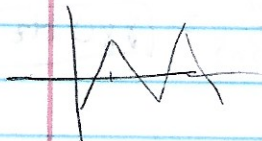


Ph. 12 ex.

12.1 $v = 10.00 \text{ m/s}$

a) $\lambda = 2 \text{ cm} \times 3 \text{ to } 2 \text{ cm} \times 3$
 $= 6 \text{ m}$ (from graph)

b) ψ vs. t
 $\text{max } \psi = -1$
 $\text{max } \psi = 2$



c) $T = \text{time for a full oscillation}$
 $v = f\lambda = \frac{\lambda}{T}$

$$T = \frac{\lambda}{v} = \frac{6 \text{ m}}{10 \text{ m/s}} = 0.60 \text{ s}$$

d) $f = \frac{1}{T} = \frac{10}{6} \text{ Hz} = 1.67 \text{ Hz}$

12.2 $v = 4.0 \text{ m/s}$

a) $v = f\lambda = \frac{\lambda}{T}$
 $T = \frac{\lambda}{v} = \frac{0.20 \text{ m}}{4.0 \text{ m/s}} = 0.05 \text{ s}$

b) $f = \frac{1}{T} = 20 \text{ Hz}$

12.3) $\psi(x, t) = 0.4 \text{ m} \cos[(6.00 \text{ rad/m})x - (10.0 \text{ rad/s})t]$

a) $A = 0.4 \text{ m}$

b) $k = \frac{2\pi}{\lambda}$
 $\lambda = \frac{2\pi}{k} = \frac{2\pi}{6.00 \text{ rad/m}} = 1.05 \text{ m}$

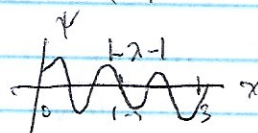
c) $\omega = 2\pi f$

$$f = \frac{\omega}{2\pi} = \frac{10 \text{ rad/s}}{2\pi} = 1.6 \text{ Hz}$$

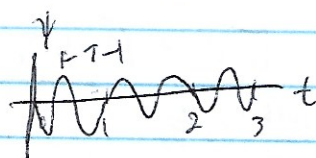
d) $v = f\lambda = (1.6 \text{ Hz})(1.05 \text{ m}) = 1.68 \text{ m/s}$

e) $\psi(5, 2) = 0.4 \text{ m} \cos(6.00 \times 5 - 10 \times 2)$
 $= -0.34 \text{ m}$

f) $t = 2.00 \text{ s}$ $\psi(x, 2) = 0.40 \text{ m} \cos(6.00\pi - 20)$



g) $\psi(x, t) = 0.40 \text{ m} \cos(80 - 10t)$



12.4) $\psi(x, t) = A \cos(kx - \omega t - \frac{\pi}{2})$

$$\psi(x, t) = A \sin(kx - \omega t)$$

$$\cos(90 - \theta) = \sin \theta$$

$$\sin(90 - \theta) = \cos \theta$$

$$\psi(x, t) = A \cos(kx - \omega t - \frac{\pi}{2})$$

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

$$= A \sin(kx - \omega t)$$

12.5) $v = \sqrt{\frac{P}{\mu}} = \sqrt{\frac{P}{\mu/\lambda}}$

$$= \sqrt{\frac{5 \text{ W}}{(0.076 \text{ kg/m})/\lambda}} = 18.3 \text{ m/s}$$

12.6) $v = \sqrt{\frac{B}{\rho}} = \sqrt{\frac{0.2 \times 10^{10} \text{ N/m}^2}{1.00 \text{ kg/m}^3}}$
 $= 1414 \text{ m/s}$

12.7) $P = \frac{1}{2} \mu \omega^2 A^2 v$

$$v = \sqrt{\frac{B}{\rho}} = \sqrt{\frac{80 \text{ N/m}^2}{0.076 \text{ kg/m}^3}} = 57 \text{ m/s}$$

$$\omega = 2\pi f = 2\pi(10 \text{ Hz}) = 63 \text{ rad/s}$$

$$A = 2.0 \text{ cm} = 0.02 \text{ m}$$

$$P = \frac{1}{2} (0.076 \text{ kg/m}) (63 \text{ rad/s})^2 (0.02 \text{ m})^2 (57 \text{ m/s})$$

 $= 10.69 \text{ W}$

$$12-8) I = \frac{P}{4\pi r^2} \quad P = 4\pi r^2 I = 4\pi r_0^2 I_0$$

$$r^2 = \frac{4\pi r_0^2 I_0}{4\pi (0.1) I_0}$$

$$= 10 r_0^2$$

$$r = \sqrt{10 r_0^2} = \sqrt{3.16} r_0$$

$$12-9) \text{ dB } \beta = 10 \text{ dB } \log_{10} \frac{I}{I_0}$$

$$\frac{I}{I_0} = 10^{\frac{\beta}{10 \text{ dB}}}$$

$$\beta + 3.00 \text{ dB} = 10 \text{ dB } \log_{10} \frac{I}{I_0}$$

$$\frac{I'}{I} = 10^{\frac{\beta+3}{10}}$$

$$= 10^{0.3} = 2.00$$

$$12-10) f_s = 261.6 \text{ Hz} \quad v_{wind} = -5.0 \text{ m/s}$$

$$v_{source} = +10.00 \text{ m/s} \quad v_{obs} = +20.00 \text{ m/s}$$

$$f' = f_s \left(\frac{v \pm v_{obs}}{v \pm v_{source}} \right)$$

$$= (261.6 \text{ Hz}) \left(\frac{343 + 5.0 + 20.0}{343 - 5.0 + 10.0} \right)$$

$$= 294 \text{ Hz}$$

$$f' = (261.6 \text{ Hz}) \left(\frac{343 - 5 - 20}{343 - 5 + 10} \right)$$

$$= 239 \text{ Hz}$$

$$12-11) l = 0.585 \text{ m} \quad \mu = 8.74 \times 10^{-5} \text{ kg/m}$$

$$f = 440 \text{ Hz}$$

$$a) v = \sqrt{\frac{E}{\mu}} = f \lambda \quad \lambda_1 = 2l$$

$$= (440 \text{ Hz}) (2 \times 0.585 \text{ m})$$

$$= 515 \text{ m/s}$$


$$b) \lambda = 2l = 2 \times 0.58 \text{ m} = 1.17 \text{ m}$$

$$c) \text{ for } \lambda_n = \frac{2l}{n}$$

$$v = f \lambda \quad \lambda_n = \frac{v}{f} = \frac{v}{\frac{2l}{n}} = \frac{n v}{2l}$$

$$f_2 = \frac{v (515 \text{ m/s})}{2 (0.585 \text{ m})} = 880 \text{ Hz}$$

d)



$$d = \frac{\lambda}{2} = \frac{2(0.585 \text{ m})}{2}$$

$$= 0.585 \text{ m}$$

$$12-12) \text{ closed pipe, } f = 440 \text{ Hz}$$

$$\lambda_n = \frac{4l}{n}, \quad n=1$$

$$\lambda_1 = 4l \quad l = \frac{\lambda_1}{4}$$

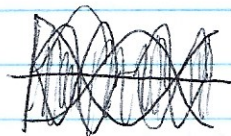
$$v = f \lambda$$

$$\lambda = \frac{v}{f} \quad l = \frac{v}{4f}$$

$$= \frac{343 \text{ m}}{4(440 \text{ Hz})} = 0.19 \text{ m}$$

$$12-13) f_1 = 8.00 \text{ Hz} \quad f_2 = 8.25 \text{ Hz}$$

$$a) \psi_1(x, t) \quad \psi_2(x, t)$$



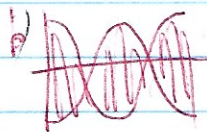
$$\psi(x, t) = A \cos(kx - \omega t)$$

$$\omega = 2\pi f$$

$$\psi_1(x, t) = A \cos(-2\pi f_1 t)$$

assume $A=1$

$$\psi_2 = \cos(-2\pi f_2 t)$$



$$c) f_b = f_2 - f_1$$

$$= 0.25 \text{ Hz}$$

$$d) T_b = \frac{1}{f} = 4 \text{ s}$$