Theoretical Ecology

How self-regulation, the storage effect and their interaction contribute to coexistence in stochastic and seasonal environments
--Manuscript Draft--

Manuscript Number:	THEE-D-18-00042R2
Full Title:	How self-regulation, the storage effect and their interaction contribute to coexistence in stochastic and seasonal environments
Article Type:	Original Article
Keywords:	coexistence; seasonality; competition; phytoplankton; Lotka-Volterra; storage effect
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Funding Information:	Agence Nationale de la Recherche (ANR-10-LABX-45) — Not applicable

| Abstract: | Explaining coexistence in species-rich communities of primary producers remains a challenge for ecologists because of their likely competition for shared resources. Following Hutchinson's seminal suggestion, many theoreticians have tried to create diversity through a fluctuating environment, which impairs or slows down competitive exclusion. However, fluctuating-environment models often only produce a dozen of coexisting species at best. Here, we investigate how to create richer communities in fluctuating environments, using an empirically parameterized model. Building on the forced Lotka-Volterra model of Scranton and Vasseur (2016), inspired by phytoplankton communities, we have investigated the effect of two coexistence mechanisms, namely the storage effect and higher intra- than interspecific competition strengths (i.e., strong self-regulation). We tuned the intra/inter competition ratio based on empirical analyses, in which self-regulation dominates interspecific interactions. Although a strong self-regulation maintained more species (50%) than the storage effect (25%), we show that none of the two coexistence mechanisms considered could ensure the coexistence of all species alone. Realistic seasonal environments only aggravated that picture, as they decreased persistence relative to a random environment. However, strong self-regulation and the storage effect combined superadditively so that all species could persist with both mechanisms at work. Our results suggest that combining different coexistence mechanisms into community models might be more fruitful than trying to find which mechanism best explains diversity. We additionally highlight that while biomass-trait distributions provide some clues regarding coexistence mechanisms, they cannot indicate unequivocally which mechanisms are at play. |

How self-regulation, the storage effect and their interaction contribute to coexistence in stochastic and seasonal environments

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February 1, 2019

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Abstract

Explaining coexistence in species-rich communities of primary producers remains a challenge for ecologists because of their likely competition for shared resources. Following Hutchinson's seminal suggestion, many theoreticians have tried to create diversity through a fluctuating environment, which impairs or slows down competitive exclusion. However, fluctuating-environment models often only produce a dozen of coexisting species at best. Here, we investigate how to create richer communities in fluctuating environments, using an empirically parameterized model. Building on the forced Lotka-Volterra model of Scranton and Vasseur (2016), inspired by phytoplankton communities, we have investigated the effect of two coexistence mechanisms, namely the storage effect and higher intra- than interspecific competition strengths (i.e., strong self-regulation). We tuned the intra/inter competition ratio based on empirical analyses, in which self-regulation dominates interspecific interactions. Although a strong self-regulation maintained more species (50%) than the storage effect (25%), we show that none of the two coexistence mechanisms considered could ensure the coexistence of all species alone. Realistic seasonal environments only aggravated that picture, as they decreased persistence relative to a random environment. However, strong self-regulation and the storage effect combined superadditively so that all species could persist with both mechanisms at work. Our results suggest that combining different coexistence mechanisms into community models might be more fruitful than trying to find which mechanism best explains diversity. We additionally highlight that while biomass-trait distributions provide some clues regarding coexistence mechanisms, they cannot indicate unequivocally which mechanisms are at play.

Number of words: 239

1 Introduction

The continued maintenance of diversity in spite of widespread competition has long bewildered ecologists, especially for primary producers such as phytoplankton that share the same basic resources (Hutchinson, 1961). A solution for the 'paradox of the plankon' was proposed by Hutchinson: temporal variation of the environment. By making the identity of the fittest species change over time, temporal variation could render competitive exclusion less likely, which was confirmed by early experiments (Sommer, 1984). However, it has been shown later that inclusion of temporal variability *per se* in competition models is not sufficient for maintaining a realistic diversity (Chesson and Huntly, 1997; Fox, 2013). Additional mechanisms such as the storage effect (Chesson, 1994; Ellner et al, 2016) or a relative nonlinearity of competition (Armstrong and McGehee, 1980; Chesson, 2000; Descamps-Julien and Gonzalez, 2005; Jiang and Morin, 2007; Fox, 2013) need to be introduced for diversity to maintain. Moreover, richness rarely exceeds a handful to a dozen of species in modeled competitive communities in fluctuating environments, except when external inputs from immigration sustain diversity (e.g., Huisman et al, 2001; Jabot and Lohier, 2016). To our knowledge, the effect of temporal variability on persistence in competition models has mostly been examined in theoretical communities of 2 to 3 species (e.g., Chesson and Huntly, 1997; Litchman and Klausmeier, 2001; Li and Chesson, 2016; Miller and Klausmeier, 2017).

One of the richest modeled communities that we identified can be found in Scranton and Vasseur (2016), which is based on temperature variation and different thermal optima for each species (Moisan et al, 2002). In this model, the synchronizing effect of the environment and the storage effect can maintain 12 phytoplankton-like species on average. Scranton and Vasseur (2016) described daily temperature as a random noise, i.e., independent and identically distributed Gaussian random variates over time. However, under most latitudes, seasonality drives part of the environmental variation: over short timescales, random temporal variations often only add noise to a largely deterministic seasonal trend (Scheffer et al, 1997; Boyce et al, 2017; Barraquand et al, 2018).

Seasonal forcing of parameters can strongly affect the dynamics of model communities by synchronizing species to the seasonal signal or even promoting oscillations with lower frequency (Rinaldi et al, 1993; Barabás et al, 2012; Miller and Klausmeier, 2017; Vesipa and Ridolfi,

2017). How seasonality affects coexistence, as opposed to a randomly fluctuating environment, is therefore a key feature of this paper. Our present work can be seen as an attempt to blend Scranton and Vasseur (2016)'s stochastic framework with the periodic environments of Barabás et al (2012), to better represent the mixture of stochastic and deterministic environmental forces affecting phytoplankton community dynamics.

What other key features of field communities should be considered when modeling phytoplankton? Strong self-regulation, with intraspecific competition much stronger than interspecific interactions, has been found to be widespread in terrestrial plant communities (Adler et al, 2018), animal communities (Mutshinda et al, 2009), and phytoplanktonic communities (Barraquand et al, 2018). We will therefore insert those niche differences, manifesting as strong self-regulation, into our models of phytoplankton competition. The interaction between environment variability and niche overlap was investigated by Abrams (1976) but his results did not extend to communities more diverse than 4 species; our objective is therefore to see how those mechanisms interact for species-rich communities.

Niche models have often been opposed to the neutral theory (Hubbell, 2001), where dispersal and drift can ensure a transient coexistence of many species, but several authors have attempted to blend niche and neutral processes (Gravel et al, 2006; Scheffer and van Nes, 2006; Carmel et al, 2017). An intriguing offshoot of these attempts is the concept of 'clumpy coexistence' (Scheffer and van Nes, 2006), whereby simultaneous influences of both niche and neutral processes create several clumps of similar species along a single trait axis. Niche differences enable coexistence of multiple clumps (Chesson, 2000) while within-clump coexistence occurs through neutral processes. This 'emergent neutrality' within groups (Holt, 2006) has been proposed as a unifying concept for niche and neutral theories (even though the neutrality of the original model has been disputed due to hidden niches, Barabás et al, 2013). Since then, clumpy coexistence has been shown to occur in theoretical models incorporating a temporally variable environment interacting with a thermal preference trait axis (Scranton and Vasseur, 2016; Sakavara et al, 2018). The relationship (or absence thereof) between biomass-trait distributions and coexistence mechanisms is currently debated (D'Andrea and Ostling, 2016), although there are suggestions that clustering on trait axes under competition may be a robust find (D'Andrea et al, 2018, 2019).

4

Here, we try to establish what are the relative contributions to coexistence of the storage effect vs strong self-regulation, in a phytoplankton-like theoretical community model with a large number of species. This led us to cross combinations of seasonality vs randomness in the forcing signal, presence of the storage effect or not, and intra- vs interspecific competition intensity, in order to disentangle the contributions of these factors to biodiversity maintenance and their potential interactions. Alongside the resulting species richness, we also report which biomass-trait distribution can be expected under a given combination of processes leading to coexistence.

2 Methods

Models

The model described in Scranton and Vasseur (2016) is based on the Lotka-Volterra competition model. Fluctuations in the environment are introduced in the model by temperature-dependent intrinsic growth rates (see Eq. 1-2, all coefficients are defined in Table 1) so that the community dynamics can be expressed as:

$$\frac{dN_i}{dt} = r_i(\tau)N_i\left(1 - \sum_{j=1}^{S} \alpha_{ij}N_j\right) - mN_i \quad (1)$$

$$r_i(\tau) = a_r(\tau_0)e^{E_r\frac{(\tau-\tau_0)}{k\tau\tau_0}}f_i(\tau) \quad (2)$$

$$\text{where } f_i(\tau) = \begin{cases} e^{-|\tau-\tau_i^{opt}|^3/b_i}, & \tau \leq \tau_i^{opt} \\ e^{-5|\tau-\tau_i^{opt}|^3/b_i}, & \tau > \tau_i^{opt} \end{cases} \quad (3)$$

$$\text{and } b_i \text{ is defined by numerically solving } \int r_i(\tau)d\tau = A \quad (4)$$

Model parameters are detailed in Table 1, and we set their values to match the features of phytoplankton communities as in Scranton and Vasseur's work (2016). The niche of each species is defined by its thermal optimum τ_i^{opt}. Thermal performance curves defined in Eq. 3 are parameterized so that all species share the same niche area (Eq. 4), which sets a trade-off between maximum growth rates and niche width.

The original environmental forcing is a normally distributed variable centered on 293 K

5

Table 1: Parameter definitions and values for the model described in Eqs. 1-4. Parameter values are not specified when they vary over time and/or with the species considered.

Name	Definition	Value (unit)
S	Initial number of species	60 (NA)
N_i	Biomass density of the ith species	(kg/area)
τ	Temperature	(K)
$r_i(\tau)$	Growth rate of species i as a function of temperature	$(\frac{\text{kg}}{\text{kg} \times \text{year}})$
α	Strength of competition	0.001 (area/kg)
b_i	Normalization constant for the thermal decay rate	(K^3)
m	Mortality rate	$15(\frac{\text{kg}}{\text{kg} \times \text{year}})$
τ_0	Reference temperature	293 (K) / 20 (°C)
$a_r(\tau_0)$	Growth rate at reference temperature	$386(\frac{\text{kg}}{\text{kg} \times \text{year}})$
E_r	Activation energy	0.467 (eV)
k	Boltzmann's constant	$8.6173324.10^{-5}(\text{eV.K}^{-1})$
$f_i(\tau)$	Fraction of the maximum rate achieved for the ith species	(NA)
μ_τ	Mean temperature	293 (K)
σ_τ	Standard deviation for temperature	5 (K)
$\tau_{\min}$	Minimum thermal optimum	288 (K)
$\tau_{\max}$	Maximum thermal optimum	298 (K)
A	Niche breadth	$10^{3.1}(\frac{\text{kg}}{\text{kg} \times \text{year}})$
τ_i^{opt}	Thermal optimum for growth of the ith species	(K)
θ	Scaling between random and seasonal noise	(0;1.3) (NA)
κ	Ratio of intra-to-interspecific competition strength	(1;10) (NA)

(20°C), with a 5 K dispersion. Temperature varies from one day to the next, but is kept constant throughout the day. At and above the daily scale, temperature could therefore be considered as a white noise (Vasseur and Yodzis, 2004). However, from a mathematical viewpoint, the noise is slightly autocorrelated as the integration process goes below the daily time step. We therefore use the expression 'random noise' to describe this forcing, as opposed to the 'seasonal noise' described hereafter. To construct the seasonal noise, we add to the random forcing signal a lower-frequency component, using a sinusoidal function with a period of 365 days (Eq. 5). We tune the ratio of low-to-high frequency with the variable θ so as to keep the same energy content - i.e., equal total variance - in the forcing signal.

$$\tau(t) = \mu_\tau + \theta\sigma_\tau \sin{(2\pi t)} + \epsilon_t, \text{where } \epsilon_t \sim \mathcal{N}\left(0, \sigma_\tau\sqrt{1 - \frac{\theta^2}{2}}\right) \tag{5}$$

Note that the upper limit for θ, $\sqrt{2}$, corresponds to a completely deterministic model which we do not explore here (but see Zhao (1991) proving bounded coexistence). We choose to keep the stochasticity in the signal and to model a plausible temperature signal with $\theta = 1.3$

6

(illustrated in Fig. 1b) when considering a seasonal forcing of the dynamics.

The formulation of the forced Lotka-Volterra model of Scranton and Vasseur (2016) implies a storage effect, as the net effect of competition exerted by species j on i is the product of the temperature-related growth rate $r_i(\tau)$ and the competitive strength α_{ij} exerted by species j multiplied by its abundance N_j. Therefore, total net competition $(\sum_{j=1}^{S} r_i(\tau)\alpha_{ij}N_j)$ covaries positively with the growth rate values $r_i(\tau)$, which defines the storage effect (Chesson, 1994; Fox, 2013; Ellner et al, 2016). To remove the assumption of an explicit storage effect, we create another version of the model using the mean value of a species' growth rate ($\bar{r}_i$) to weight the interaction coefficients (see Eq. 6). The mean growth rate value is computed by first generating the temperature time series and then averaging all r_i over the corresponding sequences of τ values.

$$\frac{dN_i}{dt} = N_i\left(r_i(\tau) - \sum_{j=1}^{S} \bar{r}_i\alpha_{ij}N_j\right) - mN_i \tag{6}$$

Following Eq. 6, net competition remains unaffected by the environmental conditions, in contrast to intrinsic growth rates, while preserving the same average magnitude of competition as in Eq. 1.

Strong self-regulation is ensured by the addition of the coefficient κ, which is the ratio of intra-to-interspecific competition strength. We can therefore re-write the interaction coefficients α_{ij} in Eq. 7

$$\alpha_{ij} = \alpha\left(1 + (\kappa - 1)\delta_{ij}\right) \tag{7}$$

where δ_{ij} is the Kronecker symbol, equal to 1 if $i = j$ and to 0 otherwise. The value of the parameter $\kappa = 10$ was chosen from analyses of phytoplanktonic data (Barraquand et al, 2018). Hereafter, the expression "strong self-regulation" characterizes dynamics where the intraspecific competition strength is 10 times higher than the interspecific competition strength, as opposed to "equal competitive strengths" where intra- and interspecific competition strengths are equal.

In addition to two types of environmental forcings (random noise with $\theta = 0$, and seasonal noise with $\theta = 1.3$), we compare the results for four versions of the original model: with and without an explicit storage effect (Eq. 1 and Eq. 6, respectively); with strong self-regulation or

equal intra- and inter-competition strength ($\kappa = 10$ or $\kappa = 1$, respectively). These are summed

145 up in Table 2.

$\frac{1}{N_i}\frac{dN_i}{dt} + m_i$	Storage effect	No storage effect
Strong self-regulation ($\kappa = 10$)	$r_i(\tau)\left(1 - \sum_{j=1}^{S} \alpha\left(1 + 9\delta_{ij}\right)N_j\right)$	$r_i(\tau) - \sum_{j=1}^{S} \bar{r}_i\alpha\left(1 + 9\delta_{ij}\right)N_j$
Equal competitive strengths ($\kappa = 1$)	$r_i(\tau)\left(1 - \sum_{j=1}^{S}\alpha N_j\right)$	$r_i(\tau) - \sum_{j=1}^{S}\bar{r}_i\alpha N_j$

Table 2: Growth rate of species i in the four models

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Set-up

147 We replicate the 'Species sorting' experiment of Scranton and Vasseur (2016) so as to investigate

149 how the structure of synthetic phytoplankton communities varies under the different scenarios

150 we described above. We focus on the dynamics of a community initialized with 60 species with

151 thermal optima uniformly spaced along the interval [15℃, 25℃], and with the same initial

152 density $\left(\frac{1}{\alpha S}\right)$. Each simulation is run for 5000 years in 1-day intervals. When the density of a

153 species drops below 10^{-6}, it is considered extinct. For each combination of parameters (type

154 of environmental signal, storage effect and self-regulation), we run 100 simulations.

155 All simulations are run with Matlab's ode45 algorithm, an adaptive Runge-Kutta (4,5)

156 integration scheme with an absolute error tolerance of 10^{-8}, and relative error tolerance of

157 10^{-3}. The code is available in a GitHub repository[1] .

3 Results

159 Typical dynamics of the community following Eq. 1 (the model of Scranton and Vasseur,

160 2016), with both a purely Gaussian noise (original choice of Scranton and Vasseur, 2016; Fig.

161 1a) and a seasonal noise described in Eq. 5 (our variant, Fig. 1b), are shown in Fig. 1c and

162 d, respectively. A sinusoidal forcing produces the strongly seasonally structured dynamics that

163 are typical of phytoplankton. Even though only 5 species can be seen in Fig. 1c, there were 14

164 species still present at the end of the simulation forced by a random noise, with large disparities

165 in the range of their biomasses. A third of the species kept a biomass above 10 kg/area (setting

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[1]https://github.com/CoraliePicoche/Seasonality

area = 1 ha, with a depth of a few meters, produces a realistic standing biomasses; Reynolds, 2006) while 6 out of the 14 species biomasses remained below the unit. All persisting species in the random noise simulation were clustered within a 3.2°C-range of thermal optima (see the biomass distribution as a function of the thermal optimum in Electronic Supplementary Material, Fig. A1). No obvious temporal patterns (e.g., cycles) could be seen in the community forced by random noise. On the contrary, seasonal cycles were clear in the seasonally-forced case of Fig. 1d. Only 4 species coexisted at the end of the simulation with seasonal noise, gathered in two groups with large thermal optimum differences (5.7°C between the maximum thermal optimum of the first group and the minimum thermal optimum of the second group). When temperatures were high, the group with higher thermal optima reached its maximum biomass, then as temperature decreases through the season, these species leave room for the growth of the low-temperature group.

The decrease in persistence due to seasonality observed in Fig. 1 was confirmed in all our simulations (Fig. 2). In cases where final species richness varied from one simulation to another (namely, the two middle cases in Fig. 2: with storage effect but without strong self-regulation, or without storage effect but with strong self-regulation), seasonality reduced the number of extant species to, on average, 27% and 48% of their original values, respectively (Fig. 2). A seasonal signal therefore led to a much smaller average persistence. There was also less variance in persistence between seasonally forced simulations compared to random noise simulations.

Both a strong self-regulation and the storage effect markedly increased persistence. Without any of these coexistence mechanisms, only one species persisted at the end of the simulations. When only the storage effect was present, the number of extant species varied between 8 and 20 (14.8 ± 2.4) with random noise, or 2 and 6 (4.1 ± 0.7) with a seasonal signal. On the other hand, when only a strong self-regulation was present, the number of extant species nearly doubled, varying between 20 and 32 (27.5 ± 2.4), or 12 and 15 (13.3 ± 0.6), with a random or a seasonal noise, respectively. Remarkably, when the storage effect and a strong self-regulation both affected the community dynamics, all species persisted in the community: the number of species coexisting with both mechanisms present is greater than the sum of the species coexisting with either mechanism alone. The two mechanisms therefore combine superadditively, as their interaction has a positive effect on the richness of the community.
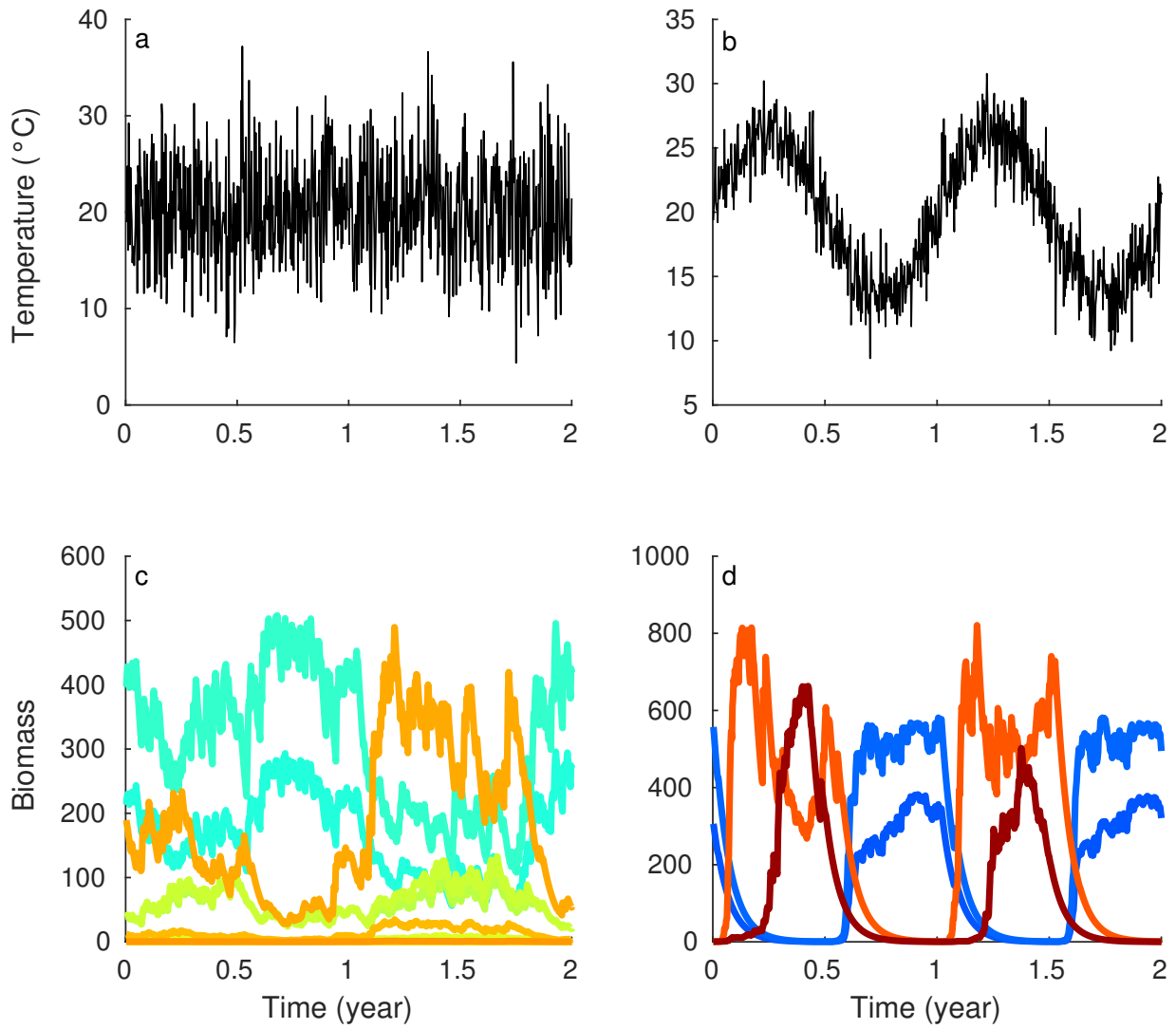
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Figure 1: Time series of temperature (top; a-b) and extant species (bottom; c-d) for the 2 last years of a 5000-year simulation, with storage effect but no differences between intraspecific and interspecific competition strengths. The forcing temperature is either a random noise (a) or a seasonal noise (b), leading to community dynamics with more erratic fluctuations (c) vs seasonally structured fluctuations (d). Line colors of species biomasses correspond to their thermal optimum (from blue, corresponding to low thermal optimum, to red, corresponding to high thermal optimum).

The trait-biomass distribution of the community was affected by the type of forcing even when the richness of the community was stable (Fig. 3). Without storage effect nor strong self-regulation, there was only one species left at the end of the simulations. A random noise favored species with intermediate thermal optima: the final species had a thermal optimum between 18.9°C and 21.4°C (only a fourth of the initial range of thermal optima) for two simulations out of three and the maximum final biomasses over 100 simulations was reached in this range (Fig. 3a). This distribution may indicate a selection for the highest long-term growth rates, averaged over time (see scaled growth rates in Fig. 3). Seasonality with no coexistence mechanisms also
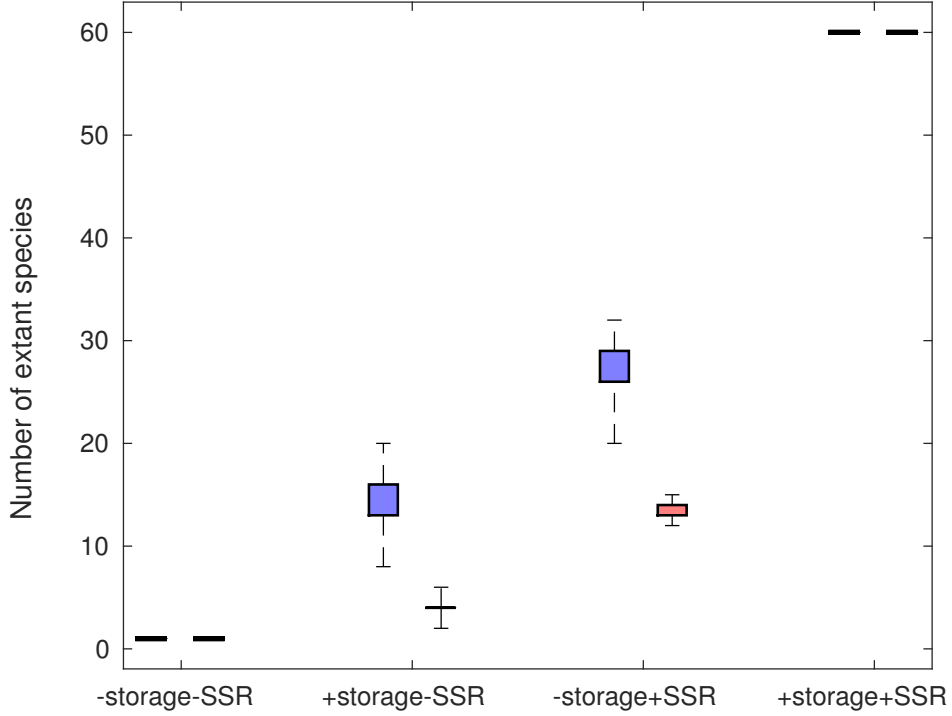
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Figure 2: Number of species still present at the end of 100 simulations (5000 years each), initialized with 60 species, with a random (blue) or a seasonal forcing signal (red). The signs + or -storage refer to presence or absence of the storage effect, respectively; + / - SSR, presence or absence of Strong Self-Regulation, respectively. Community compositions are stable in the cases -storage-SSR and +storage+SSR, for which 1 or 60 species are still present at the end of all simulations, respectively. Due to low variance, the whiskers here represent min and max rather than 1.5 interquartile range.

led to a single final species but, in this case, the species always had a higher maximum growth rate (thermal optimum above 22°C). Species with a higher thermal optimum were more likely to persist and to reach a higher biomass at the end of the simulation. 38% of the simulations therefore ended with the species having the highest temperature optimum, 25°C. The shift in trait distribution towards higher maximum growth rates with a seasonal noise vs higher average growth rates with a random noise was consistent for all model types considered.

When both the storage effect and strong self-regulation were present, the 60 initial species coexist with almost no variation in their respective biomasses from one simulation to the next (mean CV across simulations is 0.008, averaged across species, Fig. 3b and d). The forcing signal modified only the distribution of biomasses, resulting in contrasted community structures despite equal richness. With a random noise, the distribution was unimodal. On the contrary, a seasonal signal led to a bimodal distribution (centered on 17.0°C and 24.4°C), each corresponding to one season, with highest biomasses for higher thermal optima (Fig. 3d). The

11

minimum biomass was reached for the highest long-term average growth rate at an intermediate temperature (20.4°C).
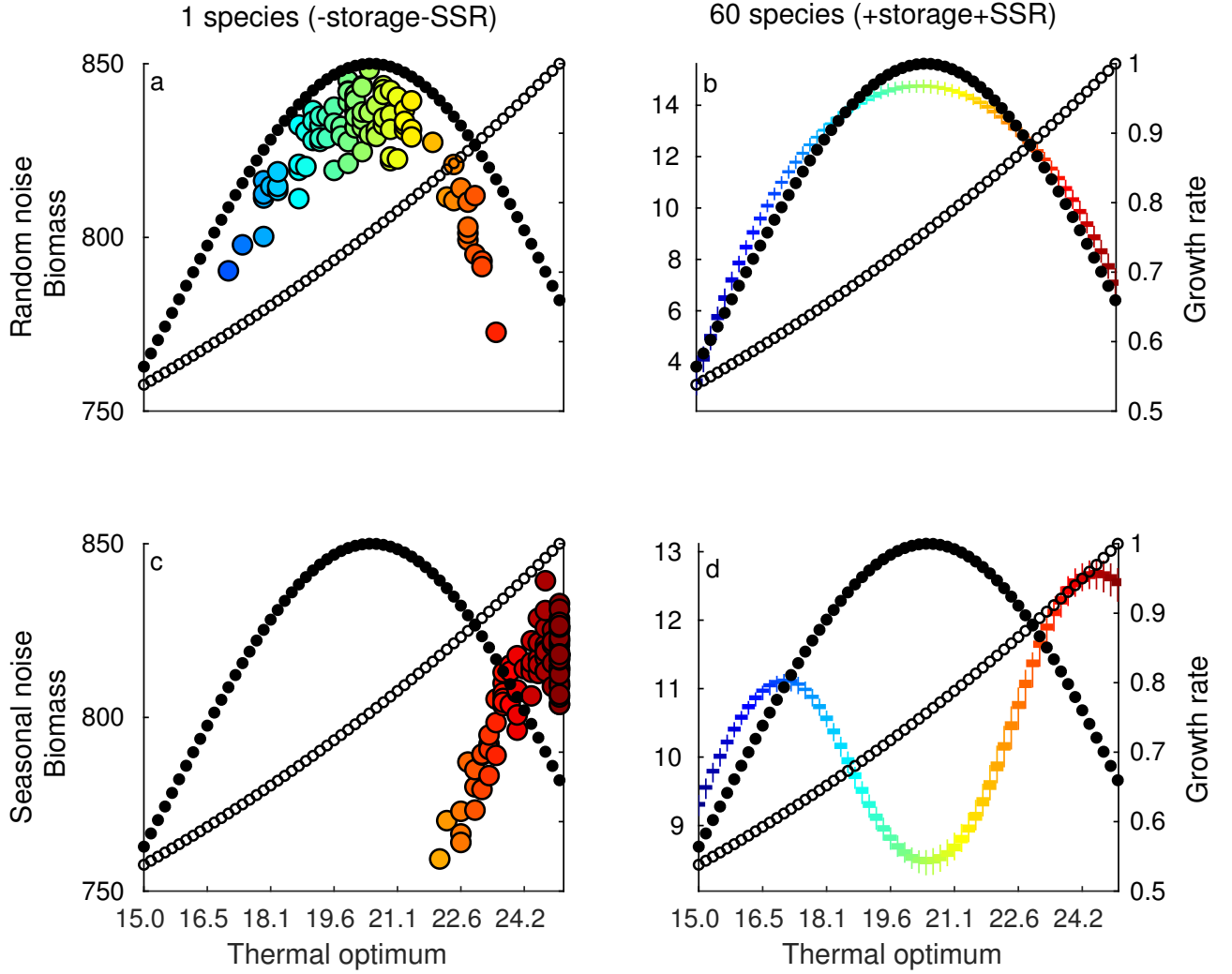

Figure 3: Mean biomass distribution over the last 200 years for 100 simulations, as a function of the species thermal optima. Here we consider the two stable-composition cases and two types of forcing signal. On the left column, simulations without storage effect nor strong self-regulation are presented. Only one species is present at the end of the simulations and its mean value is represented by one large colored circle per simulation. There can be several circles for the same species, corresponding to multiple simulations ending with this species alone. On the right column, simulations with storage effect and strong self-regulation are represented. All species are present at the end of the simulations and small boxplots present the variation in the temporal average of biomass with a given trait, for 100 simulations. The forcing signal is either a random (top) or a seasonal noise (bottom). Each species is identified by its thermal optimum through its color code. Scaled (divided by maximum) average and maximum growth rates are shown as small filled and open circles, respectively, and are indexed on the right y-axis.

In cases where the richness of the community varied, the overall shape (multimodal vs unimodal) of the marginal distribution of extant species with respect to the trait axis were similar for both types of environmental forcings (Fig. 4). By contrast, the type of coexistence mechanism generated different shapes. Indeed, the storage effect (when acting alone) led to

12

a multimodal biomass distribution with respect to thermal optima. We always observed 3 modes with a random noise and 3 modes in 95% of the seasonal simulations (Fig. 4a). With a random noise, extant species were grouped in rather similar clumps regarding species thermal optima (between 18.8°C and 22.2°C) whereas species tended to be further apart in the seasonal case, covering a total range of 7.7°C, with species grouping in the higher part of the thermal range, above 22°C. On the other hand, strong self-regulation led to a quasi-uniform biomass distribution (Fig. 4 b). Species in communities forced by a random noise stayed in the lower range of thermal optima (in 96% of the simulations, the highest thermal optimum was 22.4°C, see Fig. A2 in Electronic Supplementary Material) while they were filtered out in communities subjected to a seasonal fluctuation of their environment, for which species with thermal optima above 20.5°C persisted. As before (Fig. 3 c,d), seasonality promoted species with a higher maximum growth rate, since the autocorrelated temperatures enabled them to achieve this highest growth rate for a longer period of time than a random noise would have.

4   Discussion

We have simulated competitive Lotka-Volterra dynamics forced by a fluctuating temperature under a range of scenarios allowing more or less coexistence. Two coexistence mechanisms, the storage effect and strong self-regulation (i.e., intraspecific competition much stronger than interspecific competition), could be either present or absent, which led to four scenarios. These four scenarios were crossed with two possibilities for the forcing signal, a random noise (mostly white) and a stochastic yet seasonal signal, both with equal temporal variance. Our investigation therefore built on the model of Scranton and Vasseur (2016), which included a random forcing signal and a storage effect, but considered seven additional combinations of mechanisms. This was motivated by our wish to include two observed features of phytoplankton dynamics: seasonal cycles (Winder and Cloern, 2010; Boyce et al, 2017) and strong self-regulation (Chesson, 2000; Adler et al, 2010; Barraquand et al, 2018). Many mechanisms can lead to intraspecific competition being stronger than interspecific competition: nonlinearities in the functional forms of competition or mutualism that contribute to increasing self-regulation (Kawatsu and Kondoh, 2018), or predation as well as parasitism (see e.g., the generalist predators in Haydon, 1994). Strong self-regulation seems an ubiquitous feature in competition networks of primary
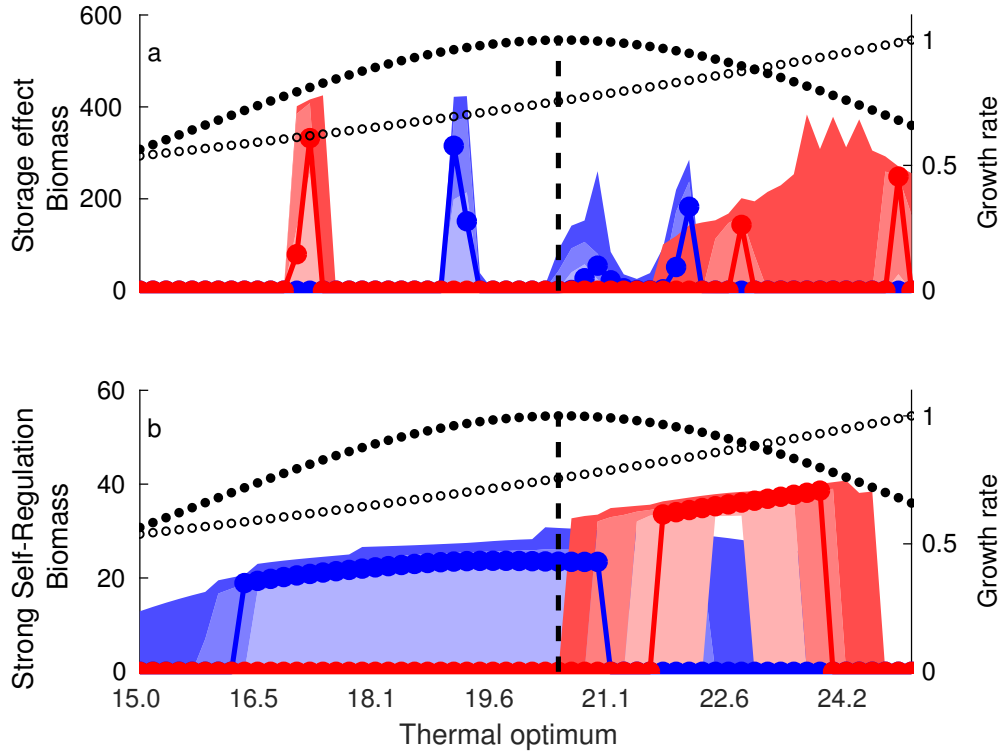
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Figure 4: Mean biomass distribution over the last 200 years for 100 simulations, as a function of thermal optima, (a) with storage effect and equal competitive strengths and (b) without storage effect, with strong self-regulation. The forcing signal is either a random (in blue) or a seasonal noise (in red). Shades of the same color correspond to the 50th, 90th and 100th percentiles of the distributions while colored lines correspond to one representative simulation. Scaled (divided by maximum) average and maximum growth rates are shown as filled and open and circles, respectively, and indexed on the right y-axis. The maximum average growth rate is indicated by the dashed line.

producers (Adler et al, 2018), and perhaps even more general networks (Barabás et al, 2017).

Before discussing the ecological interpretation of our results, we first recall some technical assumptions made in this study. All our simulations lasted for a fixed duration (5000 timesteps) as in Scranton and Vasseur (2016). While short- and medium-term transients (a few years to hundreds of years) are completely negligible at the end of the time series, very long transients can remain in this class of models (Scheffer and van Nes, 2006; Hastings et al, 2018): these are not mere artefacts but instead traduce the fact that some processes (e.g., exclusion of a species) can be really slow. We realized that convergence was incomplete after 5000 years in some cases (e.g., random noise + storage effect + equal competitive strength). Such simulations would take up to 15 000 years to converge and the rate of convergence would slow over time. We could have considered longer time intervals, but comparison with the values reported by

14

Scranton and Vasseur (2016) would then have been compromised. Another way to shorten the transients, suggested by a referee (GB), is to vary the mortality parameter. This did not alter the conclusions (see Appendix B in Electronic Supplementary Material). Unfortunately, added variability also shifts the model further away from neutral dynamics (when intra and interspecific competition strengths are equal), which renders comparisons difficult. All things considered, we therefore kept the 5000-year time window for integration.

Another strong assumption pertains to competition coefficients. To allow for comparison with Scranton and Vasseur (2016), we did not introduce variability in intraspecific competition strength or interspecific competition strength. By contrast, data-based coefficients vary between species (Barraquand et al, 2018), with a majority of weak interactions (as suggested in Wootton and Emmerson, 2005) and more variance in intraspecific coefficients. Stump (2017) recently considered the potential effects of competition coefficient variability (also called non-diffuse competition), as did Kokkoris et al (2002); more variance in interspecific competition strength is usually detrimental to coexistence for an equal amount of self-regulation (see Stump (2017) for a classification of the various effects). Setting the competition coefficients using a multidimensional trait-based framework, like that of Ashby et al (2017), would provide a natural development to the work presented here; it is in our opinion difficult to speculate on those variance effects because both intra- and interspecific competition coefficient variances may matter to community persistence.

Finally, our study is limited to communities whose species have fast population dynamics relative to the yearly timescale, like phytoplankton and likely other fast-living organisms, so that many generations can occur in a year. Persistence in community with slower dynamics may be affected differently by seasonality (Miller and Klausmeier, 2017). This especially true for species with generations that extend over multiple years. In models where trophic interactions are implemented, seasonality has been shown to promote multiyear cycles and the existence of chaotic attractors (Rinaldi et al, 1993; Taylor et al, 2013; Tyson and Lutscher, 2016). These rich dynamics of consumers may feed back into the lower trophic levels: Dakos et al (2009) present a planktonic community with seasonally-entrained chaotic dynamics which may be partly due to zooplanktonic predation. Predation probably entails additional niche differences, possibly with an emerging self-regulation created by predation processes (Chesson, 2018), but it seems

15

unlikely that we would be able to generate such dynamics with the models presented in this article. Additional nonlinearities would be needed to create intrinsically variable and chaotic dynamics.

With these assumptions in mind, we have found that first, temporally forced Lotka-Volterra dynamics cannot sustain any diversity with our phytoplankton-based set of parameters, unless the structure is geared to include either a storage effect or a strong self-regulation. Although this absence of diversity-enhancing effect of "pure" environmental variation has already been stated by other authors (Chesson and Huntly, 1997; Barabás et al, 2012; Fox, 2013; Scranton and Vasseur, 2016), this is not always intuitive (Fox, 2013), so we feel compelled to stress it once more: temporal variation in growth rate alone cannot help coexistence within competitive communities. A nice point made by Scranton and Vasseur (2016) was that a built-in storage effect in a forced Lotka-Volterra model, parameterized for phytoplankton communities, could lead to a reasonable degree of coexistence. Our investigation reproduced these results, using the random noise considered by Scranton and Vasseur (2016). However, an arguably more lifelike noisy and seasonal temperature forcing considerably lessened the richness of the community after 5000 years, decreasing from 15 to 4 species on average. Even imagining that groups represented here are genera or classes rather than species, this is a fairly low diversity for a phytoplankton-like community (see e.g., Chapter 1 in Reynolds, 2006). This suggests that the storage effect may not, on its own, be sufficient to maintain species-rich communities (e.g., dozens to hundreds of species). We have therefore sought out whether a stronger self-regulation could maintain a higher diversity, using field-based intra- vs intergroup (species or genera) competition strength ratio (Barraquand et al, 2018), where the intragroup density-dependence was estimated 10 times stronger. Implementing such strong self-regulation, in the forced Lotka-Volterra models that we considered, produced a higher level of diversity than the storage effect (almost double). Of course, the result is somehow contingent upon the strength of self-regulation. Our estimates are a little stronger than what was found in perennial plants (Adler et al, 2010), where interspecific competition was suggested 4 or 5 times stronger than intraspecific. Still, the widespread effects of natural enemies in phytoplankton (zooplankton, parasites) may contribute to an increase in the self-regulation strength (Barraquand et al, 2018; Chesson, 2018) relative to other systems, hence we believe that 10 times stronger intraspecific

16

competition constitutes a reasonable order of magnitude.

However, such strong self-regulation was still insufficient to maintain the whole community diversity (60 species) by itself, especially when the seasonal forcing was considered (always decreasing species richness). The diversity within clumps of similar values of thermal optima was considerably decreased once seasonality was implemented. This diversity reduction occurs because within a season, the signal autocorrelation gives long, contiguous time intervals to the best competitor to exclude its less adapted competitors. This makes the results likely to hold not only for seasonal environments, but more generally for autocorrelated ones above the daily scale, i.e., "red" noise. In contrast, the random noise scenario – which can be considered white noise above the daily temporal scale – generates large temperature shifts more frequently, and thereby forbids such competitive exclusion. In a seasonal setting, a species with the highest long-term (arithmetically) averaged growth rate may not be the best competitor, and can disappear as a result of a strong competition from both low- and high-temperature tolerant species. This holds with or without a storage effect.

Our results may appear at odds with recent proposals that seasonal forcing in itself would help maintain diversity (Sakavara et al, 2018). However, we compared the effect of seasonal forcing to that of other forcing signals while controlling for total variance. Thus, the contrast between our results and those of Sakavara et al (2018) may be due to the role of forcing variance over time: we compare scenarios under a constant total variance, much like what is done when examining the effect of noise color on population and community dynamics (Jiang and Morin, 2007; Ruokolainen et al, 2009). Thinking in terms of signal spectrum, while seasonality may maintain slightly more diversity than no forcing at all if a storage effect is present, the reddening of the environmental noise due to such seasonality reduces coexistence. This result may be contingent upon the correlated positive responses of the species growth rate to increases in the environmental variable (Ruokolainen et al, 2009, and references therein).

The biomass-trait relationship was affected more marginally by the type of forcing signal. The storage effect alone begot several clumps along the trait space (as observed by Scranton and Vasseur, 2016). The seasonality that we added to the temperature signal led to more distant clumps on the trait axis, with less species per clump. Conversely, strong self-regulatory mechanisms alone led to relatively uniform biomass distributions, with species forming a sin-

gle large cluster, which covered a fraction of the initial trait space. Therefore, the shape of the distribution was mostly affected by the coexistence mechanism at work while the average trait value was modified by the type of environmental forcing, even though the mean value of the environmental signal did not change. However, when both strong-self regulation and the storage effect were at play, the biomass-trait distribution could either be unimodal or multimodal depending on the type of noise driving the community dynamics (random or seasonal, respectively). This implies that the mere observation of multimodality in a thermal preference trait-biomass distribution is not a proof of a storage effect, or conversely, the proof of the influence of a seasonal environment.

The identification of multiple modes in biomass-trait distributions is relatively recent (Segura et al, 2013; Loranger et al, 2018; D'Andrea et al, 2018, 2019), so we recommend to interpret them with caution to avoid over-generalization. Barabás et al (2013) convincingly argued that multimodality could arise from the demographic stochasticity of a single model run. However, with several locations - or in a theoretical context as done here - one could average across locations. There are additional reasons to be cautious: the occurrence of clustering is very sensitive to the shape of the competition kernel; small differences in shape can shift the distribution towards either clustered or uniform (Pigolotti et al, 2010). We therefore view clustering on the thermal preference trait axis as an interesting clue suggesting to look for a storage effect, rather than any definite proof that the storage effect is at work. Finally, we recall that we focus on a trait (thermal optimum) which clearly interacts with the environment: clustering may emerge on another trait axis, such as size, which typically affects the competition coefficient, without having any relationship to the storage effect (Segura et al, 2011, 2013; D'Andrea et al, 2018, 2019).

In our previous empirical study of phytoplankton dynamics (Barraquand et al, 2018), we did not find any storage effect. This does not mean that it could not be observed in other planktonic systems: we studied a coastal ecosystem and focused a specific fraction of phytoplankton: relatively large diatoms and dinoflagellates. However, given the consequences of the storage effect for species richness and composition presented here, we are skeptical that the storage effect could, by itself, fully explain phytoplankton diversity at any location. Our results suggest that in phytoplankton-like seasonal environments, empirically-tuned self-regulation produces much

18

more diversity than the storage effect, when both are considered in isolation. The storage effect may therefore help phytoplankton diversity maintenance, but only when combined to other mechanisms. This is all the more likely that in our models, the combination storage effect + strong self-regulation is non-additive: the cases where both self-regulation and the storage effect were present showed more diversity than generated by any mechanism on its own.

The above results suggest the very exciting idea that multiple coexistence mechanisms might combine superadditively to determine the richness of the community, thus helping us to better understand the astounding diversity of primary producers. This logic could, in principle, be extended to mechanisms that we have not considered here (e.g., spatial structure, specialized natural enemies, that could be as important here for plankton as they are for tropical trees, see Bagchi et al, 2014; Comita et al, 2014; Barraquand et al, 2018). Superadditivity, i.e. the positive effect of interactions between mechanisms can be measured either on community diversity, as we did here, or on the invasion growth rates (Ellner et al, 2019). Using the latter metric, previous research has however demonstrated that generalist seed predation could weaken the storage effect (Kuang and Chesson, 2009, 2010) thus different mechanisms might not always combine superadditively as we found here.That said, superadditivity has been found in some cases, i.e., pathogens could enhance the storage effect and broaden the conditions in which species could coexist (Mordecai, 2015). Better explaining plant or microbial diversity would then not be about selecting the best unique mechanism susceptible to explain the observed diversity, but rather better combining those mechanisms together. This may obviously be an annoyance for those who like to sharpen Occam's razor, but it clearly holds opportunities for theoreticians wishing to investigate synergies between coexistence mechanisms in highly diverse communities. Aside from the synergies between predator diversity-enhancing effects, strong self-regulation through various means and the storage effect (on the temporal axis), one obvious follow-up of this research would be interactions with spatial structure. Spatial structure occurs both endogeneously, through spatially restricted movements and interactions, and exogeneously, through spatial variation in environmental covariates (Bolker, 2003). Numerous studies (e.g., Bolker and Pacala, 1999; Murrell and Law, 2002) have shown that spatially restricted movements and interactions - very small-scale spatial structure - can help coexistence, which we believe would be especially important for phytoplankton since many species

19

form colonies (Reynolds, 2006; see discussion in Barraquand et al, 2018). Moreover, although temperature is usually relatively spatially homogeneous over space, other drivers (e.g., rainfall, pH in terrestrial ecosystems; salinity in aquatic ones) may exhibit spatial variation which is a main factor for coexistence (Snyder, 2008). The odds that different (resource) niches, natural enemies, spatial limits to competition and temporal niche partitioning all interact to promote the very high-dimensional coexistence observed in the field seem much higher than for any of those mechanisms alone. Whether the diversity-enhancing effects of these mechanisms combine subadditively (as in Kuang and Chesson, 2010) or superadditively like here is therefore worthy of further research.

Acknowledgements

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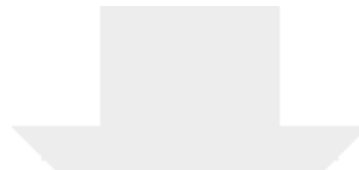
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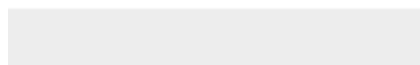
Dear Ms. Picoche:

We have received the reports from our advisors on your manuscript, "How self-regulation, the storage effect and their interaction contribute to coexistence in stochastic and seasonal environments", which you submitted to Theoretical Ecology.

Based on the advice received, your manuscript could be accepted for publication should you be prepared to incorporate minor revisions. When preparing your revised manuscript, you are asked to carefully consider the reviewer comments which are attached below and submit a list of responses to the comments.

The important point about differences between species raised by reviewer 2 needs to be addressed, as well as other more minor comments.

Your list of responses should be uploaded as a file in addition to your revised manuscript.

In order to submit your revised manuscript electronically, please access the following web site:

   https://thee.editorialmanager.com/

Click "Author Login" to submit your revision.

Please make sure to submit your editable source files (i.e. Word, Tex).

We look forward to receiving your revised manuscript on or before 08 Feb 2019.

Sincerely yours,

   Alan Hastings
   Theoretical Ecology

Dear Pr. Hastings,

We have now revised our manuscript according to the reviewers comments. We are grateful for their suggestions that helped to better highlight our results and to clarify the message of the manuscript. We answer their questions and remarks below, in bold font.

The referees required two major changes: sharpening the introduction, and checking the robustness of our results to the addition of between-species variability in the mortality parameter.

We reframed the introduction so that it better reflects the structure and contents of the article, as required by the referees. We now focus more on coexistence mechanisms in a

temporally variable environment and only briefly touch upon the niche vs neutral debate, which seemed superfluous to both reviewers.

Our analysis of new simulations with added between-species variability in the mortality rate did not alter any of our conclusions. These additional results are therefore reported only in the Electronic Supplementary Material.

We thank again the referees for the constructive feedback, and hope that the revised manuscript will now be up to the standards of Theoretical Ecology.

Sincerely,

Coralie Picoche and Frédéric Barraquand

COMMENTS FOR THE AUTHOR:

There is additional documentation related to this decision letter. To access the file(s), please click the link below. You may also login to the system and click the 'View Attachments' link in the Action column.
https://thee.editorialmanager.com/l.asp?i=16440&l=E376JRNJ

Reviewer #1: I have a clearer understanding of what this paper is about now. However, I think the framing could be crisper still. Right now, the final paragraph of the introduction --- the "here's what we're going to do" paragraph --- doesn't have a strong connection to the set-up at the beginning of the introduction. I think the last paragraph is pretty motivating, but you may lose readers before they get there. Or if they do get there, they will wonder, as I did, how the second half of the intro. connects to the first. My understanding is that the big story is what happens with various coexistence mechanisms present with various forcing types --- the 2x2x2 factorial experiment done here. And the main(?) point of that experiment is to understand how we can observe the diversity of species that we do, especially since at least for phytoplankton assemblages in temperate zones, there is likely to be seasonal forcing. A nice secondary issue is the biomass-trait distribution, but that's secondary. Is that right? To be clear, I'm not suggesting that you take anything out of the paper, just that you frame it more clearly.

>> We are grateful for this careful reading of our article. We have now rewritten the introduction to start with the effect of temporal variability in competition models, and then discuss the two coexistence mechanisms that we explore. The biomass-trait distribution is mentioned towards the end of the introduction as an aside. We hope this makes the introduction more focused on the core objectives of the paper and easier to follow. We made minor edits to the discussion in the same spirit.

I'm still a little confused about inferring mechanisms from biomass-trait distributions. My understanding is that if both the storage effect and strong self-regulation are present, the trait-biomass distribution is multi-modal if there is seasonal forcing and unimodal otherwise.

>> Yes, this is correct.

However, if only one of these coexistence mechanisms is present, the biomass distribution is multimodal if it's the storage effect and uniform if it's strong self-regulation, regardless of seasonality.

>> Indeed.

If we only observe a multimodal distribution, how do we know there's a storage effect? I guess both situations involve a storage effect, but one also requires seasonal forcing?

>> Previously, we suggested to regard multimodality only as a clue pointing towards a mechanism: there is definitely no one-to-one mapping between biomass-trait distributions and coexistence mechanisms. We now make this clearer l.356-361, where we added "However, when both strong self-regulation and the storage effect were at play, the biomass-trait distribution could either be unimodal or multimodal depending on the type of noise driving the community dynamics (random or seasonal, respectively). This implies that the mere observation of multimodality in a thermal preference trait-biomass distribution is not a proof of a storage effect, or conversely, the proof of the influence of a seasonal environment."

The idea of superadditivity doesn't come up until the discussion section. That surprised me. Any result I see discussed in the Discussion, I also expect to see analyzed in the results.

>> The word 'superadditivity' was indeed only implicit in the previous sentence: 'neither of these mechanisms was able to produce that result alone, for either random and seasonal noise'. We corrected the sentence so that superadditivity is explicitly mentioned l. 193 - 195: "the number of species coexisting with both mechanisms present is greater than the sum of the species coexisting with either mechanism alone. The two mechanisms therefore combine superadditively, as their interaction has a positive effect on the richness of the community."

Also, when Chesson or Ellner et al. 2018 talk about contributions to coexistence from various mechanisms, they mean contributions to invader growth rate from various mechnanisms (and their interactions). You haven't measured this, so I think what you mean by superadditivity is that the number of species coexisting with both mechanisms present is greater than the sum of the number of species present with either mechanism alone. Is this correct? If so, it would be worth explicitly mentioning in the results that the number of species coexisting with both mechanisms present is greater than the sum of species coexisting with either mechanism acting

alone. It would also be worth briefly defining what you mean by superadditivity (numbers of species, not strength of contribution to a single invader growth rate).

>> We now give the definition of superadditivity according to Chesson and Ellner et al. (2019) in the Discussion, and clarify the differences with our use of the term in the manuscript (l. 393-395).

Ellner, Stephen P., Snyder, Robin E., Adler, Peter B., Hooker, Giles. An expanded modern coexistence theory for empirical applications. Ecology Letters, 2018

Reviewer #2: I thank the Authors for considering my earlier comments and thoroughly addressing them. I think the article has definitely improved. I still have a few points I would like to revisit - please see them below.

>> We greatly appreciated your appraisal of the manuscript and constructive suggestions.

1) In my mind, this is the most important point. I suggested to the Authors to introduce a slight species-specific variation in the mortalities m, which were set equal across species. The Authors objected, on the grounds that this would introduce new niche differences between species, making their Figure 4 uninterpretable. In fact, extra density-independent mortalities do not introduce any niche differences. Take basic R^* competition as an example. A set of species compete for one single resource R (a single niche), with per capita growth rates $r_i = b_i R - m_i$, where b_i is the amount of growth generated from one unit of resource, and m_i is the mortality rate. The R^* of species i is then m_i / b_i. If all b's and m's were equal, then there would be neutral coexistence. Introducing variation in the mortalities means that the R^*-values will vary, and all but the single most adapted species will go extinct. Far from introducing new niches and coexistence, an extra density-independent mortality term exacerbates competitive exclusion by resolving model degeneracy caused by parameter fine-tuning.

The Authors claim that introducing variation in the m's would change the emergent neutrality pattern. I have not checked this myself, but I am sure the Authors are right (though, importantly, not because this introduces any new niches; see above). But if so, that just goes on to show that making all m's equal is an overly special parameter choice. In nature, we do not expect precisely equal mortalities. If some predicted pattern critically depends on this strict equality, then we do not expect the pattern to be a relevant prediction at all.

Therefore, I would like to ask the Authors again to consider implementing this suggestion. I think they would also agree that any result which critically depends on a precise equality of mortalities is not to be taken seriously. Including such results would simply make an otherwise strong article weaker than it could be.

>> We agree and we have performed new analyses adding a mortality rate that varies between species. The results are reported in the Electronic Supplementary Material Section B: the figures are all very similar and our conclusions are therefore robust to the addition of variable mortality.

2) This point is somewhat minor, but still has relevance for the big picture. I would be careful with making the case for exactly 5000-year-long simulations on the basis of the importance of transients. Brushing off 10000-year-long simulations on the basis of ecological relevance sounds reasonable - until one realizes that 5000-year-long ones are susceptible to the exact same criticism. Are 5000 years "just right", or maybe too long? And how about 1000 years? Or 500? And so on... To rigorously account for transients, one must include simulation time, t, as an extra control parameter, and explore everything as a function of t. Unless this is done, the arbitrary simulation time of 5000 years is no better justified than looking for equilibrium solutions. At least, equilibria and their stability do tell us something about model behavior even when the system is far away from them (as in topological analyses of phase plots using equilibrium points and their stability), and they do reveal how many species could in principle coexist indefinitely.

For these reasons, I would stick to the (admittedly weaker, but honest and still good-enough) argument that 5000-year intervals were chosen for better comparison with Scranton & Vasseur (2016 TE). I would revise lines 264-273 accordingly.

>> We have done just that, writing at l. 262-268 : "We could have considered longer time intervals, but comparison with the values reported by Scranton & Vasseur (2016) would then have been compromised [...] All things considered, we therefore kept the 5000-year time window for integration."

(Incidentally, would performing simulations for more than 5000 years really be that much more challenging computationally? I have written my own R script, which integrates 5000 years in just a few minutes on my desktop. On a computing cluster, by running different parameterizations in parallel, all simulations could be done quite fast, or so I imagine. I might have made a mistake in my code, or the Authors may not have access to a computing cluster - I am attaching my code for reference, in any case.)

>> It looks like the integration scheme with adaptive timestep of ode45 may be largely responsible for slowing down the numerical integration, by comparison to Runge Kutta (4). In Matlab, 1 simulation with ode45 takes 40 mins on an (average) laptop with ode45. Your original R code runs in 8 mins. Using your code but switching the solver to ode45 in R, the computation time increases to 3h (!). This incidentally suggests that we may be able to get an even faster code with RK4 in Matlab.

We will definitely keep in mind (for future work) to be wary of adaptive timesteps when speed is important. Many thanks for providing your code, this was most welcome to compare speeds and pinpoint what part most slows down the integration.

3) I think the Introduction could still be improved by making it more direct. Right now, one could cut practically all of lines 28-59 without loss of content or context. I would cut or shorten this part, and maybe move it towards the end of the Introduction (which would reflect its position in the main text better as well).

>> As referee #1 also highlighted, the first two paragraphs of the introduction could have induced the reader into thinking that our paper was mostly about niche vs neutrality or biomass-trait distribution. We have therefore re-centered the first paragraph of the introduction on coexistence in fluctuating environments and kept the niche vs neutral debate to the bare minimum, towards the end of the introduction. We think that this still gives some background to the concept of 'clumpy coexistence' and the biomass-trait distribution which we analyze later on.

One minor comment: in line 276, erase "or interspecific competition strength".

>> In the manuscript, competition strength refers to alpha_{i,j}. We would prefer to keep mentioning that we did not introduce "variability in either intraspecific competition strength or interspecific competition strength", because many authors have tried to introduce only variability in interspecific interaction strength (e.g. Kokkoris et al. 2002) while intraspecific interaction strength variability may be equally important (see e.g. the recent paper by Stump et al. Ecology Letters 2018).

Sincerely,
Gyuri Barabás