

CHAPTER FOUR

4.1

Ex. 4.1

$$r_1 = (400 \text{ km} \hat{i}) + r_{\text{earth}} = (400 \text{ km} + 6371 \text{ km}) \hat{j} = 6771 \text{ km} \hat{j}$$

$$r_2 = 6771 \text{ km} \text{ at } -45^\circ \quad r_{2x} = r \cos \theta = 4788 \text{ km} \hat{i}$$

$$r_{2y} = r \sin \theta = -4788 \text{ km} \hat{j}$$

$$\Delta r = r_2 - r_1 = 4788 \text{ km} \hat{i} - 4788 \text{ km} \hat{j} - 6771 \text{ km} \hat{j}$$

$$= 4788 \text{ km} \hat{i} - 11560 \text{ km} \hat{j}$$

$$\Delta r = \sqrt{r_x^2 + r_y^2} = 12510 \text{ km} \text{ at}$$

$$\theta_r = \tan^{-1}\left(\frac{r_y}{r_x}\right) = -67.5^\circ$$

Ex. 4.2

$$\Delta r_{\text{total}} = \sqrt{\Delta r_x^2 + \Delta r_y^2} = \sqrt{(2.0 \hat{i} + 3.0 \hat{j})^2 + (-7.0 \hat{i} + 3.0 \hat{j})^2} = \sqrt{4.0 \hat{i}^2 + 9.0 \hat{j}^2} = \sqrt{4.0 + 9.0} = \sqrt{13.0} \text{ m}$$

$$= 3.61 \text{ m}$$

$$\Delta r_{\text{total}} = \sqrt{r_x^2 + r_y^2} = 9.22 \text{ m} \text{ at}$$

$$\theta_r = \tan^{-1}\left(\frac{r_y}{r_x}\right) = 77.5^\circ$$

Ex. 4.3

$$\vec{r}(t) = 2.0t^2 \hat{i} + (2.0 + 3.0t) \hat{j} + 5.0t \hat{k} \text{ m}$$

$$v(t) = \vec{r}'(t) = 4.0t \hat{i} + 3.0 \hat{j} + 5.0 \hat{k} \text{ m/s}$$

$$a) v(2) = 4.0(2) \hat{i} + 3.0 \hat{j} + 5.0 \hat{k} \text{ m/s} = [8.0 \hat{i} + 3.0 \hat{j} + 5.0 \hat{k}] \text{ m/s}$$

$$b) \vec{v}(1, 3) = \vec{r}(3) - \vec{r}(1) = \frac{[20(3^2) \hat{i} + (2.0 + 3.0 \cdot 3) \hat{j} + 5.0(3) \hat{k} - 20 \hat{i} - 5.0 \hat{k}]}{2}$$

$$= (9.0 \hat{i} - 1.0 \hat{j}) + (11.0 \hat{j} - 5.0 \hat{j}) + (15.0 \hat{k} - 5.0 \hat{k})$$

$$= (9.0 \hat{i} + 3.0 \hat{j} + 5.0 \hat{k}) \text{ m/s}$$

$$(4) \text{ U 4-1} \quad \vec{r}(t) = 3.0t^3 \hat{i} + 4.0 \hat{j}$$

$$a) v(t) = \vec{r}'(t) = 9.0t^2 \hat{i}$$

$$v(3) = 9.0(3^2) \hat{i} = [81 \hat{i}] \text{ m/s}$$

$$b) \vec{v}(2, 4) = \vec{r}(4) - \vec{r}(2) = \frac{[3.0(4^3) \hat{i} + 4.0 \hat{j} - 3.0(2^3) \hat{i} - 4.0 \hat{j}]}{2}$$

4-2

Ex. 4.4

$$[84 \hat{i}] \text{ m/s}$$

$$v(t) = 5.0t \hat{i} + t^3 \hat{j} - 2.0t^3 \hat{k} \text{ m/s}$$

$$a) a(t) = \vec{v}'(t) = 5.0 \hat{i} + 2t \hat{j} - 6t^2 \hat{k} \text{ m/s}^2$$

$$b) a(2.0) = 5.0 \hat{i} + 2(2.0) \hat{j} - 6(2^2) \hat{k} \text{ m/s}^2 = 5.0 \hat{i} + 4.0 \hat{j} - 24.0 \hat{k} \text{ m/s}^2$$

$$|a(2)| = \sqrt{a_i^2 + a_j^2 + a_k^2} = [24.8 \text{ m/s}^2]$$

$$\text{Ex. 2.5 } r(t) = ((t-t^2)\hat{i} + 5t\hat{j} + 5t^2\hat{k}) \text{ m}$$

$$\text{a) } v(t) = r'(t) = (10-2t)\hat{i} + 5\hat{j} + 10t\hat{k} \text{ m/s}$$

$$\text{b) } a(t) = r''(t) = -2\hat{i} \frac{\text{m}}{\text{s}^2}$$

c) the object starting starts from the origin and has a constant negative acceleration in the x -direction. The object moves linearly in the y and z directions.

(Q10 4.2)

$$r(t) = a\hat{i} + b\hat{j} + c\hat{k} \frac{\text{m}}{\text{s}}$$

$$v(t) = \int a dt = a\hat{i} + b + ct\hat{k} \frac{\text{m}}{\text{s}} + C_1 \hat{i}$$

$$\text{Ex. 4.6: } \rightarrow \uparrow \uparrow$$

$$\text{a) } v(t) = 2.1 \text{ m/s} @ -15^\circ \quad a_x = a \cos \theta = 2.03 \text{ m/s}^2$$

$$a(t) = 2.03 \text{ m/s}^2 \quad a_y = a \sin \theta = -0.54 \text{ m/s}^2$$

$$v(t) = \int a dt = 2.0t\hat{i} - 0.54t\hat{j} + C_1 \text{ m/s}$$

$$v(0) = C_1 = 4.0\hat{i} - 1.1\hat{j} \text{ m/s}$$

$$v(t) = [(2.0t+4.0)\hat{i} - (0.54t+1.1)\hat{j}] \text{ m/s}$$

$$\text{b) } x(t) = \int v dt = 2.0(t^2 + 4.0t) - (0.27t^2 + 1.1t) \text{ m} + C_2$$

$$x(0) = C_2 = 75.0 \text{ m} - 50.0 \text{ m}$$

$$x(t) = [(t^2 + 4.0t + 75.0)\hat{i} - (0.27t^2 + 1.1t + 50.0)\hat{j}] \text{ m}$$

$$\text{b) } x(10.0) = [216\hat{i} - 88\hat{j}] \text{ m}$$

$$\text{b) } v(10.0) = [24.0\hat{i} - 6.5\hat{j}] \text{ m/s}$$

4-3 Ex-4.7 $v_0 = 70.0 \text{ m/s} @ 75.0^\circ$

$$\text{a) } v_{0x} = v_0 \cos \theta = 18.1 \text{ m/s} \quad v_{0y} = v_0 \sin \theta = 67.6 \text{ m/s}$$

$$v_{0y}^2 = v_{0y}^2 + 2ay \Delta y \quad \Delta y = \frac{-v_{0y}^2}{2a} = -(67.6 \text{ m/s})^2 / 2(-9.8 \text{ m/s}^2) = 233 \text{ m}$$

$$\text{b) } v_{0y} = v_{0y} + at \quad t = -\frac{v_{0y}}{a} = -(67.6 \text{ m/s}) / -9.8 \text{ m/s}^2 = 6.90 \text{ s}$$

$$\text{c) } \Delta x = v_{0x} t = v_{0x} t = (18.1 \text{ m/s})(6.90 \text{ s}) = 125 \text{ m}$$

$$\text{d) } r_{\text{total}} = \sqrt{\Delta x^2 + \Delta y^2} = \sqrt{(125 \text{ m})^2 + (233 \text{ m})^2} = 264 \text{ m (di)}$$

$$\theta_{\text{final}} = \tan^{-1}\left(\frac{v_{0y}}{v_{0x}}\right) = \tan^{-1}\left(\frac{67.6}{18.1}\right) = 61.8^\circ$$

(Q10 4.3)

a) origin-edge of cliff @ ground level $\int t \rightarrow t$

$$\text{b) } v_{0x} = \bar{v}_x = \frac{\Delta x}{\Delta t} \quad \text{c) } \Delta y = v_{0y}t + \frac{1}{2}at^2$$

$$\text{d) } v_{0y} = \sqrt{2ay \Delta y} = \sqrt{16.9 \times 23}(10.0 \text{ m}) \quad v_{0y}^2 = v_{0y}^2 + 2ay \Delta y \quad v_{0y} = \sqrt{v_{0y}^2 + 2ay \Delta y}$$

$$\Delta t = 44.3 \text{ m/s} / v_{0x} = 15.0 \text{ s} \quad v_f = \sqrt{v_{0y}^2 + v_{0x}^2} = 46.9 \text{ m/s}$$

$$\theta_{1/2} = \tan^{-1}\left(\frac{v_{0y}}{v_{0x}}\right) = \tan^{-1}(44.3 \text{ m/s} / 15.0 \text{ m/s}) = 71.3^\circ \text{ below horizontal.}$$

$\uparrow + \rightarrow +$

Ex. 4-8 $v_0 = 30 \text{ m/s} \text{ at } 45^\circ$

a) $v_{0x} = v_0 \cos \theta = 30 \text{ m/s} \cos 45^\circ = 21.2 \text{ m/s}$

$$v_{0y} = v_0 \sin \theta = 30 \text{ m/s} \sin 45^\circ = 21.2 \text{ m/s}$$

$$\Delta y = v_{0y}t + \frac{1}{2}at^2$$

$$\frac{1}{2}(-9.8 \frac{\text{m}}{\text{s}^2})t^2 + (21.2 \frac{\text{m}}{\text{s}})t - 10 \text{ m} = 0$$

$$-4.9 \frac{\text{m}}{\text{s}^2} t^2 + 21.2 \frac{\text{m}}{\text{s}} t - 10 \text{ m} = 0$$

$$t = \frac{-21.2 \pm \sqrt{21.2^2 - 4(-4.9)(-10)}}{2(-4.9)} = 0.539 \text{ s}, 13.77 \text{ s}$$

b) $v_f = v_{0y} + at = 21.2 \frac{\text{m}}{\text{s}} + (-9.8 \frac{\text{m}}{\text{s}^2})(0.539 \text{ s})$
 $= -15.9 \text{ m/s}$

$$v_f = \sqrt{v_{0y}^2 + v_x^2} = \sqrt{(21.2 \frac{\text{m}}{\text{s}})^2 + (21.2 \frac{\text{m}}{\text{s}})^2} = 26.5 \text{ m/s}$$

$$\theta_f = \tan^{-1}\left(\frac{v_{0y}}{v_x}\right) = 36.9^\circ \text{ below horiz.} \quad \text{tex + book error}$$

Ex. 4-9

a) $R = \frac{v_0^2 \sin 2\theta}{g} \quad v_0 = \sqrt{\frac{gR}{\sin 2\theta}} = \sqrt{\frac{(9.8 \frac{\text{m}}{\text{s}^2})(40 \text{ m})}{\sin(2 \cdot 30^\circ)}} = 31.9 \text{ m/s}$

b) $v_0 = \sqrt{\frac{R}{\sin 2\theta}} = \sqrt{\frac{(40 \text{ m})}{\sin(2 \cdot 70^\circ)}} = 37.0 \text{ m/s}$

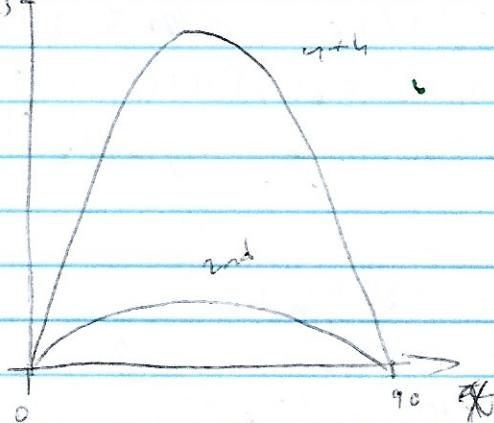
c) 1st $y = \tan(\theta_0)x - \left(\frac{g}{2v_0^2 \cos^2 \theta_0}\right)x^2$

$$= \tan(30)x - \left(\frac{9.8 \frac{\text{m}}{\text{s}^2}}{2(31.9 \cos 30)^2}\right)x^2$$

$$= 0.58x - 0.0064x^2$$

4th $y = \tan(70)x - \left(\frac{9.8 \frac{\text{m}}{\text{s}^2}}{2(37.0 \cos 70)^2}\right)x^2$ switch in calculator
 $= 2.75x - 0.0306x^2$

d)



(graphing calculator)

C4Q 4-9

$$R = \frac{v_0^2 \sin 2\theta}{g}$$

$$R_{30} = 0.866 \frac{v_0^2}{g}$$

$$R_{70} = 0.643 \frac{v_0^2}{g}$$

30° ball has greater range -

4.4 Ex. 4.10

$$a_c = \frac{v^2}{r} \quad r = v_0^2/a_c = (134.1 \text{ m/s})^2 / 9.8 \text{ m/s}^2 = 1873 \text{ m} \boxed{1835 \text{ m}}$$

4.5 Q4d

$$V = \sqrt{a_r r} = \sqrt{(900.0 \text{ cm/s})(20.0 \text{ cm})} = 134 \text{ cm/s} = 1.34 \text{ m/s}$$

Ex. 4.11

$$V(t) = (5 \times 10^4) \text{ m/s}$$

$$\cancel{\omega_0 t + \theta_0} - 5\pi d/4 = 5 \times 10^4 t + 7.8 \text{ rad}$$

$$\cancel{\omega_0 t} = 0.175 \text{ rad/s}$$

$$\cancel{\theta(t)} = 5 \times 10^4 t + 0.175 \text{ rad}$$

$$\cancel{\text{PERIOD}} \quad T = \frac{2\pi}{\omega} = \frac{2\pi}{\cancel{\omega}} = \frac{2\pi(0.175 \text{ rad})}{5 \times 10^4 \text{ rad/s}} = 2.2 \times 10^{-7} \text{ s}$$

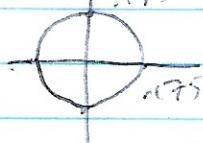
$$\omega = \frac{2\pi}{T} = 2\pi / 2.2 \times 10^{-7} \text{ s} = 2.9 \times 10^{13} \text{ rad/s}$$

$$r(t) = A \cos \omega t + A \sin \omega t$$

$$= 0.175 \text{ m} \cos(2.9 \times 10^{13} t) + 0.175 \text{ m} \sin(2.9 \times 10^{13} t)$$

$$r(2 \times 10^{-7}) = 0.175 \text{ m} \cos(2\pi c \times 7 \times 2 \times 10^{-7}) + 0.175 \text{ m} \sin(2\pi c \times 7 \times 2 \times 10^{-7})$$

$$0.175 = \cancel{0.175} \cos(2\pi c \times 7 \times 2 \times 10^{-7}) + 0.175 \sin(2\pi c \times 7 \times 2 \times 10^{-7})$$



Ex. 4.12

$$v(t) = 4.0 \text{ m/s} - \frac{6.0 \text{ m/s}}{t^2}$$

$$a(t) = v'(t) = \frac{12.0 \text{ m/s}^2}{t^3} \quad a(2) = \frac{12.0 \text{ m/s}^2}{(2)^3} = 1.5 \text{ m/s}^2$$

$$a_c = \frac{v^2}{r} = (4.0 \text{ m/s} - \frac{6.0 \text{ m/s}}{t^2})^2 / 2.0 \text{ m} = 18.0 \text{ m/s}^2 \quad 3.13 \text{ m/s}^2$$

$$a_{\text{total}} = \vec{a}_c + \vec{a}_s = \sqrt{a_c^2 + a_s^2} = \sqrt{(1.5)^2 + (3.13)^2} = 3.4 \text{ m/s}^2$$

$$\theta_A = \tan^{-1}\left(\frac{a_s}{a_c}\right) = \tan^{-1}\left(\frac{1.5 \text{ m/s}^2}{3.13 \text{ m/s}^2}\right) = 45^\circ$$

4.5 Ex. 4.13 $\overset{N+}{\uparrow} \rightarrow \overset{E+}{\uparrow}$

$$V_F = -70 \text{ km/h} \quad V_C = +80 \text{ km/h} \uparrow$$

$$V_{\text{air}} + \text{wind} = -V_F + V_C = 80 \text{ km/h} \uparrow + 70 \text{ km/h} \uparrow$$

$$V_{\text{air}} = \sqrt{V_F^2 + V_C^2} = \sqrt{80^2 + 70^2} = 106 \text{ km/h}$$

$$\theta_{\text{air}} = \tan^{-1}\left(\frac{V_C}{V_F}\right) = \tan^{-1}\left(\frac{80}{70}\right) = 44.12^\circ \text{ N of E}$$

$$\text{C4U 4.6} \quad \vec{v}_{B\bar{E}} = \vec{v}_{B\bar{P}} + \vec{v}_{\bar{P}\bar{E}}$$

$$v_{B\bar{P}} = 4.5 \text{ m/s}$$

$$v_{\bar{P}\bar{E}} = 3.0 \text{ m/s}$$

$$v_{B\bar{E}} = v_{B\bar{P}} + v_{\bar{P}\bar{E}} = 3.0 \text{ m/s} + 4.5 \text{ m/s} = \sqrt{v_x^2 + v_y^2} = 5.41 \text{ m/s}$$

$$\theta_v = \tan^{-1}\left(\frac{v_y}{v_x}\right) = 56.3^\circ \text{ North of East}$$

Ex. 4.14

$$v_{PA} = 300 \text{ km/h} \quad v_{AE} = 90 \text{ km/h} @ 45^\circ + 180^\circ = -63.6 \hat{i} - 63.6 \hat{j} \text{ m/s}$$

$$\text{a) } v_{PE} = \vec{v}_{PA} + \vec{v}_{AE} = (300 - 63.6) \hat{i} - 63.6 \hat{j} \text{ m/s}$$

$$= 236 \hat{i} - 63.6 \hat{j} \text{ m/s}$$

$$= \sqrt{v_x^2 + v_y^2} = 244 \text{ m/s}$$

~~At 270 km/h to the right~~

$$\text{b) } \theta = \tan^{-1}\left(\frac{v_y}{v_x}\right) = \tan^{-1}\left(\frac{-63.6}{236}\right) = 15.1^\circ$$

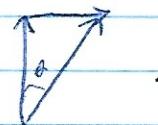
$$\text{b) } \bar{V}_{2,4} = \frac{r(1) - r(2)}{2.5} = \frac{(8.0(4^3) - 3.0(2^3)) \text{ m}}{2} = 184 \text{ m/s}$$

Ex. 4.12

$$\theta = \tan^{-1}\left(\frac{3.0}{1.5}\right) = 64.2^\circ$$

C4U 4.6

$$\theta_v = \tan^{-1}\left(\frac{v_{AE}}{v_{B\bar{P}}}\right) =$$



$$\theta_v = \tan^{-1}\left(\frac{3.0}{4.5}\right) = 33.7^\circ \text{ East of North}$$

$$\text{Ex. 4.14} \quad v_{PA} = 300 \text{ km/h} \quad v_{AE} = 90 \text{ km/h} @ 225^\circ$$

$$= -63.6 \hat{i} - 63.6 \hat{j} \text{ m/s}$$

$$\text{a) } v_{PE} = \vec{v}_{PA} + \vec{v}_{AE} = 300 \text{ km/h} \hat{i} - 63.6 \text{ m/s} \hat{i} - 63.6 \text{ m/s} \hat{j}$$

$$= 236.4 \hat{i} - 63.6 \text{ m/s} \hat{j}$$

$$= \sqrt{236.4^2 + 63.6^2} = 245 \text{ m/s}$$

$$\text{b) } \theta = \tan^{-1}\left(\frac{63.6}{236.4}\right) = 12.0^\circ$$

$$\text{C4U 4.1} - v_{2,4} = 54.0 \hat{i} \text{ m/s}$$

$$\text{Ex. 4.14} - \vec{v}_{PE} = 230 \text{ km/h}$$

Ch. 4 EDD

- 1) straight line
- 5) No
- 7) The dom b/c it fell first
- 13) It moves at the same speed as him
- 17) $\vec{r} = (1.0\hat{i} - 4.0\hat{j} + 6.0\hat{k})$
- 21) $\vec{\Delta x} = 5.0\hat{x} + (0.0 \cos(110)\hat{x} + 0.0 \sin(110)\hat{y}) - 8.0\hat{x}$
 $= -6.4\hat{x} + 9.4\hat{y}$
- 25) $\sum \Delta x = 20,000\hat{x} + 20,000 \text{ km} \cos 30^\circ + 20,000 \sin 30^\circ \hat{y}$
 $= 17.3\hat{x} + 10.02\hat{y}$
- 29) a) $v(t) = r'(t) = 6.0\hat{i} - 21\hat{t}\hat{j} + 10\hat{t}^{-3}\hat{k} \text{ m/s}$
 b) $a(t) = v'(t) = 6.0\hat{i} - 42\hat{t}\hat{j} - 30\hat{t}^{-4}\hat{k} \text{ m/s}^2$
 c) $y(t) = [2.0\hat{i} - 84\hat{j} + (26\hat{k} \text{ m/s})]$
 d) $v(3.0) = 6.0\hat{i} - 21\hat{j} + 10\hat{k} = [24 \frac{\text{m}}{\text{s}}]$
 $v(3.0) = 18\hat{i} - 190\hat{j} + 14.4\hat{k} = [191 \frac{\text{m}}{\text{s}}]$
 e) $\bar{v}_{1,2} = \frac{v(2) - v(1)}{1} = [24 - 56\hat{j} - 7.1\hat{k} - 3.0\hat{i} + 7.0\hat{j} + 5.0\hat{k} \text{ m/s}]$
 $= 9.0\hat{i} - 49\hat{j} - 2.1\hat{k}$
- 33) a) $\Delta y = V_{oy}t + \frac{1}{2}gt^2$ $t = \sqrt{\frac{2y}{g}} = \sqrt{\frac{2(1.5\text{m})}{9.8\text{m/s}^2}} = [0.55\text{s}]$
 b) $\Delta x = V_{ox}t = (200\frac{\text{m}}{\text{s}})(0.55\text{s}) = [110\text{m}]$
- 37) a) $t = \sqrt{\frac{2y}{a}} = \sqrt{\frac{2(800\text{m})}{9.8\text{m/s}^2}} = 12.8\text{s}$
 $\Delta x = V_{ox}t = (300\frac{\text{m}}{\text{s}} + 500\frac{\text{m}}{\text{s}}) \left(\frac{1000\text{m}}{\text{km}} \times \frac{1\text{h}}{3600\text{s}}\right)(12.8\text{s}) = [5620\text{m}]$
 b) $V_{fy} = V_{oy} + at = (9.8\frac{\text{m}}{\text{s}^2})(12.8\text{s}) = 125\frac{\text{m}}{\text{s}}$
 $V_{fx} = V_{ox} = (300\frac{\text{m}}{\text{s}} + 500\frac{\text{m}}{\text{s}}) = 439\frac{\text{m}}{\text{s}}$
 $V_f = \sqrt{V_{fx}^2 + V_{fy}^2} = [456 \frac{\text{m}}{\text{s}}]$
- 41) $V_0 = 2.0\hat{i} + 20\hat{t}\hat{j} + \frac{1}{2}at^2$
 $\Delta y = V_{oy}t + \frac{1}{2}gt^2$ $4.9t^2 + 2.0t - 100 = 0$
 $t = \frac{-2 \pm \sqrt{4 + 4 \cdot 4 \cdot 9.9100}}{2 \cdot 9.8} = 4.32\text{s}$
 $\Delta x = V_{ox}t = (20\frac{\text{m}}{\text{s}})(4.32\text{s}) = [86.4\text{m}]$
- 45) $V_0 = 30\hat{i}, \theta = 53^\circ = (18.1\hat{i} + 24.0\hat{j}) \frac{\text{m}}{\text{s}}$
 a) $\Delta x = V_{ox}t$ $\Delta y = V_{oy}t + \frac{1}{2}at^2$ $V_{oy} = V_0 \cdot \sin \theta$ $t = \frac{-b}{a}$
 $= \frac{c - 240 \frac{\text{m}}{\text{s}}}{-9.8 \frac{\text{m}}{\text{s}^2}} = 2.45\text{s}$ $\Delta y = (240 \frac{\text{m}}{\text{s}})(2.45\text{s}) + \frac{1}{2}(-9.8 \frac{\text{m}}{\text{s}^2})(2.45\text{s})^2$
 $\therefore [129.4\text{m}]$
 b) $\Delta x = V_{ox}t = (18.1 \frac{\text{m}}{\text{s}})(2.45\text{s}) = [44.3\text{m}]$

[45]

$$c) \Delta y = V_{0y} t + \frac{1}{2} a_y t^2$$

$$-4.9 t^2 + 24.0 t + 100 \text{ m} = 0$$

$$t = \frac{-24 + \sqrt{24^2 + 4 \cdot 4.9 \cdot 100}}{2 \cdot -4.9} = [7.59 \text{ s}]$$

$$d) R = \frac{V_0^2 \sin 2\theta}{g} = \frac{(30 \frac{\text{m}}{\text{s}})^2 \sin(2 \cdot 53^\circ)}{9.8 \frac{\text{m}}{\text{s}^2}} = [88.3 \text{ m}]$$

$$e) \text{Werte der Zeit } t \quad x_f = x_0 + V_x t \quad y_f = y_0 + V_{0y} t + \frac{1}{2} a_y t^2$$

$$r(t) = (x_0 + V_x t) \hat{i} \text{ m} + (y_0 + V_{0y} t + \frac{1}{2} a_y t^2) \hat{j} \text{ m}$$

$$r(2.0 \text{ s}) = (18.1 \frac{\text{m}}{\text{s}})(2.0 \text{ s}) \hat{i} + (100 \text{ m} + (24.0 \frac{\text{m}}{\text{s}})(2.0 \text{ s}) + \frac{1}{2} (-9.8 \frac{\text{m}}{\text{s}^2})(2.0 \text{ s})^2) \hat{j} \text{ m}$$

$$= 36.2 \hat{i} + 128.4 \hat{j} \text{ m}$$

$$r(4.0 \text{ s}) = (72.4 \hat{i} + 177.6 \hat{j} \text{ m})$$

$$r(4.0 \text{ s}) = (108.6 \hat{i} + 167.6 \hat{j} \text{ m})$$

$$a) R = \frac{V_0^2 \sin 2\theta}{g} = (15 \frac{\text{m}}{\text{s}})^2 \sin(2 \cdot 45^\circ) / 9.8 \frac{\text{m}}{\text{s}^2} = [60.8 \text{ m}]$$

$$b) R = \frac{V_0^2 \sin 2\theta}{g} = (15 \frac{\text{m}}{\text{s}})^2 \sin(50^\circ) / 9.8 \frac{\text{m}}{\text{s}^2} = [138 \text{ m}]$$

$$53) R = \frac{V_0^2 \sin 2\theta}{g} = (23.0 \frac{\text{m}}{\text{s}})^2 \sin(20^\circ) / 9.8 \frac{\text{m}}{\text{s}^2} = [27.8 \text{ m}] [8.9 \text{ m}]$$

$$57) Q = \frac{V_0^2 \sin \theta}{g} \quad A = \frac{1}{2} \sin^{-1}\left(\frac{Q R}{V_0^2}\right) = \frac{1}{2} \sin^{-1}\left(\frac{(9.8 \frac{\text{m}}{\text{s}})(69.3 \text{ m})}{(35 \frac{\text{m}}{\text{s}})^2}\right)$$

$$= [15.9^\circ]$$

$$61) a_c = \frac{V^2}{r} = (20 \frac{\text{m}}{\text{s}})^2 / 10 \text{ m} = [40 \frac{\text{m/s}^2}{\text{s}}]$$

$$65) a_c = \frac{V^2}{r} = (35 \frac{\text{m}}{\text{s}})^2 / 108 \times 10^9 \text{ m} = [1.13 \times 10^{-8} \frac{\text{m/s}^2}{\text{s}}]$$

$$69) a) r(s') = r(s) = \int v ds = (4.0 \hat{i} + 3.0 \hat{j} + 5.0 \hat{k}) \text{ m} \quad [c=0]$$

$$b) \dot{r}(t) = -r'(t) =$$

$$c) \ddot{r}(t) = \ddot{r}'(t) \quad d) \alpha(t) = -\ddot{r}(t)$$

$$73) V_{\text{still}} = 9.00 \frac{\text{m}}{\text{s}}$$

$$a) V_a = \Delta x / t = 6,000 \text{ m} / (6,000 \text{ s} \times 60 \text{ s}) = 5.00 \frac{\text{m}}{\text{s}}$$

$$V_{w,rd} = V_{air} + V_{still} = [-4.00 \frac{\text{m}}{\text{s}}]$$

$$b) t = \frac{\Delta x}{V} = (6,000 \text{ m}) / (9.00 \frac{\text{m}}{\text{s}} + 4.00 \frac{\text{m}}{\text{s}}) = [462 \text{ s}] = [7.64 \text{ min}]$$

$$77) V_{bw} = 15 \text{ km/h} @ -45^\circ \quad V_{bw} = 25 \text{ km/h} @ 45^\circ$$

$$= (10.6 \hat{i} - 10.6 \hat{j}) \frac{\text{km}}{\text{h}} = (17.7 \hat{i} + 17.7 \hat{j}) \frac{\text{km}}{\text{h}}$$

$$V_{rw} = V_{rb} + V_{bw} = (-10.6 \hat{i} + 10.6 \hat{j} + 17.7 \hat{i} + 17.7 \hat{j}) \frac{\text{km}}{\text{h}}$$

$$= 7.1 \hat{i} + 28.3 \hat{j} \frac{\text{km}}{\text{h}}$$

$$V_{wr} = -V_{rw} = -7.1 \hat{i} - 28.3 \hat{j} \frac{\text{km}}{\text{h}} = [29.2 \frac{\text{km}}{\text{h}} \text{ (a)}]$$

$$\theta = \tan^{-1}\left(\frac{28.3}{-7.1}\right) = [256^\circ]$$

$$81) a_c = \frac{v^2}{r} = \frac{(60.0 \text{ m/s})^2}{150 \text{ m}} = \frac{(60.0 \frac{\text{m}}{\text{s}} \times 1000 \frac{\text{m}}{\text{km}} \times \frac{1\text{h}}{3600\text{s}})^2}{150.0} = 1.85 \frac{\text{m}}{\text{s}^2}$$

$$a_t = \frac{\Delta v}{t} = -9.0 \frac{\text{km/h}}{\text{s}} = \frac{(-9.0 \frac{\text{m}}{\text{s}} \times 1000 \frac{\text{m}}{\text{km}} \times \frac{1\text{h}}{3600\text{s}})}{1\text{s}} = -2.5 \frac{\text{m}}{\text{s}^2}$$

$$a_{\text{total}} = \sqrt{a_c^2 + a_t^2} = \sqrt{(1.85 \frac{\text{m}}{\text{s}^2})^2 + (-2.5 \frac{\text{m}}{\text{s}^2})^2} = 3.1 \frac{\text{m}}{\text{s}^2}$$

$$85) \text{ave } v_{25} = v_0 + a_t t = (3.0 \frac{\text{m}}{\text{s}})(5.0 \text{s}) = 31.5 \text{ m/s}$$

$$a_c = \frac{v^2}{r} = (15.0 \frac{\text{m}}{\text{s}})^2 / 1.5 \text{ m} = 150 \frac{\text{m}}{\text{s}^2}$$

$$a_{\text{total}} = \sqrt{a_c^2 + a_t^2} = \sqrt{150^2 + 300^2} = 315 \frac{\text{m}}{\text{s}^2}$$

$$\theta = \tan^{-1}\left(\frac{a_c}{a_t}\right) = \tan^{-1}\left(\frac{150 \frac{\text{m}}{\text{s}^2}}{300 \frac{\text{m}}{\text{s}^2}}\right) = 88.9^\circ \text{ from tangent}$$

89) ~~DE-MATH~~

$$\Delta x = r_2 - r_1, \quad r_2 = \delta x + r_1 = (7.5 \hat{i} + 3.2 \hat{j} - 1.2 \hat{k} + 1.5 \hat{i} + 4.0 \hat{k}) \text{ m} \\ = (6.5 \hat{i} + 4.7 \hat{j} + 2.8 \hat{k}) \text{ m}$$

$$93) R = \frac{v_0^2 \sin 2\theta}{g} \quad R_1 = \frac{v_0^2}{g} \sin(2 \cdot 45^\circ) = \frac{v_0^2}{g} = 8.0 \text{ m}$$

$$R_2 = \frac{v_0^2}{g} \sin(2 \cdot 30^\circ) = 0.866 \frac{v_0^2}{g}$$

$$R_2 = 0.866 (R_1) = 0.866 (8.0 \text{ m}) = 6.93 \text{ m}$$

$$\text{he loses } 8.0 - 6.93 \text{ m} = 1.1 \text{ m}$$

$$97) w = \frac{v_0}{r} = \frac{v_0}{1.6 \text{ m}} = \frac{v_0}{8.64 \times 10^4 \text{ s}} = 7.27 \times 10^{-5} \frac{\text{rad}}{\text{s}}$$

$$N = r w = (42.3 \times 10^6 \text{ m})(7.27 \times 10^{-5} \frac{\text{rad}}{\text{s}}) = 3.07 \times 10^3 \frac{\text{N}}{\text{s}}$$

$$a_c = \frac{v^2}{r} = (3.08 \times 10^3 \frac{\text{m}}{\text{s}})^2 / 42.3 \times 10^6 \text{ m} = 7.28 \times 10^{-5} \text{ m/s}^2$$

601) ~~DE-MATH~~

$$\begin{array}{c} \uparrow 80 \text{ km/h} \quad v_{IE} = 80 \frac{\text{km}}{\text{h}} = +22.2 \frac{\text{m}}{\text{s}} \uparrow \\ \uparrow 80 \text{ km/h} \quad v_{CE} = 50 \frac{\text{km}}{\text{h}} = +13.9 \frac{\text{m}}{\text{s}} \uparrow \\ \hookrightarrow 80 \text{ km/h} \quad v_{IC} = +v_{IE} + v_{CE} = +22.2 \frac{\text{m}}{\text{s}} \uparrow + 13.9 \frac{\text{m}}{\text{s}} \uparrow \end{array}$$

$$r(t) = \sqrt{v_{IC}^2 + (3.2 \times 10^4 \text{ m})^2} = \sqrt{(-3.2 \times 10^4 \text{ m} + 22.2 \text{ m})^2 + (13.9 \text{ m})^2} \\ = (-3.2 \times 10^4 \text{ m} + 22.2 \text{ m})^2 + (13.9 \text{ m})^2$$

$$r'(t) = 0 \quad 2(-3.2 \times 10^4 \text{ m} + 22.2 \text{ m})(22.2) + 2(13.9 \text{ m})(13.9) = 0$$

$$49.36 \text{ m} + 386 \text{ m} = 1.42 \times 10^4 \text{ m} \quad 879 \text{ m} = 1.42 \times 10^4 \text{ m}$$

$$t = 1615 \text{ s}$$

$$b) r(1615) = \sqrt{(-3.2 \times 10^4 \text{ m} + 22.2 \text{ m})^2 + (13.9 \text{ m})^2}$$

$$= 22.08 \text{ km}$$

$$1615 \text{ s} \times \frac{1 \text{ min}}{60 \text{ s}} \times \frac{1 \text{ hr}}{60 \text{ min}} = 0.45 \text{ hr}$$

9) both fall at the same time

29) c) $v(2.0) = (2.0\hat{i} - 84\hat{j} + 1.25\hat{k}) \text{ m/s}$

d) $v(3.0) = (0\hat{i} - 3\hat{j}) = 0.37 \text{ m/s}$

e) $v_{12} = v(2) - v(1) = (2\hat{i} - 56\hat{j} - 1.25\hat{k} - 3.0\hat{i} + 70\hat{j} + 5.0\hat{k}) \text{ m/s}$

45) $v_y^0 = v_{0y} + a_y t \quad v_{fy}^2 = v_{0y}^2 + 2a_y \Delta y$

$$\Delta y = \frac{-v_{0y}^2}{2a_y} = \frac{-(24.0 \text{ m/s})^2}{2(-9.8 \text{ m/s}^2)} = 12.94 \text{ m}$$

$$t = \frac{-v_{0y}}{a_y} = \frac{(-24.0 \text{ m/s})}{-9.8 \text{ m/s}^2} = 2.45 \text{ s}$$

b) $\Delta x = v_{0x} t = (18.1 \text{ m/s})(2.45 \text{ s}) = 44.3 \text{ m}$

d) ~~$r(t) = v_{0y}t + \frac{1}{2}a_y t^2$~~

$$= 4.9t^2 + 24.0t + 100 \text{ m}$$

$$t = \frac{-24.0 \pm \sqrt{24.0^2 + 4 \cdot 4.9 \cdot 100}}{-9.8} = 7.59 \text{ s}$$

$$\Delta x = v_{0x} t = (18.1 \text{ m/s})(7.59 \text{ s}) = 137 \text{ m}$$

c) ~~$r(t) = v_{0x}t + \frac{1}{2}a_y t^2$~~ $r(t) = v_{0x}t + \frac{1}{2}(a_y t^2)$ m

$$r(2) = v_{0y}(t) + \frac{1}{2}a_y t^2 = 24.0 \text{ m/s}(2.0 \text{ s}) + (-4.9)(2.0)^2 = 28.4 \text{ m}$$

$$r(4.0) = (18.1 \text{ m/s})(4.0 \text{ s}) + (24.0 \text{ m/s})(4.0 \text{ s})^2 - (4.9)(4.0 \text{ s})^2 = 72.4 \text{ m} + 18.0 \text{ m}$$

$$r(6.0) = (24.0 \text{ m/s})(6.0 \text{ s}) - (4.9)(6.0 \text{ s})^2 = -31.8 \text{ m}$$

65) $T_{\text{max}} = 725 \text{ days} = 1.9 \times 10^7 \text{ s}$

$$\omega = \frac{2\pi}{T} = 3.31 \times 10^{-7} \text{ rad/s} \quad v = r\omega = (1.08 \times 10^6 \text{ m})(3.31 \times 10^{-7} \text{ rad/s})$$

$$a_C = \frac{v^2}{r} = (3.57 \times 10^4 \text{ m})^2 / (1.08 \times 10^6 \text{ m}) = 3.57 \times 10^4 \text{ m/s}^2 \\ = 0.0118 \text{ m/s}^2$$

69) b) $r(t) = r'(t) + (4.0\hat{i} + 3.0\hat{j} + 5.0\hat{k}) \text{ m}$

c) $v(t) = v'(t) + (4.0\hat{i} + 3.0\hat{j} + 5.0\hat{k}) \text{ m/s}$

d) $a(t) = a'(t)$

77) $\theta = \tan^{-1}\left(\frac{4.0}{3.0}\right) = 53.1^\circ$

$$97) a_c = \frac{v^2}{r} = (3.08 \times 10^3 \frac{\text{m}}{\text{s}})^2 / 4.23 \times 10^2 = \boxed{0.224 \frac{\text{m}}{\text{s}^2}}$$

$$101) v_{TG} = 80 \frac{\text{km}}{\text{h}} \uparrow \quad v_{LG} = 50 \frac{\text{km}}{\text{h}} \uparrow$$

$$\text{a)} v_{TC} = 80 \frac{\text{km}}{\text{h}} \uparrow + 50 \frac{\text{km}}{\text{h}} \uparrow$$

$$r_{TC} = \int v_{TC} dt = 80t \frac{\text{km}}{\text{h}} \uparrow + 50t \frac{\text{km}}{\text{h}} \uparrow + C_1, \quad C_1 = -32 \text{ km}$$

$$= (-32 + 80t) \uparrow + 50t \uparrow \text{ m}$$

$$|r^2| = (-32 + 80t)^2 + (50t)^2$$

$$(r^2)' = 0 \quad 2r \frac{dr}{dt} = 0$$

$$2(-32 + 80t)(80) + 2(50t)(50) = 0$$

~~$$2(80t) = 5120$$~~

$$17800 t = 5120$$

~~$$t = 0.292 \text{ h}$$~~

$$t = \boxed{0.29 \text{ h}}$$

$$\text{b)} r(0.29 \text{ h}) = \sqrt{(-32 + 80t)^2 + (50t)^2}$$

$$= \boxed{17.0 \text{ km}}$$

$$45) \text{a)} 29.4 \text{ m}$$

$$\text{b)} 54 \text{ m}$$

$$\text{c)} r(4.0 \text{ s}) \neq 17.6 \text{ m}$$

$$69) \text{b)} r(t) = r'(t) + (4.0 \hat{i} + 3.0 \hat{j} + 5.0 \hat{k}) t \text{ m}$$

$$\text{c)} v(t) = \omega'(t) + (4.0 \hat{i} + 3.0 \hat{j} + 5.0 \hat{k}) \hat{\text{m}}$$