

# TOA ASSIGNMENT #1

## SECTION F

SR #	NAME	ROLL #
1	Mehdi Raza Rajani	K163904
2	Tahir Raza Hemani	K163905
3	Moazzam Maqsood	K163868

### DFA 1:

DFA for the language {w : w contains 01 an odd number of times} over the alphabet { 0 , 1 }.

```
typedef struct STATE {
    string temp;
    STATE* occ0;
    STATE* occ1;
    bool isFinal;
};

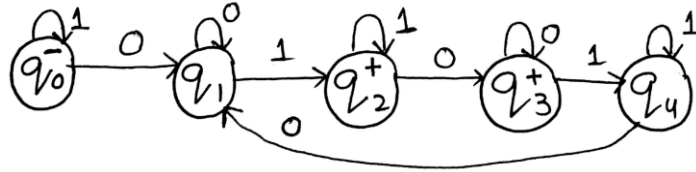
class dfal {
    STATE q0,q1,q2,q3,q4,q5;
    string lang = "01";

    public : dfal(){
        q0.temp = "q0";    q0.isFinal = false;    q0.occ0 = &q1;    q0.occ1 = &q0;
        q1.temp = "q1";    q1.isFinal = false;    q1.occ0 = &q1;    q1.occ1 = &q2;
        q2.temp = "q2";    q2.isFinal = true;     q2.occ0 = &q3;    q2.occ1 = &q2;
        q3.temp = "q3";    q3.isFinal = true;     q3.occ0 = &q3;    q3.occ1 = &q4;
        q4.temp = "q4";    q4.isFinal = false;    q4.occ0 = &q1;    q4.occ1 = &q4;
    }

    public : bool validate(string s){
        STATE* cur = &q0;
        for (int i = 0 ; i < s.size(); ++i ){
            cout << cur->temp << " -> " << "(" << s[i] << ")" -> " ";

            if ( s[i] == '0' ) cur = cur->occ0;
            else if ( s[i] == '1' ) cur = cur->occ1;
            else {
                cout << " ( " << s[i] << " is not part of ALPHABETS.)" << endl;
                return false;
            }
        }
        cout << cur->temp << " ";
        if (!cur->isFinal) {
            cout << "(it is not a final state.)" << endl;
            return false;
        }
        cout << "(it is a final state.)" << endl;
        return true;
    }
};
```

**DFA:**



**TEST CASES:**

Enter you string you want to check for: 0101010

q0 -> (0) -> q1 -> (1) -> q2 -> (0) -> q3 -> (1) -> q4 -> (0) -> q1 -> (1) -> q2 -> (0) -> q3 (it is a final state.)  
Yes!

Enter you string you want to check for: 1111010101111101

q0 -> (1) -> q0 -> (1) -> q0 -> (1) -> q0 -> (1) -> q0 -> (0) -> q1 -> (1) -> q2 -> (0) -> q3 -> (1) -> q4 -> (0) -> q1 -> (1) -> q2 -> (1) -> q2 -> (1) -> q2 -> (1) -> q2 -> (0) -> q3 -> (1) -> q4 (it is not a final state.)  
No!

## DFA 2:

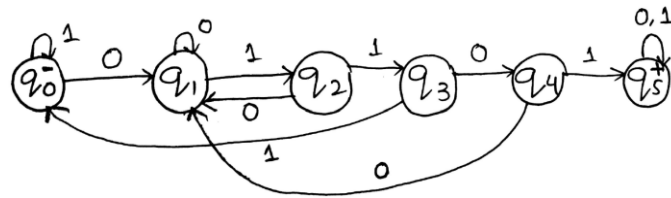
**DFA for the language of words over the alphabet { 0 , 1 } that contain the substring 01101.**

```

typedef struct STATE {
    string temp;
    STATE* occ0;
    STATE* occ1;
    bool isFinal;
};

class dfa2 {
    STATE q0,q1,q2,q3,q4,q5;
    string lang = "01";
    public : dfa2(){
        q0.temp = "q0";    q0.isFinal = false;    q0.occ0 = &q1;    q0.occ1 = &q0;
        q1.temp = "q1";    q1.isFinal = false;    q1.occ0 = &q1;    q1.occ1 = &q2;
        q2.temp = "q2";    q2.isFinal = false;    q2.occ0 = &q1;    q2.occ1 = &q3;
        q3.temp = "q3";    q3.isFinal = false;    q3.occ0 = &q4;    q3.occ1 = &q0;
        q4.temp = "q4";    q4.isFinal = false;    q4.occ0 = &q1;    q4.occ1 = &q5;
        q5.temp = "q5";    q5.isFinal = true;     q5.occ0 = &q5;    q5.occ1 = &q5;
    }
    public : bool validate(string s){
        STATE* cur = &q0;
        for (int i = 0 ; i < s.size(); ++i ){
            cout << cur->temp << " -> " << "(" << s[i] << ")" -> " ";
            if ( s[i] == '0' ) cur = cur->occ0;
            else if ( s[i] == '1' ) cur = cur->occ1;
            else {
                cout << " ( " << s[i] << " is not part of ALPHABETS.)" << endl;
                return false;
            }
        }
        cout << cur->temp << " ";
        if (!cur->isFinal) {
            cout << "(it is not a final state.)" << endl;
            return false;
        }
        cout << "(it is a final state.)" << endl;
        return true;
    }
};
  
```

## DFA:



## TEST CASES:

Enter you string you want to check for: 110110110

q0 -> (1) -> q0 -> (1) -> q0 -> (0) -> q1 -> (1) -> q2 -> (1) -> q3 -> (0) -> q4 -> (1) -> q5 -> (1) -> q5 -> (0) -> q5 (it is a final state.)  
Yes!

Enter you string you want to check for: 1101145

q0 -> (1) -> q0 -> (1) -> q0 -> (0) -> q1 -> (1) -> q2 -> (1) -> q3 -> (4) -> ( 4 is not part of ALPHABETS.)  
No!

## DFA 3:

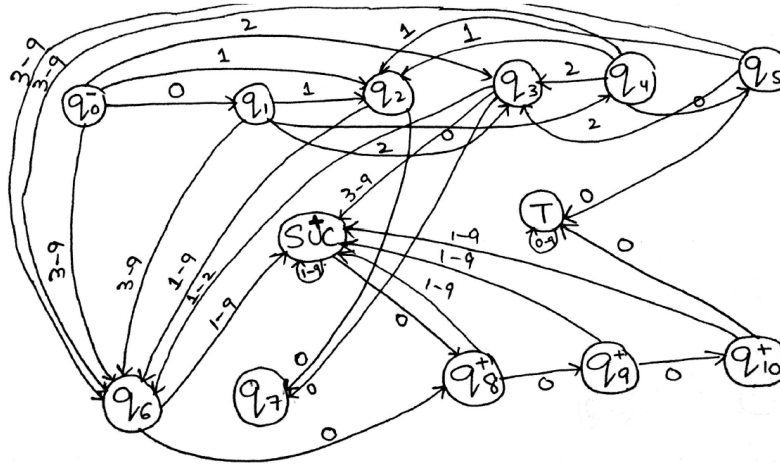
**DFA for the language {w : w is an integer at least 23} over the alphabet { 0 , 1 , . . . , 9 }. Words in this language should not have max three leading 0s.**

```
typedef struct STATE2 {
    string temp;
    STATE2* occ0;
    STATE2* occ1;
    STATE2* occ2;
    STATE2* occ3p;
    bool isFinal;
};

class dfa3 {
    STATE2 q0,q1,q2,q3,q4,q5,q6,q7,q8,q9,q10,SUC,T;
    string lang = "0123456789";
public : dfa3 () {
    q0.temp = "q0";    q0.isFinal = false;    q0.occ0 = &q1;    q0.occ1 = &q2;    q0.occ2 = &q3;    q0.occ3p = &q6;
    q1.temp = "q1";    q1.isFinal = false;    q1.occ0 = &q4;    q1.occ1 = &q2;    q1.occ2 = &q3;    q1.occ3p = &q6;
    q2.temp = "q2";    q2.isFinal = false;    q2.occ0 = &q7;    q2.occ1 = &q6;    q2.occ2 = &q6;    q2.occ3p = &q6;
    q3.temp = "q3";    q3.isFinal = false;    q3.occ0 = &q7;    q3.occ1 = &q6;    q3.occ2 = &q6;    q3.occ3p = &SUC;
    q4.temp = "q4";    q4.isFinal = false;    q4.occ0 = &q5;    q4.occ1 = &q2;    q4.occ2 = &q3;    q4.occ3p = &q6;
    q5.temp = "q5";    q5.isFinal = false;    q5.occ0 = &T;    q5.occ1 = &q2;    q5.occ2 = &q3;    q5.occ3p = &q6;
    q6.temp = "q6";    q6.isFinal = false;    q6.occ0 = &q8;    q6.occ1 = &SUC;    q6.occ2 = &SUC;    q6.occ3p = &SUC;
    q7.temp = "q7";    q7.isFinal = false;    q7.occ0 = &q9;    q7.occ1 = &SUC;    q7.occ2 = &SUC;    q7.occ3p = &SUC;
    q8.temp = "q8";    q8.isFinal = true;     q8.occ0 = &q9;    q8.occ1 = &SUC;    q8.occ2 = &SUC;    q8.occ3p = &SUC;
    q9.temp = "q9";    q9.isFinal = true;     q9.occ0 = &q10;   q9.occ1 = &SUC;    q9.occ2 = &SUC;    q9.occ3p = &SUC;
    q10.temp = "q10";  q10.isFinal = true;    q10.occ0 = &T;    q10.occ1 = &SUC;    q10.occ2 = &SUC;    q10.occ3p = &SUC;
    SUC.temp = "SUC";  SUC.isFinal = true;    SUC.occ0 = &q8;    SUC.occ1 = &SUC;    SUC.occ2 = &SUC;    SUC.occ3p = &SUC;
    T.temp = "T";      T.isFinal = false;     T.occ0 = &T;      T.occ1 = &T;      T.occ2 = &T;      T.occ3p = &T;
}

public : bool validate(string s){
    STATE2* cur = &q0;
    for (int i = 0 ; i < s.size(); ++i) {
        cout << cur->temp << " -> " << "(" << s[i] << ") -> ";
        if ( s[i] == '0' ) cur = cur->occ0;
        else if ( s[i] == '1' ) cur = cur->occ1;
        else if ( s[i] == '2' ) cur = cur->occ2;
        else if ( s[i] >= '3' && s[i] <= '9' ) cur = cur->occ3p;
        else {
            cout << " ( " << s[i] << " is not part of ALPHABETS.)" << endl;
            return false;
        }
    }
    cout << cur->temp << " ";
    if (!cur->isFinal) {
        cout << "(it is not a final state.)" << endl;
        return false;
    }
    cout << "(it is a final state.)" << endl;
    return true;
}
};
```

**DFA:**



### TEST CASES:

Enter you string you want to check for: 0000142

q0 -> (0) -> q1 -> (0) -> q4 -> (0) -> q5 -> (0) -> T -> (1) -> T -> (4) -> T -> (2) -> T (it is not a final state.)  
No!

Enter you string you want to check for: 2354

q0 -> (2) -> q3 -> (3) -> SUC -> (5) -> SUC -> (4) -> SUC (it is a final state.)

Yes!

### DFA 4:

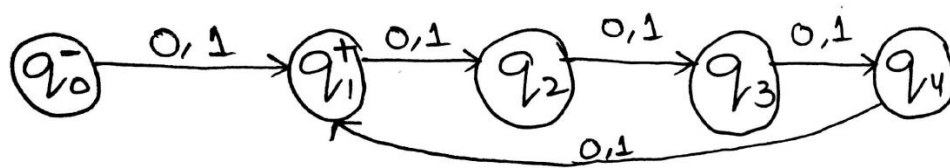
$$S = \{0, 1\}, L = \{w \in S \mid |w| \bmod 4 = 1\}.$$

```
typedef struct STATE {
    string temp;
    STATE* occ0;
    STATE* occ1;
    bool isFinal;
};

class dfa4 {
    STATE q0,q1,q2,q3,q4;
    string lang = "01";
public : dfa4(){
    q0.temp = "q0";    q0.isFinal = false;    q0.occ0 = &q1;    q0.occ1 = &q1;
    q1.temp = "q1";    q1.isFinal = true;       q1.occ0 = &q2;    q1.occ1 = &q2;
    q2.temp = "q2";    q2.isFinal = false;       q2.occ0 = &q3;    q2.occ1 = &q3;
    q3.temp = "q3";    q3.isFinal = false;       q3.occ0 = &q4;    q3.occ1 = &q4;
    q4.temp = "q4";    q4.isFinal = false;       q4.occ0 = &q1;    q4.occ1 = &q1;
}

public : bool validate(string s){
    STATE* cur = &q0;
    for (int i = 0 ; i < s.size(); ++i){
        cout << cur->temp << " -> " << "(" << s[i] << " ) -> " ;
        if ( s[i] == '0' ) cur = cur->occ0;
        else if ( s[i] == '1' ) cur = cur->occ1;
        else {
            cout << " ( " << s[i] << " is not part of ALPHABETS." << endl;
            return false;
        }
    }
    cout << cur->temp << " ";
    if (!cur->isFinal) {
        cout << "(it is not a final state.)" << endl;
        return false;
    }
    cout << "(it is a final state.)" << endl;
    return true;
}
};
```

DFA:



TEST CASES:

Enter you string you want to check for: 1010101

q0 -> (1) -> q1 -> (0) -> q2 -> (1) -> q3 -> (0) -> q4 -> (1) -> q1 -> (0) -> q2 -> (1) -> q3 (it is not a final state.)  
No!

Enter you string you want to check for: 0101011110101

q0 -> (0) -> q1 -> (1) -> q2 -> (0) -> q3 -> (1) -> q4 -> (0) -> q1 -> (1) -> q2 -> (1) -> q3 -> (1) -> q4 -> (1) -> q1  
-> (0) -> q2 -> (1) -> q3 -> (0) -> q4 -> (1) -> q1 (it is a final state.)  
Yes!

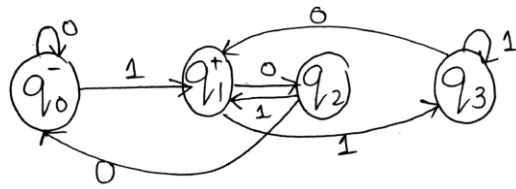
DFA 5:

$S = \{0, 1\}$ ,  $L = \{w \in S \mid w \bmod 4 = 1\}$ .

```
typedef struct STATE {
    string temp;
    STATE* occ0;
    STATE* occ1;
    bool isFinal;
};

class dfa5 {
    STATE q0, q1, q2, q3;
    string lang = "01";
    public : dfa5(){
        q0.temp = "q0";    q0.isFinal = false;    q0.occ0 = &q0;    q0.occ1 = &q1;
        q1.temp = "q1";    q1.isFinal = true;     q1.occ0 = &q2;    q1.occ1 = &q3;
        q2.temp = "q2";    q2.isFinal = false;    q2.occ0 = &q0;    q2.occ1 = &q1;
        q3.temp = "q3";    q3.isFinal = false;    q3.occ0 = &q2;    q3.occ1 = &q3;
    }
    public : bool validate(string s){
        STATE* cur = &q0;
        for (int i = 0 ; i < s.size(); ++i ){
            cout << cur->temp << " -> " << "(" << s[i] << " ) -> " ;
            if ( s[i] == '0' ) cur = cur->occ0;
            else if ( s[i] == '1' ) cur = cur->occ1;
            else {
                cout << " ( " << s[i] << " is not part of ALPHABETS.)" << endl;
                return false;
            }
        }
        cout << cur->temp << " ";
        if (!cur->isFinal) {
            cout << "(it is not a final state.)" << endl;
            return false;
        }
        cout << "(it is a final state.)" << endl;
        return true;
    }
};
```

## DFA:



## TEST CASES:

Enter you string you want to check for: 10011011

q0 -> (1) -> q1 -> (0) -> q2 -> (0) -> q0 -> (1) -> q1 -> (1) -> q3 -> (0) -> q2 -> (1) -> q1 -> (1) -> q3 (it is not a final state.)

No!

Enter you string you want to check for: 00111001

q0 -> (0) -> q0 -> (0) -> q0 -> (1) -> q1 -> (1) -> q3 -> (1) -> q3 -> (0) -> q2 -> (0) -> q0 -> (1) -> q1 (it is a final state.)

Yes!