- Stabilizing niche differences are still required to maintain
- species-rich communities in temporally variable

environments

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8 Abstract

Explaining coexistence in species-rich communities of primary producers (e.g., tropical trees, phytoplankton) remains a challenge for ecologists because of the likely competition for shared basal resources. Following Hutchinson's seminal suggestion, many theoreticians have tried to create diversity through a fluctuating environment, which impairs or slows down competitive exclusion. There are now several fluctuating-environments models that allow coexistence, but they often produce only a dozen of coexisting species at best. Here, we investigate what it would take to create even richer communities in fluctuating environments using an empirically parameterized model. Building on the forced multi-species Lotka-Volterra model of Scranton and Vasseur (2016), we have investigated the effect of two coexistence mechanisms, namely the storage effect and stabilizing niche differences (SNDs). SNDs occur when intraspecific competition is stronger than interspecific (as opposed to neutral models where competition is symmetric), and we tuned the competition ratio based on empirical phytoplankton data. Although SNDs maintained more species than the storage effect (50 % w.r.t 25%), we show that none of the two coexistence mechanisms considered could, by itself, ensure the

coexistence of all species present at the beginning of our simulations. Realistic seasonal environments only aggravated that picture, as they decreased persistence relative to white noise. Our results suggest that combining different mechanisms for biodiversity maintenance into community models might be more fruitful than trying to find which explains best the observed diversity levels. Our results on community composition (formation of clumps, biomass distribution) in the different scenarios give further hints on how to empirically weight the influence of coexistence mechanisms.

1 Introduction

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There has been a rich debate in theoretical ecology on how to reconcile niche and neutral perspectives on species coexistence (Gravel et al, 2006; Carmel et al, 2017). Under the neutral perspective, all species have equal birth and death rates and compete equally (for space) whilst under the niche perspective, birth and death rates can vary between species and various mechanisms contribute to increasing intraspecific over interspecific competition (Hubbell, 2001). But as it has been pointed out repeatedly, niche and neutral processes are not mutually exclusive, and may actually act together to produce observed species coexistence (Gravel et al, 2006; Mutshinda et al, 2009; Götzenberger et al, 2012).

For instance, Scheffer and van Nes (2006) put forward the concept of 'clumpy coexistence', whereby 36 niche and neutral community assembly may be simultaneously at work, creating several clumps of similar 37 species along a single trait axis. Classical stabilizing niche differences enable coexistence of multiple clumps through stronger net intraspecific competition (Chesson, 2000), while within-clump coexistence occurs through neutral processes (Hubbell, 2001; Munoz and Huneman, 2016), as species that differ too little in their fitnesses cannot exclude themselves out on reasonable timeframes. Indeed, clumps on the trait axis eventually thin out in absence of immigration, but transient coexistence can last for extended 42 periods of time. This 'emergent neutrality' within groups (Holt, 2006) has been proposed as a unifying concept for the niche and neutral theories. However, the findings of Scheffer and van Nes (2006) have been disputed due to hidden niches in the original model (Barabás et al, 2013). Hidden niches emerge 45 through stronger intraspecific competition mediated by a an additional intraspecific predation-like term 46 (Barabás et al, 2013). This makes coexistence in the Scheffer and van Nes model more similar to that of the classical Lotka-Volterra model (Barabás et al, 2016), so that coexistence within clumps is not exactly

49 neutral.

Still, the idea that niche and neutral assembly can mould communities stays potent (Vergnon et al, 2013). Since then, several studies have suggested that 'clumpy coexistence' can occur in theoretical models, most notably models incorporating temporal variation (Scranton and Vasseur, 2016; Sakavara et al, 2018). In these temporal-variation models, equal competitive strengths are combined with other mechanisms like the storage effect that increase the possibility of coexistence by making the interaction strength covary with a fluctuating environment (see also Barabás et al, 2012).

Here, we build on the work of Scranton and Vasseur (2016) to investigate the possibility of coex-56 istence through species response to fluctuating environments (the so-called storage effect or temporal 57 niche partitioning, that are equivalent concepts for forced Lotka-Volterra models, Barabás et al, 2012; Scranton and Vasseur, 2016). Our enthusiasm for the Scranton and Vasseur (2016) model stems from our interest in phytoplankton communities, that were the key inspiration for the thermal preferences curves modelling intrinsic growth rates in Scranton and Vasseur (2016). However, Scranton and Vasseur (2016) described temperature as a white noise, i.e. independent and identically distributed Gaussian random variates over time. This appeared to us as a key assumption to relax. Under most latitudes, tempera-63 ture is indeed a seasonal signal, and seasonal forcing can strongly affect the dynamics of the community considered (Vesipa and Ridolfi, 2017). Over short timescales, random temporal variation therefore often 65 only add noise to a largely deterministic seasonal trend. Our present work can therefore be seen as an 66 attempt to blend Scranton and Vasseur (2016)'s framework with the periodic environments of Barabás 67 et al (2012), to better represent the mixture of stochastic and deterministic environmental forces affecting 68 phytoplankton community dynamics. 69

Because many phytoplankton species or genera respond in similar ways to temperature despite having different optimas (Moisan et al, 2002), we hypothetized that a large seasonal variation might not
necessarily foster species coexistence. In fact, similar responses to seasonal fluctuations should lead to
an increased synchrony of species abundances which, in turn, should theoretically mitigate the expected
temporal partitioning. How seasonality affects coexistence (as opposed to a purely randomly fluctuating
environment) is therefore a key feature of this paper. In particular, we contrast cases where the storage
effect is present vs. absent, which conveniently maps to two different parameterizations of the forced

Lotka-Volterra model. Moreover, we realized while running Scranton and Vasseur (2016)'s model that
the overall diversity obtained after 5000 years was relatively low compared to what we usually observe in
phytoplankton communities (several dozens to hundreds of species). We have therefore sought out which
mechanisms to add to attain a truly species-rich community for extended periods of time.

In an empirical study combining phytoplankton community-level time series and multivariate au-81 toregressive models Barraquand et al, 2017, we found that despite a large influence of the environment 82 (including temperature, irradiance, and other factors), intraspecific (or intragenus) competition was rather 83 large and most likely the key driver of species coexistence. In other words, stabilizing niche differences 84 had a large role to play in maintaining species diversity in coastal phytoplankton (Barraquand et al, 2017) 85 Here, we therefore try to establish what are the relative contributions of the storage effect vs intraspe-86 cific density-dependence to coexistence in a phytoplankton-like theoretical community model. This led 87 us to cross different combinations of seasonality in the forcing signal, presence of the storage effect or 88 not, and intra- vs interspecific competition, in order to disentangle the contributions of all these factors to biodiversity maintenance.

91 2 Methods

92 Models description

The model described in Scranton and Vasseur (2016) is based on a variant of the Lotka-Volterra competition model. Fluctuations in the environment are introduced in the model by temperature-dependent intrinsic growth rates (see eq. 1-2, all coefficients are defined in Tab. 1) so that species growth rates can be expressed as:

$$\frac{dN_{i}}{dt} = r_{i}(\tau)N_{i}\left(1 - \sum_{j=1}^{S} \alpha_{ij}N_{j}\right) - mN_{i}$$

$$r_{i}(\tau) = a_{r}(\tau_{0})e^{E_{r}\frac{(\tau-\tau_{0})}{k\tau\tau_{0}}}f_{i}(\tau)$$

$$\begin{cases} e^{-|\tau-\tau_{i}^{opt}|^{3}/b_{i}}, & \tau \leq \tau_{i}^{opt} \\ e^{-5|\tau-\tau_{i}^{opt}|^{3}/b_{i}}, & \tau > \tau_{i}^{opt} \end{cases}$$
and b_{i} defined by numerically solving
$$\int r_{i}(\tau)d\tau = A$$

$$(4)$$

Model parameters are detailed in Table 1, and we set their values to match the features of phytoplankton communities as in Scranton and Vasseur's work (2016). The niche of each species is defined by its thermal optimum τ_i^{opt} . Thermal performance curves defined in eq. 3 are parameterized so that all species share the same niche area (eq. 4), which sets a trade-off between maximum growth rates and niche width.

Table 1: Parameter definition and values of the model described in eq. 1-4

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Name	Definition	Value (unit)					
S	Number of species	60					
N_i	Biomass density of the <i>i</i> th species	(kg/area)					
au	Temperature	K					
$r_i(au)$	Growth rate of species i as a function of temperature	kg kg*year					
$lpha_{ij}$	Strength of competition of species j on species i	0.001 area/kg					
b_i	Normalization of the thermal decay rate						
m	Mortality rate	$15\frac{\mathrm{kg}}{\mathrm{kg*year}}$					
$ au_0$	Reference temperature	293 K					
$a_r(\tau_0)$	Growth rate at reference temperature	$386 \frac{\text{kg}}{\text{kg*year}}$					
E_r	Activation energy	0.467 eV					
k	Boltzmann's constant	$8.6173324.10^{-5} \text{eV.K}^{-1}$					
$f_i(au)$	Fraction of the maximum rate achieved for the <i>i</i> th species						
$\mu_{ au}$	Mean temperature	293 K					
$\sigma_{ au}$	Standard deviation for temperature	5 K					
$ au_{ m min}$	Minimum thermal optimum	288K					
$ au_{ m max}$	Maximum thermal optimum	298 K					
A	Niche breadth	$10^{3.1} \frac{\text{kg}}{\text{kg*year}}$					
$ au_i^{ ext{opt}}$	Thermal optimum for growth of the ith species	K					
θ	Scaling between white noise to seasonal signal	$[0,\sqrt(2)]$					
ρ	Ratio of intra-to-intergroup competition strengths	(1;10)					

We kept the mean and standard deviation of the forcing signal but included a lower-frequency component using a sinusoidal function with a period of 365 days (1 time unit being one day, eq.5). We tune the ratio of low-to-high frequency with the variable θ so as to keep the same energy content - equal total variance - in the forcing signal.

$$\tau(t) = \mu_{\tau} + \theta \sigma_{\tau} \sin\left(\frac{2\pi t}{365}\right) + \varepsilon_{t}, \text{ where } \varepsilon_{t} \sim \mathcal{N}(0, \sigma_{\tau} \sqrt{1 - \frac{\theta^{2}}{2}})$$
 (5)

Note that the upper limit for θ , $\sqrt{2}$, corresponds to a completely determinist model which we do not explore here (but see Zhao, 1991 proving bounded coexistence). We chose to keep the stochasticity in the signal and to model a plausible temperature signal with $\theta = 1.3$ with temperature ranging from ## to ## over one year (see Fig. 1b, Moisan et al, 2002) when considering a seasonal forcing of the dynamics.

The formulation of the forced Lotka-Volterra model of Scranton and Vasseur (2016) implies a storage effect, as the competition strengths covary positively with the growth rate value $r_i(\tau)$ (Ellner et al, 2016). To test for the effect of an explicit storage effect in the model, we formulated a new version of this model, where we removed this assumption by using the mean value of a species' growth rate ($\bar{r_i}$) to weight the interaction coefficients.

$$\frac{dN_i}{dt} = N_i \left(r_i(\tau) - \sum_{j=1}^{S} \bar{r}_i \alpha_{ij} N_j \right) - mN_i \tag{6}$$

In this way, competition strengths remain unaffected by the environmental conditions, in contrast to growth rates (eq. 6), while preserving the same average magnitude as in eq. 1.

Stabilizing niche differences are ensured by the addition of the coefficient ρ , which is the ratio of intra-to-intergroup competition strength. We can therefore re-write the interaction coefficients α_{ij} in eq. 7

$$\alpha_{ij} = \alpha \left(1 + (\rho - 1)\delta_{ij} \right) \tag{7}$$

where δ_{ij} is the Kronecker symbol, equal to 1 if i=j and to 0 otherwise. The value of the parameter $\rho=10$ was chosen from analyses of phytoplanktonic data (Barraquand et al, 2017).

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In addition to two types of environmental forcings (white noise with $\theta = 0$, and seasonal forcing

with $\theta = 1.3$), we therefore compare the results for four formulations of the model: with and without 122 an explicit storage effect (eq. 1 and eq. 6, respectively); with and without stabilizing niche differences 123 $(\rho = 10 \text{ or } \rho = 1, \text{ respectively})$. These are summed up in Table 2. 124

$\frac{dN_i}{dt} + mN_i$	Storage effect	No storage effect	
Stabilizing niche differences	$r_i(\tau)N_i\left(1-\sum_{j=1}^S\alpha\left(1+9\delta_{ij}\right)N_j\right)$	$N_i \left(r_i(\tau) - \sum_{j=1}^{S} \bar{r}_i \alpha \left(1 + 9 \delta_{ij} \right) N_j \right)$	
No stabilizing niche differences	$r_i(\tau)N_i\left(1-\sum_{j=1}^S\alpha N_j\right)$	$N_i \left(r_i(\tau) - \sum_{j=1}^S \bar{r}_i \alpha N_j \right)$	

Table 2: Growth rate of species i in the four formulations of the model we present

Set-up

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We replicate the 'Species sorting' experiment of Scranton and Vasseur (2016) so as to investigate on 127 how synthetic phytoplankton communities structure under the various scenarios we described above. We focused on the dynamics of a community initialized with 60 species with thermal optima uniformly 129 spaced along the interval [15°C, 25°C], and with the same initial density $(\frac{1}{\alpha S})$. Each simulation was run 130 for 5000 years in 1-day intervals. When the density of a species dropped below 10^{-6} , it was considered 131 extinct. For each combination of the parameters of the model (type of environmental signal, storage 132 effect and stabilizing niche differences), we ran 100 simulations. 133

with an absolute error tolerance of 10^{-8} , and relative error tolerance 10^{-3} .

All simulations were ran with Matlab's ode45 algorithm, an explicit Runge-Kutta (4,5) algorithm

Results 3

Typical dynamics of the community following Eq. 1 (the model of Scranton and Vasseur, 2016), with both the environmental signals described in Eq. 1 (original choice of Scranton and Vasseur, 2016) and 138 5 (our variant), are shown in Fig. 1. Forcing by a sinusoidal signal produces the strongly seasonally 139 structured dynamics that are typical of phytoplankton. Even though only 5 species can be seen in Fig. 140 1c), there were 14 species still present at the end of the simulation forced by a white noise, with large

disparities in the range of variation of their biomasses. A third of the species kept a biomass above 10 142 kg/area while 6 out of the 14 remained below the unit. All species in the white noise simulations were 143 clustered along a 3.2°C-range of thermal optima (Fig. 5). No obvious temporal patterns (e.g., cycles) 144 could be seen in the communities forced by white noise. On the other hand, seasonal cycles were clear 145 in the seasonally-forced case of Fig. 1 d). Only 4 species coexisted at the end of the simulation with 146 seasonal forcing, gathered in two groups with large thermal optimum differences (5.7°C between the 147 maximum thermal optimum of the first group and the minimum thermal optimum of the second group). 148 When temperatures are high, the group with a higher thermal optima reach maximum biomass, then as 149 temperature decreases through the season, they leave room for the growth of the low-temperature group. 150

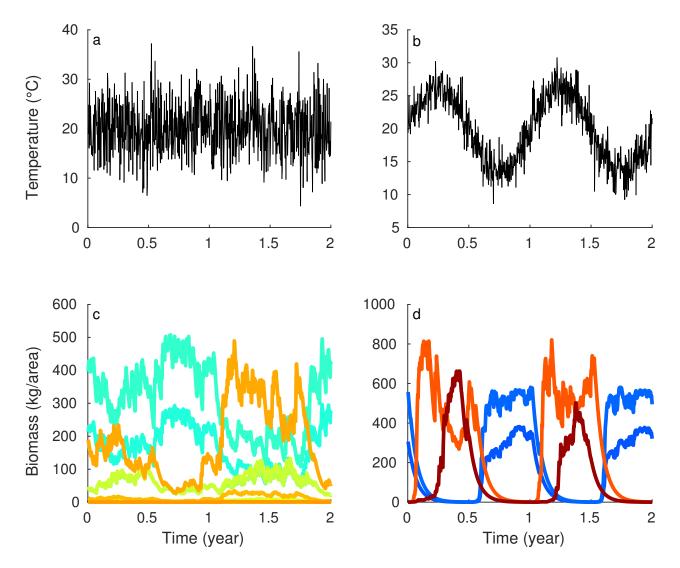


Figure 1: Times series of temperature (top) and extant species (bottom) for the 2 last years of a 5000 year simulation, with storage effect and no stabilizing niche differences. The forcing temperature is either a white noise (left) or a noisy seasonal signal (right). Line colors of species biomasses correspond to their thermal optima (from blue, corresponding to low thermal optima, to red, corresponding to high thermal optima. The whole range of the biomass distribution is shown on Fig. 3).

The decrease in persistence due to seasonality observed in Fig. 1 was confirmed in all our simulations (Fig. 2). In cases where final species richness varied from one simulation to another (namely, the two middle cases in Fig. 2): with storage effect but without stabilizing niche differences, or without storage effect but with stabilizing niche differences), seasonality reduced the number of extant species to, on average, 27% and 48% of its original value, respectively (Fig. 2). A seasonal signal therefore led to a much smaller average persistence. There was also less variance in persistence between seasonally forced simulations when compared to white noise simulations.

Both the stabilizing niche differences and the storage effect have a marked effect on increasing persistence. Without any of these coexistence mechanisms, only one species persisted at the end of the simulations. When only the storage effect was present, the number of extant species varied between 8 and 20 with a white noise, or 2 and 6 with a seasonal signal. On the other hand, when only stabilizing niche differences were present, the number of extant species nearly doubled, varying between 20 and 32, or 12 and 15, with a white noise or a seasonal signal respectively. Remarkably, when the storage effect and stabilizing niche differences (SNDs) both affected the community dynamics, all species persisted in the community, while neither the storage nor SNDs were able to produce that result alone, for both white noise and seasonal forcing.

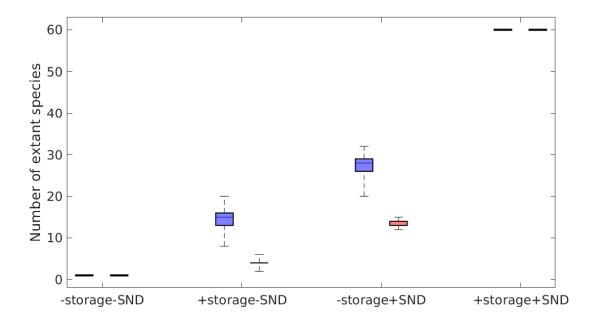


Figure 2: Number of species still present at the end of 5000-year simulations, initialized with 60 species, with a white noise forcing signal (blue) or a noisy seasonal signal (red). For each model type (with and without storage effect, + / - storage, respectively; with and without Stabilizing Niche Differences, + / - SND, respectively), 100 simulations were launched. Community compositions are stable in the cases -storage-SND and +storage+SND (1 or 60 species are still present at the end of all simulations, respectively).

When the richness of the community was stable (either 1 or 60 species at the end of the simulation, Fig. 3), there were still large differences in the structure of the community due to both stochasticity and the type of forcing (Fig. 3). Without storage effect and SNDs, a white noise forcing favoured species with intermediate thermal optima, with two thirds of the simulations ending with a species with a thermal

optima between 18.9°C and 21.4°C (corresponding to 25% of the range of thermal optima present at the beginning of the simulation) and reaching a maximum average biomass in this range (Fig. 3 a). This distribution can be related to a selection for the highest long-term growth rates, averaged over time (see normalized growth rates in Fig. 4). On the contrary, seasonality tended to favour species with larger maximum growth rates, with thermal optima above 22°C, their frequency of persistence and mean biomass increasing with the thermal optimum (Fig. 3). 38% of the simulations therefore ended with the species having the highest temperature optimum, 25°C.

When both coexistence mechanisms were present, the 60 initial species coexisted with small varia-178 tions in biomasses over the 50 simulations (mean CV=0.008 across simulations with either a white noise 179 or a seasonal forcing signal, Fig. 3b and d). The forcing signal modified only the distribution of biomasses 180 resulting in contrasted community structures despite equal richness in both simulation types. With a white 181 noise, the distribution was unimodal with a maximum biomass reached for the second best long-term av-182 erage growth rate (corresponding to a thermal optimum of 20.2°C). On the contrary, a seasonal signal 183 led to a bi-modal distribution (centered on 17.0°C and 24.4°C), each corresponding to one season, with highestr biomasses for higher thermal optima (Fig. 3 d). The minimum biomass was reached for the best long-term average growth rate at an intermediate temperature (20.4°C), one species apart from the max-186 imum biomass in the white noise case ., thus there are quite broad changes in community composition 187 even though the richness is equal for the two forcing signals. The two modes in the seasonal biomass 188 distribution correspond to the two modes in the seasonal signal (winter and summer). 189

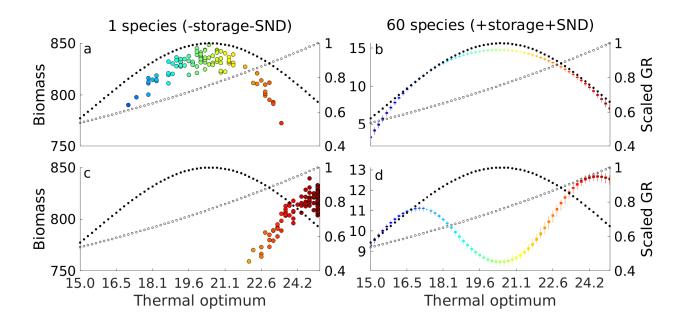


Figure 3: Mean biomass distribution over the last 200 years of 100 simulations, as a function of thermal optima, for the two stable-composition cases: without storage effect nor stabilizing niche differences (left, only one species is extant at the end of simulation, its mean value is represented by a dot for one simulation. There can be several dots for the same species, corresponding to multiple simulations ending with this species alone) and with storage effect and stabilizing niche differences (right, all species are present at the end of the simulation, their mean biomass is represented by boxplots of the mean value for 50 simulations). The forcing signal is either a white noise (top) or a seasonal signal (bottom). Each species is identified by its thermal optimum and its color code. Mean (filled circles) and maximum (open circles) growth rates for each species are indexed on the right axis [CP: Not sure about showing GR on this figure, though. I have another one without GR if necessary Fred: if you do this, you need to make it a yy-plot, with a right-hand y-axis labelled "Growth rate"].

In cases where the richness of the community varied, the overall shape (multimodal vs. unimodal) 190 of the marginal distribution of extant species with respect to the trait axis were similar for both types 191 of environmental forcings (Fig. 4). By contrast, the type of coexistence mechanism generated different 192 shapes. Indeed, the storage effect led to a multi-modal biomass distribution with respect to thermal 193 optima. We always observed 3 modes with a white noise and 3 modes in 95% of the seasonal simulations, 194 Fig. 4a. With a white noise, extant species are grouped in rather similar clumps regarding species thermal 195 optimum (between 18.8°C and 22.2°C whereas clumps tended to be further apart in the seasonal case, 196 covering a total range of 7.7°C, with species grouping in the higher part of the thermal range, above 197 22°C. On the other hand, stabilizing niche differences led to a quasi-uniform biomass distribution (Fig. 4 198 b). Species characterising communities forced by a white noise stayed in the lower range of temperatures 199 (in 96% of the simulations, the highest thermal optimum was 22.4°C) while they were filtered out in 200

communities subjected to a seasonal fluctuations of their environment, for which species with thermal optima above 20.5°C persisted.

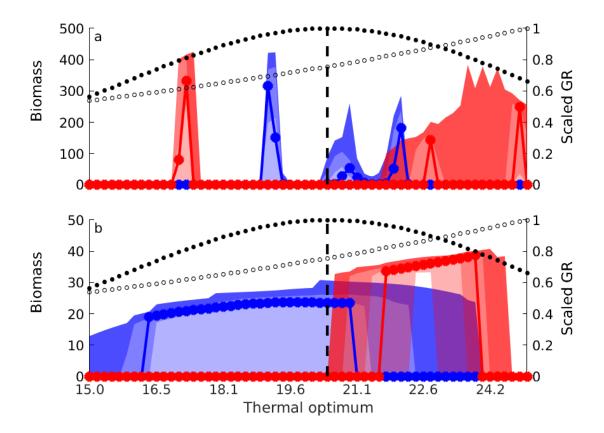


Figure 4: Mean biomass distribution over the last 200 years of 100 simulations, as a function of thermal optima, with storage effect and no stabilizing niche differences (top) and without storage effect, with stabilizing niche differences (bottom). The forcing signal is either a white noise (blue) or a seasonal signal (red). Shades of the same colour corresponds to the 50th, 90th and 100th percentiles of the distributions while coloured lines correspond to one representative simulation. Scaled average (whose optimum is indicated by the dashed line) and maximum growth rates are shown as filled and open and circles, respectively, and indexed on the left y-axis. [F: Add a right-handed y-axis labelled "Growth rates"]

4 Discussion

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We have simulated competitive Lotka-Volterra dynamics forced by a fluctuating environment (e.g., temperature fluctuations) under a range of scenarios allowing more or less coexistence. Two coexistence
mechanisms, the storage effect and stabilizing niches differences, could be either present or absent, which
led to four scenarios. These four scenarios were crossed with two possibilities for the forcing signal, a

white noise and a stochastic yet seasonal signal, both with equal temporal variance. Our investigation
therefore built on the model of Scranton and Vasseur (2016), which included a white noise forcing and a
storage effect, but considered seven additional combinations of mechanisms. This was motivated by our
wish to include two observed features of phytoplankton dynamics: seasonal cycles (Winder and Cloern,
2010) and stabilizing niche differences (Barraquand et al, 2017).

We have found that first, forced Lotka-Volterra dynamics cannot sustain any diversity with our 213 phytoplankton-based set of parameters, unless the structure is geared to include either a storage effect 214 or SNDs. Although this absence of diversity-enhancing effect of "pure" environmental variation has al-215 ready been stated by other authors (Barabás et al, 2012; Fox, 2013; Scranton and Vasseur, 2016), this is 216 not always intuitive (Fox, 2013), so we feel compelled to stress it once more: temporal variation in growth 217 rate alone cannot help coexistence within competitive communities. A nice point made by Scranton and 218 Vasseur (2016) was that a built-in storage effect in a forced Lotka-Volterra model, parameterised for phy-219 toplankton communities, could lead to some degree of coexistence. Our investigation reproduced these 220 results, using the white noise forcing considered by Scranton and Vasseur (2016), but an arguably more 221 realistic seasonal forcing by temperature (thinking of phytoplankton) considerably lessened the number of species coexisting after 5000 timesteps, decreasing from 15 on average to 4 on average. Even imagin-223 ing that groups represented here are genera or classes rather than species, this is a fairly low diversity for 224 a phytoplankton-like community (Reynolds, 2006). 225

We have therefore sought out whether stabilizing niche differences (SNDs) could produce a higher diversity maintenance, using field-based intra- vs inter-group (species or genera) competition coefficient ratio (Barraquand et al, 2017), where the intra-group density-dependence is approximately 10 times stronger. On their own, SNDs produced a higher level of diversity than the storage effect (almost double for white noise).

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However, the seasonal forcing still considerably reduced diversity when SNDs were considered, especially the "neutral" kind of diversity, i.e., diversity within clumps of similar traits. This diversity reduction occurs because within a season, the signal autocorrelation gives long, contiguous chunks of time to the best competitor to exclude its less adapted heterospecifics, while white noise generates large temperature shifts more frequently, and thereby forbid such competitive exclusion. In a seasonal setting, even though

a species has the best long-term averaged growth rate, it can disappear as a result of a strong competition from both low- and high-temperature tolerant species, with and without storage effect.

Our results may appear at odds with recent proposals that seasonal forcing in itself would help maintain diversity (Sakavara et al, 2018). However, we compared the effect of seasonal forcing to that of other forcing signals while controlling total variance. Thus, the contrast between our results and those of Sakavara et al (2018) may be due to the role of forcing variance over time. Overall, seasonality may be slightly better than no forcing at all in maintaining diversity, but on its own, seasonal forcing of parameters does little to improve coexistence and it does not really foster diversity within clumps here.

In our previous empirical study of coastal phytoplankton dynamics (Barraquand et al, 2017), we have not found any storage effect (which certainly does not mean that it could not be observed in other systems). Given the results on species richness and composition presented here, we are skeptical that even if it was present, the storage effect alone could help explaining phytoplankton diversity. This is all the more likely that SNDs seem fairly strong when estimated from phytoplankton time series (Barraquand et al, 2017). However, our results suggest that in phytoplankton-like seasonal environments, even though empirically-based SNDs produce more diversity than the storage effect when considered in isolation, the storage effect can help diversity maintenance when combined to other mechanisms. Indeed, the combination storage effect + SNDs is non-additive: the cases were both SNDs and the storage effect were present showed more diversity than generated by any mechanism on its own.

The above results suggest the very exciting idea that multiple coexistence mechanisms might com-bine superadditively, thus helping us to better understand the astounding diversity of primary producers. This logic could, in principle, be extended to mechanisms that we have not considered here (e.g., spa-tial structure, specialized natural enemies, that could be as important here for plankton as they are for tropical trees Bagchi et al; Comita et al; Stump and Chesson; Barraquand et al). Previous research has however demonstrated that generalist seed predation could weaken the storage effect (Kuang and Ches-son, 2009, 2010) thus different mechanisms might not always combine superadditively as we found here. That said, other models have shown that pathogens could enhance the storage effect (Mordecai, 2015) or that equalizing mechanisms due to optimally foraging predators are not greatly affected by environ-mental variation (Stump and Chesson, 2017). Better explaining plant or microbial diversity would then

not be about selecting the best unique mechanism susceptible to explain the observed diversity, but rather 264 better combining those mechanisms together. This may obviously be an annoyance for those who like to 265 sharpen Occam's razor, but it clearly holds opportunities for theoreticians wishing to investigate syner-266 gies between coexistence mechanisms in highly diverse communities. Aside from the synergies between 267 predator diversity-enhancing effects and SNDs or storage effects (on the temporal axis), one obvious 268 follow-up of this research would be interactions with spatial structure. Spatial structure occurs both en-269 dogeneously, through spatially restricted movements and interactions, and exogeneously, through spatial 270 variation in environmental covariates Bolker (2003) (Bolker TPB 2003). Numerous studies (Bolker and 271 Pacala Am Nat 2000Bolker and Pacala (1999), Murrell and Law Ecology 2002) have shown that spa-272 tially restricted movements and interactions - very small-scale spatial structure - can help coexistence, 273 which we believe would be especially important for phytoplankton since many species form colonies 274 (Reynolds, 2006; see discussion in Barraquand et al, 2017). Moreover, although temperature is usually 275 relatively spatially homogeneous over space, other drivers (e.g., rainfall, pH in terrestrial ecosystems; salinity in aquatic ones) may exhibit spatial variation which is a main factor for coexistence (Snyder, 2008). The odds that different (resource) niches, natural enemies, spatial limits to competition and temporal niche partitioning all interact to promote the very high-dimensional coexistence observed in the field seem much higher than for any of those mechanisms alone. Whether the diversity-enhancing effects 280 of these mechanisms combine sub-additively (as in Kuang and Chesson, 2010) or super-additively like 281 here is therefore worthy of further research. 282

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358 A Supplementary Material

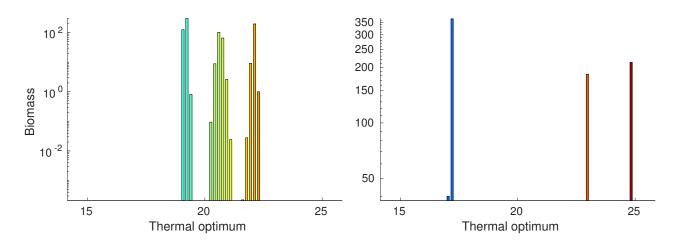


Figure 5: Mean biomasses over the last 200 years of 5000-year simulations as a function of the thermal optimum defining each species, for a white noise (left) or a seasonal signal (right) with storage effect and no stabilizing niche differences. This simulation is the one described in Fig. 1.

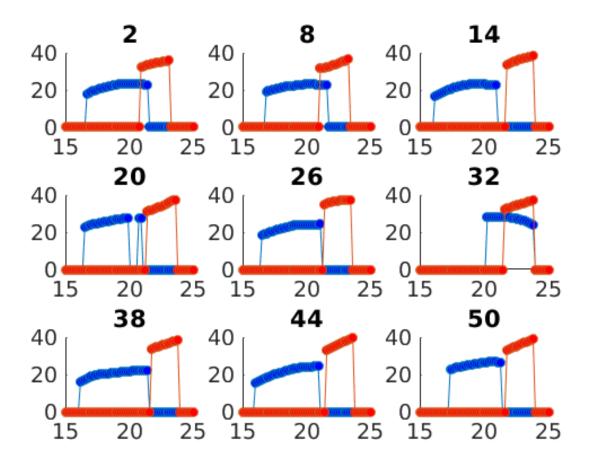


Figure 6: Mean biomass distribution over the last 200 years of 9 representative simulations, as a function of thermal optima, without storage effect with stabilizing niche differences, in which temperature is either a seasonal signal (red) or a white noise (blue). The distribution induced by a white noise overlaps the one obtained with a seasonal signal in only 2 simulations out of 50.

NOTE: figures below are here for discussion between us. I am not sure we should keep them in the paper.

360 I think this illustrates an issue (?) in the model: when I removed the storage effect, I must have changed

the total carrying capacity of the environment. Should we correct it? Note from Fred: there is clear underyielding

I also computed the evenness, not as an explanation but as a further exploration of the community.

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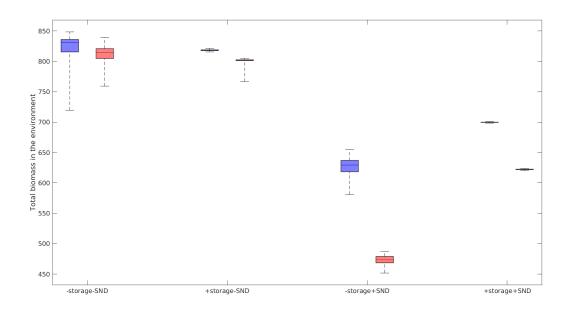


Figure 7: Sum of the average biomasses of all species for the last 200 years of a 5000-year simulation, initialized with 60 species with total initial biomass 10³, with a white noise forcing signal (blue) or a noisy seasonal signal (red). For each model type (with and without storage effect, + / - storage, respectively; with and without Stabilizing Niche Differences, + / - SND, respectively), 100 simulations were launched.

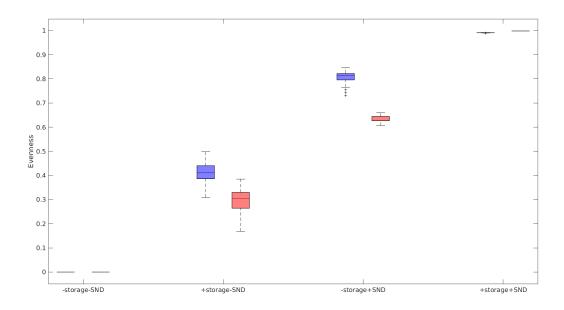


Figure 8: Normalized species evenness of the community, initialized with 60 species with total initial biomass 10³, with a white noise forcing signal (blue) or a noisy seasonal signal (red). For each model type (with and without storage effect, + / - storage, respectively; with and without Stabilizing Niche Differences, + / - SND, respectively), 100 simulations were launched.

White noise	Storage effect	No storage effect	Season+White noise	Storage ef
Stabilizing niche differences	60	28 [20-32]	Stabilizing niche differences	60
No stabilizing niche differences	15 [8-20]	1	No stabilizing niche differences	4 [2-6]

Table 3: Table corresponding to Fig. 2. Which one to choose?