

White Matter Multi-Resolution Segmentation Using Fuzzy Set Theory

*Alessandro Delmonte^{1,2}, *Corentin Mercier^{1,3}, Johan Pallud⁴, Isabelle Bloch^{1,2}, Pietro Gori¹

¹LTCI, Télécom ParisTech, Université Paris-Saclay, Paris, France

²IMAG2 Laboratory, Imagine Institute, Paris, France

³LIX, Ecole Polytechnique, Palaiseau, France

⁴Neurosurgery Department, Sainte-Anne Hospital, Paris, France

* equally contributed to this work



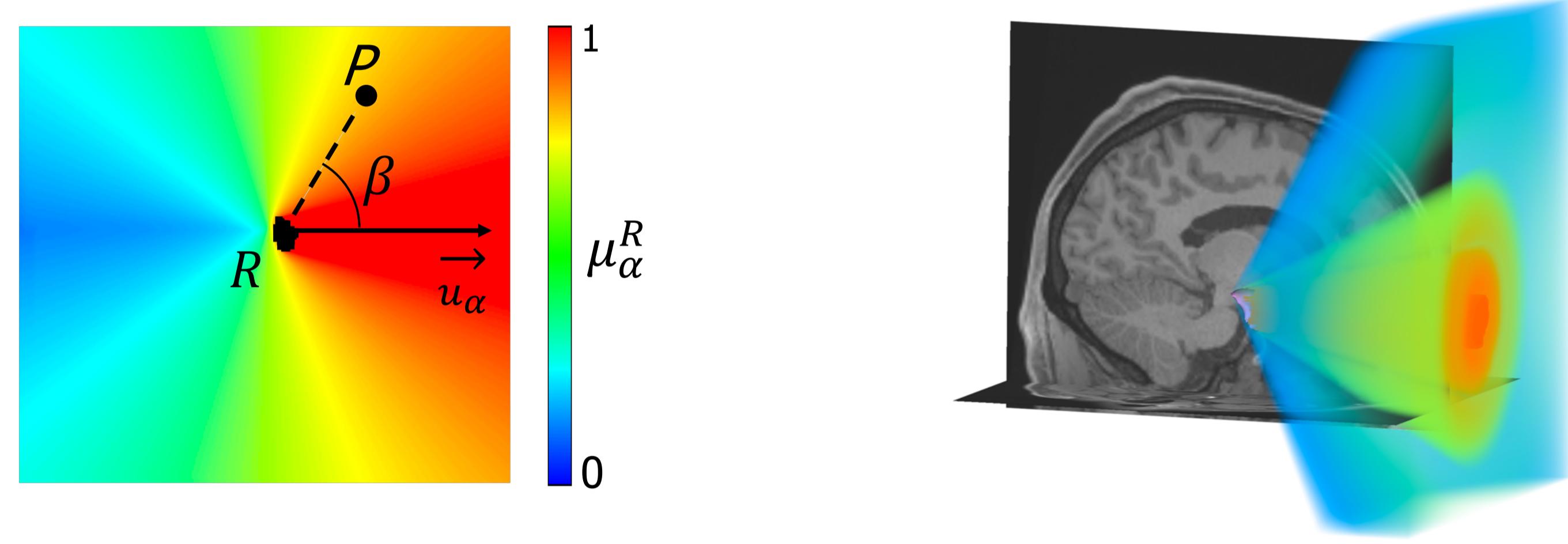
INTRODUCTION / OBJECTIVE

White matter fiber bundles are often described using qualitative spatial relationships (e.g. anterior of Amygdala) [1]. We propose to model their inherent vagueness using the theory of fuzzy sets [2]. Furthermore, to cope with the high redundancy of tractograms and ease interpretation, we introduce an interactive navigation and exploration technique based on a multi-resolution representation.

SPATIAL RELATIONS MODELING

Bundles are defined as a logic combination of spatial (*anterior of*, ...), connectivity (*endpoint in*, ...) and trajectory (*crossing*, ...) relations.

Every voxel P in the space is assigned a membership value μ describing the degree of satisfaction of the combined relations. A FS score is computed for each fiber (with endpoints f) as the weighted average of μ values of the voxels the fiber passes through.



$$\text{Directional: } \mu_{\alpha}^R(P) = \max(0, g(\beta_{\min})), g(\beta_{\min}) = \frac{1-2\beta_{\min}}{\pi}$$

$$\text{Connectivity: } EP = \min_{r \in R}(e^{-\frac{\|f-r\|_2^2}{\lambda^2}})$$

An anatomical coherence score (ACS) [3] is obtained for each fiber/cylinder in a conjunctive way.

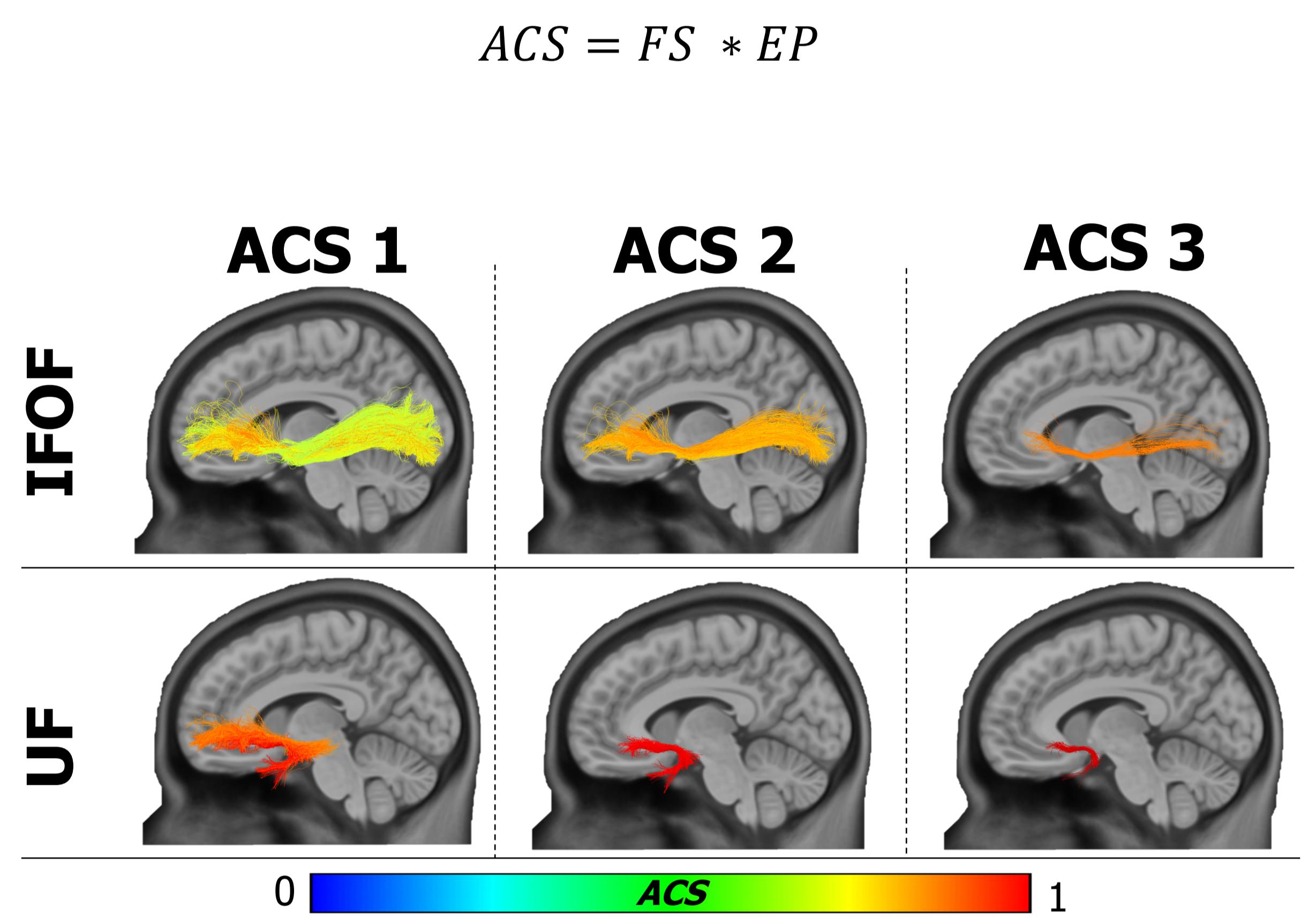


Fig. 1: Fibers of interest can be selected via an ACS based thresholding operation.

MULTI-RESOLUTION REPRESENTATION

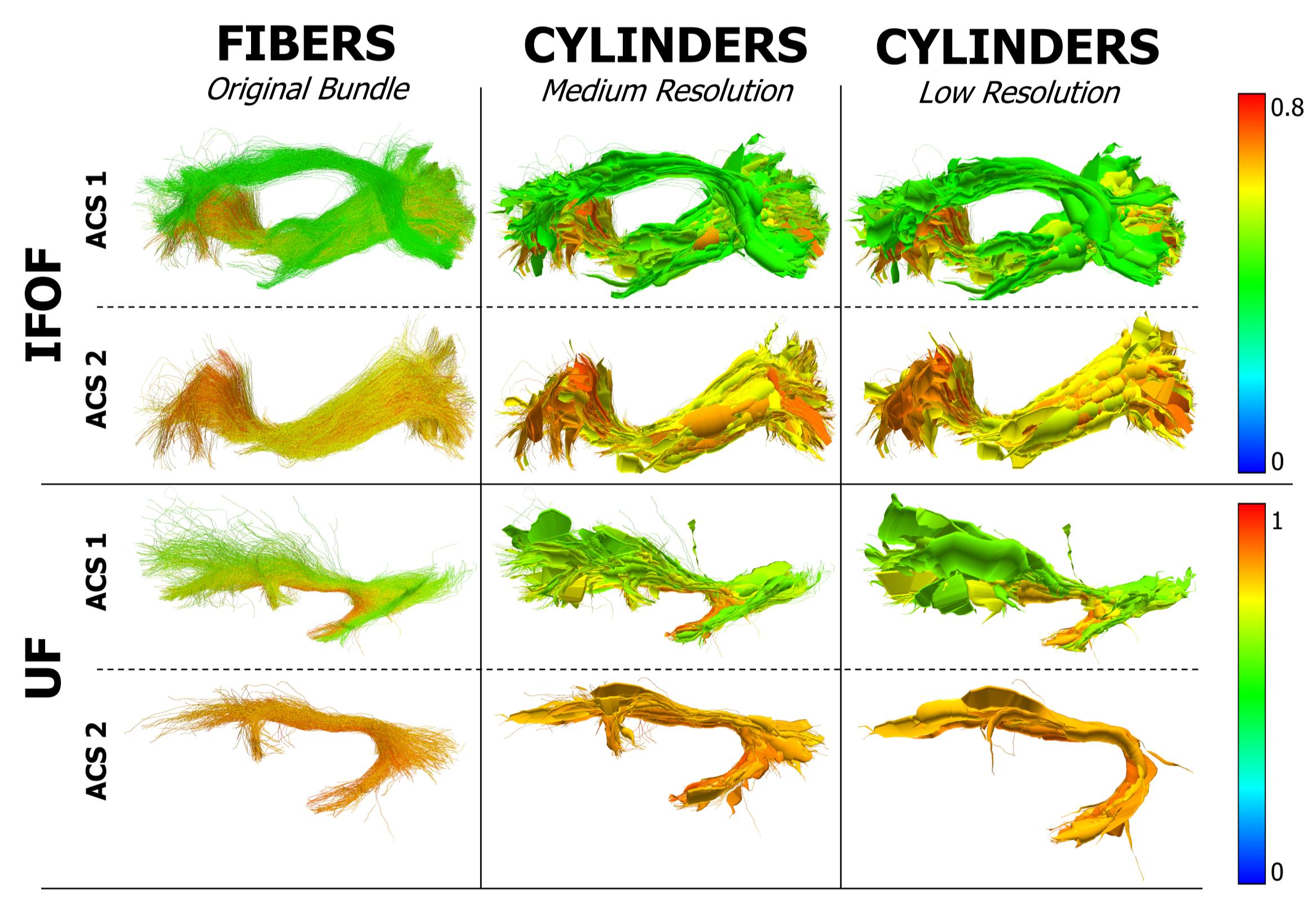


Fig. 2: Multi-resolution fiber bundles visualization

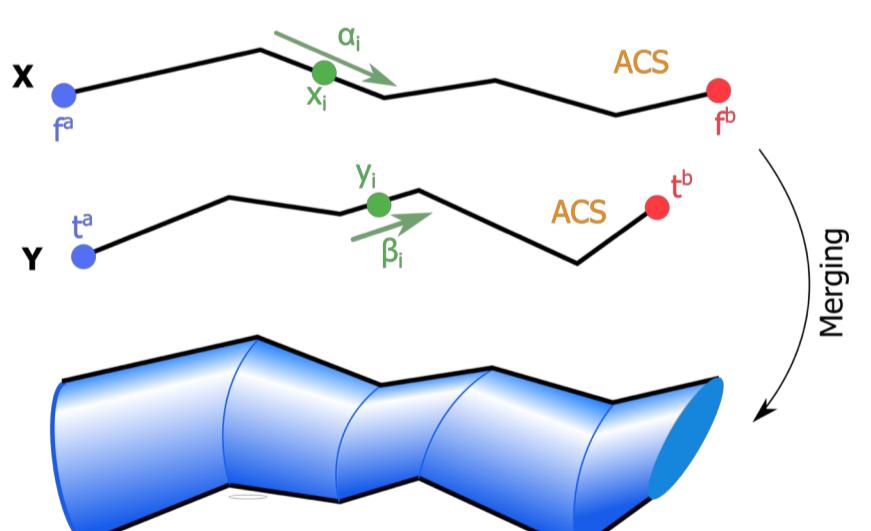
White matter multi-resolution [4] technique progressively merges fibers together in generalized cylinders.

- Real-time multi-resolution navigation
- Interactive ACS thresholding for segmentation

Fibers are selected using an extension of the Weighted Currents [5] similarity, containing an ACS term.

$$WC_{ext} = K_c(|ACS_x - ACS_y|)K_a(\|t_a - t_b\|_2)K_b(\|f_a - f_b\|_2) \left[\sum_{i=1}^{N-1} \sum_{j=1}^{M-1} K_g(\|x_i - y_j\|_2) \beta_j \right]$$

with $K_c(|A - B|) = 1 - |A - B|$, and K_a , K_b , K_g being Gaussian kernels.



RESULTS

- We validated our results on 5 unrelated healthy adults subjects from the HCP dataset.
- The interactive analysis helped neurosurgeons to better understand the structure of the bundles and find an optimal ACS threshold for the segmentation of IFOF and UF.
- A smaller fiber dispersion, compared to state-of-the-art methods, can be observed.
- ACS thresholds were reproducible among different subjects.

FUTURE WORKS

We plan to extend the proposed technique to more fiber bundles, implementing more fuzzy relations, and perform statistical analyses.

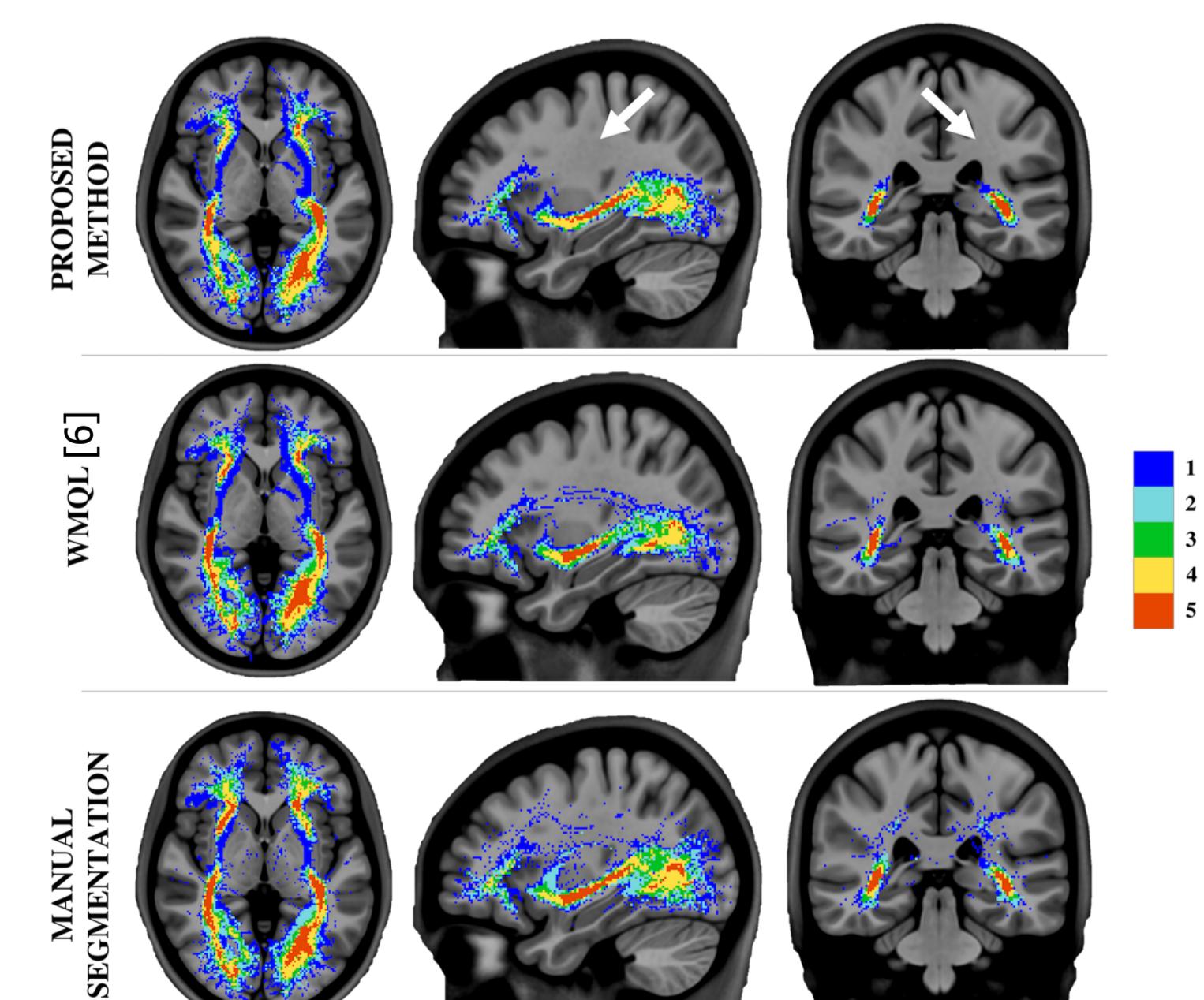


Fig. 3: Tracts dispersion map

Poster n°582

<https://github.com/CorentinMercier/FBTS>



References

- [1] S. Wakana et al., "Reproducibility of quantitative tractography methods applied to cerebral white matter", *NeuroImage*, vol. 36, no. 3, pp. 630-644, 2007.
- [2] I. Bloch, "Fuzzy spatial relationships for image processing and interpretation: a review", *Image and Vision Computing*, vol. 23, no. 2, pp. 89-110, 2005.
- [3] A. Delmonte et al., "Segmentation of White Matter Tractograms Using Fuzzy Spatial Relations", in *Organization for Human Brain Mapping (OHBM)*, Singapore, 2018.
- [4] C. Mercier et al., "Progressive and Efficient Multi-Resolution Representations for Brain Tractograms", in *EG VCBM*, 2018.
- [5] P. Gori et al., "Parsimonious Approximation of Streamline Trajectories in White Matter Fiber Bundles," *IEEE TMI*, vol. 35, no. 12, pp. 2609-2619, 2016.
- [6] D. Wassermann et al., "The white matter query language: a novel approach for describing human white matter anatomy," *Brain Structure and Function*, vol. 221, no. 9, pp. 4705-4721, 2016.