

my radius of both top and bottom along with the height will be controlled by the parameters

Steps I take

First I lofted my cup and extruded/lofted my lid.  
My cup would be a conical frustum

$$V = \frac{\pi h}{3} (r^2 + R^2 + rR)$$

This approach allowed me to directly control the top and bottom radii independently while maintaining a tapered geometry.

I converted my fluid ounces to cubic inches with

$$\text{Fluid Volume} = 1.804688 \times \frac{\text{Volume oz}}{\text{fl. oz}}$$

To maintain a realistic cup taper, I defined an angle parameter which creates the relationship,

$$R = r + h \tan(\text{Angle})$$

↳ this connects the top & bottom radii through taper angle

Since the volume is a driving parameter, I rearranged the frustum volume equation to solve for height in terms of angle & V.

After mathematical manipulation

$$V = \frac{\pi h}{3} \left( 1.5^2 + \frac{h^2}{4} \tan^2 \theta - \frac{3h}{2} \tan \theta + 1.5^2 + \frac{h^2}{4} \tan^2 \theta + \frac{3h}{2} \tan \theta + 2.25 + .75h \tan \theta - .75h^2 \tan^2 \theta \right)$$

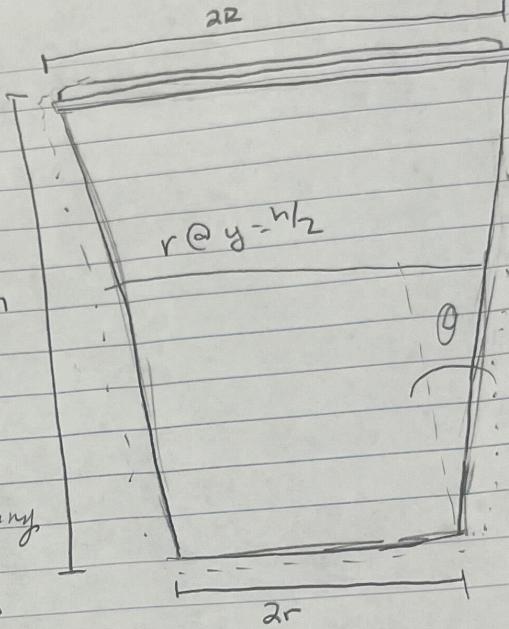
$$\therefore V = 2.25\pi rh + \frac{\pi h^3}{12} \tan^2 \theta$$

The inner bottom radius is defined

$$Inner R = 1.5 - \frac{Height}{2} \tan(\text{Angle})$$

To ensure top D remains under 3 inches, cup fits in cupholder, and geometry scales proportionally with height

$$Outer R = Inner R + Height \tan(\text{Angle})$$



2 additional parameters were

Wall thick = .1 in

Lip thick = .1 in

The cup body is hollowed using shell feature driven by  
Wall thickness and same goes for lid.

