

my radius of both top and bottom along with the height will be controlled by the parameters.

steps I take

First I lofted my cup and extruded/lofted my lid. my cup would be a conical frustum

$$V = \frac{\pi h}{3} (r^2 + R^2 + rR)$$

This approach allowed me to directly control the top and bottom radii independently while maintaining a tapered geometry.

I converted my fluid ounces to cubic inches with

$$\text{Fluid Volume} = 1.804688 \times \frac{\text{Volume oz}}{\text{fl. oz}}$$

To maintain a realistic cup taper, I defined an angle parameter which created the relationship

$$R = r + h \tan(\text{Angle})$$

↳ this connects the top & bottom radii through taper angle

Since the volume is a driving parameter, I rearranged the frustum volume equation to solve for height in terms of angle & V.

after mathematical manipulation

$$V = \frac{\pi h}{3} (1.5^2 + \frac{h^2}{4} \tan^2 \theta - \frac{3h}{2} \tan \theta + 1.5^2 + \frac{h^2}{4} \tan^2 \theta + \frac{3h}{2} \tan \theta + 2.25 + .75 h \tan \theta - \frac{h^2}{4} \tan^2 \theta)$$

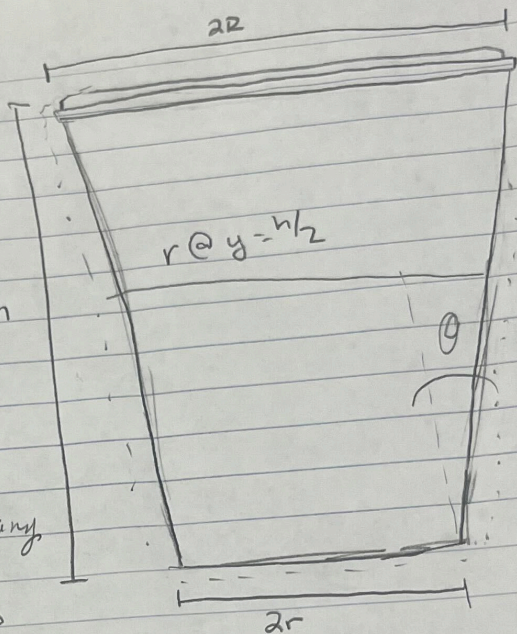
$$\text{So } V = 2.25\pi h + \frac{\pi h^3 \tan^2 \theta}{12}$$

The inner bottom radius is defined

$$\text{Inner } R = 1.5 - \frac{\text{Height}}{2} \tan(\text{Angle})$$

to ensure top D remains under 3 inches, cup fits in cup holder, and geometry scales proportionally with height

$$\text{Outer } R = \text{Inner } R + \text{Height} \tan(\text{Angle})$$



2 additional parameters were

Wallthick = .1 in

Lipthick = .1 in

The cup body is hollowed using shell feature driven by
Wall thickness and same goes for lid.

