

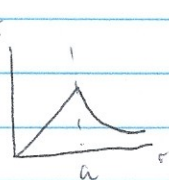
1)  $E = \begin{cases} \alpha r^2, & r \leq a \quad (1) \text{ region I} \\ \frac{\beta}{r^2}, & r > a \quad (2) \text{ region II} \end{cases}$

a)  $\alpha r = \frac{\beta}{r^2}$

$\alpha a = \frac{\beta}{a^2}$

when  $r=a$

$\alpha = \frac{\beta}{a^3}$



b) region I:  $E = -\frac{dV}{dr}$

$\int E dr = -\int dV$   
 $V = -\int E dr$

$V = -\int E dr$

area

$V = -\alpha \int r^2 dr$

$= -\alpha \cdot \frac{1}{3} r^3 + C$

$= -\frac{\alpha r^3}{3}$

$(=0 \quad r=0 \quad E=0 \quad V=0)$

c)  $V_{max}$  is when  $r=0$

$\frac{1}{2} m V_{max}^2 = q V_0$

$\frac{1}{2} m v^2 = (-e) \left( -\frac{\alpha a^3}{3} \right)$

$\frac{1}{2} m v^2 = \frac{e \alpha a^3}{3}$

$v^2 = \frac{2 e \alpha a^3}{3 m}$

$v = \sqrt{\frac{2 e \alpha a^3}{3 m}}$

towards the center

region II:  $V = -\int E dr$

(-) negative potential means charges are more attracted towards the center and (-) charges are attracted towards  $\hat{r}$

region II:  $V = -\int E dr$

$= -\beta \int \frac{dr}{r^2}$

$= \beta \left[ \frac{1}{r} \right]_a^r$

$= \frac{\beta}{r} - \frac{\beta}{a} = \beta \left( \frac{1}{r} - \frac{1}{a} \right)$

f) the electron executes SHM from  $a$  to  $-a$  through the center, in the radial direction.

g) yes, it gets all the way to the other side b/c of conservation of E



a)

2)  $E \perp$  to equipotential (sur.  
 $E$  is radially outwards or inwards  
 from the origin

c)  $\Delta V = 10V$

(1)  $KE = -\Delta PE = q \Delta V = 10V (10^{-19}C)$   
 $= 10^{-18} J$

for both electron &  
 proton  $+1 +1$

because voltage increases as  
 $r$  increases,  $V \propto \frac{1}{r}$ , so the  
 charges must have more potential  
 energy the further they get, so  
 they would be attracted towards  
 the origin. therefore, the  $E$   
 points radially towards the  
 origin.

$KE_e = 0$   $+1$

(2) electron:  $KE = \frac{1}{2}mv^2$   $+1$

$v = \sqrt{\frac{2KE}{m}} = \sqrt{\frac{2(10^{-18}J)}{9.11 \times 10^{-31}kg}}$   
 $= 1.49 \times 10^6 m/s$   $+1$

proton:  $v = \sqrt{\frac{2KE}{m}}$

$= \sqrt{\frac{2(10^{-18}J)}{1.67 \times 10^{-27}kg}} = 1.1 \times 10^4 m/s$   $+1$

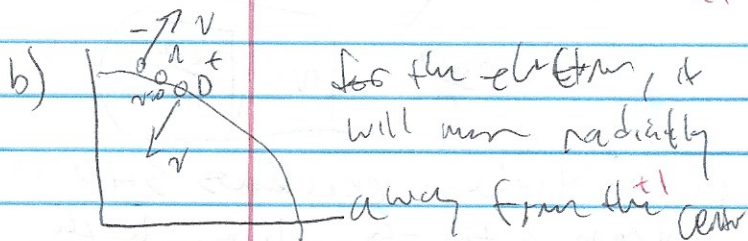
$v_p = 0$   $+1$

at (c),  $V = -E/r$

$E = \frac{V}{r} = \frac{20V}{2m} = 10 \frac{N}{C}$

at (d),  $E = \frac{V}{r} = \frac{30V}{3m} = 10 \frac{N}{C}$

both towards the origin.  $+1$   
 $+1$



the neutron will stay in place.  $+1$   
 the proton will move towards  
 the center.  $+1$

3)  $B = \begin{cases} \beta r \hat{\theta} & r \leq r_0 \\ \frac{\lambda}{r} \hat{\theta} & r > r_0 \end{cases}$

a) when  $r = r_0$ ,  $\beta r = \frac{\lambda}{r}$   $+1$

$\beta = \frac{\lambda}{r^2}$   $+1$

b) at  $r = r_0$ ,  $F = qvB \sin \theta$   
 $\sin \theta$  instead of  $\times$  product  $\sin \theta = 1$   
 $= qv \cdot \beta r_0$

$v_0$  is towards the center

$-e v_0 \beta r_0 = ma$

$a = -e v_0 \beta r_0$

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perpendicular to the velocity

c)  $v_{max} = v_0$   $+1$

d) the electron takes an elliptical orbit within the inner region

e)  $I = \frac{dq}{dt}$   $\frac{ds}{dt} = v$

4) a) grav. field points towards origin.

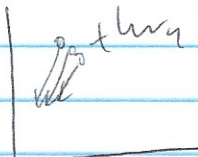
at (c):  $V = \frac{PE}{m}$   $g = \frac{V}{r}$

$= \frac{20 \text{ J/kg}}{2 \text{ m}}$

$= 10 \frac{\text{m}}{\text{s}^2}$

at  $P$ :  $g = \frac{V}{r} = \frac{30 \text{ J/kg}}{3 \text{ m}} = 10 \frac{\text{m}}{\text{s}^2}$

both towards center.  $+1 +1$

b)  they will all move towards the origin.  $+1 +1 +1$

c)  $\Delta KE = -\Delta PE = m\Delta V = 10 \text{ J/kg} \cdot m$   $+1$

1) electron:  $KE = (10 \text{ J/kg})(10^{-30} \text{ kg})$   
 $= 10^{-29} \text{ J}$   $+1$

proton:  $KE = (10 \text{ J/kg})(10^{-27} \text{ kg})$   
 and neutron:  $= 10^{-26} \text{ J}$   $+1 +1$

2) electron:  $v = \sqrt{\frac{2KE}{m}} = \sqrt{\frac{2(10^{-29} \text{ J})}{10^{-30} \text{ kg}}}$   
 $= 4.47 \text{ m/s}$

proton & neutron:  $v = \sqrt{\frac{2KE}{m}} = \sqrt{\frac{2(10^{-26} \text{ J})}{10^{-27} \text{ kg}}}$   
 $= 4.47 \text{ m/s}$   $+1 +1 +1$

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