

$$\begin{aligned}
 \Phi &= \int_0^b \left[\hat{a}_z B_0 \cos \frac{\pi r}{2b} \sin \omega t \right] \cdot \left(\hat{a}_z \cdot 2\pi r \right) dr \\
 &= 2\pi B_0 \sin \omega t \int_0^b \cos \frac{\pi r}{2b} \cdot r dr \\
 &= 2\pi B_0 \sin \omega t \cdot \frac{2b}{\pi} \int_0^b r d\left(\sin \frac{\pi}{2b} r\right) \\
 &= 4b B_0 \sin \omega t \left[r \cdot \sin \frac{\pi r}{2b} \Big|_0^b - \int_0^b \sin \frac{\pi r}{2b} dr \right] \\
 &= 4b B_0 \sin \omega t \left[b + \frac{2b}{\pi} \cos \frac{\pi r}{2b} \Big|_0^b \right] \\
 &= 4b B_0 \sin \omega t \left[b - \frac{2b}{\pi} \right] \\
 &= 8b^2 B_0 \sin \omega t \left[\frac{1}{2} - \frac{1}{\pi} \right] = \frac{8b^2 B_0 \sin \omega t}{\pi} \left[\frac{\pi}{2} - 1 \right]
 \end{aligned}$$

$$V = -N \frac{d\Phi}{dt} = -N \frac{8b^2 B_0 \omega \cos \omega t}{\pi} \left[\frac{\pi}{2} - 1 \right]$$

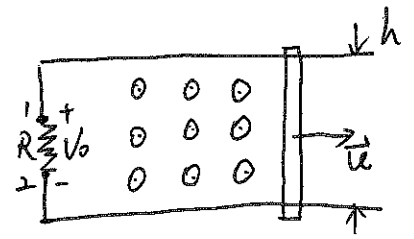
A circular loop of N turns of conducting wire lies in the x - y plane with its centre at the origin of a magnetic field specified by $\vec{B} = \hat{a}_z B_0 \cos\left(\frac{\pi r}{2b}\right) \sin \omega t$, where b is the radius of the loop and ω is the angular frequency. Find the EMF induced in the loop.

A metal bar slides over a pair of conducting rails in a uniform magnetic field $\vec{B} = \hat{a}_z B_0$ with a constant velocity \vec{u} .

a). Determine the open-circuit voltage V_0 .

b). Assume R is connected. Find dissipated power over R .

c) Prove electric power = mechanical power



$$a). V_0 = \frac{d\mathcal{E}}{dt} = \frac{-d[\hat{a}_z B_0 \cdot \hat{a}_z h \frac{dl}{dt}]}{dt} = -B_0 h \frac{dl}{dt} = -B_0 h u \quad (V)$$

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$$b). P_e = \frac{(V_0)^2}{R} = \frac{(u B_0 h)^2}{R}$$

$$c). I = \frac{V_0}{R} = - \frac{B_0 h u}{R} \quad (A) \quad \text{"-"} \text{ current in Bar pointing downward.}$$

$$\vec{F}_m = \cancel{I \vec{u} \times \vec{B}} = \vec{I}$$

$$F_m = \int \vec{v} \times \vec{B} = \int I \cdot h \cdot B_0 \hat{a}_z$$

$$W_m = F_m \cdot dl$$

$$P_m = |F_m \cdot dl/ds| = |F_m \cdot u| = \frac{B_0 h u}{R} \cdot h B_0 u = \frac{(u h B_0)^2}{R}$$