

## Week 7 Tutorial 5

The purpose of this program is to demonstrate how to use linear, semilog, and loglog graphs to determine the functional form of a set of data. Once the functional form is identified, the `polyfit()` function is used to determine the coefficients of the fit function.

```
% Always clear workspace variables before a new tutorial or program.
clear
clc
close all % closes all figure windows
```

Edit the code below and update the variable named **name** with your name for this tutorial in the code below.

```
name="";
fprintf("Output for Tutorial_07_5 run by %s.\n\n", name)
```

### Input

Our goal is to find the functions that best fit the three datasets.

```
% Data set 1
x1=1:2:12;
y1=[25 170 420 750 1170 1660];

% Data set 2
x2=1:6;
y2=[30 75 150 360 750 1650];

% Data set 3
x3=5:1:10;
y3=[625 700 775 850 925 1000];
```

### Figure 1

Add code to the following where necessary (see comments).

```
% Open figure 1 and create a subplot of two plots, one on top of the other.
% Activate the first plot

% plot all three data sets on one graph using the default settings.
plot(x1,y1,x2,y2,x3,y3)

% Add a title "Linear Graph with 3 Sets of Data"
title('Linear Graph with 3 Sets of Data')

% Add axis labels, text, and legend.
xlabel('x');
ylabel('y');

% Add axis labels and text
```

```
text(4,500,'Data Set 3 can be fit with the linear function:   $y = m*x + b$ ',...
      'color','r','fontsize',12)
% Add a legend, we can specify the location using polar coordinates
legend('Data set 1', 'Data set 2','Data set 3','Location','northwest')
```

Notice that data set 3 is a straight line on the linear (default) graph. Data set 3 therefore has a functional form of  $y=mx+b$  (linear). We can fit a polynomial of order 1 to this data set so we'll use the `polyfit()` function passing in `x3`, `y3`, and 1 for an order of 1 on the `x3` and `y3` dataset. Polyfit will return the two coefficients needed (`m` and `b`) for  $y=mx+b$ .

```
% Notice that data set 3 is a straight line on the linear (default) graph.
% Data set 3 therefore has a functional form of  $y=mx+b$  (linear).
% We can fit a polynomial of order 1 to this data set
linearCoeff=polyfit(x3,y3,1); % Two coefficients are produced
m=linearCoeff(1);
b=linearCoeff(2);
```

We can now use `m` and `b` to calculate the best fit line by plugging these values into a function for `x`. We could use the `polyval()` function but so that you can see how it works, we'll do it manually.

```
% Calculate the best fit values using a linear model ( $y=mx+b$ )
xp3=linspace(5,10,100); % 100 linearly spaced values between 5 and 10
yp3=m*xp3+b; % alternately we could use yp3=polyval(LinearCoeff,x3)

% Activate the second plot in the subplot set for this figure

% Plot the data with asterisks (*) and the best fit function with a red line
plot(x3,y3,'*',xp3,yp3,'r');
% Add a title, axis labels and legend.
title('Data Set 3 with the Fit Equation  $y = m*x + b$ ')
xlabel('x')
ylabel('y')
legend('Data Set 3',' $Y=mx+b$  Fit','Location','southeast')
```

## Figure 2

In Figure 2, we'll see how the data looks on a `semilogy()` plot. We already know the third dataset is a linear dataset and we computed the best fit so now we'll only look at the first and second dataset.

```
% Open figure 2 and create a subplot of two plots, one on top of the other.
% Activate the first plot

% Create a semilogy graph with x1,y1 and x2,y2.
semilogy(x1,y1,x2,y2)

% Add title, axis labels, text, and legend
title('Semilogy Graph of Data Sets 1 and 2')
xlabel('x')
```

```
ylabel('y')
text(10E3,3,'Data Set 2 can be fit with an exponential function:  $y = b \cdot e^m$ ',...
     'color','r','fontsize',12)
legend('Data set 1', 'Data set 2','Location','southeast')
```

Notice that data set 2 is a straight line on the semilogy graph. This indicates that it has the functional form:

$y = b \cdot \exp(m \cdot x)$  (exponential)

The linear form of an exponential function (which is found by taking the log of both sides) is:  $\log(y) = m \cdot x + \log(b)$ . As before, if we do a 1st order polyfit we can find  $m$  and  $\log(b)$ .

```
expCoeff=polyfit(x2,log(y2),1); % Two coefficients are produced
m=expCoeff(1);
logb=expCoeff(2);
b=exp(logb);

% Calculate the best fit values using a linear model (y=mx+b)
xp2=linspace(1,6,100); % 100 values between 1 and 6
yp2=b*exp(m*xp2); % find the fit values
```

Here we'll display our best fit function. We will plot data set 2 and the fit function on a **linear** graph

```
% Activate the second plot in this Figure's subplot

% Plot the data with asterisks (*) and the best fit function with a red line
plot(x2,y2,'*',xp2,yp2,'r');

% add a title, axis labels, and legend
title('Data Set 2 with an Exponential Fit Equation:  $Y = b \cdot e^x$ ')
xlabel('x')
ylabel('y')
legend('Data Points', 'Y=b*e^x Fit','Location','southeast')
```

### Figure 3

Finally, let's look at a loglog example; where both axes are logarithmic. The only dataset left to identify is  $x_1$  and  $y_1$  so we'll only plot these values.

```
% Open figure 3 and create a subplot of two plots, one on top of the other.

% Plot the x1,y1 dataset on a loglog plot.
loglog(x1,y1)

% add a title, axis labels, text, and legend.
title('Loglog Graph with Data Set 1')
xlabel('x')
```

```

ylabel('y')
text(2,50,'Data Set 1 can be fit with a power function:  y = b*x^m',...
      'color','b','fontsize',12)
legend('Data set 1','Location','southeast')

```

Notice that data set 1 is a straight line on the loglog graph. This indicates that it has the functional form:

$y=b*x.^m$  (Power)

The linear form of a power function (found by taking the log of both sides) is:  $\log(y)=m*\log(x)+\log(b)$ . If we do a 1st order polyfit we can find m and b. Again, we'll compute the values to be displayed a **linear** graph.

```

powerCoeff=polyfit(log(x1),log(y1),1); % Two coefficients are produced
m=powerCoeff(1);
logb=powerCoeff(2);
b=exp(logb);

% Calculate the best fit values using a linear model (y=mx+b)
xp1=linspace(1,12,100); % 100 values between 1 and 12
yp1=b*xp1.^m; % find the fit values
% Plot data set 1 and the power function fit on a linear graph

% Activate the second plot in this Figure's subplot

% Plot the data with asterisks (*) and the best fit function with a red line

% add a title, axis labels, and legend
title('Data Set 1 with a Power Fit Equation: Y=b*x.^m')
xlabel('x')
ylabel('y')
legend('Data Points','Y=b*x.^m Fit','Location','southeast')

```

## Example Output:

Run this tutorial from the **Command Window** and ensure your output matches the following.





