

How self-regulation, storage effect and their interaction contribute to coexistence in stochastic and seasonal environments

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Abstract

Explaining coexistence in species-rich communities of primary producers remains a challenge for ecologists because of the likely competition for shared resources. Following Hutchinson's seminal suggestion, many theoreticians have tried to create diversity through a fluctuating environment, which impairs or slows down competitive exclusion. There are now several fluctuating-environment models allowing coexistence, but they often produce only a dozen of coexisting species at best. Here, we investigate how to create even richer communities in fluctuating environments, using an empirically parameterized model. Building on the forced Lotka-Volterra model of Scranton and Vasseur (2016) inspired by phytoplankton communities, we have investigated the effect of two coexistence mechanisms, namely the storage effect and ~~differences in~~ higher intra- ~~and~~ than interspecific competition strengths (i.e., strong self-regulation). We tuned the competition ratio on empirical data, in which self-regulation ~~supercedes~~ usually dominates interspecific interactions ~~in phytoplankton dynamics. stabilizing niche differences (SNDs). SNDs occur when intraspecific competition is stronger than interspecific; we tuned the competition ratio based on empirical data.~~ Although SNDs ~~a strong self-regulation~~ maintained more species (50%) than the storage effect (25%), we show that none of the two coexistence mechanisms considered could, by itself, ensure the coexistence of all species present at the beginning of our simulations. Realistic seasonal environments only aggravated that picture, as they decreased persistence relative to ~~white noise~~ a random environment. Our results suggest that combining different mechanisms for biodiversity maintenance into community models might be more fruitful than trying to find which mechanism explains best the observed diversity levels. Our results on community composition (formation of clumps, biomass distribution) in the different scenarios give further hints about likely coexistence mechanisms at work.

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Keywords: coexistence; seasonality; competition; phytoplankton; Lotka-Volterra; storage effect

1 Introduction

There has been a rich debate in theoretical ecology on how to reconcile niche and neutral perspectives on species coexistence (Gravel et al, 2006; Carmel et al, 2017). Under the neutral perspective, all species have equal birth and death rates and compete equally (since space is limited) whilst under the niche perspective, birth and death rates can vary between species and various mechanisms contribute to increasing intraspecific over interspecific competition (Hubbell, 2001). However, as it has been pointed out repeatedly, niche and neutral processes are not mutually exclusive: they may actually act together to produce observed species coexistence (Gravel et al, 2006; Mutshinda et al, 2009; Götzenberger et al, 2012).

For instance, Scheffer and van Nes (2006) put forward the concept of ‘clumpy coexistence’, whereby a simultaneous influence of both niche and neutral processes create several clumps of similar species along a single trait axis. Classical stabilizing niche differences (SNDs), [such as a stronger net intraspecific competition than interspecific competition](#), enable coexistence of multiple clumps ~~through stronger net intraspecific competition~~ (Chesson, 2000), while within-clump coexistence occurs through neutral processes (Hubbell, 2001; Munoz and Huneman, 2016), as species that differ too little in their fitnesses cannot exclude themselves out on reasonable timeframes. Indeed, clumps on the trait axis eventually thin out in absence of immigration, but transient coexistence can last for extended periods of time. This ‘emergent neutrality’ within groups (Holt, 2006) has been proposed as a unifying concept for the niche and neutral theories. The findings of Scheffer and van Nes (2006) have been disputed due to hidden niches in the original model (Barabás et al, 2013). Hidden niches emerge through stronger intraspecific competition mediated by an additional intraspecific predation-like term (Barabás et al, 2013). This makes coexistence in the Scheffer and van Nes model more similar to that of the classical Lotka-Volterra model (Barabás et al, 2016), so that coexistence within clumps is not exactly neutral. Still, the idea that niche and neutral assembly can mould communities stays potent (Vergnon et al, 2013). Since then, several studies have suggested that ‘clumpy coexistence’ can occur in theoretical models, most notably models incorporating temporal variation (Scranton and Vasseur, 2016; Sakavara et al, 2018). In these temporal-variation models, equal competitive strengths are combined with other

mechanisms like the storage effect (or temporal niche partitioning, that is an equivalent concept for forced Lotka-Volterra models, Barabás et al, 2012; Scranton and Vasseur, 2016). The storage effect increases the possibility of coexistence by making the interaction strength covary positively with a fluctuating environment (see also Barabás et al, 2012).

Here, we build on the work of Scranton and Vasseur (2016) to investigate the possibility of coexistence through species response to fluctuating environments. Our enthusiasm for the Scranton and Vasseur (2016) model stems from our interest in phytoplankton communities, that inspired their thermal preference curves modeling intrinsic growth rates. However, Scranton and Vasseur (2016) described temperature as a random noise, i.e., independent and identically distributed Gaussian random variates over time. This appeared to us a key assumption to relax. Under most latitudes, temperature is indeed a seasonal signal, and seasonal forcing can strongly affect the dynamics of the community considered (Vesipa and Ridolfi, 2017). Hence, over short timescales, random temporal variations often only add noise to a largely deterministic seasonal trend. Our present work can therefore be seen as an attempt to blend Scranton and Vasseur (2016)’s framework with the periodic environments of Barabás et al (2012), to better represent the mixture of stochastic and deterministic environmental forces affecting phytoplankton community dynamics.

Because many phytoplankton species or genera respond in similar ways to temperature despite having different optimas (Moisan et al, 2002), we hypothesized that a large seasonal variation might not necessarily foster species coexistence. In fact, similar responses to seasonal fluctuations should lead to an increased synchrony of species abundances which, in turn, should theoretically mitigate the expected temporal partitioning. How seasonality affects coexistence (as opposed to a purely randomly fluctuating environment) is therefore a key feature of this paper. In particular, we contrast cases where the storage effect is present vs. absent, which conveniently maps to two different parameterizations of the forced Lotka-Volterra model. Moreover, the overall diversity obtained at the end of the simulations with Scranton and Vasseur (2016)’s model was relatively low compared to what we usually observe in phytoplankton communities (several dozens to hundreds of species). We have therefore sought out which mechanisms would foster a truly species-rich community for extended periods of time.

84 In an empirical study combining phytoplankton community-level time series and multivariate
85 autoregressive models (Barraquand et al, 2018)¹, we found that despite a large influence of the
86 environment (including temperature, irradiance, and other factors), a strong intraspecific (or in-
87 tragenus) competition, when compared to interspecific interaction coefficients, was most likely the
88 key driver of species coexistence. In other words, strong self-regulation had a large role to play
89 in maintaining species diversity in coastal phytoplankton (Barraquand et al, 2018). These high
90 intraspecific interaction strengths mirror those found in a number of terrestrial plant communities
91 (Adler et al, 2018) and in animal communities (Mutshinda et al, 2009).

92 Here, we therefore try to establish what are the relative contributions of the storage effect vs
93 strong self-regulation to coexistence in a phytoplankton-like theoretical community model. This
94 led us to cross different combinations of seasonality in the forcing signal, presence of the storage
95 effect or not, and intra- vs interspecific competition, in order to disentangle the contributions of
96 all these factors to biodiversity maintenance.

97 **2 Methods**

98 *Models description*

99 The model described in Scranton and Vasseur (2016) is based on a variant of the Lotka-Volterra
100 competition model. Fluctuations in the environment are introduced in the model by temperature-
101 dependent intrinsic growth rates (see Eq. 1-2, all coefficients are defined in Table 1) so that species
102 growth rates can be expressed as:

¹Preprint version available: see Barraquand et al (2017) in the reference list

$$\frac{dN_i}{dt} = r_i(\tau)N_i \left(1 - \sum_{j=1}^S \alpha_{ij}N_j\right) - mN_i \quad (1)$$

$$r_i(\tau) = a_r(\tau_0)e^{E_r \frac{(\tau - \tau_0)}{k\tau\tau_0}} f_i(\tau) \quad (2)$$

$$\text{where } f_i(\tau) = \begin{cases} e^{-|\tau - \tau_i^{opt}|^3/b_i}, & \tau \leq \tau_i^{opt} \\ e^{-5|\tau - \tau_i^{opt}|^3/b_i}, & \tau > \tau_i^{opt} \end{cases} \quad (3)$$

$$\text{and } b_i \text{ defined by numerically solving } \int r_i(\tau)d\tau = A \quad (4)$$

103 Model parameters are detailed in Table 1, and we set their values to match the features of
 104 phytoplankton communities as in Scranton and Vasseur's work (2016). The niche of each species is
 105 defined by its thermal optimum τ_i^{opt} . Thermal performance curves defined in Eq. 3 are parameter-
 106 ized so that all species share the same niche area (Eq. 4), which sets a trade-off between maximum
 107 growth rates and niche width.

Table 1: Parameter definition and values of the model described in Eq. 1-4. Parameter values are not specified when they vary with time and/or the species considered.

Name	Definition	Value (unit)
S	Number of species	60 ()
N_i	Biomass density of the i th species	(kg/area)
τ	Temperature	(K)
$r_i(\tau)$	Growth rate of species i as a function of temperature	($\frac{\text{kg}}{\text{kg}^*\text{year}}$)
α_{ij}	Strength of competition of species j on species i	0.001 (area/kg)
b_i	Normalization of the thermal decay rate	(K^3)
m	Mortality rate	$15(\frac{\text{kg}}{\text{kg}^*\text{year}})$
τ_0	Reference temperature	293 (K)
$a_r(\tau_0)$	Growth rate at reference temperature	$386(\frac{\text{kg}}{\text{kg}^*\text{year}})$
E_r	Activation energy	0.467 (eV)
k	Boltzmann's constant	$8.6173324 \cdot 10^{-5}(\text{eV} \cdot \text{K}^{-1})$
$f_i(\tau)$	Fraction of the maximum rate achieved for the i th species	(NA)
μ_τ	Mean temperature	293 (K)
σ_τ	Standard deviation for temperature	5 (K)
τ_{\min}	Minimum thermal optimum	288 (K)
τ_{\max}	Maximum thermal optimum	298 (K)
A	Niche breadth	$10^{3.1}(\frac{\text{kg}}{\text{kg}^*\text{year}})$
τ_i^{opt}	Thermal optimum for growth of the i th species	(K)
θ	Scaling between white random and seasonal noise and seasonal signal	$[0, \sqrt{(2)}]$ (NA)
ρ	Ratio of intra-to-intergroup competition strengths	(1;10) (NA)

108 The original environmental forcing is a normally distributed variable centered on 293 K (XX
109 C [indicate in Celsius as well, do that also in the Table]), with a 5K dispersion. This vari-
110 able varies from one day to ~~another~~the next, but is kept constant throughout the day. At the
111 ~~macro-temporal~~monthly or annual temporal scale usually used in ecological studies, temperature
112 could therefore be considered as a white noise (Vasseur and Yodzis, 2004). However, from a mathe-
113 matical viewpoint, the noise ~~but it~~ is slightly auto-correlated as the integration process goes slightly
114 below the daily time step. We ~~have therefore chosen to use the word~~ ‘random noise’ to describe
115 this forcing ~~and remain coherent with the~~, as opposed to ‘seasonal noise’ described hereafter. To
116 construct our seasonal noise, wWe ~~kept~~keep the mean and standard deviation of the forcing signal
117 but included a lower-frequency component using a sinusoidal function with a period of 365 days
118 (~~1-time-unit-being-one-day~~, Eq. 5). We tune the ratio of low-to-high frequency with the variable
119 θ so as to keep the same energy content - i.e., equal total variance - in the forcing signal.

$$\tau(t) = \mu_\tau + \theta\sigma_\tau \sin(2\pi t) + \epsilon_t, \text{ where } \epsilon_t \sim \mathcal{N}(0, \sigma_\tau \sqrt{1 - \frac{\theta^2}{2}}) \quad (5)$$

120

121 Note that the upper limit for θ , $\sqrt{2}$, corresponds to a completely deterministic model which we
 122 do not explore here (but see Zhao (1991) proving bounded coexistence). We choose to keep the
 123 stochasticity in the signal and to model a plausible temperature signal with $\theta = 1.3$ (see Fig. 1b)
 124 when considering a seasonal forcing of the dynamics.

125 The formulation of the forced Lotka-Volterra model of Scranton and Vasseur (2016) implies
 126 a storage effect, as the net effect of competition on a given species exerted by species j on i is
 127 the product of the temperature-related growth rate $r_i(\tau)$ and the sum of competitive strengths
 128 α_{ij} exerted by other species an individual of species j . . Therefore, ~~competition strengths~~ net
 129 competition covaries positively with the growth rate values $r_i(\tau)$ (Chesson, 1994; Ellner et al,
 130 2016). ~~To test for the effect of an explicit storage effect in the model, we formulated a new version of~~
 131 ~~this model, where we removed.~~ To remove this assumption of an explicit storage effect, we created
 132 in another version of the model by using the mean value of a species' growth rate (\bar{r}_i) to weight the
 133 interaction coefficients (see Table 2). The mean growth rate value was computed by first generating
 134 the temperature time series and averaging all r_i over the corresponding simulation sequences of τ
 135 values. .

$$\frac{dN_i}{dt} = N_i \left(r_i(\tau) - \sum_{j=1}^S \bar{r}_i \alpha_{ij} N_j \right) - mN_i \quad (6)$$

136 In this way, ~~competition strengths~~ net competition remain unaffected by the environmental con-
 137 ditions, in contrast to intrinsic growth rates (Eq. 6), while preserving the same average magnitude
 138 as in Eq. 1.

139 ~~Stabilizing niche differences are~~ Strong self-regulation is ensured by the addition of the coefficient
 140 ρ , which is the ratio of intra-to-intergroup competition strength. We can therefore re-write the
 141 interaction coefficients α_{ij} in Eq. 7

$$\alpha_{ij} = \alpha(1 + (\rho - 1)\delta_{ij})$$

$$\alpha_{ij} = \alpha(1 + (\rho - 1)\delta_{ij}) \quad (7)$$

where δ_{ij} is the Kronecker symbol, equal to 1 if $i = j$ and to 0 otherwise. The value of the parameter $\rho = 10$ was chosen from analyses of phytoplanktonic data (Barraquand et al, 2018)². Hereafter, the phrase “strong (and respectively, weak) self-regulation” characterizes dynamics where the intraspecific competition strength is 10 times higher than (and respectively, equal to) the interspecific competition strength. When we use the word “strong”, we therefore consider a “relatively stronger” self-regulation but do not wish to compare our interaction values to those used outside of our framework.

In addition to two types of environmental forcings (random noise with $\theta = 0$, and seasonal noise with $\theta = 1.3$), we compare the results for four formulations of the model: with and without an explicit storage effect (Eq. 1 and Eq. 6, respectively) ; with and without strong self-regulation ($\rho = 10$ or $\rho = 1$, respectively). These are summed up in Table 2

$\frac{dN_i}{dt} + mN_i$	Storage effect	No
Strong self-regulation ($\rho = 10$)	$r_i(\tau)N_i \left(1 - \sum_{j=1}^S \alpha(1 + 9\delta_{ij}) N_j\right)$	$N_i \left(r_i(\tau) - \sum_{j=1}^S \alpha N_j\right)$
Weak self-regulation Equal competitive strengths ($\rho = 1$)	$r_i(\tau)N_i \left(1 - \sum_{j=1}^S \alpha N_j\right)$	$N_i \left(r_i(\tau) - \sum_{j=1}^S \alpha N_j\right)$

Table 2: Growth rate of species i in the four formulations of the model we present

Set-up

We replicate the ‘Species sorting’ experiment of Scranton and Vasseur (2016) so as to investigate how the structure of synthetic phytoplankton communities varies under the different scenarios we described above. We focused on the dynamics of a community initialized with 60 species with thermal optima uniformly spaced along the interval $[15^\circ\text{C}, 25^\circ\text{C}]$, and with the same initial density

²The values of non-zero interspecific competition coefficients reported in Fig. 5 of Barraquand et al (2018) are somewhat higher than here (and ρ lower, closer to 4) because the best-fitting model actually set to zero some intergroup competition coefficients; using a model where all α_{ij} are non-zero leads in contrast to $\rho = 10$.

161 $(\frac{1}{\alpha S})$. Each simulation was run for 5000 years in 1-day intervals. When the density of a species
162 dropped below 10^{-6} , it was considered extinct. For each combination of parameters (type of
163 environmental signal, storage effect and stabilizing niche differences), we ran 100 simulations.

164 All simulations were ran with Matlab's ode45 algorithm, an explicit Runge-Kutta (4,5) algo-
165 rithm with an absolute error tolerance of 10^{-8} , and relative error tolerance 10^{-3} . The code is
166 available in a GitHub repository ³.

167 3 Results

168 Typical dynamics of the community following Eq. 1 (the model of Scranton and Vasseur, 2016),
169 with both the environmental signals described in Eq. 1 (original choice of Scranton and Vasseur,
170 2016; Fig. 1a) and Eq. 5 (our variant, Fig. 1b), are shown in Fig. 1c and d. A sinusoidal forcing
171 produces the strongly seasonally structured dynamics that are typical of phytoplankton. Even
172 though only 5 species can be seen in Fig. 1c, there were 14 species still present at the end of
173 the simulation forced by a random noise, with large disparities in the range of variation of their
174 biomasses. A third of the species kept a biomass above 10 kg/area (setting area = 1 ha, with a
175 depth of a few meters, produce a realistic standing biomasses; Reynolds, 2006) while 6 out of the
176 14 remained below the unit. All persisting species in the random noise simulations were clustered
177 within a 3.2°C-range of thermal optima (see the biomass distribution as a function of the thermal
178 optimum in Fig. A1 in the Supplementary Material). No obvious temporal patterns (e.g., cycles)
179 could be seen in the communities forced by random noise. On the contrary, seasonal cycles were
180 clear in the seasonally-forced case of Fig. 1d. Only 4 species coexisted at the end of the simulation
181 with seasonal noise, gathered in two groups with large thermal optimum differences (5.7°C between
182 the maximum thermal optimum of the first group and the minimum thermal optimum of the second
183 group). When temperatures are high, the group with higher thermal optima reaches its maximum
184 biomass, then as temperature decreases through the season, these species leave room for the growth
185 of the low-temperature group.

³<https://github.com/CoraliePicoche/Seasonality>, will be made public upon acceptance or at the reviewer's request

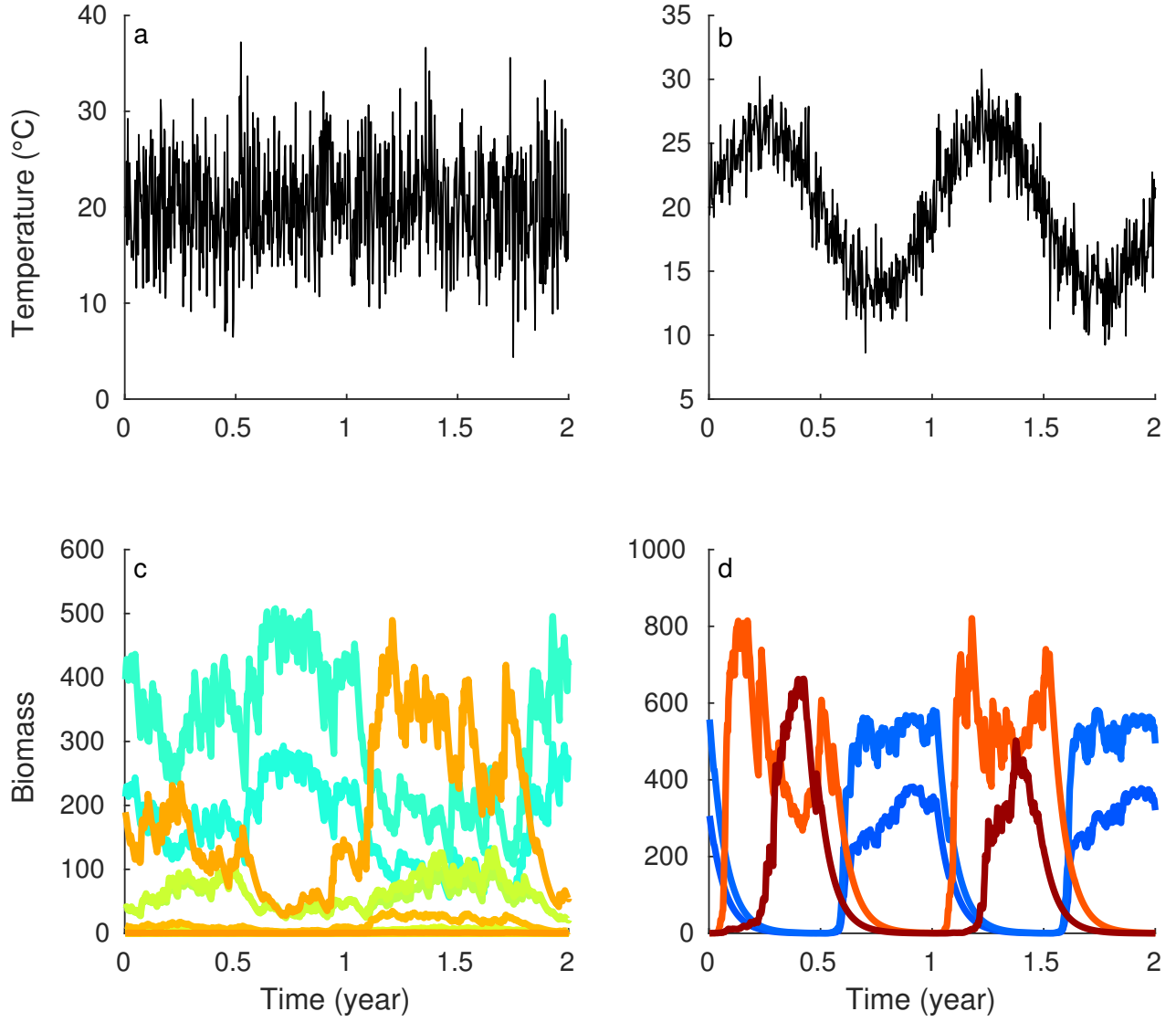


Figure 1: Time series of temperature (top; a-b) and extant species (bottom; c-d) for the 2 last years of a 5000 years simulation, with storage effect and no differences between intraspecific and interspecific competition strengths. The forcing temperature is either a random noise (a) or a seasonal noise (b), leading to community dynamics with more erratic fluctuations (c) vs seasonally structured fluctuations (d). Line colors of species biomasses correspond to their thermal optimum (from blue, corresponding to low thermal optimum, to red, corresponding to high thermal optimum).

186 The decrease in persistence due to seasonality observed in Fig. 1 was confirmed in all our
 187 simulations (Fig. 2). In cases where final species richness varied from one simulation to another
 188 (namely, the two middle cases in Fig. 2: with storage effect but without strong self-regulation, or
 189 without storage effect but with strong self-regulation), seasonality reduced the number of extant
 190 species to, on average, 27% and 48% of their original values, respectively (Fig. 2). A seasonal signal

191 therefore led to a much smaller average persistence. There was also less variance in persistence
 192 between seasonally forced simulations when compared to random noise simulations.

193 Both a strong self-regulation and the storage effect markedly increased persistence. Without
 194 any of these coexistence mechanisms, only one species persisted at the end of the simulations.
 195 When only the storage effect was present, the number of extant species varied between 8 and 20
 196 (14.8 ± 2.4) with a white noise, or 2 and 6 (4.1 ± 0.7) with a seasonal signal. On the other hand,
 197 when only a strong self-regulation was present, the number of extant species nearly doubled, varying
 198 between 20 and 32 (27.5 ± 2.4), or 12 and 15 (13.3 ± 0.6), with a random or a seasonal noise,
 199 respectively. Remarkably, when the storage effect and a strong self-regulation both affected the
 200 community dynamics, all species persisted in the community, while neither of these mechanisms
 201 was able to produce that result alone, for either random and seasonal noise.

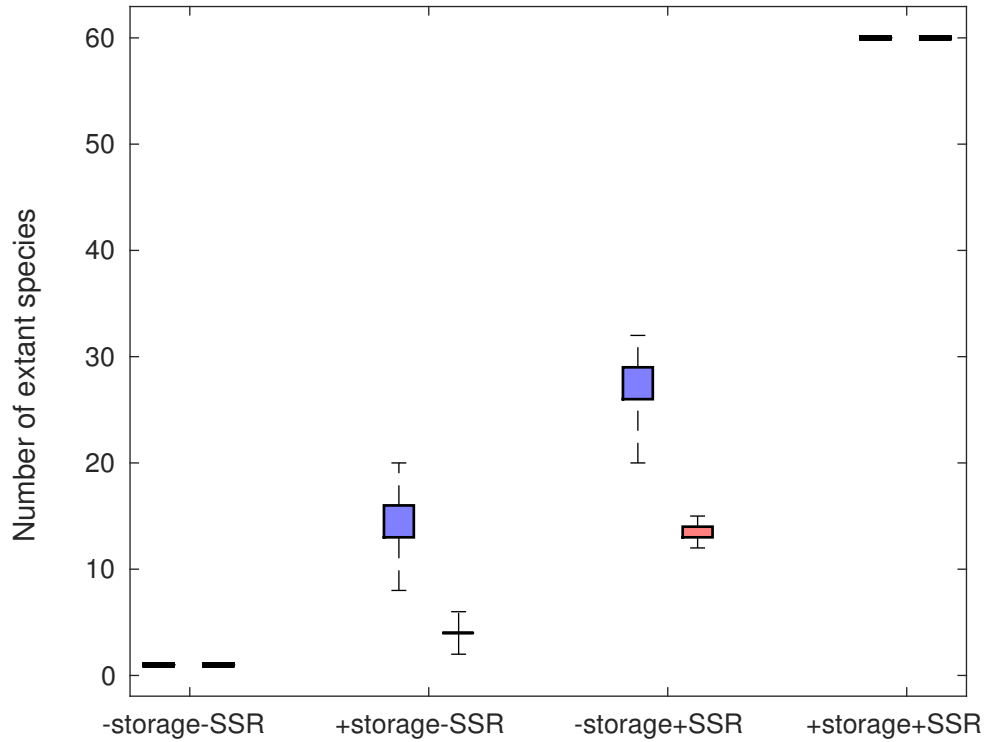


Figure 2: Number of species still present at the end of 100 simulations (5000 years each), initialized with 60 species, with a random noise forcing signal (blue) or a seasonal noise (red). The signs + or - storage refer to presence or absence of a storage effect, respectively; + / - SSR, presence or absence of Strong Self-Regulation, respectively. Community compositions are stable in the cases -storage-SSR and +storage+SSR, for which 1 or 60 species are still present at the end of all simulations, respectively. Due to low variance, the whiskers here represent min and max rather than 1.5 interquartile range.

202 The trait pattern of the community was affected by the type of forcing even when the richness
 203 of the community was stable (Fig. 3). Without storage effect nor strong self-regulation, there was
 204 only one species left at the end of a simulation. A random noise favored species with intermediate
 205 thermal optima: the final species had a thermal optimum between 18.9°C and 21.4°C (only a
 206 fourth of the initial range of thermal optima) for two simulation out of three and the maximum
 207 final biomasses over 100 simulations was reached in this range (Fig. 3a). [[[This distribution can
 208 be related to a selection for the highest long-term growth rates, averaged over time (see scaled
 209 growth rates in Fig. 3).]]]. Seasonality with no coexistence mechanisms also led to a single
 210 final species but, in this case, the species always had a higher maximum growth rate (thermal
 211 optimum above 22°C). Species with a higher thermal optimum were more likely to persist and to
 212 reach a higher biomass at the end of the simulation. 38% of the simulations therefore ended with
 213 the species having the highest temperature optimum, 25°C. The shift in trait distribution towards
 214 higher maximum growth rates with seasonality vs. higher average growth rates with a random
 215 noise was consistent infor all sets of simulationsmodel types considered (see below).

216 When both storage effect and strong self-regulation were present, the 60 initial species coexisted
 217 with small variations in biomasses for each species over the 100 simulations (mean CV=0.008
 218 across simulations with either a random or a seasonal noise, Fig. 3b and d). The forcing signal
 219 modified only the distribution of biomasses resulting in contrasted community structures despite
 220 equal richness in both simulation types. With a random noise, the distribution was unimodal with
 221 a maximum biomass reached for the second best long-term average growth rate (corresponding to
 222 a thermal optimum of 20.2°C). On the contrary, a seasonal signal led to a bi-modal distribution
 223 (centered on 17.0°C and 24.4°C), each corresponding to one season, with highest biomasses for
 224 higher thermal optima (Fig. 3d). The minimum biomass was reached for the best long-term
 225 average growth rate at an intermediate temperature (20.4°C), one species apart from the maximum
 226 biomass in the random noise case.

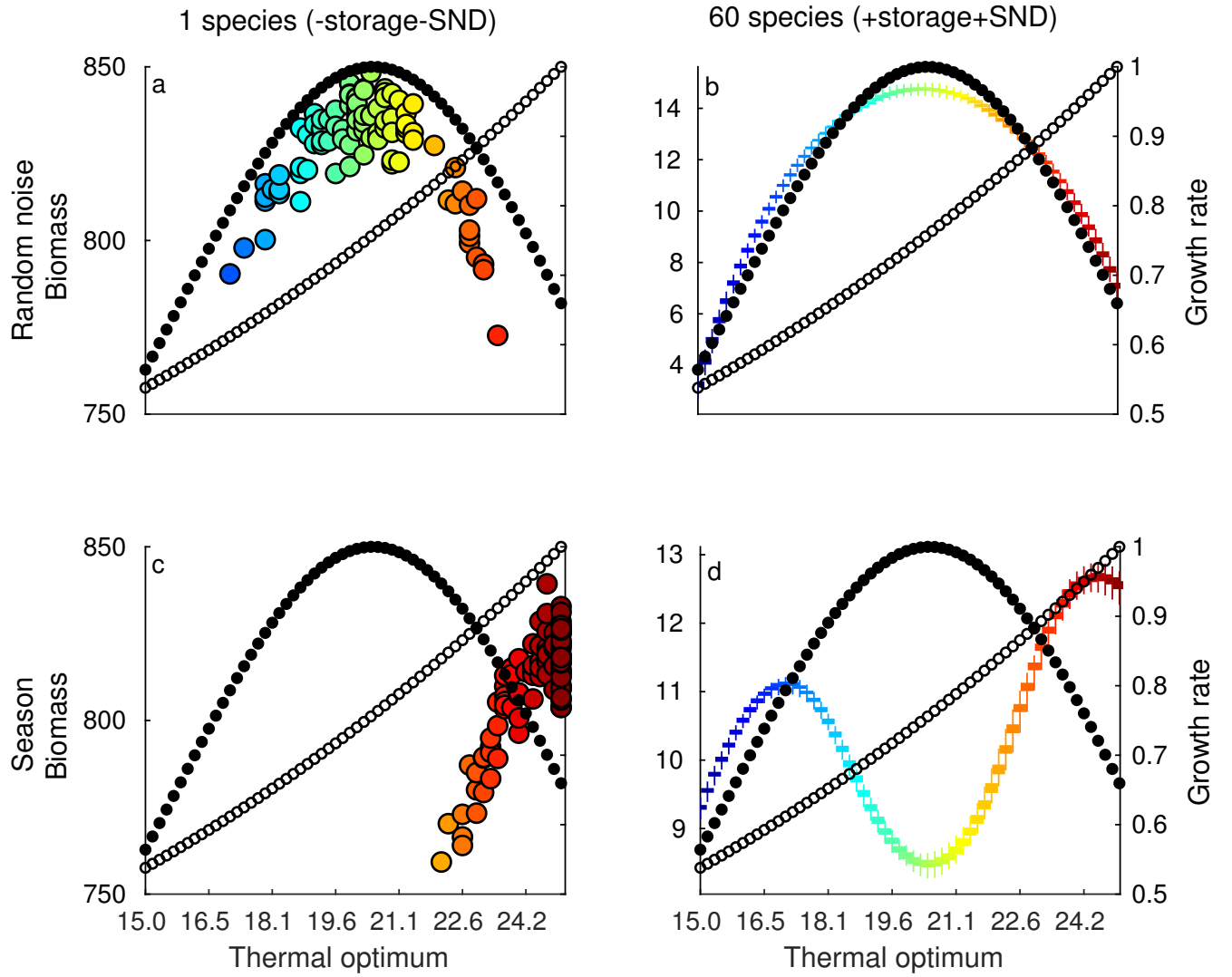


Figure 3: Mean biomass distribution over the last 200 years for 100 simulations, as a function of the species thermal optima. Here we consider the two stable-composition cases and two types of forcing signal. On the left column, simulations without storage effect nor *stabilizing niche differences* *strong self-regulation* are presented. Only one species is present at the end of the simulations and its mean value is represented by one large colored circle per simulation. There can be several circles for the same species, corresponding to multiple simulations ending with this species alone. On the right column, simulations with storage effect and *stabilizing niche differences* *strong self-regulation* are represented. All species are present at the end of the simulations and small boxplots present the variation in the temporal average of biomass with a given trait, for 100 simulations. The forcing signal is either a random (top) or a seasonal noise (bottom). Each species is identified by its thermal optimum through its color code. Scaled (divided by maximum) average and maximum growth rates are shown as small filled and open circles, respectively, and are indexed on the right y-axis.

227 In cases where the richness of the community varied, the overall shape (multimodal vs. uni-
 228 modal) of the marginal distribution of extant species with respect to the trait axis were similar
 229 for both types of environmental forcings (Fig. 4). By contrast, the type of coexistence mechanism

230 generated different shapes. Indeed, the storage effect led to a multimodal biomass distribution with
231 respect to thermal optima. We always observed 3 modes with a random noise and 3 modes in 95%
232 of the seasonal simulations (Fig. 4a). With a random noise, extant species are grouped in rather
233 similar clumps regarding species thermal optima (between 18.8°C and 22.2°C) whereas clumps
234 tended to be further apart in the seasonal case, covering a total range of 7.7°C, with species group-
235 ing in the higher part of the thermal range, above 22°C. On the other hand, strong self-regulation
236 led to a quasi-uniform biomass distribution (Fig. 4 b). Species characterising communities forced
237 by a random noise stayed in the lower range of temperatures (in 96% of the simulations, the highest
238 thermal optimum was 22.4°C, see Fig. A2 in the Supplementary Material) while they were filtered
239 out in communities subjected to a seasonal fluctuation of their environment, for which species with
240 thermal optima above 20.5°C persisted. As before (Fig. 3), seasonality promoted species with a
241 higher maximum growth rates since the autocorrelated temperatures enabled them to achieve this
242 highest growth rate for a longer period of time than a random noise would have.

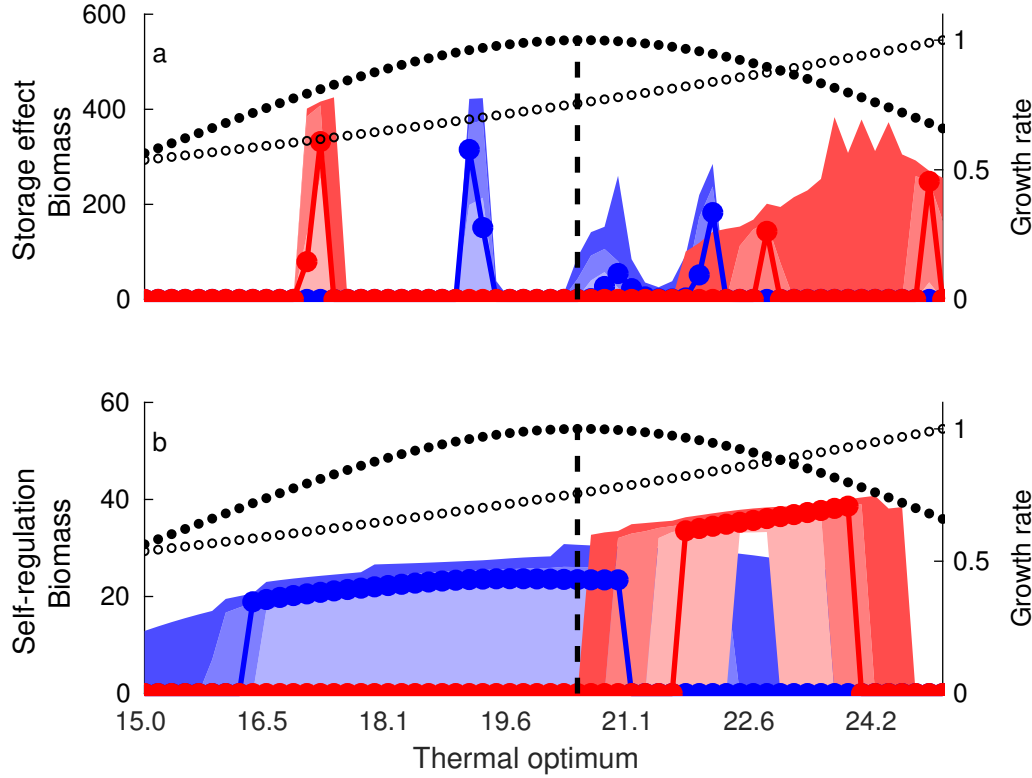


Figure 4: Mean biomass distribution over the last 200 years for 100 simulations, as a function of thermal optima, with storage effect and ~~weak self-regulation~~ equal competitive strengths (a) and without storage effect, with strong self-regulation (b). The forcing signal is either a random (in blue) or a seasonal noise (in red). Shades of the same color correspond to the 50th, 90th and 100th percentiles of the distributions while colored lines correspond to one representative simulation. Scaled (divided by maximum) average (whose maximum is indicated by the dashed line) and maximum growth rates are shown as filled and open circles, respectively, and indexed on the right y-axis.

4 Discussion

We have simulated competitive Lotka-Volterra dynamics forced by a fluctuating environment (e.g., temperature fluctuations) under a range of scenarios allowing more or less coexistence. Two coexistence mechanisms, the storage effect and strong self-regulation (i.e., intraspecific competition much stronger than interspecific competition), could be either present or absent, which led to four scenarios. These four scenarios were crossed with two possibilities for the forcing signal, a random noise (mostly white) and a stochastic yet seasonal signal, both with equal temporal variance. Our

investigation therefore built on the model of Scranton and Vasseur (2016), which included a random forcing and a storage effect, but considered seven additional combinations of mechanisms. This was motivated by our wish to include two observed features of phytoplankton dynamics: seasonal cycles (Winder and Cloern, 2010) and strong self-regulation (Chesson, 2000; Adler et al, 2010; Barraquand et al, 2018). Many mechanisms can lead to intraspecific competition being stronger than interspecific competition: nonlinearities in the functional forms of competition or mutualism that contribute to increasing self-regulation (Kawatsu and Kondoh, 2018), predation or parasitism (see e.g., the generalist predators in Haydon, 1994), etc. They seem nonetheless an ubiquitous feature in primary producers (Adler et al, 2018).

We have found that first, temporally forced Lotka-Volterra dynamics cannot sustain any diversity with our phytoplankton-based set of parameters, unless the structure is geared to include either a storage effect or a strong self-regulation. Although this absence of diversity-enhancing effect of “pure” environmental variation has already been stated by other authors (Barabás et al, 2012; Fox, 2013; Scranton and Vasseur, 2016), this is not always intuitive (Fox, 2013), so we feel compelled to stress it once more: temporal variation in growth rate alone cannot help coexistence within competitive communities. A nice point made by Scranton and Vasseur (2016) was that a built-in storage effect in a forced Lotka-Volterra model, parameterized for phytoplankton communities, could lead to some degree of coexistence. Our investigation reproduced these results, using the random noise considered by Scranton and Vasseur (2016). However, an arguably more lifelike noisy and seasonal temperature forcing considerably lessened the richness of the community after 5000 years, decreasing from 15 to 4 species on average. Even imagining that groups represented here are genera or classes rather than species, this is a fairly low diversity for a phytoplankton-like community (see Chapter 1 in Reynolds, 2006). This suggests that the storage effect may not, on its own, be sufficient to maintain species-rich communities (e.g., dozens to hundreds of species). We have therefore sought out whether a stronger self-regulation could maintain a higher diversity, using field-based intra- vs intergroup (species or genera) competition strength ratio (Barraquand et al, 2018), where the intragroup density-dependence was chosen 10 times stronger. – The Our comparison of both coexistence mechanisms, the storage effect and a strong self-regulation, depends on the chosen

intensity of self-regulation of each species and the type of dynamics considered - although ,which
calls for further analyses on different networks before drawing a general conclusion. On their
own, in a Lotka-Volterra model applied to phytoplankton species, SNDsa stronger self-regulation
produced a higher level of diversity than the storage effect (almost double for whiterandom noise),
which not only aligns with our results on phytoplankton but also with results on perennial plants
(Adler et al, 2010).-

However, self-regulation was still insufficient to maintain the whole community diversity by
itself, especially when the seasonal forcing was considered. The diversity within clumps of similar
values of growth rates was considerably decreased. This diversity reduction occurs because within
a season, the signal autocorrelation gives long, contiguous time intervals to the best competitor
to exclude its less adapted heterospecifics. This makes the results likely to hold not only for
seasonal environments, but more generally for autocorrelated ones, i.e., “red” noise. This could
be relevant for species whose population dynamics occurs at timescales largely above one year.
In contrast, a truly random noise, which can be considered white noise above the daily temporal
scales, generates large temperature shifts more frequently, and thereby forbids such competitive
exclusion. In a seasonal setting, a species with the highest long-term (arithmetically) averaged
growth rate may not be the best competitor, and can disappear as a result of a strong competition
from both low- and high-temperature tolerant species. This holds with or without a storage effect.

Our results may appear at odds with recent proposals that seasonal forcing in itself would help
maintain diversity (Sakavara et al, 2018). However, we compared the effect of seasonal forcing
to that of other forcing signals while controlling for total variance. Thus, the contrast between
our results and those of Sakavara et al (2018) may be due to the role of forcing variance over
time (we compare scenarios under a constant total variance). Overall, while seasonality may be
slightly better than no forcing at all in maintaining diversity, seasonal forcing of parameters does
not improve coexistence: diversity within clumps is lower when seasonality is included.

In addition to community diversity, the biomass-trait relationship also varied from one simula-
tion to another. Some regularities did emerge across simulations though. The storage effect begot
several clumps along the trait space (as observed by Scranton and Vasseur, 2016). The seasonality

that we added to the temperature signal led to more distant clumps on the trait axis (as said above, less species per clump). Conversely, ~~SNDs~~ strong self-regulatory mechanisms alone led to relatively uniform biomass distributions, with species forming a single large cluster, which covers a fraction of the initial trait space. Therefore, the shape of the distribution was affected by the coexistence mechanism at stake while the average trait value was modified by the type of environmental forcing, even though the mean value of the environmental signal did not change. The relationships between trait patterns and filters applied on local communities are complex and still need to be clarified but they biomass-trait distributions therefore constitute an additional clue on species clues to interpret community dynamics (D’Andrea and Ostling, 2016; Loranger et al, 2018), although we certainly recommend to interpret them with caution to avoid over-generalization. The identification of multiple modes in biomass-trait relationships and SADs is relatively recent (Dornelas and Connolly, 2008; Matthews et al, 2014) and is a rare pattern in theoretical models (McGill et al, 2007). Barabás et al (2013) convincingly argued that multimodality could arise from the demographic stochasticity of a single model run (with either self-regulation or neutrality, but without the clumpy coexistence emerging from a storage effect). However, our results are based on many model runs, for which either the storage effect alone or a storage effect + strong self-regulation in a seasonal context consistently produced multimodal distributions, while simulations without the storage effect always led to a single cluster along the trait axis. Our suggestion for empirical studies is as follows: if only one spatial location is observed, caution in interpreting multiple clumps on the trait axis is of course required, as Barabás et al (2013) highlighted. However, with several locations - or in a theoretical context - one could average across locations to reproduce similar graphs to the ones produced here. Clumps in the trait axis when averaged across model runs/locations is therefore a signature of the storage effect for the cases that we considered in the article. Of course, other mechanisms that we did not include in our models may produce similar patterns (Rael et al, 2018). Still, clustering on the trait axis, in scenarios where the environment fluctuates strongly in time, suggests that storage effects could be at work.

In our previous empirical study of coastal phytoplankton dynamics (Barraquand et al, 2018), we did not find any storage effect (which does not mean that it could not be observed in other systems).

334 Given the results on species richness and composition presented here, we are skeptical that the
335 storage effect alone could help explaining phytoplankton diversity. However, our results suggest
336 that in phytoplankton-like seasonal environments, even though empirically-based self-regulation
337 produce much more diversity than the storage effect when considered in isolation, the storage effect
338 can help diversity maintenance when combined to other mechanisms. Indeed, the combination
339 storage effect + strong self-regulation is non-additive: the cases where both self-regulation and the
340 storage effect were present showed more diversity than generated by any mechanism on its own.

341 The above results suggest the very exciting idea that multiple coexistence mechanisms might
342 combine superadditively, thus helping us to better understand the astounding diversity of primary
343 producers. This logic could, in principle, be extended to mechanisms that we have not considered
344 here (e.g., spatial structure, specialized natural enemies, that could be as important here for plank-
345 ton as they are for tropical trees, see Bagchi et al, 2014; Comita et al, 2014; Barraquand et al, 2017).
346 Previous research has however demonstrated that generalist seed predation could weaken the stor-
347 age effect (Kuang and Chesson, 2009, 2010) thus different mechanisms might not always combine
348 superadditively as we found here. That said, superadditivity has been found in some cases, i.e.,
349 pathogens could enhance the storage effect (Mordecai, 2015). Better explaining plant or microbial
350 diversity would then not be about selecting the best unique mechanism susceptible to explain the
351 observed diversity, but rather better combining those mechanisms together. This may obviously
352 be an annoyance for those who like to sharpen Occam's razor, but it clearly holds opportunities
353 for theoreticians wishing to investigate synergies between coexistence mechanisms in highly di-
354 verse communities. Aside from the synergies between predator diversity-enhancing effects, [strong](#)
355 [self-regulation through various means](#) and ~~SNDs~~ or storage effects (on the temporal axis), one
356 obvious follow-up of this research would be interactions with spatial structure. Spatial structure
357 occurs both endogeneously, through spatially restricted movements and interactions, and exoge-
358 neously, through spatial variation in environmental covariates (Bolker, 2003). Numerous studies
359 (e.g., Bolker and Pacala, 1999; Murrell and Law, 2002) have shown that spatially restricted move-
360 ments and interactions - very small-scale spatial structure - can help coexistence, which we believe
361 would be especially important for phytoplankton since many species form colonies (Reynolds, 2006;

see discussion in Barraquand et al, 2018). Moreover, although temperature is usually relatively spatially homogeneous over space, other drivers (e.g., rainfall, pH in terrestrial ecosystems; salinity in aquatic ones) may exhibit spatial variation which is a main factor for coexistence (Snyder, 2008). The odds that different (resource) niches, natural enemies, spatial limits to competition and temporal niche partitioning all interact to promote the very high-dimensional coexistence observed in the field seem much higher than for any of those mechanisms alone. Whether the diversity-enhancing effects of these mechanisms combine sub-additively (as in Kuang and Chesson, 2010) or super-additively like here is therefore worthy of further research.

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