

Strong self-regulation and widespread facilitative interactions in phytoplankton communities

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Abstract

1. The persistence of phytoplanktonic diversity in spite of competition for basic resources has long been a source of wonder and inspiration to ecologists. To sort out, among the many coexistence mechanisms suggested by theory and experiments, which ones actually maintain diversity in natural ecosystems, long-term field studies are paramount.
2. We analysed a large dataset of phytoplankton abundance time series using dynamic, multivariate autoregressive models. Phytoplankton was counted and identified down to the genus level, every two weeks over twenty years, at ten sites along the French coastline. Multivariate autoregressive models allowed to estimate biotic interaction networks, while also accounting for abiotic variables that may drive part of the phytoplankton fluctuations. We then analysed the ratio of intra- to inter-taxa interactions (measuring self-regulation, itself a measure of niche differentiation), the frequency of negative vs positive interactions, and how stability metrics (both at the network and genus level) relate to network complexity and genus self-regulation or abundance.
3. We showed that a strong self-regulation, with competition strength within a taxon (genus) an order of magnitude higher than between taxa, was present in all phytoplanktonic interaction networks. This much stronger intragenus competition suggests that niche differentiation - rather than neutrality - is commonplace in phytoplankton. Furthermore, interaction networks were dominated by positive net effects between phytoplanktonic taxa (on average, more than 50% of interactions were positive). While network stability (*sensu* resilience) was unrelated to complexity measures, we unveiled links between self-regulation, intergenus interaction strengths and abundance. The less common taxa tend to be more strongly self-regulated and can therefore maintain in spite of competition with more abundant ones.
4. *Synthesis:* We demonstrate that strong niche differentiation, widespread facilitation between phytoplanktonic taxa and stabilizing covariances between interaction strengths should be common features of coexisting phytoplankton communities in the field. These are structural

properties that we can expect to emerge from plausible mechanistic models of phytoplankton communities. We discuss mechanisms, such as predation or restricted microscale movement, that are consistent with these findings, which paves the way for further research.

Keywords: phytoplankton; coexistence; facilitation; mutualism; niche theory; time series; networks

1 Introduction

2 How species or close genera can coexist together in spite of competition is one of the main puzzles of
3 community ecology, especially for primary producers that seemingly share the same basic resources
4 ([Hutchinson, 1961](#)). Many theoretical studies of competition models have shown that competitive
5 exclusion is likely in those circumstances, unless mechanisms involving spatial or temporal variation
6 are at play ([Armstrong & McGehee, 1976, 1980](#); [Chesson & Huntly, 1997](#); [Huisman & Weissing, 2001](#);
7 [Li & Chesson, 2016](#); [Chesson, 2018](#)). Neutral theory, that assumes a non-equilibrium coexistence
8 maintained by dispersal and equal competitive abilities for all species ([Hubbell 2001](#), though there
9 are exceptions, see [Volkov *et al.* 2003, 2007](#)), has been proposed as a solution to explain highly
10 diverse communities ([Hubbell, 2001](#); [Rosindell *et al.*, 2011](#)).

11 However, the evidence gathered from terrestrial plant communities starts to suggest that, in fact,
12 niche rather than neutral processes may be paramount to explain coexistence, with intraspecific
13 competition dwarfing interspecific competition in most cases ([Adler *et al.*, 2010, 2018b](#)). Whether
14 these conclusions drawn mostly from studies of terrestrial plants apply to other ecosystems and taxa
15 is currently little known (but see [Mutshinda *et al.* 2009](#)).

16 Moreover, competition may not be the rule: the meta-analysis by [Adler *et al.* \(2018b\)](#) reported a
17 large number of facilitative interactions (30%) and several reviews ([Brooker *et al.*, 2008](#); [McIntire
18 & Fajardo, 2014](#); [Kinlock, 2019](#)) have highlighted that facilitation may be much more widespread
19 than ecologists usually tend to think. Although some theoretical studies suggest that facilitative
20 interactions can be destabilizing (*sensu* resilience) and therefore undermine coexistence in Lotka-
21 Volterra models ([Coyte *et al.*, 2015](#)), multiple other modelling ([Gross, 2008](#)) and empirical ([Brooker
22 *et al.*, 2008](#); [Cavieres & Badano, 2009](#)) studies have suggested that facilitative interactions can
23 to a large degree benefit coexistence, especially when multiple interaction types are considered
24 simultaneously ([Mougi & Kondoh, 2012](#); [García-Callejas *et al.*, 2018](#)).

25 Here, we analyse a spatially replicated, long-term community-level dataset, consisting of ten
26 multivariate time series of phytoplankton abundance along the French coastline. The time series are
27 modelled using multivariate autoregressive (MAR) models, allowing for interactions between genera.

28 Although many ecological studies focus on interactions between species, competition has been shown
29 experimentally to occur between different genera of phytoplankton ([Titman, 1976](#); [Descamps-Julien](#)
30 [& Gonzalez, 2005](#)). The genus level is also a rather fine taxonomic scale for phytoplankton interaction
31 studies, as most studies are restricted to interactions between different classes or even phyla ([Ives](#)
32 [et al., 2003](#); [Hampton et al., 2008](#); [Griffiths et al., 2015](#)). Studying interactions between different
33 genera of phytoplankton therefore both makes empirical sense in light of competition experiments
34 and allows to estimate better-resolved networks. We focus here on genera that belong mostly to
35 diatoms and dinoflagellates. To put our results into a more general context, we then compare our
36 interaction strength estimates to previously published interaction networks produced under the same
37 statistical framework, both in plankton and other empirical systems.

38 Material and methods

39 Sampling methods

40 All phytoplankton samples were collected by Ifremer coastal laboratories as part of the National
41 Phytoplankton and Phycotoxin Monitoring Network ([REPHY, 2017](#)). Since 1987, this monitoring
42 program has required the sampling of 26 sites along the French coastline every 2 weeks within 2
43 hours of high tide to document both biotic (phytoplankton counts) and abiotic (water temperature,
44 salinity) variables. We focused on sites which had the longest time series. We also excluded time
45 series which had missing data for over 6 months or an average delay between sampling dates above
46 20 days. This reduced the number of study sites to 10 sites nested within 4 regions (Brittany, Oléron,
47 Arcachon and the Mediterranean Sea; Fig. S1 and Table S1).

48 Abiotic variables (temperature, salinity) were measured directly from the boat during the sampling
49 process while water samples for biotic analyses were fixed with a Lugol's solution and examined later.
50 Phytoplankton cells above 20 μm were identified at the lowest possible taxonomic level and counted
51 with the Utermöhl method using an optical microscope ([Utermöhl, 1958](#)). Throughout the years
52 and sites, more than 600 taxa were identified at different taxonomic levels. We aggregated them at
53 the genus (or group of genera when not possible) level based on previous work (Table S2; [Hernández](#)

54 [Fariñas *et al.* 2015](#); [Barraquand *et al.* 2018](#)), except for cryptophytes and euglenophytes in Arcachon,
 55 which could not be identified below the family level. Although the taxonomic resolution used here
 56 may seem coarse in comparison to land plants, it is in fact more refined than 86% of the MAR(1)
 57 studies of phytoplankton listed in Table S4.

58 For each region, the MAR(1) analysis focused on the most abundant and most frequently observed
 59 genera to avoid most of the gaps in the time series. Time series are plotted in Fig. S2. When gaps
 60 did not exceed a month, missing values were linearly interpolated; remaining missing values were
 61 replaced by a random number between 0 and half of the lowest observed abundance ([Hampton
 62 *et al.*, 2006](#)). We tested extensively this and other methods to deal with missing data in a previous
 63 publication on a subset of this dataset ([Barraquand *et al.*, 2018](#)). All time series were scaled and
 64 centered before MAR analyses.

65 **MAR(1) model**

66 Multivariate autoregressive (MAR) models are used to determine the interspecific interactions and
 67 abiotic effects shaping a community’s dynamics ([Ives *et al.*, 2003](#)). MAR(1) models are based on a
 68 stochastic, discrete-time Gompertz equation which relates the log-abundance of each of the S taxa
 69 at time $t + 1$ to log-abundances of the whole community at time t , with possible interactions between
 70 taxa, and effects of V abiotic variables at time $t + 1$. These assumptions are encapsulated in eq. 1:

$$\mathbf{n}_{t+1} = \mathbf{B}\mathbf{n}_t + \mathbf{C}\mathbf{u}_{t+1} + \mathbf{e}_t, \mathbf{e}_t \sim \mathcal{N}_S(0, \mathbf{Q}) \quad (1)$$

71 where \mathbf{n}_t is the $1 \times S$ vector of log-abundance of phytoplankton taxa, \mathbf{B} is the $S \times S$ community
 72 (interaction) matrix, \mathbf{C} is the $S \times V$ environment matrix describing the effects of V variables (stacked
 73 in vector \mathbf{u}_{t+1}) on growth rates, with $V = 2$ in our case (temperature and salinity). The noise \mathbf{e}_t
 74 is a $1 \times S$ noise vector which covers both process and observation error, following a multivariate
 75 normal distribution with a variance-covariance matrix \mathbf{Q} . \mathbf{Q} is diagonal and we have previously
 76 showed that this parsimonious choice did not affect qualitatively the results ([Barraquand *et al.*,
 77 2018](#)). We used the MARSS package ([Holmes *et al.*, 2014](#)) v3.9, in R v3.3.2 ([Venables & Smith,](#)

78 2013), to estimate parameters with a maximum likelihood procedure.

79 Our previous analysis of the Arcachon region, for which more covariables were available (Bar-
80 raquand *et al.*, 2018), revealed that hydrodynamics and hydrology had more influence on phyto-
81 plankton dynamics than nutrients on the two-week timescale. Because temperature and salinity sum
82 up seasonal changes in light as well as hydrology (salinity is inversely related to freshwater inflow),
83 these represent the two key drivers needed to account for abiotic influences (Scheef *et al.*, 2013).
84 They are therefore used to summarize the abiotic environment in the remainder of the article.

85 The analysis of real data in Barraquand *et al.* (2018) was complemented by that of simulated
86 data mimicking the study design, which confirmed the ability of MAR(1) models to infer biotic
87 interactions and abiotic forcings. Fitting a more sophisticated model (threshold autoregressive
88 model) did not reveal extra non-linearities or a storage effect in the Arcachon subset of the data
89 (Barraquand *et al.*, 2018). Other aspects of the MAR(1) modelling are likewise quite robust: using
90 two abiotic variables (temperature and salinity) in this study rather than the full set used in
91 Barraquand *et al.* (2018) led to almost identical covariate effects and interaction estimates for the
92 Arcachon study sites. Even if some departures from the true data-generating model may not always
93 be detectable through MAR(1) diagnostics (e.g., residuals), the analysis of nonlinear simulations
94 has showed that MAR(1) models are in general robust to nonlinearities if the inference focuses on
95 interaction sign and order of magnitude of model coefficients (Certain *et al.*, 2018), which is how
96 these models are used here. For ease of interpretation of MAR(1) interaction coefficients, we also
97 prove the correspondence between the magnitude of intra/inter interaction strength in a MAR(1)
98 model and a multispecies Beverton-Holt model, i.e., a discrete-time Lotka-Volterra model (Cushing
99 *et al.*, 2004), in the Supporting Information.

100 In this study, the number of phytoplankton taxa (S) and the community composition vary
101 slightly between regions but sites share on average 67% of their taxa. In order to have comparable
102 models, we also keep the same 2 covariates, i.e., water temperature and salinity, that were measured
103 at all study sites. Therefore, the dimension of the dynamical system depends on the (square of
104 the) number of phytoplankton taxa we study, which ranges between 7 (Mediterranean Sea) and
105 14 (Brittany). The smallest system still requires 63 parameters to be estimated (49 for the 7×7

106 interaction matrices and 14 for the 7×2 environment matrices) if we consider all possible interactions
 107 between taxa. To reduce this dimensionality and remove unnecessary parameters, we built different
 108 ‘interaction scenarios’ based on known phylogenetic information (as suggested in [Violle *et al.*, 2011](#);
 109 [Narwani *et al.*, 2017](#)). The null interaction scenario assumed no interaction between genera (diagonal
 110 interaction matrix) and was compared to four other interaction scenarios. The first interaction
 111 scenario assumed that interactions could only occur between phylogenetically close organisms, i.e.,
 112 within a class (groups were then diatoms, dinoflagellates, and other phytoplanktonic organisms)
 113 while the second interaction scenario further differentiated pennate and centric diatoms. The third
 114 interaction scenario considered the reverse hypothesis, that only unrelated organisms could interact
 115 (i.e., a diatom could only interact with a dinoflagellate or a cryptophyte, but not with another
 116 diatom), and the last interaction scenario did not constrain the interactions at all (full interaction
 117 matrix). We selected the best scenario by comparing BIC (Fig. S3), which proved to be satisfactory
 118 in our previous analyses of both real data and similar simulated datasets ([Barraquand *et al.*, 2018](#),
 119 Appendix 2). The second interaction scenario, hereafter called the pennate-centric scenario, had the
 120 lowest BIC for all sites (Fig. S3). This parsimonious scenario was therefore chosen as the basis for
 121 further investigations of network structure.

122 **Analysis of interaction strengths**

123 The interaction matrix obtained from MAR(1) analyses can be used to determine the stability of
 124 a discrete-time dynamical system ([Ives *et al.*, 1999, 2003](#)). We compared the maximum modulus
 125 of the eigenvalues of the pennate/centric matrices for each site to network descriptors, such as
 126 the interaction strength distribution (sign, mean and variance) and weighted connectance ([Bersier
 127 *et al.*, 2002](#)). The maximum modulus is analogous to the real part of the leading eigenvalue for
 128 continuous time models and measures resilience while still accounting for some variability properties
 129 ([Ives *et al.*, 1999](#)). Weighted connectance is a measure of the proportion of realized links compared
 130 to all possible links, taking into account the shape of the flux distribution. This metric is adapted to
 131 weighted interaction matrices but cannot accommodate for both positive and negative coefficients: we
 132 therefore chose to focus on interaction strength only (absolute values of the coefficients), irrespective

133 of interaction sign. In contrast, mean and variance of the off-diagonal coefficients, which can affect
 134 the stability of a community (Allesina & Tang, 2015), are computed on raw values of the coefficients.
 135 Interaction coefficient variance is multiplied by the number of taxa, according to theory (Allesina &
 136 Tang, 2015).

137 In addition to these network-level metrics, we also computed the average vulnerability (average
 138 effect of other taxa on a focal taxon, eq. S5) and impact (average effect of a focal taxon on other
 139 taxa, eq. S6) on both raw and absolute values of the coefficients. Vulnerability and impact can be
 140 related to in-strength and out-strength in the meta-analysis of Kinlock (2019). We then compared
 141 these to the regulation a focal species exerted on itself. Raw values indicate the average effect that
 142 can be expected on the growth rate of a taxon from the rest of the community (i.e., is the effect of
 143 others mostly positive or negative?), while absolute effects characterise the strength of all types of
 144 interactions on a taxon (i.e., is a taxon strongly affected by the others?).

145 Finally, we compared the observed ratio between mean self-regulation (intrataxon interaction
 146 strength) and mean intertaxa interaction strength to other published studies based on a MAR(1)
 147 model. A list of references is given in Table S4. Authors usually reported only coefficients that were
 148 significant at the 95% significance threshold, thus ignoring potentially many weak effects, which we
 149 had to set to 0. There are therefore two ways of computing the mean intertaxa interactions, i.e.,
 150 taking the mean value of all coefficients outside of the matrix diagonal, including zeroes (which
 151 decreases the estimated mean intertaxa interaction strength, Fig. 4), or taking the mean value of
 152 statistically significant intertaxa coefficients only (which increases the estimated mean intertaxa
 153 interaction strength, Fig. S9). We considered both.

154 Results

155 Interaction estimates

156 Using MAR(1) autoregressive models, we produced interaction matrices (Ives *et al.*, 2003; Hampton
 157 *et al.*, 2013) – i.e., Jacobian community matrices on the logarithmic abundance scale (Ives *et al.*,
 158 2003). Best-fitting models corresponded to a phylogenetically-structured interaction scenario, where

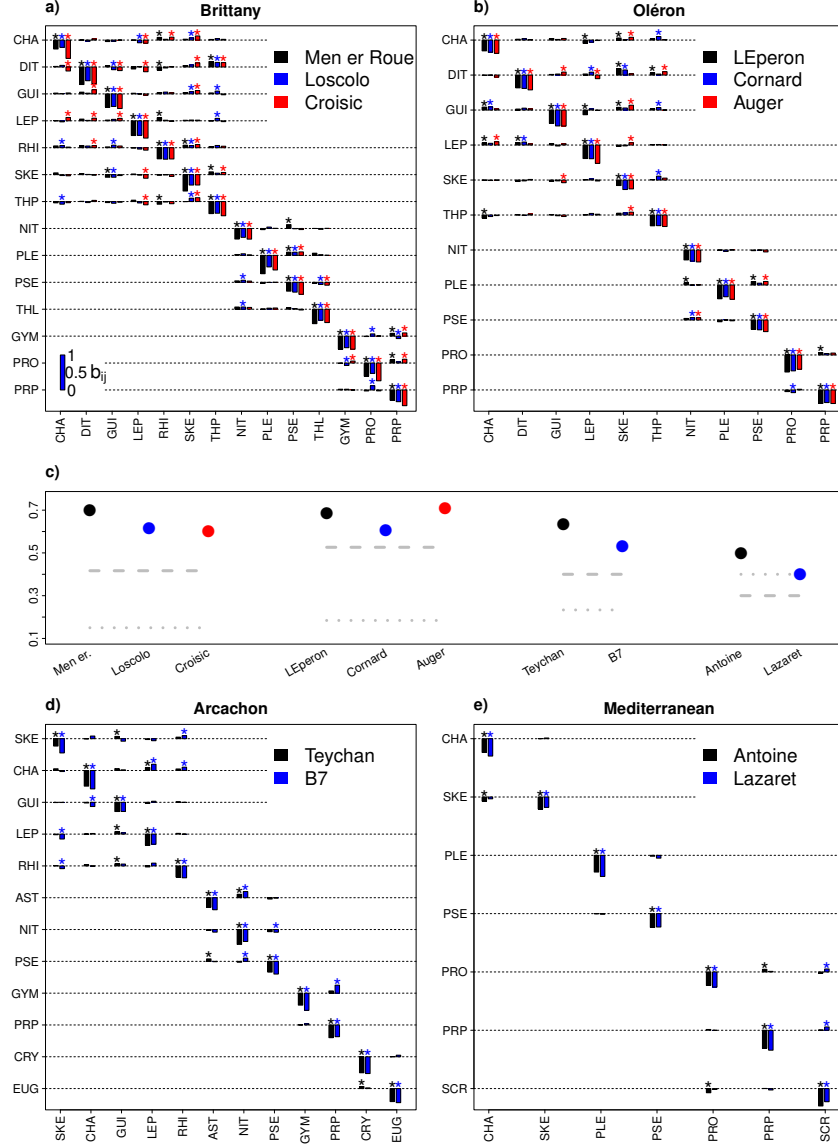


Figure 1: **Interaction matrices estimated in 10 sites along the French coastline.** The most parsimonious interaction scenario is presented. Taxon j (in columns) has an effect on taxon i 's growth rate (in rows) proportional to the bar height, which corresponds to the $\mathbf{B} - \mathbf{I}$ matrix (community composition in Table S2). The scale for the coefficient values is given at the bottom left of panel a). 95% significance of coefficients is marked by asterisks (*). The fraction of positive interactions in each matrix is given by points in c) while the dashed (resp., dotted) line represents the ratio of interactions remaining positive (resp., negative) for all sites of a given region.

interactions only occurred between closely related genera (Fig. S3). This led to sparse, modular matrices that have two main features. First, we observed a strong self-regulation for all sites (Fig. 1, diagonal elements of all matrices), a feature that we had previously highlighted in a more detailed analysis on one of the considered study regions (Barraquand *et al.*, 2018). The ratio of mean intragenus to intergenus interaction coefficients varied between 6 and 10, not counting coefficients set to 0 in the estimation process. When we included the zeroes in the interaction matrix in the computation of the intra/inter mean interaction strength, the ratio rose to 21-43. Therefore, intragenus interactions were on average one order of magnitude stronger than intergenus interactions.

Second, although the percentage of facilitative interactions varied among sites (between 40% and 71% of interactions in the selected models), facilitation remained predominant in 9 sites out of 10 (only Lazaret, in the Mediterranean Sea, has 60% negative interactions). Our observational setup being nested, with sites within regions, we could examine whether locally positive interactions remain positive in a regional context: the percentage of consistently positive interactions at the regional level varied between 30% and 53%, higher than the percentage of similarly defined negative interactions (between 15% and 40%), except for sites in the Mediterranean Sea.

We found that the percentage of true mutualism (+/+) was substantial: averaged over all sites, 32% of all interactions were (+/+) while only 12% of them were (-/-), see also Fig. S5. The sign correspondence was not always maintained between regions: the only interaction that was non-zero in the 10 sites (CHA/SKE) was mutualistic in Men er Roue only (Brittany) and mixed (+/-) in all other sites. Within the same region, however, interactions measured in different sites tended to keep the same sign. In the 3 sites of Oléron, for instance, there were 4 interactions which remained positive for both taxa involved (CHA/GUI, DIT/GUI, LEP/THP, SKE/THP), 3 of them being also mutualistic in some of the Brittany sites. This contradicts previous observations that mutualistic interactions tend to be more context-dependent than competitive interactions (Chamberlain *et al.*, 2014).

Interaction network analysis

The stability (*sensu* resilience, Ives & Carpenter 2007) of all interaction matrices was not strongly affected by the percentage of positive interactions or the mean and variance of the intergenus interactions (Fig. 2). There was a slight increase in stability with weighted connectance, with a drop in eigenvalue modulus for weighted connectances between 0.09 and 0.1. The maximum modulus of the interaction matrix eigenvalues remained between 0.65 and 0.80.

Given that a direct complexity-stability (*sensu* resilience) link was not obvious, we investigated whether the matrix coefficients had some particular structure that could help theoretical ecology to make better null models of joint community dynamics and interactions (James *et al.*, 2015). We defined two scores, vulnerability (summed effect of others on the focal taxon growth rate, eq. S5) and impact (summed effect of the focal taxon onto other taxa's growth rates, eq. S6). Relations between inter- and intra-genus interactions emerged (Fig. 3): genera that were more self-regulating also had also a higher vulnerability score and a lower impact score. Those two influences are likely to trade-off: a high degree of self-regulation somehow buffers the effect of outside influences on population dynamics. Taxa that were less self-regulating were also more likely to have a stronger effect onto other taxa. As these genera tended to be more abundant (Fig. S7), this could be mediated by the average density of a genus. It is important to note, however, that these trends are weak and there is therefore a considerable amount of randomness dominating the interaction matrix: many scenarios of self-regulation vs limitation by others are therefore possible.

Aside from the trade-offs of Fig. 3, we found no remarkable patterns of covariation between matrix elements (Fig. S5) other than a mean-variance scaling of interaction coefficients (Fig. S6).

Literature comparison

Finally, we sought to put these results in a broader context by compiling the intra vs inter group estimates of previous MAR(1) studies of long-term observational count data (listed in Table S4). We found that the order of magnitude of intra/inter interaction strengths considered here is not particularly above those found for most planktonic systems to which MAR(1) models have been

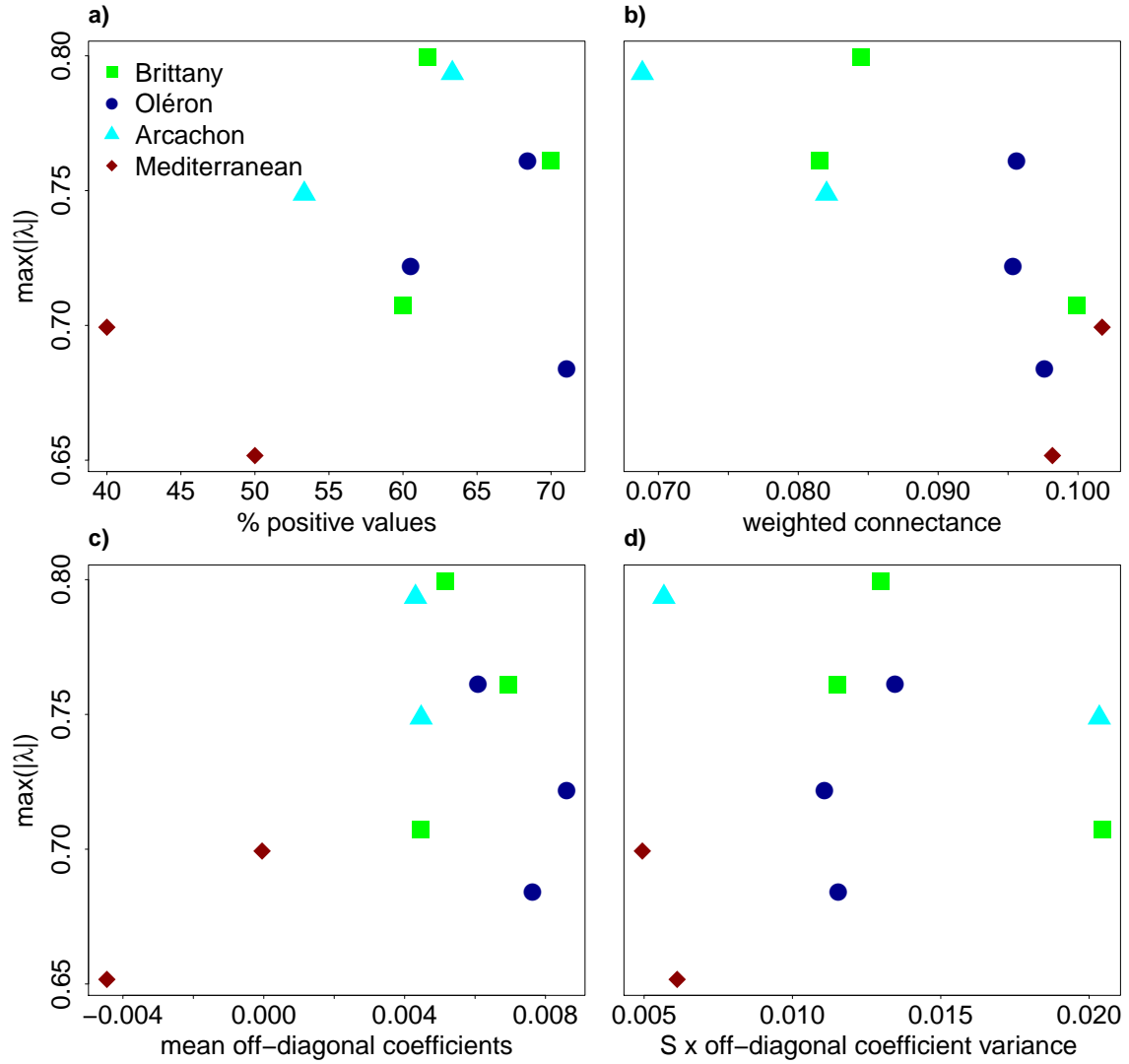


Figure 2: **Relation between stability and complexity of the interaction networks.** The maximum modulus of the eigenvalues of the interaction matrix \mathbf{B} indicates stability *sensu* resilience. Off-diagonal coefficient variance is multiplied by the dimension of the network, that is the number of species in the region. Each color or shape corresponds to a given region. The formula for weighted connectance is given in the Supporting Information.

210 fitted, considering that our systems are relatively high-dimensional and that the higher the number
 211 of taxa, the larger the intraspecific regulation (Barabás *et al.*, 2017). We included in Fig. 4 not only



Figure 3: **Relation between vulnerability/impact and self-regulation.** Average vulnerability (effects of others on the focal taxon growth rate, a-b) and impact (effects of the focal taxon on others' growth rates, c-d), as well as self-regulation, are computed for untransformed (a-c) or absolute (b-d) values of the coefficients of the interaction matrix ($\mathbf{B} - \mathbf{I}$) for the 10 study sites. Each color corresponds to a given region (Fig S1). Linear regressions are shown as black lines.

212 plankton studies but also a couple of vertebrate or insect studies on less diverse communities, where
 213 interactions are stronger, in order to provide lower bounds for the intra/inter ratio. The conclusion

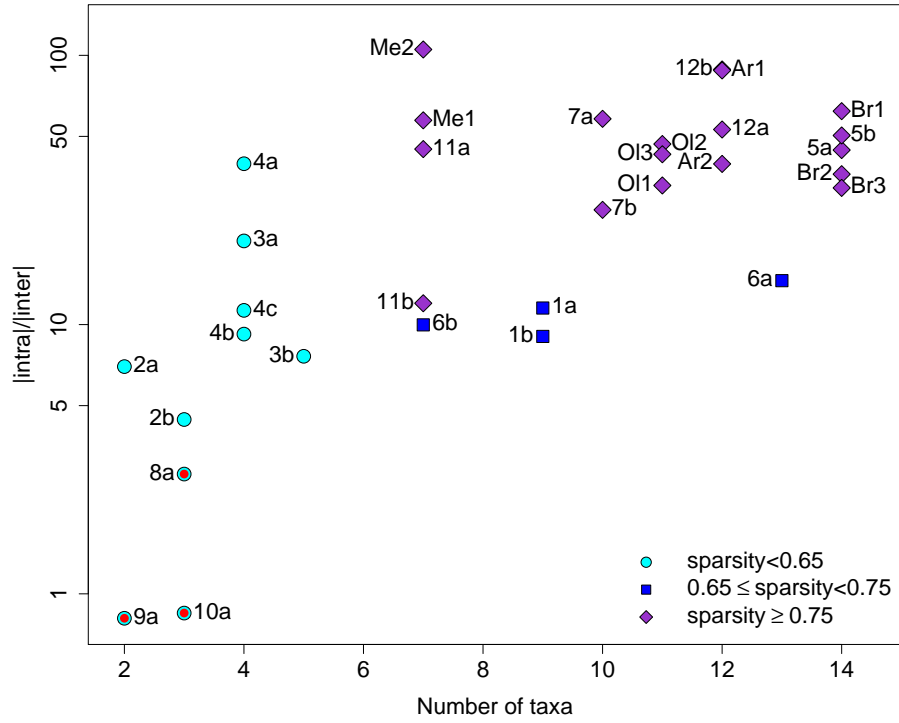


Figure 4: **Ratio of intra- to inter-group interaction strength in Multivariate AutoRegressive (MAR) models.** The reference for each study is given in Table S4. Codes beginning with letters correspond to the present study (Ar: Arcachon; Ol: Oléron; Br: Brittany; Me: Mediterranean Sea). The symbol color and shape correspond to the sparsity of the interaction matrix (e.g., the proportion of null interactions in the matrix). Red dots correspond to terrestrial and/or low dimension predator-prey systems, giving a lower bound for the intra/inter ratio. Intergroup interactions were set to 0 when they were not specified in the articles (in most cases, authors removed non-significant interactions at the 95% threshold; Fig. S9 is the same figure taking into account only significant interactions)

from this comparison seems to be that, unlike small communities that can be tight-knit, any diverse field system of competitors and facilitators has evolved large niche differences making intragroup competition much larger in magnitude than intergroup interactions.

Discussion

Strong self-regulation and facilitation

We found very large niche differences between genera, translating into much higher intragenus than intergenus effects on growth rates (i.e., strong self-regulation), together with a high degree of facilitative net interactions.

The intra/intertaxa interaction strength ratio (Levine & HilleRisLambers, 2009) that we found, from 6–10 to above 20, depending on whether one includes interactions set to zero in the estimation process, could appear very high in light of previous intra/interspecific competition strength estimates of 4 to 5 by Adler *et al.* (2018b). Additional estimates using the unconstrained interaction matrix yielded ratios between 8 and 11 depending on the site (Table S3 and Fig. S8 in the Supporting Information), but weak interspecific effects are likely to be inflated in the full model. Therefore, a intra/inter ratio of 10 seems like a conservative estimate, twice that of Adler *et al.* (2018b). Even though their model is a different one, i.e., Lotka-Volterra competition, we prove in the Supporting Information that the intra/inter ratio should remain commensurate in a MAR(1) model. The difference in the intra/inter ratio that we found should therefore lie elsewhere, which requires some explanation. One could argue that such high intra/inter ratio arises because we consider the genus as our baseline taxonomic unit, rather than the species. It is logical that niche differentiation increases as one gets up the phylogenetic tree, and that getting down to the species level could slightly decrease that ratio (but see Narwani *et al.*, 2017, in which phylogenetic closeness decreases competition strength). However, there are two arguments suggesting that the niche differences found here extend to the species level. First, phytoplankton species belonging to different genera are often found to compete in experiments (Titman, 1976; Tilman *et al.*, 1982; Descamps-Julien & Gonzalez, 2005). In the field-based dataset studied here, the same genera that are considered in experiments are found not to compete (or only weakly), hence there must be some niche differentiation occurring in the field but not in the lab. Second, the only other study that managed to provide MAR(1) estimates down to the species level for phytoplankton, that of Huber & Gaedke (2006), provides an intra/interspecific strength ratio similar to ours (point 7a in Fig. 4). Strong self-regulation seems

therefore a genuine feature of field phytoplanktonic communities.

Another main finding of our study is the large frequency of positive interactions, with 30% truly mutualistic (+/+) interactions and between 40 and 70% facilitative effects. Although a seasonal environment can generate some positive covariation between taxa, those effects have already been filtered out by the inclusion of our 2 abiotic covariates (Fig. S4). The facilitative effects shown here are therefore residual effects, once abiotic trends are accounted for. Between 40 and 70% facilitation can be compared to the meta-analysis by [Adler *et al.* \(2018b\)](#) who also found facilitative interactions, but less than here ($\approx 30\%$). However, [Adler *et al.* \(2018b\)](#)'s review contains many experiments while the plant literature is replete with field examples of facilitation ([Brooker *et al.*, 2008](#); [McIntire & Fajardo, 2014](#)), so that plant facilitation could be higher in the field. At the moment, it is therefore unknown how the predominance of facilitative interactions that we found in phytoplankton compares to facilitation in terrestrial plants. We note that several authors using MAR(1) models previously forbade positive interactions within the same trophic level, so that the fraction of facilitative interactions in plankton cannot be computed from literature-derived MAR(1) estimates.

The large niche differences and facilitative interactions that arise when considering a single trophic level are an emergent property, resulting from hidden effects of resource or predator partitioning/sharing ([Chesson, 2018](#)). In our previous publication investigating in detail the Arcachon study sites ([Barraquand *et al.*, 2018](#)), we have argued that for phytoplankton, the strong intragroup density-dependence could arise from effects of natural enemies ([Haydon, 1994](#)). Natural enemies could also very well create apparent mutualism between prey species ([Abrams *et al.*, 1998](#); [de Ruiter & Gaedke, 2017](#)). We believe this to be likely for the present study, given that the study regions (Arcachon, Oléron, Brittany, Mediterranean) have similar predators (zooplankton, e.g., [Jamet *et al.*, 2001](#); [Modéran *et al.*, 2010](#); [Tortajada *et al.*, 2012](#)) and parasites (viruses, e.g., [Ory *et al.*, 2010](#); fungi). Though natural enemies are good candidates to explain the observed niche differences and emerging facilitation, one must bear in mind that other known drivers of phytoplankton dynamics such as allelopathy ([Felpeto *et al.*, 2018](#)), auxotrophy ([Tang *et al.*, 2010](#)) or hydrodynamics ([Lévy *et al.*, 2018](#)) can all, in theory, help create different niches and an emerging facilitation (see last

subsection of the Discussion). Finally, resources that are usually considered limiting for all species might in fact not always be: [Burson *et al.* \(2018\)](#) show that phytoplanktonic taxa specialize on different components of the light spectrum. This constitutes an example of fine-scale resource partitioning of one resource, light, that all species and genera are usually thought to compete for.

No complexity-stability relationship but connections between self-regulation and intergroup interactions

There was no relation between the complexity of the communities (measured as either the weighted connectance or the interaction coefficient variance) and their stability (measured by the largest modulus of the eigenvalues, which quantifies the return time to a point equilibrium, i.e., resilience). This result is conditional upon our model being a good approximate description of the system (i.e., no multiyear limit cycles or chaotic attractors as the mapping between eigenvalues and actual stability is distorted in that case, [Certain *et al.*, 2018](#)). However, we already showed on a subset of this data that a fixed point in a MAR(1) model, perturbed by seasonality and abiotic variables, is an accurate description of the system ([Barraquand *et al.*, 2018](#)). Therefore, we are confident that the absence of complexity-resilience relationship found here is not a mere artefact of an inadequate model. This absence of direct link between complexity and stability could be an actual feature of empirical systems, as shown previously by [Jacquet *et al.* \(2016\)](#) using a different technique. This result seems to contradict theory based on random matrices, especially for competitive and/or mutualistic networks ([Allesina & Tang, 2012](#)). However, one must bear in mind that such result could also be generated by the limited size of our networks, as random matrix theory relies on asymptotics ([Allesina & Tang, 2015](#)). We should also mention that our interaction matrices (discrete-time model) are not strictly analogous to the ones used most frequently in theoretical ecology (continuous-time model), though the spectral radius (largest modulus) can be tightly related to the real part of the lead eigenvalue. Thus the jury is still out regarding the absence of complexity-resilience relation found here, though it may well be a genuine absence. In addition to complexity metrics, we also found that the percentage of mutualistic interactions, that is thought to affect the stability of a network, either positively or negatively ([Mougi & Kondoh, 2012](#); [Coyte *et al.*, 2015](#); [García-Callejas](#)

299 *et al.*, 2018), does not in fact have a major impact on our networks' resilience.

300 In addition to weighted connectance and interaction variance, indices at the genus level (vulnera-
301 bility and impact) approximate the average effects exerted and sustained by any given taxa in the
302 different study sites. While, at the network level, network structure (either complexity measures
303 or the percentage of mutualistic interactions) did not affect resilience, a relation emerged between
304 self-regulation, necessary for coexistence, and genus-level indices. We found that the more a genus is
305 self-regulated, the more it tends to be vulnerable to other genera's impacts and the less it impacts
306 other genera. We examined whether vulnerability and impact could be affected by phylogenetic
307 correlations; they were not, as on Fig. 3, points were not clustered according to genus, family or
308 phylum. High self-regulation usually indicates large niche differences with the rest of the community,
309 and it makes therefore sense that a species/genus whose needs strongly differ from the others only
310 marginally impacts the resources of the other coexisting species. This is what we expect under strong
311 niche partitioning. A low self-regulation was also correlated with high average abundance, which
312 echoes findings by Yenni *et al.* (2017) who demonstrated that rare species usually show stronger
313 self-regulation. This correlation between relative rarity and self-regulation could explain the lesser
314 impact of highly self-regulated species/genus: a taxon which dominates the community composition
315 can have a major effect on the others, especially as they usually cover more space, while it is harder
316 for the less common taxa to have large impacts. In contrast, it was more difficult to explain the
317 relationship between self-regulation and vulnerability: a genus that is more self-regulated and less
318 common was found here to be on average more vulnerable to other genera's increases in densities.
319 Such relation implies greater stability (*sensu* resilience, Ives *et al.* 2003, and also invariability,
320 Arnoldi *et al.* 2019) for the network as a whole, because the taxa that are the more vulnerable
321 to other taxa's impacts are also those whose dynamics are intrinsically more buffered. By which
322 mechanisms this could happen is so far unclear and open to speculation. It could just be a "mass
323 effect": common taxa are in high enough numbers to deplete resources or change the environment in
324 ways that affects the less common ones, but the reverse is not true. As a final note on relationships
325 between interaction matrix coefficients, we caution that the trends evidenced are all relatively weak:
326 considerable stochasticity still dominates the distribution of interaction matrix coefficients.

Ghosts of competition past and present

Overall, the dominance of niche differentiation in observational plankton studies – based on our analysis of the REPHY dataset and re-analysis of the MAR(1) literature – is similar to what has been recently found in plant community studies (Volkov *et al.*, 2007; Adler *et al.*, 2018b) or empirically parameterized food webs including horizontal diversity (Barabás *et al.*, 2017). Large niche differences might be due to the ghost of competition past, i.e., competition has occurred in the past, leading to strong selection and subsequent evolution, and then to progressive niche separation. In this scenario, species have evolved niches that allow them not to compete or to interact only weakly (very strong facilitative effects might be likewise destabilizing, Coyte *et al.*, 2015). The likely predator effects that we highlighted above could be comprised within such niche differentiation *sensu largo*: specialized predators can make strong conspecific density-dependence emerge (Bagchi *et al.*, 2014; Comita *et al.*, 2014), while switching generalists can also promote diversity (Vallina *et al.*, 2014). Both predators and resources have often symmetrical effects and can therefore contribute almost equally to such past niche differentiation (Chesson, 2018).

An intriguing new possibility, dubbed the “ghost of competition present” (Tuck *et al.*, 2018), suggests by contrast that spatial distributions in relation to abiotic factors might have a large impact on the interaction strengths inferred from temporal interaction models such as ours. Recent combinations of model fitting and removal experiments have shown that model fitting usually underestimates the effect of competitors that are uncovered by removal experiments (Tuck *et al.*, 2018; Adler *et al.*, 2018a). This could occur for instance if species are spatially segregated (at a small scale) because each species only exists within a domain where it is relatively competitive (Pacala’s spatial segregation hypothesis, Pacala & Levin 1997), while a focal species could spread out if competitors were removed. This means that a species can be limited by competitors, but act so as to minimize competition (a little like avoidance behaviour in animals) and maximize opportunities for positive interactions, which implies that competition is in effect hard to detect when all species are present. This mechanism would require spatial segregation between phytoplankton species at the scale of interactions, i.e., at the microscale. At the moment, it is known that the fine-

scale hydrodynamics generate inhomogeneities at the microscale (Barton *et al.*, 2014; Breier *et al.*, 2018) but it is quite unclear how microscale hydrodynamics affects multivariate spatial patterns of species distributions (*sensu* Bolker & Pacala 1999, or Murrell & Law 2003). Moreover, even if microscale hydrodynamics generates spatial structure with segregation between species, the “ghost of competition present” mechanism might not work for phytoplankton as in terrestrial plants, because turbulence rather than active organism movement dictates where the phytoplankton patches can or cannot appear.

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Supporting Information

This article contains supporting information.

Authors’ contributions

CP and FB contributed equally to the project design. CP wrote the code for the analyses. FB and CP interpreted the results and wrote the manuscript.

Data accessibility

The REPHY dataset has already been published (REPHY, 2017) and all scripts for MAR and subsequent network analyses are available online in a GitHub repository (<https://github.com/CoraliePicoche/REPHY-littoral>). This repository will be made public upon acceptance and codes can be shared with referees should they wish to access them.

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