

How self-regulation, the storage effect and their interaction contribute to coexistence in stochastic and seasonal environments

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Abstract

Explaining coexistence in species-rich communities of primary producers remains a challenge for ecologists because of their likely competition for shared resources. Following Hutchinson's seminal suggestion, many theoreticians have tried to create diversity through a fluctuating environment, which impairs or slows down competitive exclusion. However, fluctuating-environment models often only produce a dozen of coexisting species at best. Here, we investigate how to create richer communities in fluctuating environments, using an empirically parameterized model. Building on the forced Lotka-Volterra model of Scranton and Vasseur (*Theor Ecol* 9(3):353–363, 2016), inspired by phytoplankton communities, we have investigated the effect of two coexistence mechanisms, namely the storage effect and higher intra- than interspecific competition strengths (i.e., strong self-regulation). We tuned the intra/inter competition ratio based on empirical analyses, in which self-regulation dominates interspecific interactions. Although a strong self-regulation maintained more species (50%) than the storage effect (25%), we show that none of the two coexistence mechanisms considered could ensure the coexistence of all species alone. Realistic seasonal environments only aggravated that picture, as they decreased persistence relative to a random environment. However, strong self-regulation and the storage effect combined superadditively so that all species could persist with both mechanisms at work. Our results suggest that combining different coexistence mechanisms into community models might be more fruitful than trying to find which mechanism best explains diversity. We additionally highlight that while biomass-trait distributions provide some clues regarding coexistence mechanisms, they cannot indicate unequivocally which mechanisms are at play.

Keywords: coexistence; seasonality; competition; phytoplankton; Lotka-Volterra; storage effect

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1 Introduction

The continued maintenance of diversity in spite of widespread competition has long bewildered ecologists, especially for primary producers such as phytoplankton that share the same basic resources (Hutchinson, 1961). A solution for the ‘paradox of the plankton’ was proposed by Hutchinson: temporal variation of the environment. By making the identity of the fittest species change over time, temporal variation could render competitive exclusion less likely, which was confirmed by early experiments (Sommer, 1984). However, it has been shown later that inclusion of temporal variability *per se* in competition models is not sufficient for maintaining a realistic diversity (Chesson and Huntly, 1997; Fox, 2013). Additional mechanisms such as the storage effect (Chesson, 1994; Ellner et al, 2016) or a relative nonlinearity of competition (Armstrong and McGehee, 1980; Chesson, 2000; Descamps-Julien and Gonzalez, 2005; Jiang and Morin, 2007; Fox, 2013) need to be introduced for diversity to maintain. Moreover, richness rarely exceeds a handful to a dozen of species in modeled competitive communities in fluctuating environments, except when external inputs from immigration sustain diversity (e.g., Huisman et al, 2001; Jabot and Lohier, 2016). To our knowledge, the effect of temporal variability on persistence in competition models has mostly been examined in theoretical communities of 2 to 3 species (e.g., Chesson and Huntly, 1997; Litchman and Klausmeier, 2001; Li and Chesson, 2016; Miller and Klausmeier, 2017).

One of the richest modeled communities that we identified can be found in Scranton and Vasseur (2016), which is based on temperature variation and different thermal optima for each species (Moisan et al, 2002). In this model, the synchronizing effect of the environment and the storage effect can maintain 12 phytoplankton-like species on average. Scranton and Vasseur (2016) described daily temperature as a random noise, i.e., independent and identically distributed Gaussian random variates over time. However, under most latitudes, seasonality drives part of the environmental variation: over short timescales, random temporal variations often only add noise to a largely deterministic seasonal trend (Scheffer et al, 1997; Boyce et al, 2017; Barraquand et al, 2018).

Seasonal forcing of parameters can strongly affect the dynamics of model communities by synchronizing species to the seasonal signal or even promoting oscillations with lower frequency (Rinaldi et al, 1993; Barabás et al, 2012; Miller and Klausmeier, 2017; Vesipa and Ridolfi, 2017). How seasonality affects coexistence, as opposed to a randomly fluctuating environment, is therefore a key feature of this paper. Our present work can be seen as an attempt to blend Scranton and Vasseur (2016)’s stochastic framework with the periodic environments of Barabás et al (2012), to better represent the mixture of stochastic and deterministic environmental forces affecting phytoplankton community dynamics.

What other key features of field communities should be considered when modeling phytoplankton? Strong self-regulation, with intraspecific competition much stronger than interspecific interactions, has been found to be widespread in terrestrial plant communities (Adler et al, 2018), animal communities (Mutshinda et al, 2009), and phytoplanktonic communities (Barraquand et al, 2018). We will therefore

insert those niche differences, manifesting as strong self-regulation, into our models of phytoplankton competition. The interaction between environment variability and niche overlap was investigated by [Abrams \(1976\)](#) but his results did not extend to communities more diverse than 4 species; our objective is therefore to see how those mechanisms interact for species-rich communities.

Niche models have often been opposed to the neutral theory ([Hubbell, 2001](#)), where dispersal and drift can ensure a transient coexistence of many species, but several authors have attempted to blend niche and neutral processes ([Gravel et al, 2006](#); [Scheffer and van Nes, 2006](#); [Carmel et al, 2017](#)). An intriguing offshoot of these attempts is the concept of ‘clumpy coexistence’ ([Scheffer and van Nes, 2006](#)), whereby simultaneous influences of both niche and neutral processes create several clumps of similar species along a single trait axis. Niche differences enable coexistence of multiple clumps ([Chesson, 2000](#)) while within-clump coexistence occurs through neutral processes. This ‘emergent neutrality’ within groups ([Holt, 2006](#)) has been proposed as a unifying concept for niche and neutral theories (even though the neutrality of the original model has been disputed due to hidden niches, [Barabás et al, 2013](#)). Since then, clumpy coexistence has been shown to occur in theoretical models incorporating a temporally variable environment interacting with a thermal preference trait axis ([Scranton and Vasseur, 2016](#); [Sakavara et al, 2018](#)). The relationship (or absence thereof) between biomass-trait distributions and coexistence mechanisms is currently debated ([D’Andrea and Ostling, 2016](#)), although there are suggestions that clustering on trait axes under competition may be a robust find ([D’Andrea et al, 2018, 2019](#)).

Here, we try to establish what are the relative contributions to coexistence of the storage effect vs strong self-regulation, in a phytoplankton-like theoretical community model with a large number of species. This led us to cross combinations of seasonality vs randomness in the forcing signal, presence of the storage effect or not, and intra- vs interspecific competition intensity, in order to disentangle the contributions of these factors to biodiversity maintenance and their potential interactions. Alongside the resulting species richness, we also report which biomass-trait distribution can be expected under a given combination of processes leading to coexistence.

2 Methods

Models

The model described in [Scranton and Vasseur \(2016\)](#) is based on the Lotka-Volterra competition model. Fluctuations in the environment are introduced in the model by temperature-dependent intrinsic growth rates (see Eq. 1-2, all coefficients are defined in Table 1) so that the community dynamics can be expressed as:

$$\frac{dN_i}{dt} = r_i(\tau)N_i \left(1 - \sum_{j=1}^S \alpha_{ij}N_j \right) - mN_i \quad (1)$$

$$r_i(\tau) = a_r(\tau_0)e^{E_r \frac{(\tau - \tau_0)}{k\tau\tau_0}} f_i(\tau) \quad (2)$$

$$\text{where} \quad f_i(\tau) = \begin{cases} e^{-|\tau - \tau_i^{opt}|^3/b_i}, & \tau \leq \tau_i^{opt} \\ e^{-5|\tau - \tau_i^{opt}|^3/b_i}, & \tau > \tau_i^{opt} \end{cases} \quad (3)$$

$$\text{and } b_i \text{ is defined by numerically solving } \int r_i(\tau)d\tau = A \quad (4)$$

Model parameters are detailed in Table 1, and we set their values to match the features of phytoplankton communities as in Scranton and Vasseur’s work (2016). The niche of each species is defined by its thermal optimum τ_i^{opt} . Thermal performance curves defined in Eq. 3 are parameterized so that all species share the same niche area (Eq. 4), which sets a trade-off between maximum growth rates and niche width.

The original environmental forcing is a normally distributed variable centered on 293 K (20°C), with a 5 K dispersion. Temperature varies from one day to the next, but is kept constant throughout the day. At and above the daily scale, temperature could therefore be considered as a white noise ([Vasseur and Yodzis, 2004](#)). However, from a mathematical viewpoint, the noise is slightly autocorrelated as the integration process goes below the daily time step. We therefore use the expression ‘random noise’ to describe this forcing, as opposed to the ‘seasonal noise’ described hereafter. To construct the seasonal noise, we add to the random forcing signal a lower-frequency component, using a sinusoidal function with a period of 365 days (Eq. 5). We tune the ratio of low-to-high frequency with the variable θ so as to keep the same energy content - i.e., equal total variance - in the forcing signal.

$$\tau(t) = \mu_\tau + \theta\sigma_\tau \sin(2\pi t) + \epsilon_t, \text{ where } \epsilon_t \sim \mathcal{N}\left(0, \sigma_\tau \sqrt{1 - \frac{\theta^2}{2}}\right) \quad (5)$$

Note that the upper limit for θ , $\sqrt{2}$, corresponds to a completely deterministic model which we do not explore here (but see [Zhao \(1991\)](#) proving bounded coexistence). We choose to keep the stochasticity in the signal and to model a plausible temperature signal with $\theta = 1.3$ (illustrated in Fig. 1b) when

Table 1: Parameter definitions and values for the model described in Eqs. 1-4. Parameter values are not specified when they vary over time and/or with the species considered.

Name	Definition	Value (unit)
S	Initial number of species	60 (NA)
N_i	Biomass density of the i^{th} species	(kg/area)
τ	Temperature	(K)
$r_i(\tau)$	Growth rate of species i as a function of temperature	$(\frac{\text{kg}}{\text{kg} \times \text{year}})$
α	Baseline strength of competition	0.001 (area/kg)
b_i	Normalization constant for the thermal decay rate	(K^3)
m	Mortality rate	$15(\frac{\text{kg}}{\text{kg} \times \text{year}})$
τ_0	Reference temperature	293 (K) / 20 ($^{\circ}\text{C}$)
$a_r(\tau_0)$	Growth rate at reference temperature	$386(\frac{\text{kg}}{\text{kg} \times \text{year}})$
E_r	Activation energy	0.467 (eV)
k	Boltzmann's constant	$8.6173324 \cdot 10^{-5} (\text{eV} \cdot \text{K}^{-1})$
$f_i(\tau)$	Fraction of the maximum rate achieved for the i^{th} species	(NA)
μ_τ	Mean temperature	293 (K)
σ_τ	Standard deviation for temperature	5 (K)
τ_{\min}	Minimum thermal optimum	288 (K)
τ_{\max}	Maximum thermal optimum	298 (K)
A	Niche breadth	$10^{3.1}(\frac{\text{kg}}{\text{kg} \times \text{year}})$
τ_i^{opt}	Thermal optimum for growth of the i^{th} species	(K)
θ	Scaling between random and seasonal noise	(0;1.3) (NA)
κ	Ratio of intra-to-interspecific competition strength	(1;10) (NA)

considering a seasonal forcing of the dynamics.

The formulation of the forced Lotka-Volterra model of [Scranton and Vasseur \(2016\)](#) implies a storage effect, as the net effect of competition exerted by species j on i is the product of the temperature-related growth rate $r_i(\tau)$ and the competitive strength α_{ij} exerted by species j multiplied by its abundance N_j . Therefore, total net competition ($\sum_{j=1}^S r_i(\tau) \alpha_{ij} N_j$) covaries positively with the growth rate values $r_i(\tau)$, which defines the storage effect ([Chesson, 1994](#); [Fox, 2013](#); [Ellner et al, 2016](#)). To remove the assumption of an explicit storage effect, we create another version of the model using the mean value of a species' growth rate (\bar{r}_i) to weight the interaction coefficients (see Eq. 6). The mean growth rate value is computed by first generating the temperature time series and then averaging all r_i over the corresponding sequences of τ values.

$$\frac{dN_i}{dt} = N_i \left(r_i(\tau) - \sum_{j=1}^S \bar{r}_i \alpha_{ij} N_j \right) - m N_i \quad (6)$$

Following Eq. 6, net competition remains unaffected by the environmental conditions, in contrast to intrinsic growth rates, while preserving the same average magnitude of competition as in Eq. 1.

Strong self-regulation is ensured by the addition of the coefficient κ , which is the ratio of intra-to-interspecific competition strength. We can therefore re-write the interaction coefficients α_{ij} in Eq. 7

$$\alpha_{ij} = \alpha (1 + (\kappa - 1) \delta_{ij}) \quad (7)$$

where δ_{ij} is the Kronecker symbol, equal to 1 if $i = j$ and to 0 otherwise. The value of the parameter $\kappa = 10$ was chosen from analyses of phytoplanktonic data (Barraquand et al, 2018). The values of non-zero interspecific competition coefficients reported in Fig. 5 of Barraquand et al (2018) are somewhat higher than here (and κ lower, closer to 4) because the best-fitting model actually sets to zero some intergroup competition coefficients; using a model where all α_{ij} are non-zero leads in contrast to $\kappa = 10$). Hereafter, the expression “strong self-regulation” characterizes dynamics where the intraspecific competition strength is 10 times higher than the interspecific competition strength, as opposed to “equal competitive strengths” where intra- and interspecific competition strengths are equal.

In addition to two types of environmental forcings (random noise with $\theta = 0$, and seasonal noise with $\theta = 1.3$), we compare the results for four versions of the original model: with and without an explicit storage effect (Eq. 1 and Eq. 6, respectively); with strong self-regulation or equal intra- and inter-competition strength ($\kappa = 10$ or $\kappa = 1$, respectively). These are summed up in Table 2.

$\frac{1}{N_i} \frac{dN_i}{dt} + m$	Storage effect	No storage effect
Strong self-regulation ($\kappa = 10$)	$r_i(\tau) \left(1 - \sum_{j=1}^S \alpha (1 + 9\delta_{ij}) N_j \right)$	$r_i(\tau) - \sum_{j=1}^S \bar{r}_i \alpha (1 + 9\delta_{ij}) N_j$
Equal competitive strengths ($\kappa = 1$)	$r_i(\tau) \left(1 - \sum_{j=1}^S \alpha N_j \right)$	$r_i(\tau) - \sum_{j=1}^S \bar{r}_i \alpha N_j$

Table 2: Growth rate of species i in the four models

Set-up

We replicate the ‘Species sorting’ experiment of Scranton and Vasseur (2016) so as to investigate how the structure of synthetic phytoplankton communities varies under the different scenarios we described above. We focus on the dynamics of a community initialized with 60 species with thermal optima uniformly spaced along the interval $[15^\circ\text{C}, 25^\circ\text{C}]$, and with the same initial density ($\frac{1}{\alpha S}$). Each simulation is run for 5000 years in 1-day intervals. When the density of a species drops below 10^{-6} , it is considered extinct. For each combination of parameters (type of environmental signal, storage effect and self-regulation), we run 100 simulations.

All simulations are run with Matlab’s ode45 algorithm, an adaptive Runge-Kutta (4,5) integration scheme with an absolute error tolerance of 10^{-8} , and relative error tolerance of 10^{-3} . The code is available in a GitHub repository¹.

¹<https://github.com/CoraliePicoche/Seasonality>

3 Results

Typical dynamics of the community following Eq. 1 (the model of [Scranton and Vasseur, 2016](#)), with both a purely Gaussian noise (original choice of [Scranton and Vasseur, 2016](#); Fig. 1a) and a seasonal noise described in Eq. 5 (our variant, Fig. 1b), are shown in Fig. 1c and d, respectively. A sinusoidal forcing produces the strongly seasonally structured dynamics that are typical of phytoplankton. Even though only 5 species can be seen in Fig. 1c, there were 14 species still present at the end of the simulation forced by a random noise, with large disparities in the range of their biomasses. A third of the species kept a biomass above 10 kg/area (setting area = 1 ha, with a depth of a few meters, produces realistic standing biomasses; [Reynolds, 2006](#)) while 6 out of the 14 species biomasses remained below the unit. All persisting species in the random noise simulation were clustered within a 3.2°C-range of thermal optima (see the biomass distribution as a function of the thermal optimum in Electronic Supplementary Material, Fig. A1). No obvious temporal patterns (e.g., cycles) could be seen in the community forced by random noise. On the contrary, seasonal cycles were clear in the seasonally-forced case of Fig. 1d. Only 4 species coexisted at the end of the simulation with seasonal noise, gathered in two groups with large thermal optimum differences (5.7°C between the maximum thermal optimum of the first group and the minimum thermal optimum of the second group). When temperatures were high, the group with higher thermal optima reached its maximum biomass, then as temperature decreases through the season, these species leave room for the growth of the low-temperature group.

The decrease in persistence due to seasonality observed in Fig. 1 was confirmed in all our simulations (Fig. 2). In cases where final species richness varied from one simulation to another (namely, the two middle cases in Fig. 2: with storage effect but without strong self-regulation, or without storage effect but with strong self-regulation), seasonality reduced the number of extant species to, on average, 27% and 48% of their original values, respectively (Fig. 2). A seasonal signal therefore led to a much smaller average persistence. There was also less variance in persistence between seasonally forced simulations compared to random noise simulations.

Both a strong self-regulation and the storage effect markedly increased persistence. Without any of these coexistence mechanisms, only one species persisted at the end of the simulations. When only the storage effect was present, the number of extant species varied between 8 and 20 (14.8 ± 2.4) with random noise, or 2 and 6 (4.1 ± 0.7) with a seasonal signal. On the other hand, when only a strong self-regulation was present, the number of extant species nearly doubled, varying between 20 and 32 (27.5 ± 2.4), or 12 and 15 (13.3 ± 0.6), with a random or a seasonal noise, respectively. Remarkably, when the storage effect and a strong self-regulation both affected the community dynamics, all species persisted in the community: the number of species coexisting with both mechanisms present is greater than the sum of the species coexisting with either mechanism alone. The two mechanisms therefore combine superadditively, as their interaction has a positive effect on the richness of the community.

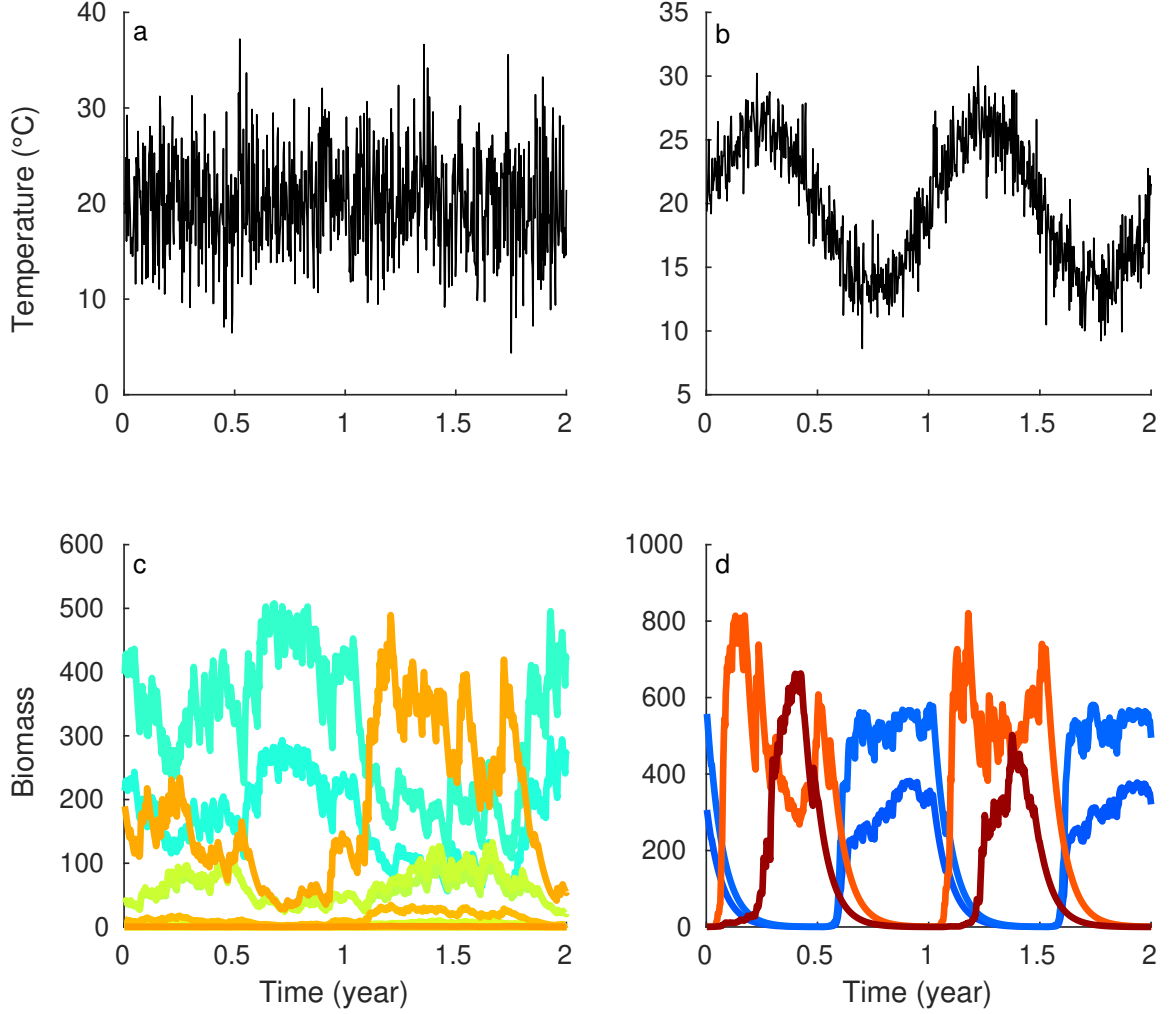


Figure 1: Time series of temperature (top; a-b) and extant species (bottom; c-d) for the 2 last years of a 5000-year simulation, with storage effect but no differences between intraspecific and interspecific competition strengths. The forcing temperature is either a random noise (a) or a seasonal noise (b), leading to community dynamics with more erratic fluctuations (c) vs seasonally structured fluctuations (d). Line colors of species biomasses correspond to their thermal optimum (from blue, corresponding to low thermal optimum, to red, corresponding to high thermal optimum).

The trait-biomass distribution of the community was affected by the type of forcing even when the richness of the community was stable (Fig. 3). Without storage effect nor strong self-regulation, there was only one species left at the end of the simulations. A random noise favored species with intermediate thermal optima: the final species had a thermal optimum between 18.9°C and 21.4°C (only a fourth of the initial range of thermal optima) for two simulations out of three and the maximum final biomasses over 100 simulations was reached in this range (Fig. 3a). This distribution may indicate a selection for the highest long-term growth rates, averaged over time (see scaled growth rates in Fig. 3). Seasonality with no coexistence mechanisms also led to a single final species but, in this case, the species always had a higher maximum growth rate (thermal optimum above 22°C). Species with a higher thermal optimum were more likely to persist and to reach a higher biomass at the end of the simulation. 38% of the simulations therefore ended with the species having the highest temperature optimum, 25°C. The shift in

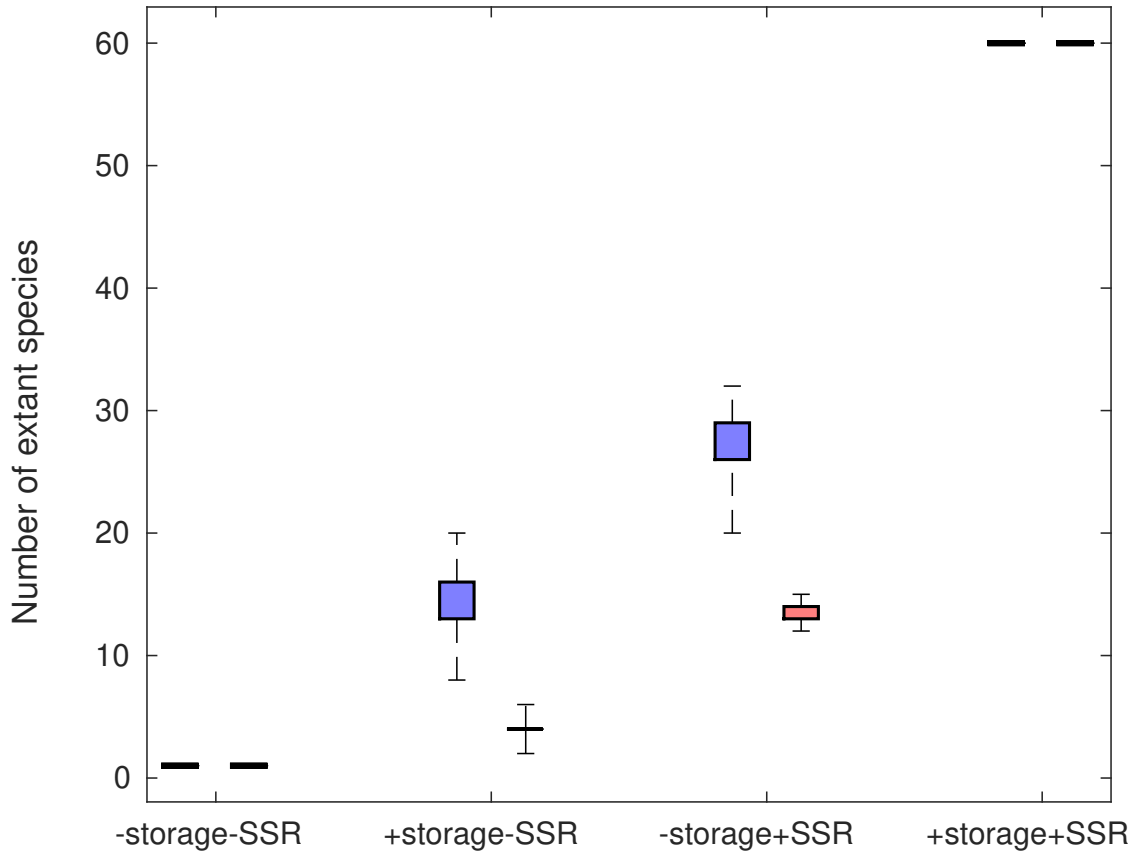


Figure 2: Number of species still present at the end of 100 simulations (5000 years each), initialized with 60 species, with a random (blue) or a seasonal forcing signal (red). The signs + or -storage refer to presence or absence of the storage effect, respectively; + / - SSR, presence or absence of Strong Self-Regulation, respectively. Community compositions are stable in the cases -storage-SSR and +storage+SSR, for which 1 or 60 species are still present at the end of all simulations, respectively. Due to low variance, the whiskers here represent min and max rather than 1.5 interquartile range.

trait distribution towards higher maximum growth rates with a seasonal noise vs higher average growth rates with a random noise was consistent for all model types considered.

When both the storage effect and strong self-regulation were present, the 60 initial species coexisted with almost no variation in their respective biomasses from one simulation to the next (mean CV across simulations is 0.008, averaged across species, Fig. 3b and d). The forcing signal modified only the distribution of biomasses, resulting in contrasted community structures despite equal richness. With a random noise, the distribution was unimodal. On the contrary, a seasonal signal led to a bimodal distribution (centered on 17.0°C and 24.4°C), each corresponding to one season, with highest biomasses for higher thermal optima (Fig. 3d). The minimum biomass was reached for the highest long-term average growth rate at an intermediate temperature (20.4°C).

In cases where the richness of the community varied, the overall shape (multimodal vs unimodal) of the marginal distribution of extant species with respect to the trait axis were similar for both types of environmental forcings (Fig. 4). By contrast, the type of coexistence mechanism generated different

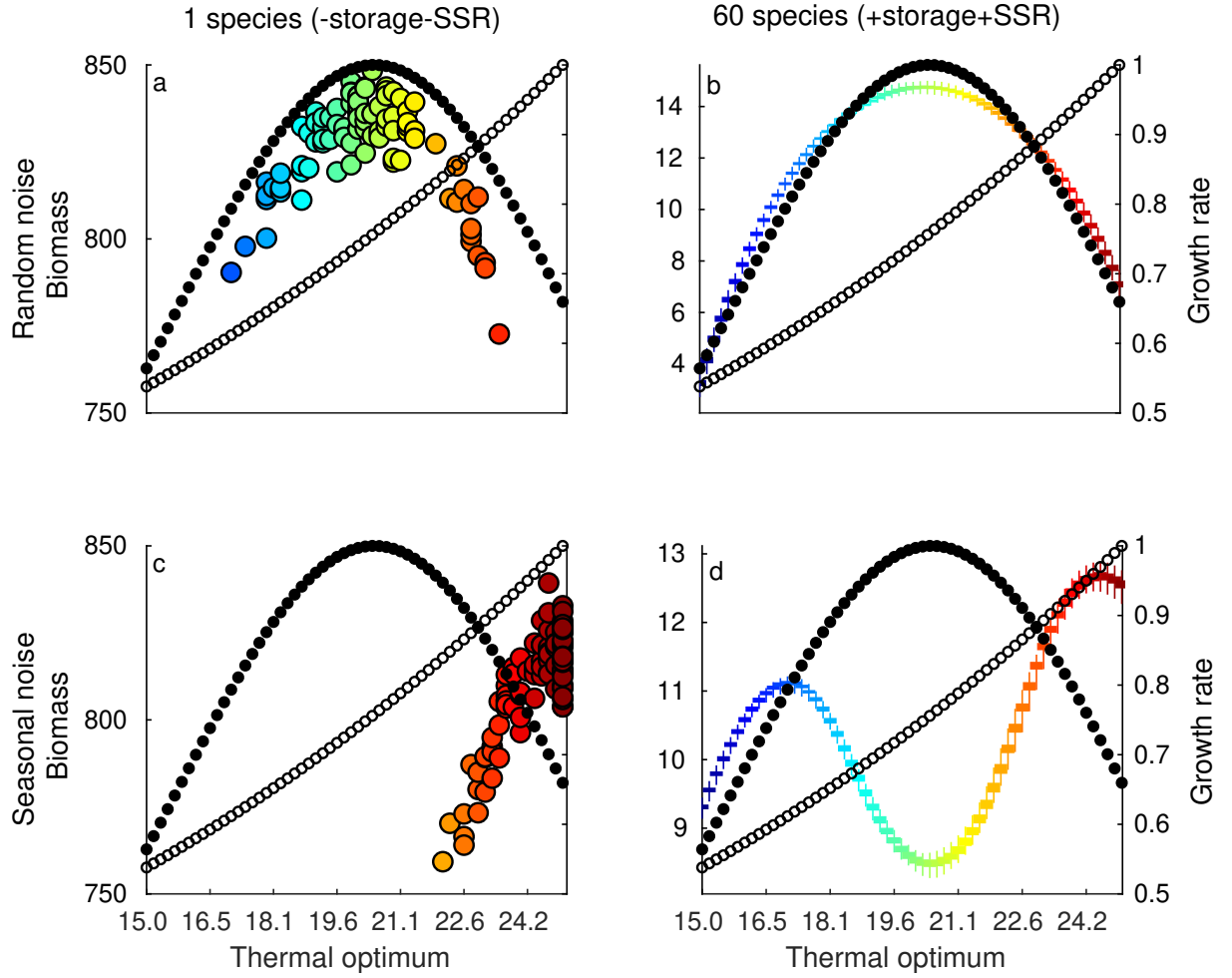


Figure 3: Mean biomass distribution over the last 200 years for 100 simulations, as a function of the species thermal optima. Here we consider the two stable-composition cases and two types of forcing signal. On the left column, simulations without storage effect nor strong self-regulation are presented. Only one species is present at the end of the simulations and its mean value is represented by one large colored circle per simulation. There can be several circles for the same species, corresponding to multiple simulations ending with this species alone. On the right column, simulations with storage effect and strong self-regulation are represented. All species are present at the end of the simulations and small boxplots present the variation in the temporal average of biomass with a given trait, for 100 simulations. The forcing signal is either a random (top) or a seasonal noise (bottom). Each species is identified by its thermal optimum through its color code. Scaled (divided by maximum) average and maximum growth rates are shown as small filled and open circles, respectively, and are indexed on the right y-axis.

shapes. Indeed, the storage effect (when acting alone) led to a multimodal biomass distribution with respect to thermal optima. We always observed 3 modes with a random noise and 3 modes in 95% of the seasonal simulations (Fig. 4a). With a random noise, extant species were grouped in rather similar clumps regarding species thermal optima (between 18.8°C and 22.2°C) whereas species tended to be further apart in the seasonal case, covering a total range of 7.7°C, with species grouping in the higher part of the thermal range, above 22°C. On the other hand, strong self-regulation led to a quasi-uniform biomass distribution (Fig. 4 b). Species in communities forced by a random noise stayed in the lower range of thermal optima (in 96% of the simulations, the highest thermal optimum was 22.4°C, see Fig. A2 in Electronic Supplementary Material) while they were filtered out in communities subjected to a seasonal

fluctuation of their environment, for which species with thermal optima above 20.5°C persisted. As before (Fig. 3 c,d), seasonality promoted species with a higher maximum growth rate, since the autocorrelated temperatures enabled them to achieve this highest growth rate for a longer period of time than a random noise would have.

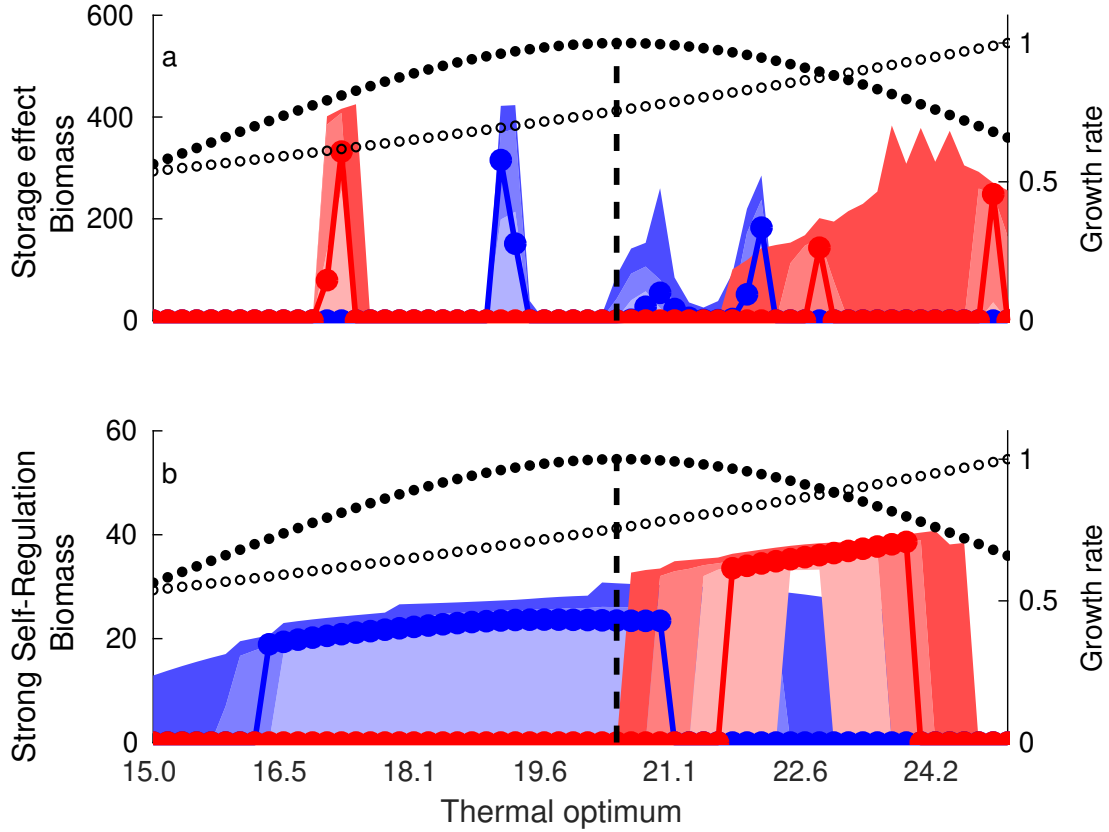


Figure 4: Mean biomass distribution over the last 200 years for 100 simulations, as a function of thermal optima, (a) with storage effect and equal competitive strengths and (b) without storage effect, with strong self-regulation. The forcing signal is either a random (in blue) or a seasonal noise (in red). Shades of the same color correspond to the 50th, 90th and 100th percentiles of the distributions while colored lines correspond to one representative simulation. Scaled (divided by maximum) average and maximum growth rates are shown as filled and open circles, respectively, and indexed on the right y-axis. The maximum average growth rate is indicated by the dashed line.

4 Discussion

We have simulated competitive Lotka-Volterra dynamics forced by a fluctuating temperature under a range of scenarios allowing more or less coexistence. Two coexistence mechanisms, the storage effect and strong self-regulation (i.e., intraspecific competition much stronger than interspecific competition), could be either present or absent, which led to four scenarios. These four scenarios were crossed with two possibilities for the forcing signal, a random noise (mostly white) and a stochastic yet seasonal signal, both with equal temporal variance. Our investigation therefore built on the model of [Scranton and Vasseur \(2016\)](#), which included a random forcing signal and a storage effect, but considered seven additional combinations of mechanisms. This was motivated by our wish to include two observed features of phytoplankton dynamics: seasonal cycles ([Winder and Cloern, 2010](#); [Boyce et al, 2017](#)) and strong self-regulation ([Chesson, 2000](#); [Adler et al, 2010](#); [Barraquand et al, 2018](#)). Many mechanisms can lead to intraspecific competition being stronger than interspecific competition: nonlinearities in the functional forms of competition or mutualism that contribute to increasing self-regulation ([Kawatsu and Kondoh, 2018](#)), or predation as well as parasitism (see e.g., the generalist predators in [Haydon, 1994](#)). Strong self-regulation seems an ubiquitous feature in competition networks of primary producers ([Adler et al, 2018](#)), and perhaps even more general networks ([Barabás et al, 2017](#)).

Before discussing the ecological interpretation of our results, we first recall some technical assumptions made in this study. All our simulations lasted for a fixed duration (5000 timesteps) as in [Scranton and Vasseur \(2016\)](#). While short- and medium-term transients (a few years to hundreds of years) are completely negligible at the end of the time series, very long transients can remain in this class of models ([Scheffer and van Nes, 2006](#); [Hastings et al, 2018](#)): these are not mere artefacts but instead traduce the fact that some processes (e.g., exclusion of a species) can be really slow. We realized that convergence was incomplete after 5000 years in some cases (e.g., random noise + storage effect + equal competitive strength). Such simulations would take up to 15 000 years to converge and the rate of convergence would slow over time. We could have considered longer time intervals, but comparison with the values reported by [Scranton and Vasseur \(2016\)](#) would then have been compromised. Another way to shorten the transients, suggested by a referee (GB), is to vary the mortality parameter. This did not alter the conclusions (see Appendix B in Electronic Supplementary Material). Unfortunately, added variability also shifts the model further away from neutral dynamics (when intra and interspecific competition strengths are equal), which renders comparisons difficult. All things considered, we therefore kept the 5000-year time window for integration.

Another strong assumption pertains to competition coefficients. To allow for comparison with [Scranton and Vasseur \(2016\)](#), we did not introduce variability in intraspecific competition strength or interspecific competition strength. By contrast, data-based coefficients vary between species ([Barraquand et al, 2018](#)), with a majority of weak interactions (as suggested in [Wootton and Emmerson, 2005](#)) and

more variance in intraspecific coefficients. [Stump \(2017\)](#) recently considered the potential effects of competition coefficient variability (also called non-diffuse competition), as did [Kokkoris et al \(2002\)](#); more variance in interspecific competition strength is usually detrimental to coexistence for an equal amount of self-regulation (see [Stump \(2017\)](#) for a classification of the various effects). Setting the competition coefficients using a multidimensional trait-based framework, like that of [Ashby et al \(2017\)](#), would provide a natural development to the work presented here; it is in our opinion difficult to speculate on those variance effects because both intra- and interspecific competition coefficient variances may matter to community persistence.

Finally, our study is limited to communities whose species have fast population dynamics relative to the yearly timescale, like phytoplankton and likely other fast-living organisms, so that many generations can occur in a year. Persistence in community with slower dynamics may be affected differently by seasonality ([Miller and Klausmeier, 2017](#)). This is especially true for species with generations that extend over multiple years. In models where trophic interactions are implemented, seasonality has been shown to promote multiyear cycles and the existence of chaotic attractors ([Rinaldi et al, 1993](#); [Taylor et al, 2013](#); [Tyson and Lutscher, 2016](#)). These rich dynamics of consumers may feed back into the lower trophic levels: [Dakos et al \(2009\)](#) present a planktonic community with seasonally-entrained chaotic dynamics which may be partly due to zooplanktonic predation. Predation probably entails additional niche differences, possibly with an emerging self-regulation created by predation processes ([Chesson, 2018](#)), but it seems unlikely that we would be able to generate such dynamics with the models presented in this article. Additional nonlinearities would be needed to create intrinsically variable and chaotic dynamics.

With these assumptions in mind, we have found that first, temporally forced Lotka-Volterra dynamics cannot sustain any diversity with our phytoplankton-based set of parameters, unless the structure is geared to include either a storage effect or a strong self-regulation. Although this absence of diversity-enhancing effect of “pure” environmental variation has already been stated by other authors ([Chesson and Huntly, 1997](#); [Barabás et al, 2012](#); [Fox, 2013](#); [Scranton and Vasseur, 2016](#)), this is not always intuitive ([Fox, 2013](#)), so we feel compelled to stress it once more: temporal variation in growth rate alone cannot help coexistence within competitive communities. A nice point made by [Scranton and Vasseur \(2016\)](#) was that a built-in storage effect in a forced Lotka-Volterra model, parameterized for phytoplankton communities, could lead to a reasonable degree of coexistence. Our investigation reproduced these results, using the random noise considered by [Scranton and Vasseur \(2016\)](#). However, an arguably more lifelike noisy and seasonal temperature forcing considerably lessened the richness of the community after 5000 years, decreasing from 15 to 4 species on average. Even imagining that groups represented here are genera or classes rather than species, this is a fairly low diversity for a phytoplankton-like community (see e.g., Chapter 1 in [Reynolds, 2006](#)). This suggests that the storage effect may not, on its own, be sufficient to maintain species-rich communities (e.g., dozens to hundreds of species). We have therefore sought out

whether a stronger self-regulation could maintain a higher diversity, using field-based intra- vs intergroup (species or genera) competition strength ratio (Barraquand et al, 2018), where the intragroup density-dependence was estimated 10 times stronger. Implementing such strong self-regulation, in the forced Lotka-Volterra models that we considered, produced a higher level of diversity than the storage effect (almost double). Of course, the result is somehow contingent upon the strength of self-regulation. Our estimates are stronger than what was found in perennial plants (Adler et al, 2010), where interspecific competition was suggested 4 or 5 times stronger than intraspecific. Still, the widespread effects of natural enemies in phytoplankton (zooplankton, parasites) may contribute to an increase in the self-regulation strength (Barraquand et al, 2018; Chesson, 2018) relative to other systems, hence we believe that 10 times stronger intraspecific competition constitutes a reasonable order of magnitude.

However, such strong self-regulation was still insufficient to maintain the whole community diversity (60 species) by itself, especially when the seasonal forcing was considered (always decreasing species richness). The diversity within clumps of similar values of thermal optima was considerably decreased once seasonality was implemented. This diversity reduction occurs because within a season, the signal autocorrelation gives long, contiguous time intervals to the best competitor to exclude its less adapted competitors. This makes the results likely to hold not only for seasonal environments, but more generally for autocorrelated ones above the daily scale, i.e., “red” noise. In contrast, the random noise scenario – which can be considered white noise above the daily temporal scale – generates large temperature shifts more frequently, and thereby forbids such competitive exclusion. In a seasonal setting, a species with the highest long-term (arithmetically) averaged growth rate may not be the best competitor, and can disappear as a result of a strong competition from both low- and high-temperature tolerant species. This holds with or without a storage effect.

Our results may appear at odds with recent proposals that seasonal forcing in itself would help maintain diversity (Sakavara et al, 2018). However, we compared the effect of seasonal forcing to that of other forcing signals while controlling for total variance. Thus, the contrast between our results and those of Sakavara et al (2018) may be due to the role of forcing variance over time: we compare scenarios under a constant total variance, much like what is done when examining the effect of noise color on population and community dynamics (Jiang and Morin, 2007; Ruokolainen et al, 2009). Thinking in terms of signal spectrum, while seasonality may maintain slightly more diversity than no forcing at all if a storage effect is present, the reddening of the environmental noise due to such seasonality reduces coexistence. This result may be contingent upon the correlated positive responses of the species growth rate to increases in the environmental variable (Ruokolainen et al, 2009, and references therein).

The biomass-trait relationship was affected more marginally by the type of forcing signal. The storage effect alone begot several clumps along the trait space (as observed by Scranton and Vasseur, 2016). The seasonality that we added to the temperature signal led to more distant clumps on the trait axis, with

less species per clump. Conversely, strong self-regulatory mechanisms alone led to relatively uniform biomass distributions, with species forming a single large cluster, which covered a fraction of the initial trait space. Therefore, the shape of the distribution was mostly affected by the coexistence mechanism at work while the average trait value was modified by the type of environmental forcing, even though the mean value of the environmental signal did not change. However, when both strong-self regulation and the storage effect were at play, the biomass-trait distribution could either be unimodal or multimodal depending on the type of noise driving the community dynamics (random or seasonal, respectively). This implies that the mere observation of multimodality in a thermal preference trait-biomass distribution is not a proof of a storage effect, or conversely, the proof of the influence of a seasonal environment.

The identification of multiple modes in biomass-trait distributions is relatively recent (Segura et al, 2013; Loranger et al, 2018; D’Andrea et al, 2018, 2019), so we recommend to interpret them with caution to avoid over-generalization. Barabás et al (2013) convincingly argued that multimodality could arise from the demographic stochasticity of a single model run. However, with several locations - or in a theoretical context as done here - one could average across locations. There are additional reasons to be cautious: the occurrence of clustering is very sensitive to the shape of the competition kernel; small differences in shape can shift the distribution towards either clustered or uniform (Pigolotti et al, 2010). We therefore view clustering on the thermal preference trait axis as an interesting clue suggesting to look for a storage effect, rather than any definite proof that the storage effect is at work. Finally, we recall that we focus on a trait (thermal optimum) which clearly interacts with the environment: clustering may emerge on another trait axis, such as size, which typically affects the competition coefficient, without having any relationship to the storage effect (Segura et al, 2011, 2013; D’Andrea et al, 2018, 2019).

In our previous empirical study of phytoplankton dynamics (Barraquand et al, 2018), we did not find any storage effect. This does not mean that it could not be observed in other planktonic systems: we studied a coastal ecosystem and focused a specific fraction of phytoplankton, relatively large diatoms and dinoflagellates. However, given the consequences of the storage effect for species richness and composition presented here, we are skeptical that the storage effect could, by itself, fully explain phytoplankton diversity at any location. Our results suggest that in phytoplankton-like seasonal environments, empirically-tuned self-regulation produces much more diversity than the storage effect, when both are considered in isolation. The storage effect may therefore help phytoplankton diversity maintenance, but only when combined to other mechanisms. This is all the more likely that in our models, the combination storage effect + strong self-regulation is non-additive: the cases where both self-regulation and the storage effect were present showed more diversity than generated by any mechanism on its own.

The above results suggest the very exciting idea that multiple coexistence mechanisms might combine superadditively to determine the richness of the community, thus helping us to better understand the astounding diversity of primary producers. This logic could, in principle, be extended to mechanisms

that we have not considered here (e.g., spatial structure, specialized natural enemies, that could be as important here for plankton as they are for tropical trees, see [Bagchi et al, 2014](#); [Comita et al, 2014](#); [Barraquand et al, 2018](#)). Superadditivity, i.e. the positive effect of interactions between mechanisms can be measured either on community diversity, as we did here, or on the invasion growth rates ([Ellner et al, 2019](#)). Using the latter metric, previous research has however demonstrated that generalist seed predation could weaken the storage effect ([Kuang and Chesson, 2009, 2010](#)) thus different mechanisms might not always combine superadditively as we found here. That said, superadditivity has been found in some cases, i.e., pathogens could enhance the storage effect and broaden the conditions in which species could coexist ([Mordecai, 2015](#)). Better explaining plant or microbial diversity would then not be about selecting the best unique mechanism susceptible to explain the observed diversity, but rather better combining those mechanisms together. This may obviously be an annoyance for those who like to sharpen Occam’s razor, but it clearly holds opportunities for theoreticians wishing to investigate synergies between coexistence mechanisms in highly diverse communities. Aside from the synergies between predator diversity-enhancing effects, strong self-regulation through various means and the storage effect (on the temporal axis), one obvious follow-up of this research would be interactions with spatial structure. Spatial structure occurs both endogeneously, through spatially restricted movements and interactions, and exogeneously, through spatial variation in environmental covariates ([Bolker, 2003](#)). Numerous studies (e.g., [Bolker and Pacala, 1999](#); [Murrell and Law, 2002](#)) have shown that spatially restricted movements and interactions - very small-scale spatial structure - can help coexistence, which we believe would be especially important for phytoplankton since many species form colonies ([Reynolds, 2006](#); see discussion in [Barraquand et al, 2018](#)). Moreover, although temperature is usually relatively spatially homogeneous over space, other drivers (e.g., rainfall, pH in terrestrial ecosystems; salinity in aquatic ones) may exhibit spatial variation which is a main factor for coexistence ([Snyder, 2008](#)). The odds that different (resource) niches, natural enemies, spatial limits to competition and temporal niche partitioning all interact to promote the very high-dimensional coexistence observed in the field seem much higher than for any of those mechanisms alone. Whether the diversity-enhancing effects of these mechanisms combine subadditively (as in [Kuang and Chesson, 2010](#)) or superadditively like here is therefore worthy of further research.

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Electronic Supplementary Material

Biomass-trait distributions

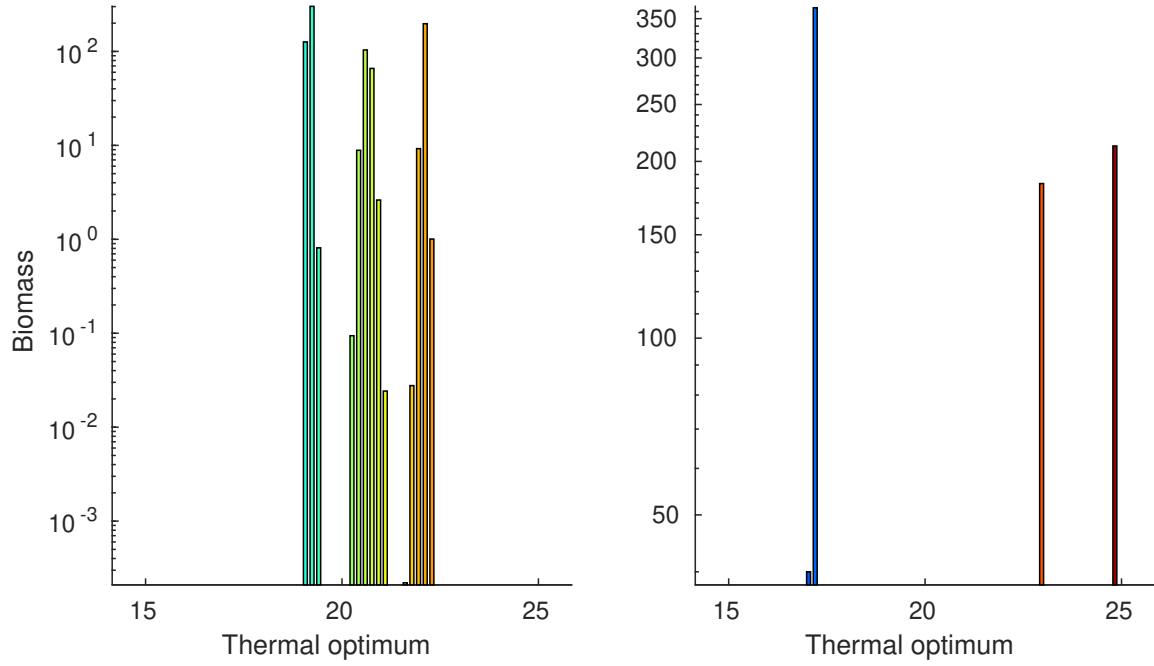


Figure A1: Temporal mean of biomass as a function of the thermal optimum defining each species. The temporal means are computed over the last 200 years of a simulation spanning 5000 years. We considered both a random (left) and a seasonal signal for the temperature (right). The coexistence mechanism implemented is the storage effect, and the intra and interspecific competition coefficients are equal. This simulation is the one described in Fig. 1 in the main text. 99 other simulations have been performed to produce the main text results in Figs. 2-4.

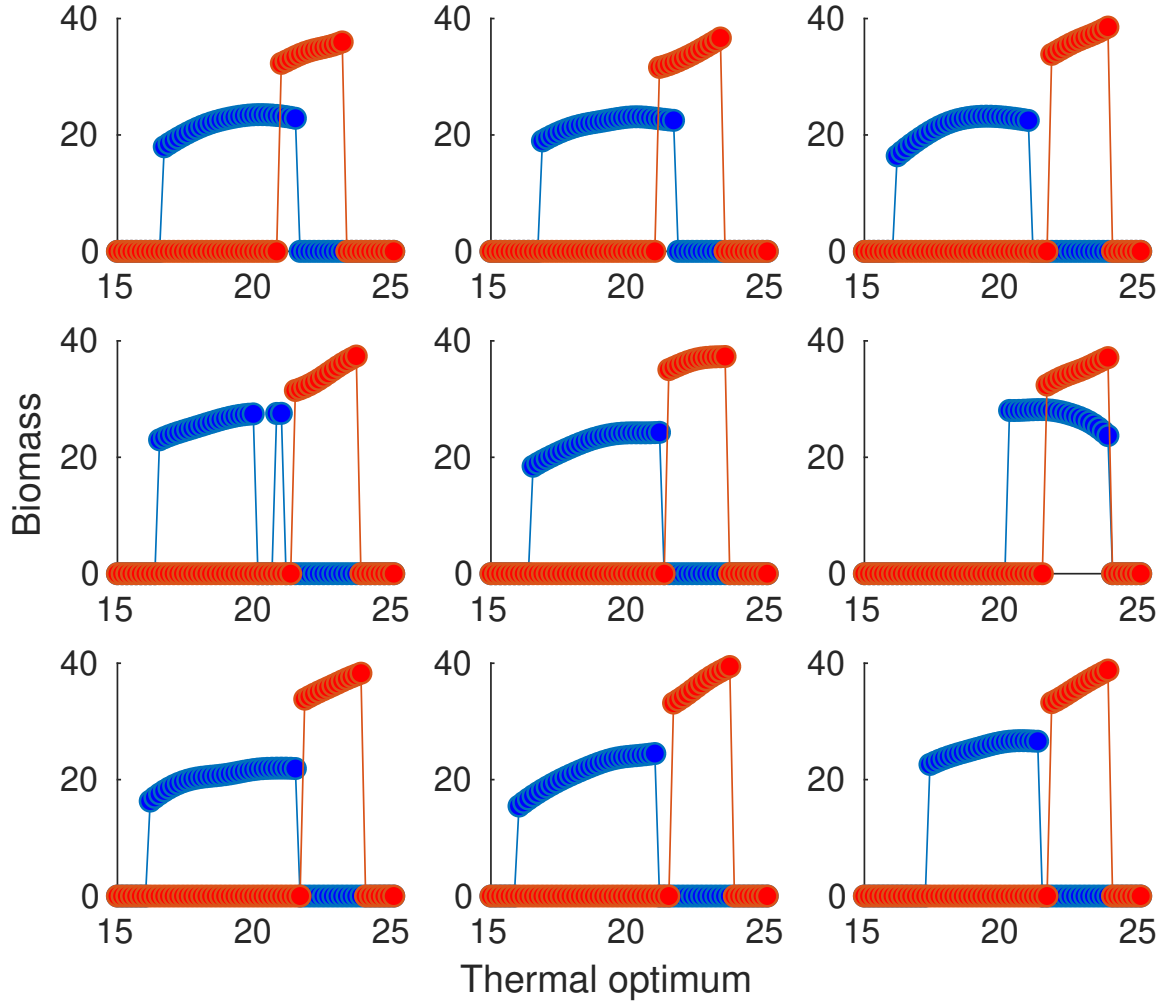


Figure A2: Temporal mean biomass distribution, computed over the last 200 years, for 9 representative simulations, as a function of the thermal optimum of the species. These simulations are done without storage effect but with a strong self-regulation. Temperature is either a seasonal signal (red) or a random noise (blue). The distribution induced by a random noise overlaps the one obtained with a seasonal noise in only 2 simulations out of 100, hence the 2 signals lead in general to non-overlapping biomass distributions on the trait axis.

Variation in mortality rates

To test the robustness of our conclusions while accelerating convergence, we conducted the same analyses with a species-specific mortality rate. For each set of simulations, covering 4 different competition scenarios and 2 types of environmental forcing, the mortality rate was drawn from a uniform distribution between 14.9 and 15.1 year^{-1} so that we only changed the variability, but not the mean, of this parameter.

The main results of our analyses were not altered by this modification (Fig. A3). The absence of coexistence mechanisms led to competitive exclusion of all species but one and the presence of both coexistence mechanisms maintained all species (Fig. A4). Strong self-regulation on its own maintained between 23 and 31 species (vs 20 to 32 in the case of constant mortality) with a random noise, and between 12 and 14 (vs 12 to 15 with a constant mortality) with a seasonal noise. The storage effect alone also led to similar results with a seasonal noise with regards to the richness of the community.

As shown on Fig. A5, biomass-trait distributions remained qualitatively similar (multimodality with the storage effect and uniform distribution with a strong self-regulation, with different partitioning on the trait axis depending on the type of noise). The only case which led to slightly different results was the combination of a storage effect and random noise. In this case, the final number of species in the community ranged from 2 to 6, with nearly 50% of the simulations ending with 3 species only. Richness is therefore approximately 4 times lower than what was obtained with a constant mortality. The remaining species had approximately the same positions on the trait axis as in the case of a constant mortality.

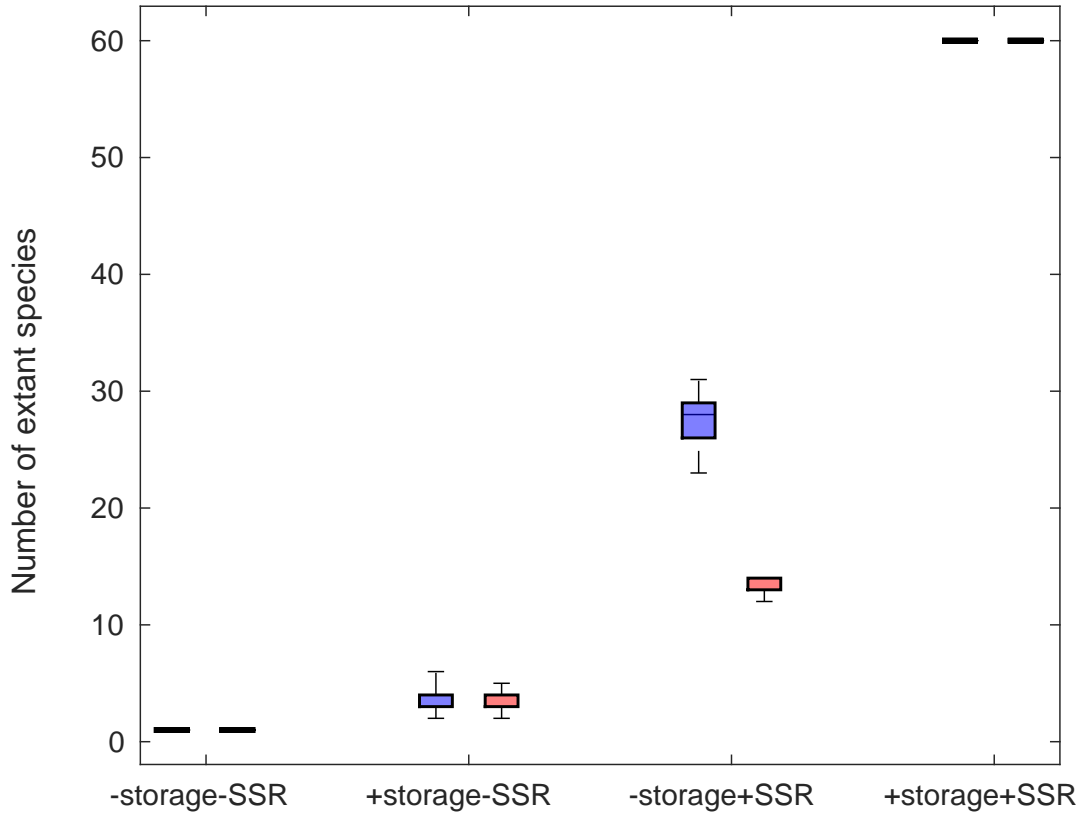


Figure A3: Number of species still present at the end of 100 simulations (5000 years each) with a variable mortality, initialized with 60 species, with a random forcing signal (blue) or a seasonal noise (red). The signs + or -storage refer to presence or absence of the storage effect, respectively; + / - SSR, presence or absence of Strong Self-Regulation, respectively. Community compositions are stable in the cases -storage-SSR and +storage+SSR, for which 1 or 60 species are still present at the end of all simulations. Due to low variance, the whiskers here represent min and max rather than 1.5 interquartile range.

Competitive exclusion within clumps was therefore accelerated by the variation in mortality. This can be explained by the departure from neutral dynamics which, in the absence of immigration, led to the exclusion of species being even marginally more vulnerable than the others within their clumps. We can assume that the results obtained with a variable mortality mimic the ones that could be obtained with a constant mortality but for much longer runtimes, after the longest transients.

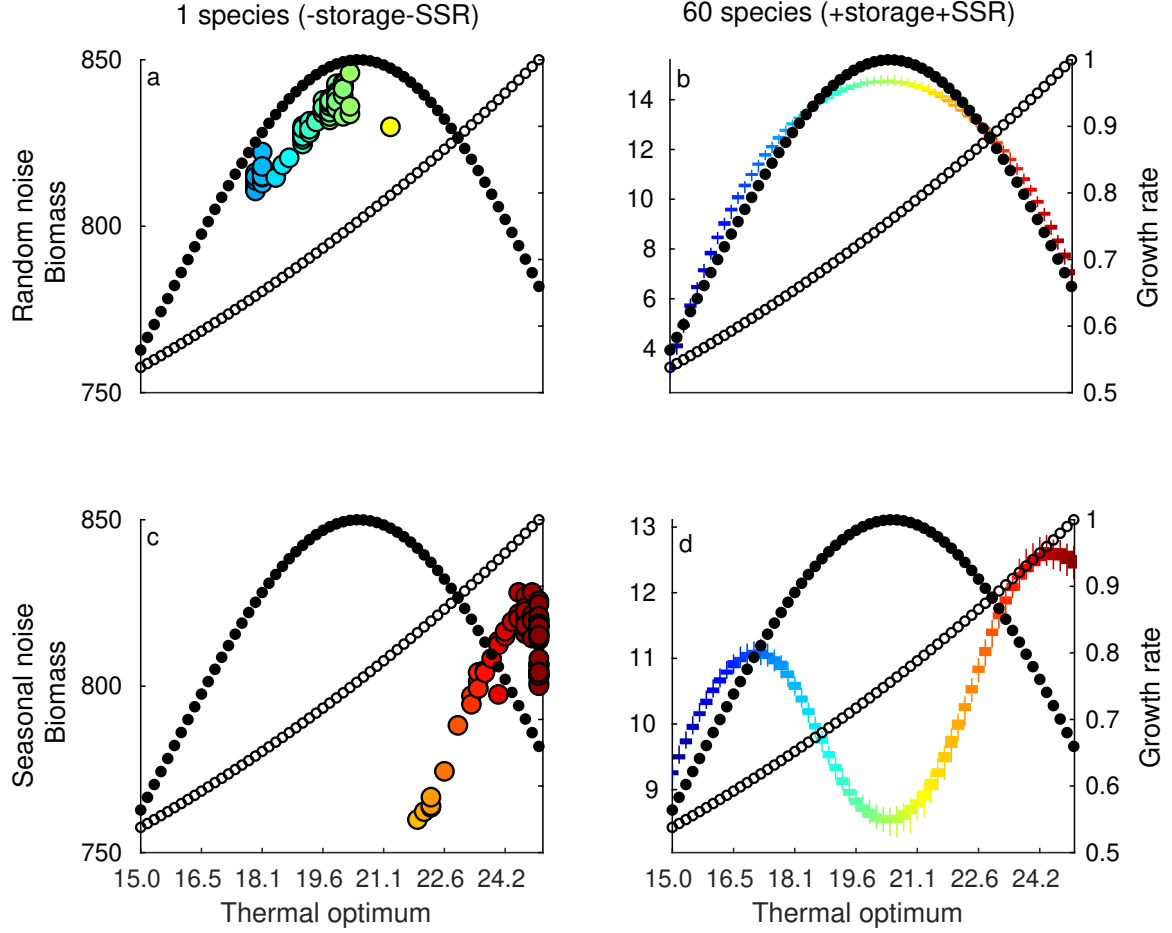


Figure A4: Mean biomass distribution over the last 200 years for 100 simulations, as a function of the species thermal optima. We consider here a variable mortality between species. Here we consider the two stable-composition cases and two types of forcing signal. On the left column, simulations without storage effect nor strong self-regulation are presented. Only one species is present at the end of the simulations and its mean value is represented by one large colored circle per simulation. There can be several circles for the same species, corresponding to multiple simulations ending with this species alone. On the right column, simulations with storage effect and strong self-regulation are represented. All species are present at the end of the simulations and small boxplots present the variation in the temporal average of biomass with a given trait, for 100 simulations. The forcing signal is either a random (top) or a seasonal noise (bottom). Each species is identified by its thermal optimum through its color code. Scaled (divided by maximum) average and maximum growth rates are shown as small filled and open circles, respectively, and are indexed on the right y-axis.

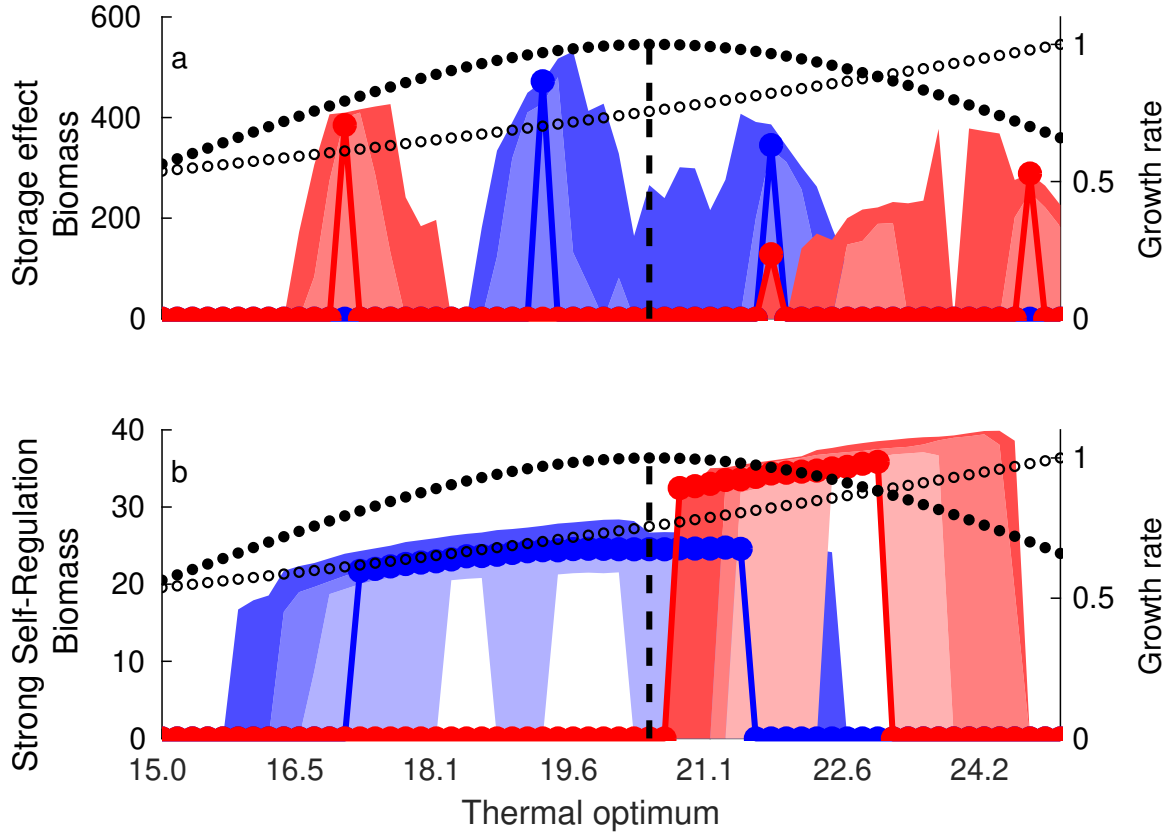


Figure A5: Mean biomass distribution over the last 200 years for 100 simulations as a function of thermal optima. We consider here a variable mortality between species. The two cases considered are (a) with storage effect and equal competitive strengths and (b) without storage effect, with strong self-regulation. The forcing signal is either a random (in blue) or a seasonal noise (in red). Shades of the same color correspond to the 50th, 90th and 100th percentiles of the distributions while colored lines correspond to one representative simulation. Scaled (divided by maximum) average (whose maximum is indicated by the dashed line) and maximum growth rates are shown as filled and open circles, respectively, and indexed on the right y-axis.