R_{\text{ext}}} \Rightarrow W = kAdr$$

$$(c) \checkmark \quad (a) \checkmark$$

$$\text{When } V_{\text{max}} = \int E_{\text{max}} dA = \frac{Q_{\text{max}}}{\epsilon_0}$$

$$\int E_{\text{max}} dA = Q_{\text{max}} \quad E_{\text{max}} = 0$$

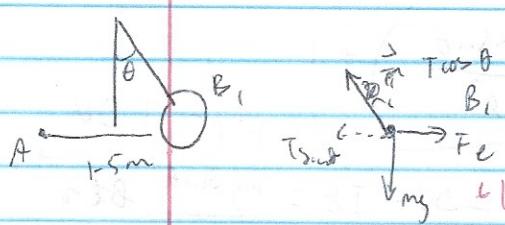
$$V = \int E dr \approx$$

(b) \checkmark

1998 EM FF

34
WS

1)
a)



$$E = \frac{\lambda}{2\pi\epsilon_0 r} = \frac{0.10 \text{ NC/m}}{2\pi(8.85 \times 10^{-12} \frac{\text{C}^2}{\text{Nm}^2})r}$$

$$= \frac{1.80 \times 10^3}{r} \text{ N/C}$$

$$T \cos \theta = mg$$

$$T = \frac{mg}{\cos \theta}$$

$$T \sin \theta = F_e = \frac{k Q_B Q_A}{r^2}$$

$$mg \tan \theta = k Q_B Q_A / r^2$$

$$Q_B = \frac{mg \tan \theta r^2}{k Q_A}$$

$$= \frac{(0.025 \text{ kg})(9.8 \text{ m/s}^2) \tan(20^\circ)(1.5 \text{ m})^2}{(9.0 \times 10^9 \frac{\text{N} \cdot \text{m}^2}{\text{C}^2})(1.8 \times 10^{-6} \text{ C})}$$

$$= [18.6 \mu\text{C}] = [1.86 \times 10^{-7} \text{ C}]$$

$$d) F_g = g E = (120 \mu\text{C}) \left(\frac{1.8 \times 10^3 \text{ N/C}}{1.5 \text{ m}} \right) = 10.144 \text{ N}$$

$$e) \Delta V = - \int E dr$$

$$= + \int_{0.3}^{1.5} (1.59 \times 10^3) \frac{dr}{r} = +$$

$$= +1.50 \times 10^3 (\ln 1.51 - \ln 1.031)$$

$$= +2.90 \times 10^3 \text{ V}$$

b) the equilibrium angle will remain

the same since the mass, radius,

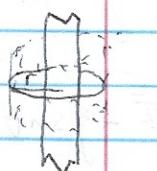
or charge didn't change; the conducting

sphere will still have the charge distributed evenly through the outer

surface. The force still acts through the center of the sphere.

$$c) \int E dA = \frac{Q_{ext}}{\epsilon_0} \quad \lambda = \frac{Q}{l} \quad +1$$

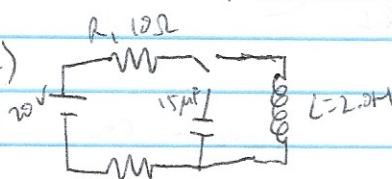
$$\cancel{M. M. \text{ and } \cancel{F. F.}}$$



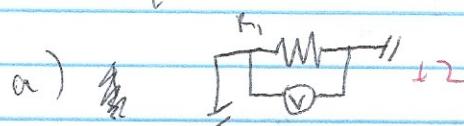
$$A = 2\pi r l$$

$$\int E \cdot 2\pi r dl = \frac{Q}{\epsilon_0} \quad +1$$

$$E \cdot 2\pi r = \frac{Q}{\epsilon_0} \quad \rightarrow -2$$



$$R_2 = 20 \Omega$$



$$b) V = IR, \quad I = \frac{dQ}{dt}$$

$$V = \frac{Q}{C}, \quad Q = CV$$



$$R_{eq} = 30 \Omega$$

$$C = 15 \mu\text{F} \quad \tau = RC = 4.5 \times 10^{-3} \text{ s}$$

$$I = C \frac{dV}{dt} = \frac{E}{R_{eq}}$$

$$\frac{dV}{dt} = \frac{E}{RC} \quad V(t) = \int \frac{E}{RC} dt$$

$$\boxed{V \neq 0?}$$

-3

ANSWER

-3

$$c) I=0 \quad V=0 \quad +2$$

$$(ii) Q = CV = (15 \mu F)(20V)$$

$$= 3 \times 10^{-4} C$$

$$300 \mu C = 3 \times 10^{-4} C$$

$$V = \frac{mg R \sin \theta}{B^2 l^2} \quad +1$$

$$P = I^2 R = 30W \quad +1$$

$$c) P = IDV = IE = \frac{mg \sin \theta}{Bl} \cdot Blv \quad +1$$

$$= mg v \sin \theta = mg \sin \theta \cdot \frac{mg R \sin \theta}{B^2 l^2}$$

$$d) t = T$$



$$V = IR = \frac{(20V)}{30\Omega} (10\Omega) = 6.67V \quad -2$$

$$I = \frac{E}{R+L}$$

$$e) (i) I_f = \frac{E}{R+L} = \frac{20V}{30\Omega} = 0.67A \quad +2$$

$$(ii) V_L = \frac{1}{2} L I^2 = \frac{1}{2} (20H)(0.67A)^2 = 0.45J \quad +1$$

$$d) \oint \vec{E} \cdot d\vec{l} = mg \sin \theta - IlB = m \frac{dv}{dt}$$

$$I = \frac{d\theta}{dt} = \frac{V}{R} = \frac{Blv}{R} \quad +1$$

$$mg \sin \theta - \frac{B^2 l^2 v}{R} = m \frac{dv}{dt}$$

$$gsin\theta - \frac{B^2 l^2 v}{mR} = \frac{dv}{dt}$$

$$dt = \frac{dv}{gsin\theta - \frac{B^2 l^2 v}{mR}} \quad +1$$

$$u = g \sin \theta - \frac{B^2 l^2 v}{mR} \sim$$

$$\frac{du}{dv} = - \frac{B^2 l^2}{mR}$$

$$dv = - \frac{mR}{B^2 l^2} du$$

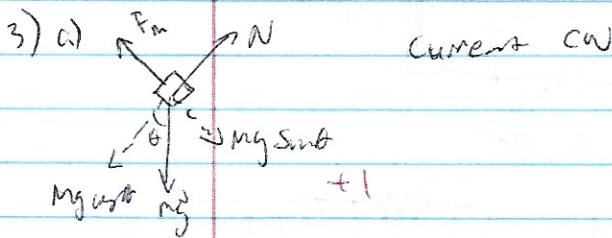
$$t = - \frac{mR}{B^2 l^2} \ln \left| g \sin \theta - \frac{B^2 l^2}{mR} v(v) \right|$$

$$-\frac{B^2 l^2 t}{mR} = \ln \left(\frac{v(v)}{g \sin \theta - \frac{B^2 l^2}{mR} v(v)} \right)$$

$$g \sin \theta - \frac{B^2 l^2}{mR} v(v) = e^{-\frac{B^2 l^2 t}{mR}}$$

$$v(v) = \frac{mR}{B^2 l^2} \left(e^{-\frac{B^2 l^2 t}{mR}} - g \sin \theta \right)$$

At $t=0$



$$F_m = IlB = mg \sin \theta \quad +1$$

$$(I = \frac{mg \sin \theta}{Bl}) \quad +1$$

$$E = Blv \quad +1 \quad I = \frac{E}{R} \quad +1$$

$$\text{since } \frac{mg \sin \theta}{Bl} = \frac{Blv}{R}$$

At $t=0$

(e) the final speed will be less. +1

Because power is being dissipated through both resistors now, because of Conservation of Energy, the bar must move at a slow speed since more energy is being dissipated through the resistors.

this is reasonable, right? +1

1998 BR

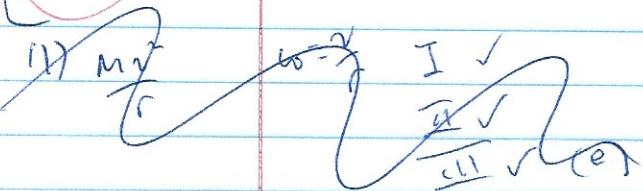
Mech MC

$$(1) T = \sqrt{\frac{F}{g}} \quad T_f = 2T$$

$$\frac{1}{\sqrt{g_s}} = 2 \frac{1}{g}$$

$$\sqrt{g_s} = \frac{1}{2} \quad g_s = \frac{1}{4} \quad (\text{a}) \checkmark$$

(a) ?



$$(2) J = \partial p = Fdt = \rho N(2s) - \rho N(2s)$$

$$= 20 \quad (\text{c}) \checkmark$$

$$(3) m v_r + m v_r = (3m) v_r$$

$$v_r = \frac{2}{3} v \quad (\text{c}) \checkmark$$

$$(2) \sum \tau = I \alpha$$

$$\text{Ansatz: } \omega_f = \omega_0 + \alpha t$$

$$\alpha = \frac{\omega_0}{t}$$

$$\tau = \frac{I \omega_0}{t} \quad (\text{e}) \checkmark$$

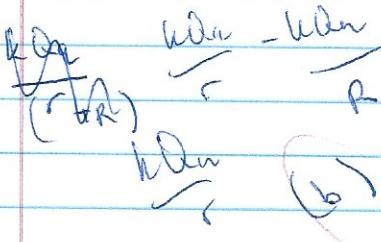
(g) d

E/M MR

(67)(g).

52) c ✓ ~~for A~~

$$(63) W = \int \vec{F} \cdot d\vec{r} \Delta U$$



67) (b) 47) d 63) e 67) a

Mech FR

$$(2) \Delta E = KE_f - KE_i = -\frac{1}{2}mv_0^2$$

3) (ii)

$$[m_1] \quad F=0$$

(v)

$$[m_2] \quad F_g = Mg$$

$$F_f = M_g \quad (\text{v}) \checkmark$$

E/M FR

1) b) The angle will be less b/c the conductive sphere allows the charges to gather on the far end of the sphere away from A, thus increasing the distance & decreasing the electrostatic force.

$$2) b) \Delta V = I R_{\text{ext}}$$

$$I = \frac{E}{R_{\text{ext}}} = \frac{10 \text{ V}}{(0.02 \text{ m})(0.02 \text{ m})} = 0.667 \text{ A} \quad (\text{v}) \checkmark$$

$$V = IR = (0.667 \text{ A})(10 \Omega) = 6.67 \text{ V} \quad (\text{v}) \checkmark$$

$$d) V_f = 0 ; I_o = 0 \quad (+2)$$

(f) ?

$$3) a) \mathcal{E} = -\frac{d\Phi}{dt} \Rightarrow \frac{B \cdot dA}{dt} = B L \cdot \frac{dr}{dt} \\ = BLv$$

(d)

$$2) b) Q - I(R_1 + R_2) - L \frac{dI}{dt} = 0 \quad +I$$

$$3) d) n(t) = \frac{m \cdot g \cdot s \cdot m}{R^2 \cdot e^2} \left(1 - e^{-\frac{B^2 t^2}{m h}} \right) \cdot I$$