Introduction to Coq

Coq Andes Summer School 2020

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A Versatile Prover

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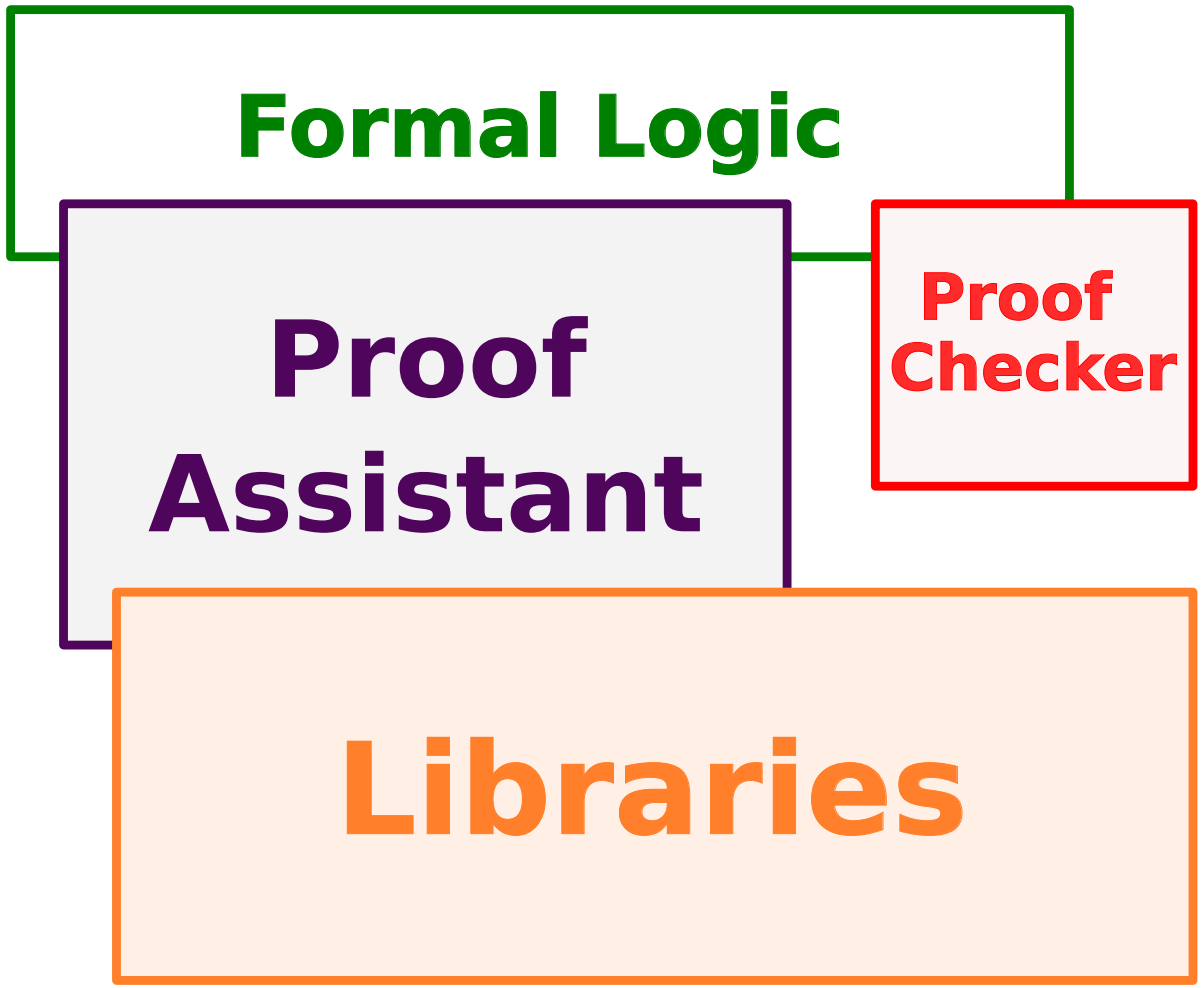
- Teaching
  - Software Foundations
  - ...

Interactive Theorem Provers



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Coq, Agda, Matita, Lean, NuPRL, etc.

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Languages

- Logical foundations
- Libraries
- Meta-Language(s)

Two Sides of Automation

Filling gaps:

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- in proofs

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Filling gaps:

- in proofs
- in statements.