

## HINTS AND ANSWERS OF Tutorial Sheet-2

AUTUMN 2018

MATHEMATICS-I (MA10001)

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- 1.a. 0,    b. 1,    c. e,  
d. 1,    e. 1,    f.  $-1/2$ ,  
g. 1,    h. 1,    i.  $1/e$ ,  
j.  $\infty$ ,    k.  $1/120$ .

2.a. Ans. 1.22656, Hint: Consider a function  $f(x) = \sqrt{1+x}$  and expand it using Taylor's Series Expansion with  $x=0.5$ .

b. Hint: Consider a function  $f(x) = \sin x$  and expand it using Taylor's Series Expansion with  $x=46^\circ$ .

3.  $1.105 < e^{0.1} < 1.1052$

4. Hint: Use Taylor's theorem with Lagranges form of remainder.

5. Hint: Take the hypothesis  $f(x) = a_0 + a_1(x-x_0) + E(x)(x-x_0)$  where  $\lim_{x \rightarrow x_0} f(x) = a_0$ .

6.a.  $\sqrt{2}$     b. 0    c. 1    d.  $3/2$

7. Hint: Use Maclaurin's theorem with Lagranges form of remainder after  $n$  terms and show that  $\lim_{n \rightarrow \infty} R_n = 0$

8. Ans. Can not expand. Hint: Expand the given function and get the limit which is not finite.

9. Hint: Use Maclaurin's Theorem with remainder and approximate the result.

10. Ans:  $\frac{e^x}{1+e^x} = 1/2 + x/4 - x^3/48 + \dots$ , Hint: Get the derivatives of the given function and use Maclaurin's Theorem.