

Introduction to Electric and Magnetic Fields B38EM

Tutorial #2 – Problems

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ Fm}^{-1}, \quad q_{e^-} = 1.6 \times 10^{-19} \text{ C}$$

1. A charge of $Q_1 = 3 \cdot 10^{-4} \text{ C}$ is located at $M(1,2,3)$ and a charge of $Q_2 = -10^{-4} \text{ C}$ is located at $N(2,0,5)$ in a vacuum. Calculate the force exerted on Q_2 by Q_1 ?
2. Two equal but opposite charges Q are separated by a distance $2a$. Use Coulomb's law and the principle of superposition to find expressions for the electric field \mathbf{E} and electric potential V along the line through the midpoint between the charges and normal to the axis of the charges.
3. A charge of 3 nC is located at the origin, and another charge of $+5 \text{ nC}$ is located at 0.3 m along the positive x -axis. Determine the position where the electric field is zero. (remark: nC means nanocoulomb, which is 10^{-9} C .)
4. Four positive identical charges of 50 nC each are located at $A(1,0,0)$, $B(-1,0,0)$, $C(0,1,0)$, and $D(0,-1,0)$ in free space (the coordinates are in meters). Find the total force on the charge at A .
5. A charged circular annulus is defined by two circles of centre O , and radii a and R ($a < R$), of surface charge density σ .
 - a. Calculate the E -field generated by these charges at a point M , of height z , situated directly above the point O .
 - b. What becomes the expression of the field when a tends to zero. Draw the curve $E(z)$ as a function of z .
 - c. When a is different from zero, what becomes the expression of the field when R increases to infinity. Draw the curve $E(z)$ as a function of z .
 - d. What is the expression of the field when a tends to zero and R goes to infinity. Draw the curve $E(z)$ as a function of z .